

machine-learning-assignment-7

December 8, 2023

Q1. Implement Holt-winters exponential smoothing on air-passengers dataset and observe the metrics difference in them.

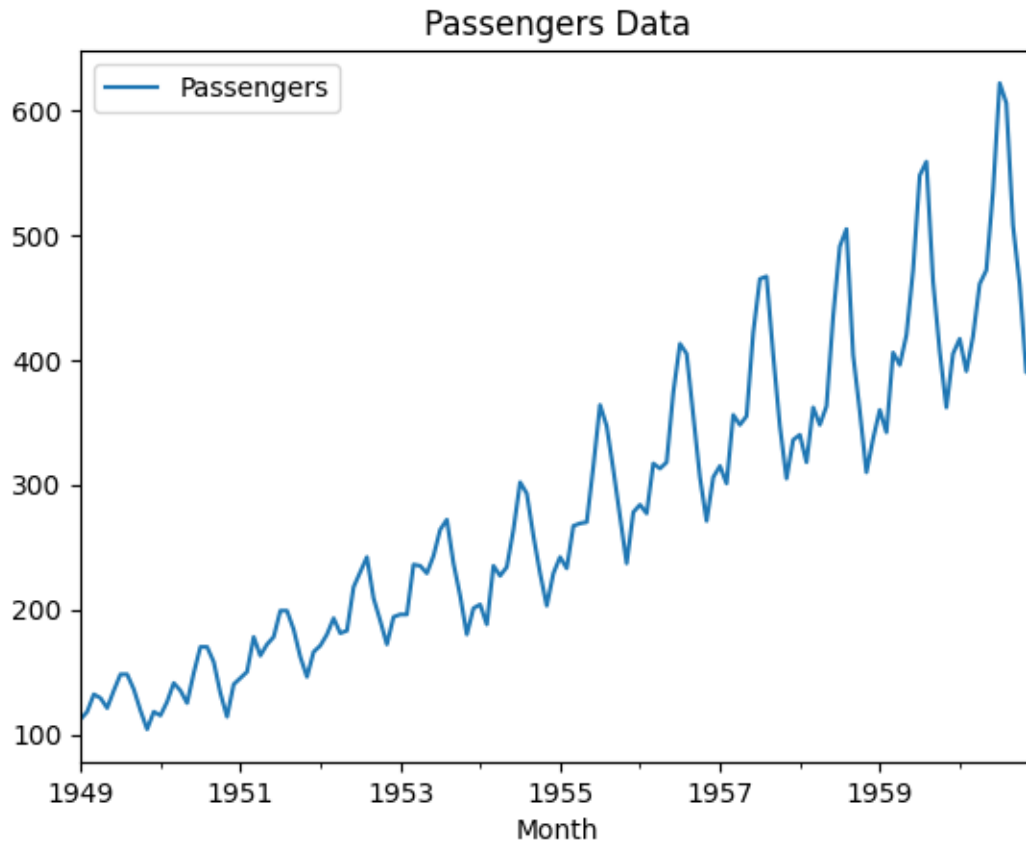
```
[8]: # dataframe operations - pandas
import pandas as pd
# plotting data - matplotlib
from matplotlib import pyplot as plt
# time series - statsmodels
# Seasonality decomposition
from statsmodels.tsa.seasonal import seasonal_decompose
# holt winters
# single exponential smoothing
from statsmodels.tsa.holtwinters import SimpleExpSmoothing
# double and triple exponential smoothing
from statsmodels.tsa.holtwinters import ExponentialSmoothing
```

```
[9]: airline = pd.read_csv('airline_passengers.
    ↪ csv', index_col='Month', parse_dates=True)
# finding shape of the dataframe
print(airline.shape)
# having a look at the data
print(airline.head())
# plotting the original data
airline[['Passengers']].plot(title='Passengers Data')
```

(144, 1)

	Passengers
Month	
1949-01-01	112
1949-02-01	118
1949-03-01	132
1949-04-01	129
1949-05-01	121

```
[9]: <Axes: title={'center': 'Passengers Data'}, xlabel='Month'>
```

