

Problem Discussion

Topological Sorting (SPOJ) (C++)

+ Cycle finding demonstration

#csspre

Online

Topological Sorting

Link: <https://www.spoj.com/problems/TOPOSORT/>

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What this problem asks for:

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1. Topologically Sort given relations

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1. Topologically Sort given relations
2. Indicate if sorting is not possible (graph has cycle)

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What this problem asks for:

1. Topologically Sort given relations
2. Indicate if sorting is not possible (graph has cycle)
3. If multiple sorting possible, print lexicographically smallest one

Cycle Finding

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Since GRAY means right now it's children are being explored.

Cycle Finding

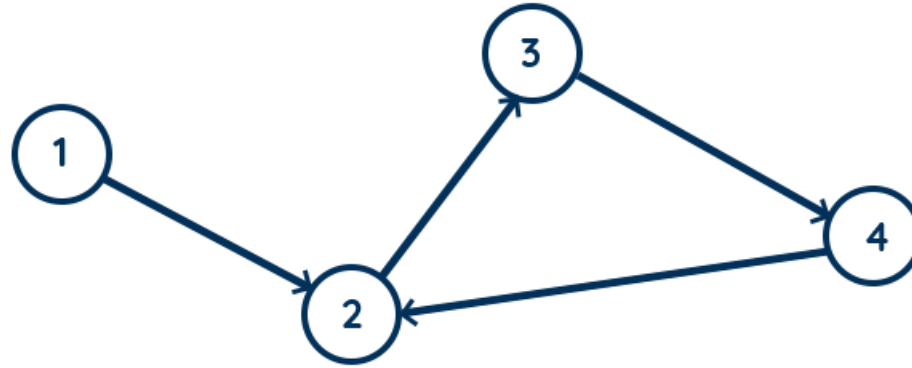
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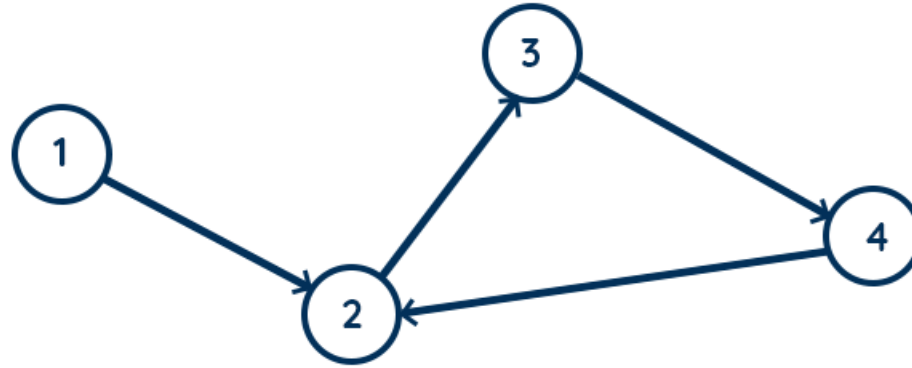
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Since GRAY means right now it's children are being explored. **And an edge from child to ancestor means there is a cycle.**

Cycle Finding



Cycle Finding



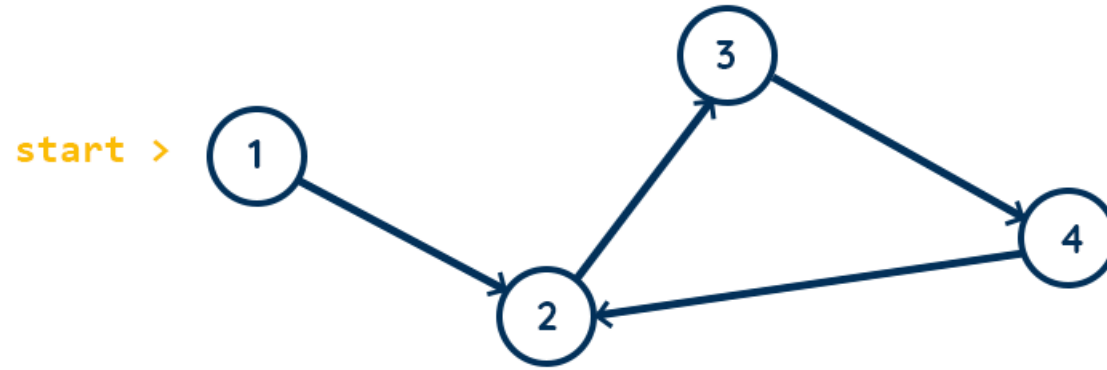
`color[] =`

0	0	0	0
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1 2 3 4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

