

276. Paint Fence

n Posts, K colors.

Example:

$n=3, K=2$

o/p: 6

	P_1	P_2	P_3
c_1	1	2	3
c_2	1	2	3

= 6

$n=5, K=3$

o/p: 180

	P_1	P_2	P_3	P_4	P_5
c_1	1	2	$6+2=8$	$16+6=22$	$44+16=60$
c_2	1	2	8	22	60
c_3	1	2	8	22	60

= 180

Recurrence Relation:

$P_i \in \{P_1, P_2, \dots, P_n\}$; $c_j \in \{c_1, c_2, \dots, c_K\}$

$$N(P_i, c_j) = \begin{cases} 1 & ; n=1 \\ \sum_{x=1}^K N(P_1, c_x) & ; n=2 \\ \sum_{\substack{x=1 \\ x \neq j}}^K N(P_{i-1}, c_x) + \sum_{\substack{x=1 \\ x \neq j}}^K N(P_{i-2}, c_x) & ; \text{otherwise } n > 2 \end{cases}$$