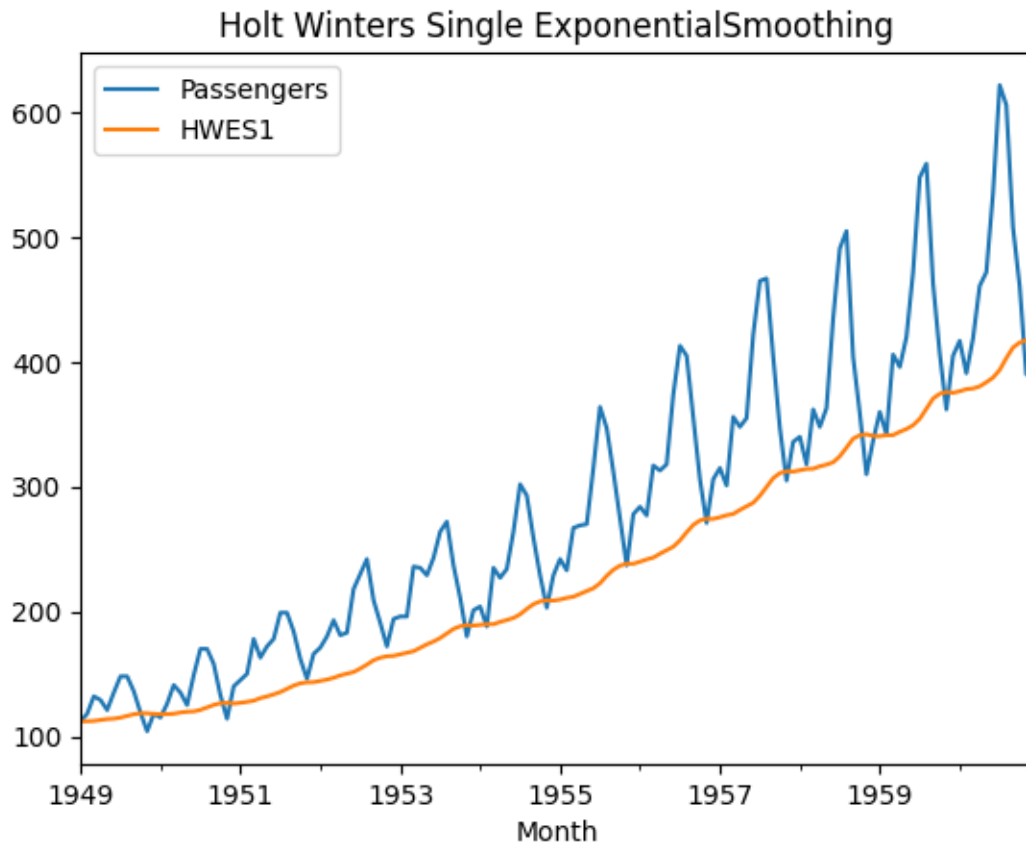


```
[10]: # Set the frequency of the date time index as Monthly start as indicated by the
      ↪data
      airline.index.freq = 'MS'
      # Set the value of Alpha and define m (Time Period)
      m = 12
      alpha = 1/(2*m)
      alpha
```

```
[10]: 0.041666666666666664
```

```
[11]: airline['HWES1'] = SimpleExpSmoothing(airline['Passengers']).
      ↪fit(smoothing_level=alpha,optimized=False,use_brute=True).fittedvalues
      airline[['Passengers','HWES1']].plot(title='Holt Winters Single
      ↪ExponentialSmoothing')
```

```
[11]: <Axes: title={'center': 'Holt Winters Single ExponentialSmoothing'},
      xlabel='Month'>
```



```
[63]: tlen=120
      train=airline[0:tlen]
      test=airline[tlen:]
      print(train.shape)
```

```
(120, 2)
```

```
[64]: print(test.shape)
```

```
(24, 2)
```

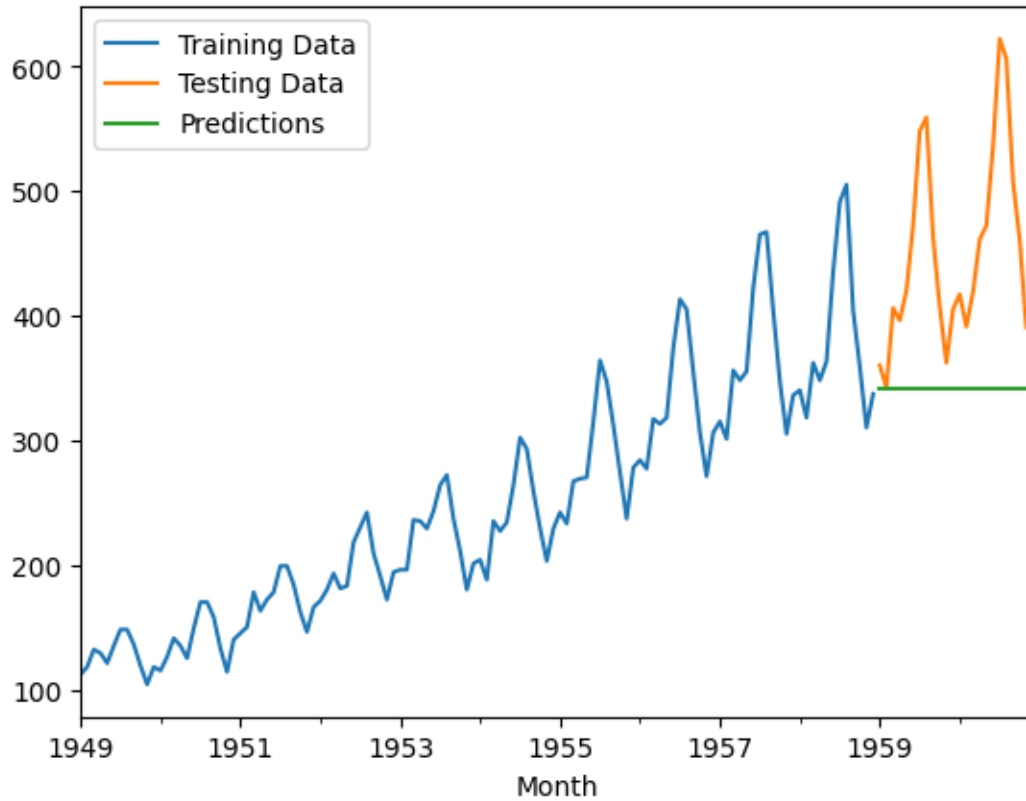
```
[66]: #Forecasting for the test data
      #Developing model
      sexpsmooth_model=SimpleExpSmoothing(train['Passengers']).
      ↪fit(smoothing_level=alpha,optimized=False,use_brute=True)
```

```
[67]: test_pred1=sexpsmooth_model.forecast(24)
```

```
[68]: train['Passengers'].plot(label='Training Data')
      test['Passengers'].plot(label='Testing Data')
```

```
test_pred1.plot(label='Predictions')
plt.legend(loc='best')
```