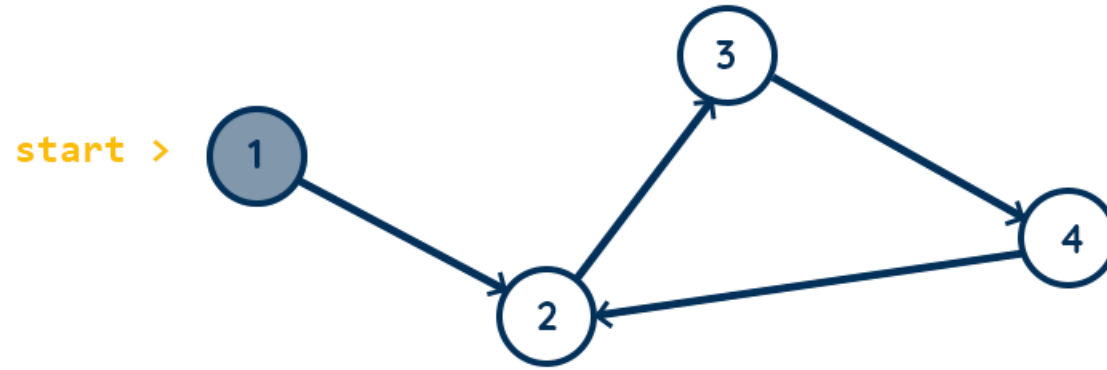


color[] =

0	0	0	0
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

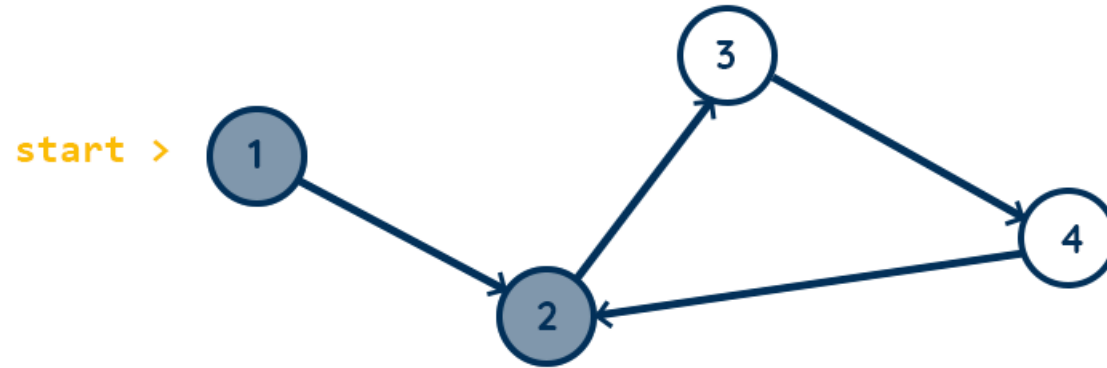


color[] =

1	0	0	0
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

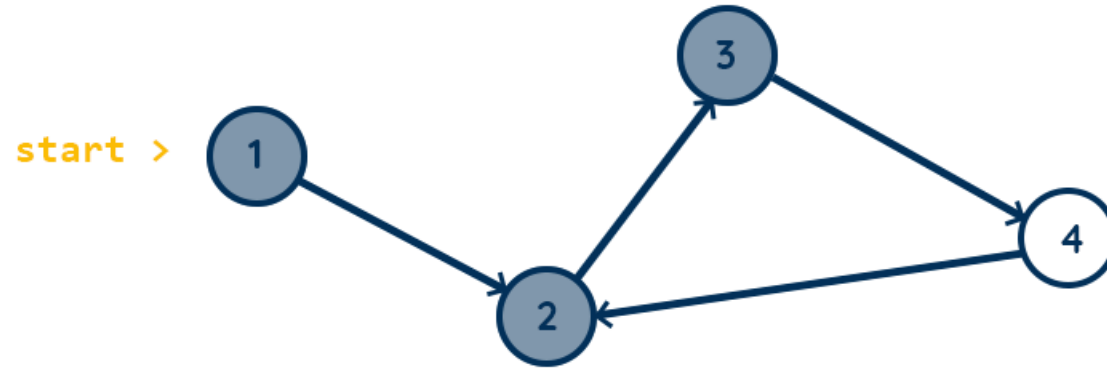


color[] =

1	1	0	0
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

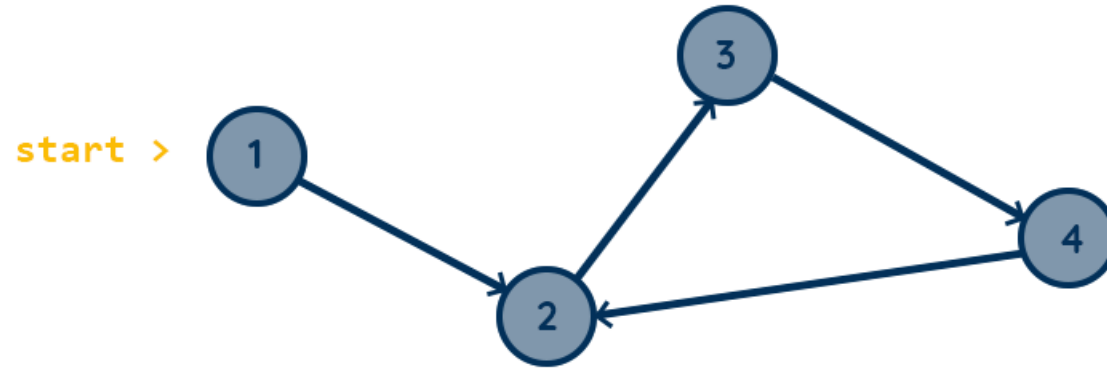