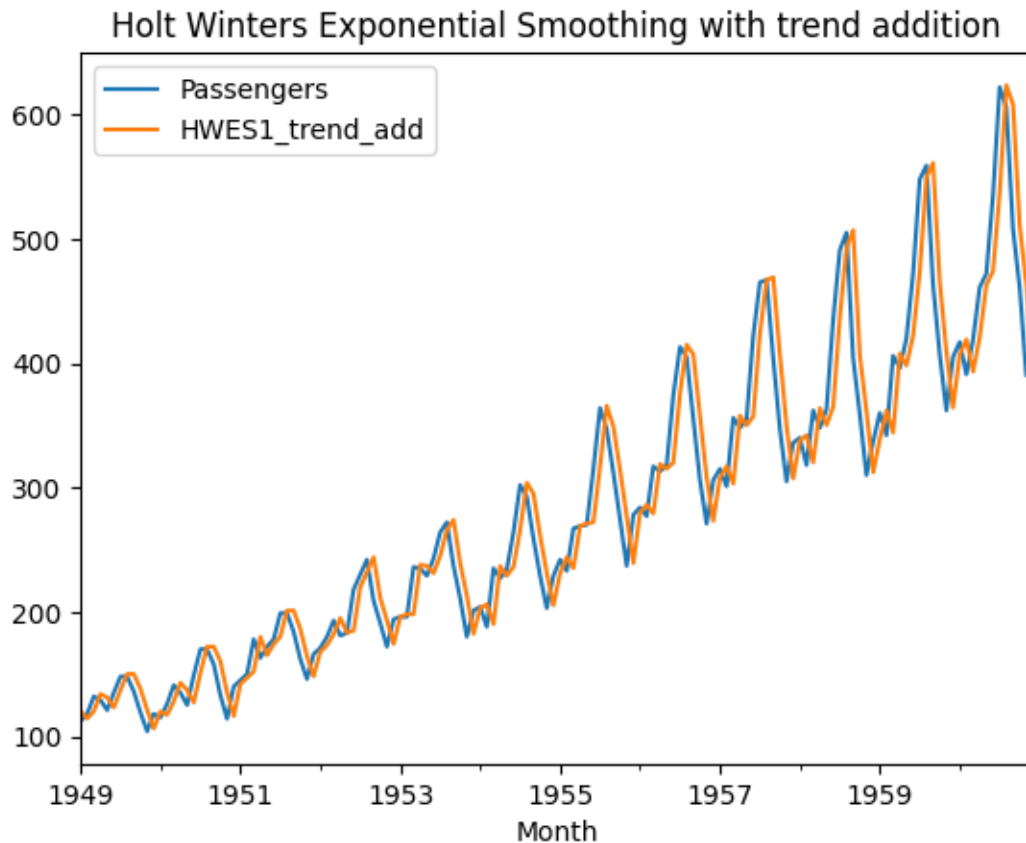
[68]: <matplotlib.legend.Legend at 0x78e9099b0df0>



```
[69]: #Finding trend with holt-linear trend methods
airline['HWES1_trend_add']=ExponentialSmoothing(airline['Passengers'],trend='add').
    ↪fit().fittedvalues
```

```
[70]: airline[['Passengers','HWES1_trend_add']].plot(title='Holt Winters Exponential_
    ↪Smoothing with trend addition')
```

[70]: <Axes: title={'center': 'Holt Winters Exponential Smoothing with trend addition'}, xlabel='Month'>

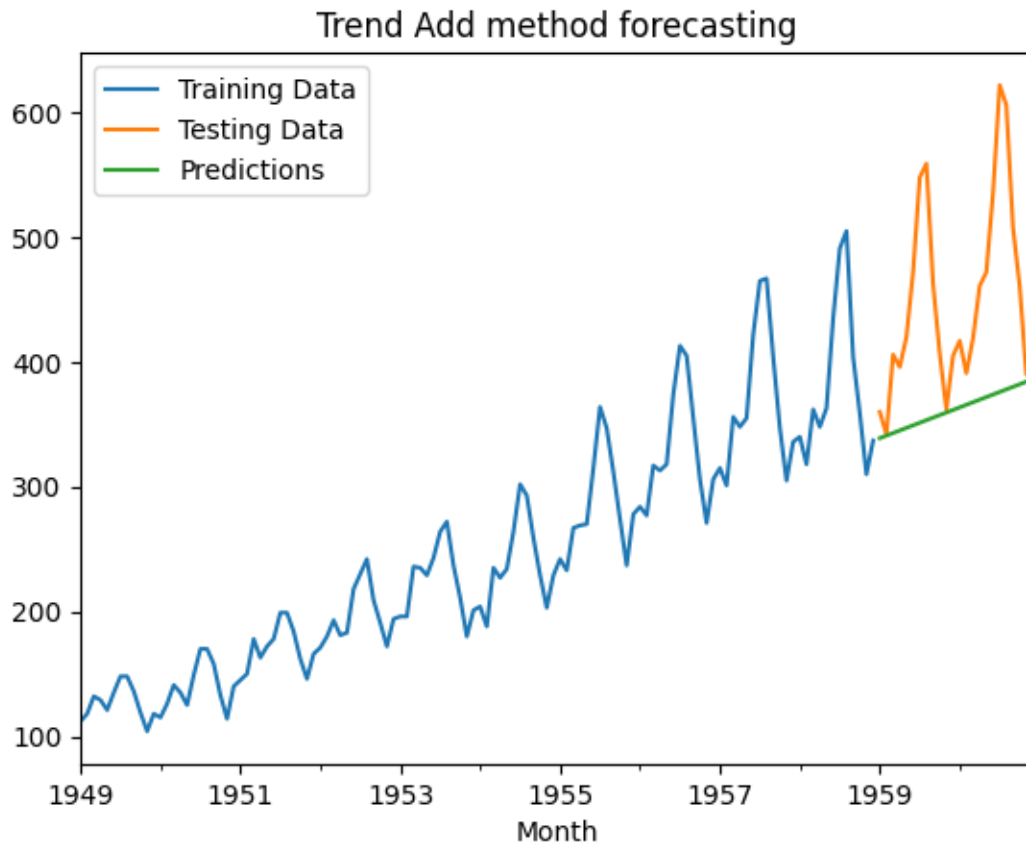


```
[71]: #Forecasting with trend add method
exp_trend_add_model=ExponentialSmoothing(train['Passengers'],trend='add').fit()
```

```
[72]: test_pred2=exp_trend_add_model.forecast(24)
```

```
[73]: train['Passengers'].plot(label='Training Data')
test['Passengers'].plot(label='Testing Data')
test_pred2.plot(label='Predictions')
plt.legend(loc='best')
plt.title("Trend Add method forecasting")
```

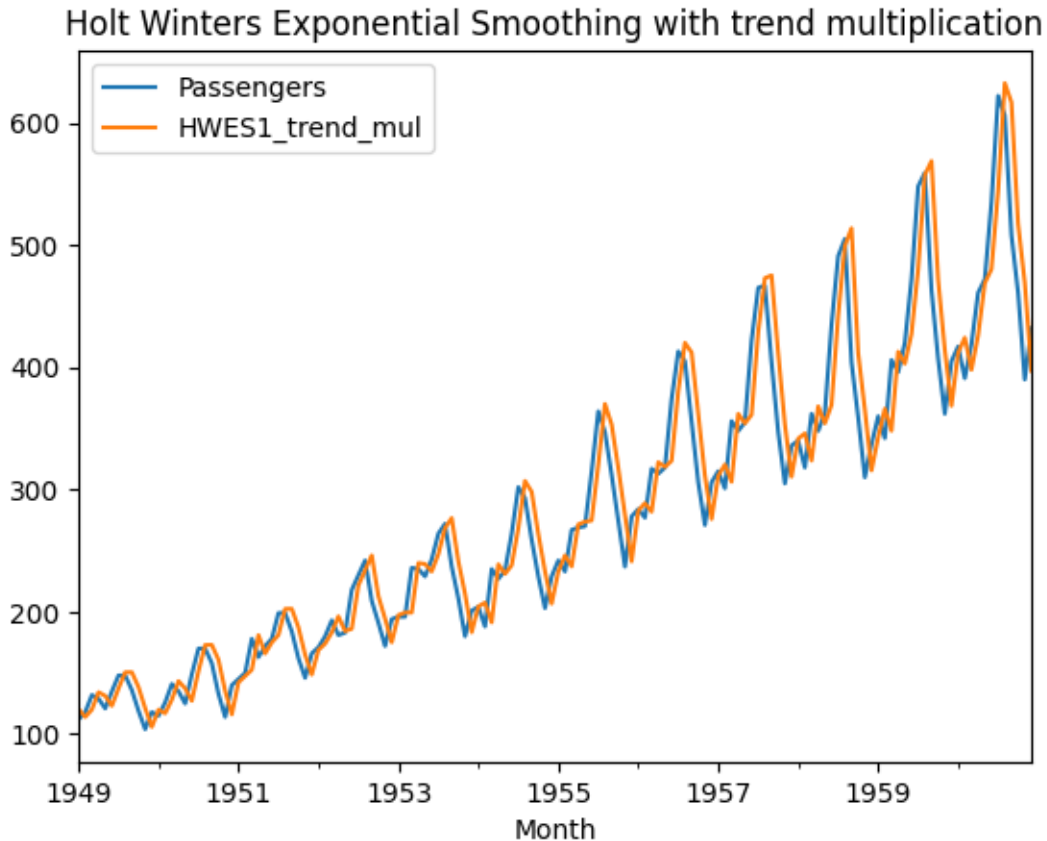
```
[73]: Text(0.5, 1.0, 'Trend Add method forecasting')
```



```
[74]: #Plotting trend with trend multiplication method
airline['HWES1_trend_mul']=ExponentialSmoothing(airline['Passengers'],trend='mul').
    ↪fit().fittedvalues
```

```
[75]: airline[['Passengers','HWES1_trend_mul']].plot(title='Holt Winters Exponential_
    ↪Smoothing with trend multiplication')
```

```
[75]: <Axes: title={'center': 'Holt Winters Exponential Smoothing with trend
multiplication'}, xlabel='Month'>
```



Q2.Explain ARMA and ARIMA model, what is purpose of these models in time series and Explain difference between them.

Ans= ARMA (AutoRegressive Moving Average) and ARIMA (AutoRegressive Integrated Moving Average) are models used in time series analysis to forecast future values based on past observations.

ARMA Model:

Combines autoregression (AR) and moving average (MA) components.

AR Component: Current value depends on its own past values (autocorrelation).

MA Component: Current value depends on the average of past error terms.

Denoted as $ARMA(p, q)$, where 'p' represents AR order, and 'q' represents MA order.

Assumes the time series data is stationary (constant mean, variance).

ARIMA Model:

Includes autoregressive (AR) and moving average (MA) components with an additional integration

AR and MA Components: Similar to ARMA.

Integration Component: Involves differencing the original data to make it stationary.

Denoted as $ARIMA(p, d, q)$, where 'p' represents AR order, 'd' represents differencing order, and 'q' represents MA order.

Suitable for handling non-stationary data by differencing to achieve stationarity.

Q3.Implement different ARIMA models on shampoo sales dataset. Display the sum-

mary of each model, and observe the metrics difference in them.

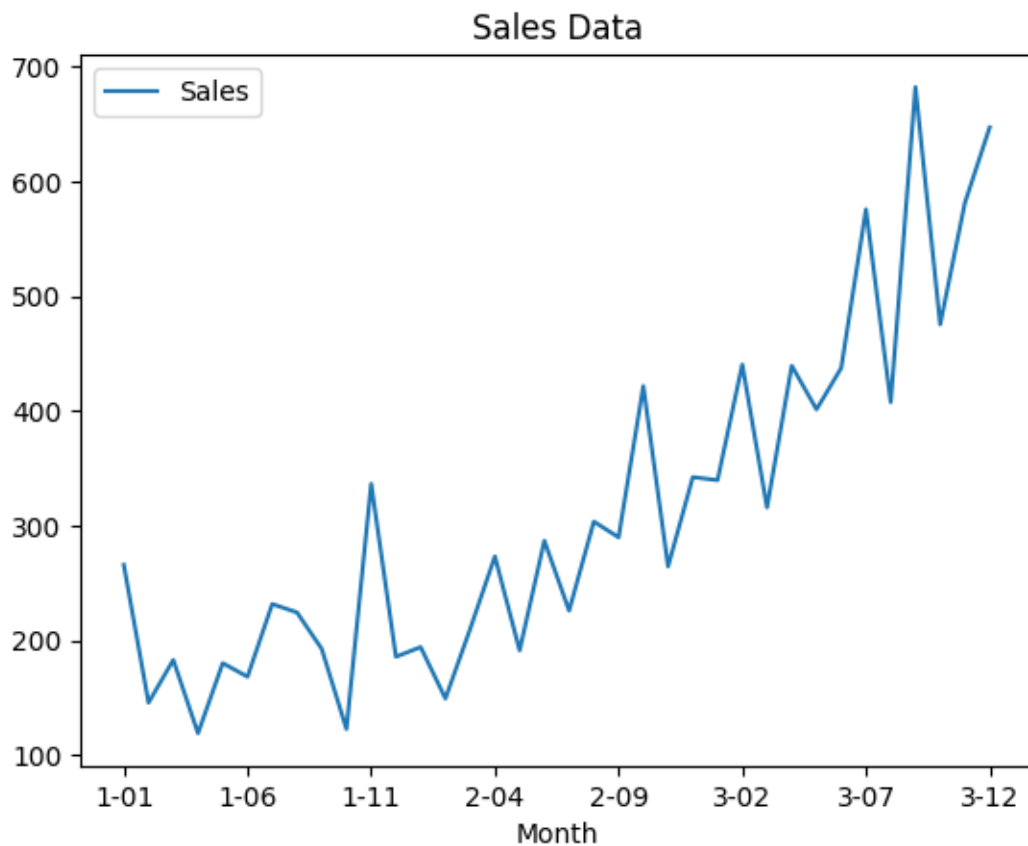
```
[2]: import pandas as pd
import matplotlib.pyplot as plt
from statsmodels.tsa.arima.model import ARIMA
```

```
[3]: shampoo = pd.read_csv('shampoo.csv', index_col='Month', parse_dates=True)
shampoo.head()
```

```
[3]:      Sales
Month
1-01  266.0
1-02  145.9
1-03  183.1
1-04  119.3
1-05  180.3
```

```
[4]: # plotting the original data
shampoo[['Sales']].plot(title='Sales Data')
```

```
[4]: <Axes: title={'center': 'Sales Data'}, xlabel='Month'>
```




```
[16]: tlen=12
      train=shampoo[0:tlen]
      test=shampoo[tlen:]
```

```
[17]: test
```

```
[17]:      Sales
      Month
2-01   194.3
2-02   149.5
2-03   210.1
2-04   273.3
2-05   191.4
2-06   287.0
2-07   226.0
2-08   303.6
2-09   289.9
2-10   421.6
2-11   264.5
2-12   342.3
3-01   339.7
3-02   440.4
3-03   315.9
3-04   439.3
3-05   401.3
3-06   437.4
3-07   575.5
3-08   407.6
3-09   682.0
3-10   475.3
3-11   581.3
3-12   646.9
```

```
[18]: arima_model1=ARIMA(train,order=(1,0,0)).fit()
      arima_model2=ARIMA(train,order=(0,1,0)).fit()
      arima_model3=ARIMA(train,order=(0,0,1)).fit()
```

```
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
```

```
    self._init_dates(dates, freq)
```

```
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
```

```
    self._init_dates(dates, freq)
```

```
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
```

```

ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
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/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)

```

```

[19]: pred1=arima_model1.forecast(12)
      pred2=arima_model2.forecast(12)
      pred3=arima_model3.forecast(12)

```

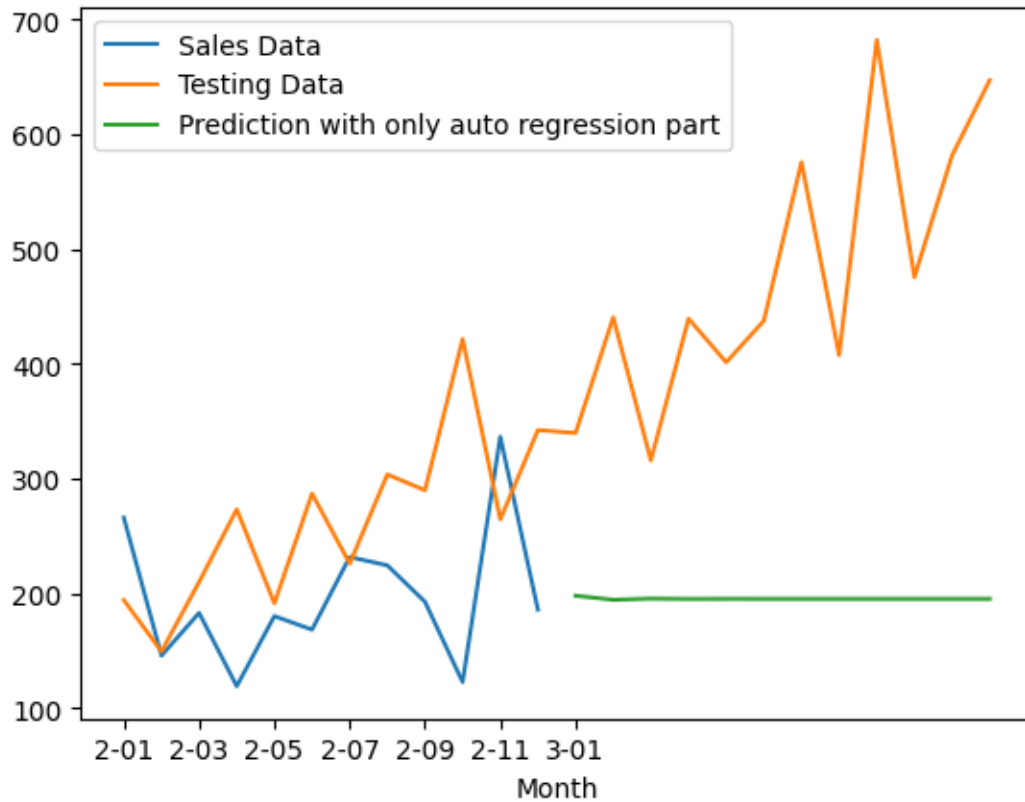
```

/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:836:
ValueWarning: No supported index is available. Prediction results will be given
with an integer index beginning at `start`.
    return get_prediction_index(
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:836:
FutureWarning: No supported index is available. In the next version, calling
this method in a model without a supported index will result in an exception.
    return get_prediction_index(
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:836:
ValueWarning: No supported index is available. Prediction results will be given
with an integer index beginning at `start`.
    return get_prediction_index(
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:836:
ValueWarning: No supported index is available. Prediction results will be given
with an integer index beginning at `start`.
    return get_prediction_index(

```

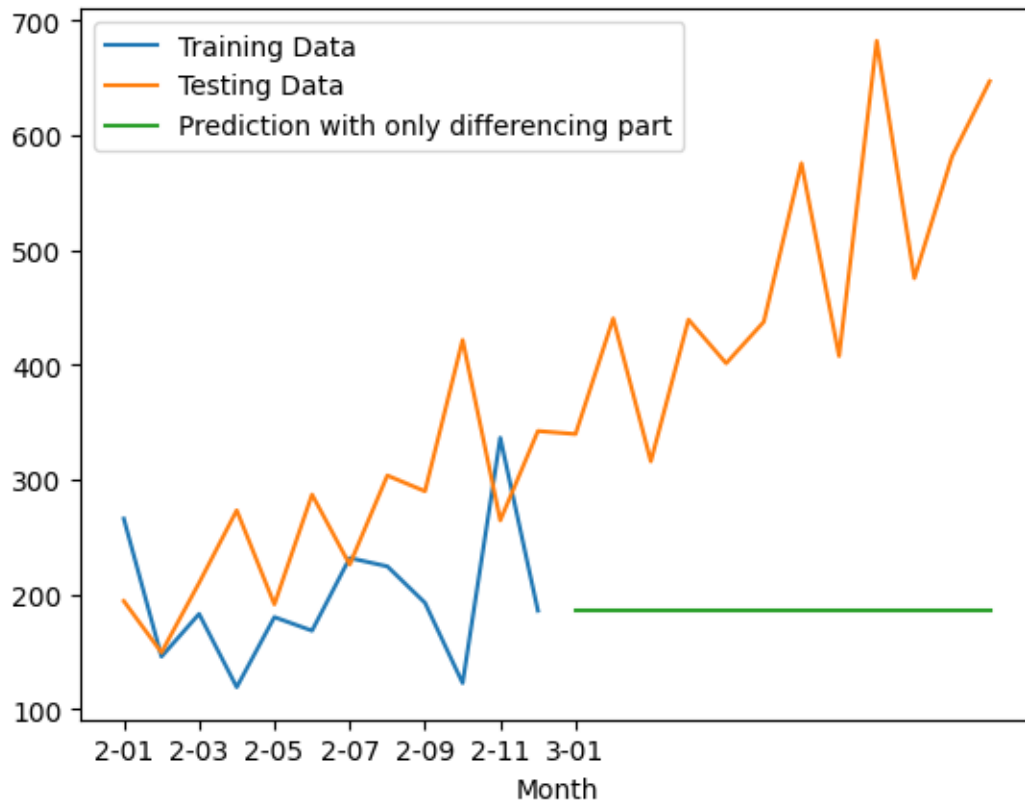
```
[20]: train['Sales'].plot(label="Sales Data")
test['Sales'].plot(label="Testing Data")
pred1.plot(label="Prediction with only auto regression part")
plt.legend(loc='best')
```

[20]: <matplotlib.legend.Legend at 0x7e5c46c04160>



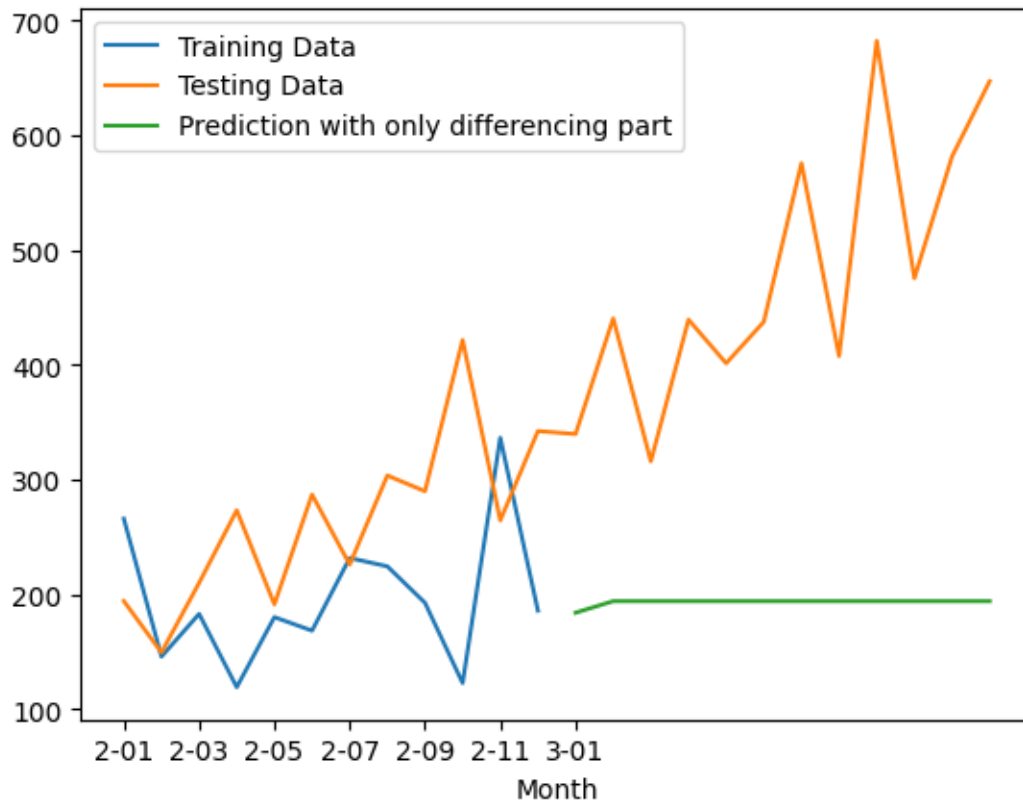
```
[21]: train['Sales'].plot(label="Training Data")
test['Sales'].plot(label="Testing Data")
pred2.plot(label="Prediction with only differencing part")
plt.legend(loc='best')
```

[21]: <matplotlib.legend.Legend at 0x7e5c48d57820>



```
[22]: train['Sales'].plot(label="Training Data")
      test['Sales'].plot(label="Testing Data")
      pred3.plot(label="Prediction with only differencing part")
      plt.legend(loc='best')
```

```
[22]: <matplotlib.legend.Legend at 0x7e5c46a2fca0>
```



```
[34]: model_pdq=ARIMA(train,order=(3,2,2)).fit()
      pred_pdq=model_pdq.forecast(24)
```

```
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:473:
ValueWarning: An unsupported index was provided and will be ignored when e.g.
forecasting.
    self._init_dates(dates, freq)
/usr/local/lib/python3.10/dist-
packages/statsmodels/tsa/statespace/sarimax.py:966: UserWarning: Non-stationary
starting autoregressive parameters found. Using zeros as starting parameters.
    warn('Non-stationary starting autoregressive parameters'
/usr/local/lib/python3.10/dist-
packages/statsmodels/tsa/statespace/sarimax.py:978: UserWarning: Non-invertible
```

```

starting MA parameters found. Using zeros as starting parameters.
warn('Non-invertible starting MA parameters found.')
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:836:
ValueWarning: No supported index is available. Prediction results will be given
with an integer index beginning at `start`.
return get_prediction_index(
/usr/local/lib/python3.10/dist-packages/statsmodels/tsa/base/tsa_model.py:836:
FutureWarning: No supported index is available. In the next version, calling
this method in a model without a supported index will result in an exception.
return get_prediction_index(

```

```

[35]: train['Sales'].plot(label="Training Data")
test['Sales'].plot(label="Testing Data")
pred_pdq.plot(label="Prediction ")
plt.legend(loc='best')

```

[35]: <matplotlib.legend.Legend at 0x7e5c45b02e00>



```

[36]: print(model_pdq.summary())

```

SARIMAX Results

=====

```

Dep. Variable:          Sales    No. Observations:          12
Model:                ARIMA(3, 2, 2)    Log Likelihood          -103189353.154
Date:                Fri, 08 Dec 2023    AIC                    206378718.309
Time:                05:33:59    BIC                    206378720.124
Sample:                0    HQIC                    206378716.317
                        - 12

```

```

Covariance Type:          opg

```

	coef	std err	z	P> z	[0.025	0.975]
ar.L1	-6.491e-07	2.45e-08	-26.539	0.000	-6.97e-07	-6.01e-07
ar.L2	2.607e-07	3.46e-08	7.544	0.000	1.93e-07	3.28e-07
ar.L3	1.426e-08	7.16e-08	0.199	0.842	-1.26e-07	1.55e-07
ma.L1	-6.491e-07	2.45e-08	-26.539	0.000	-6.97e-07	-6.01e-07
ma.L2	2.607e-07	3.46e-08	7.544	0.000	1.93e-07	3.28e-07
sigma2	0.0014	7.9e-11	1.73e+07	0.000	0.001	0.001

```

===
Ljung-Box (L1) (Q):          4.27    Jarque-Bera (JB):
0.26
Prob(Q):                    0.04    Prob(JB):
0.88
Heteroskedasticity (H):      4.25    Skew:
-0.39
Prob(H) (two-sided):        0.27    Kurtosis:
3.14
=====
===

```

```

Warnings:
[1] Covariance matrix calculated using the outer product of gradients (complex-
step).
[2] Covariance matrix is singular or near-singular, with condition number
9.7e+16. Standard errors may be unstable.

```

```
[37]: from sklearn.metrics import mean_squared_error
mse = mean_squared_error(test['Sales'],pred_pdq)
mse
```

[37]: 5648812.082357357