color[] =

1	1	1	0
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

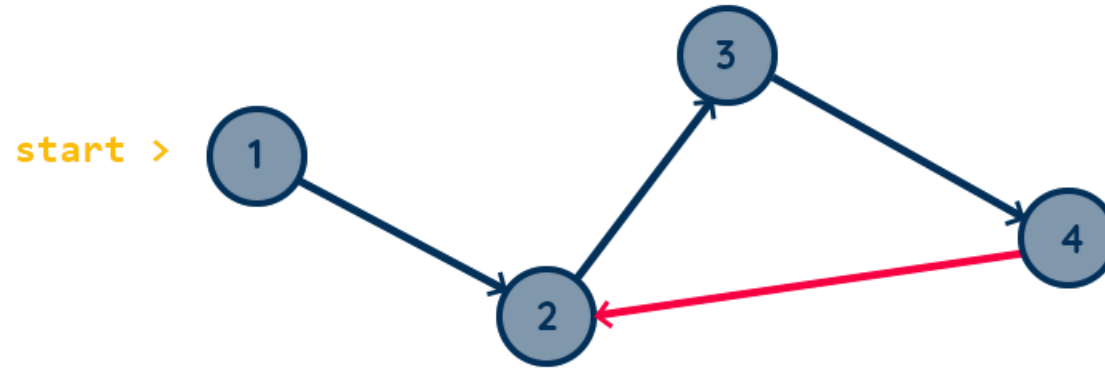


color[] =

1	1	1	1
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding



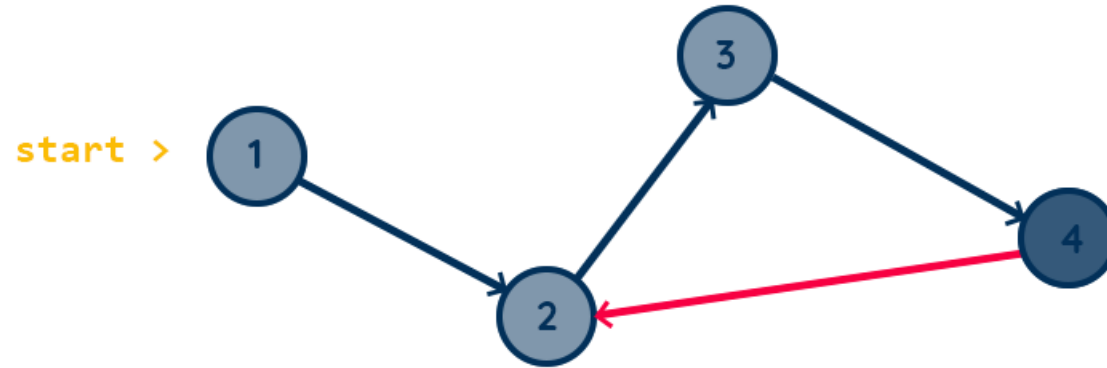
4 is 2's successor
2 is 4's successor!
Prerequisite conflict!!

color[] =

1	1	1	1
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

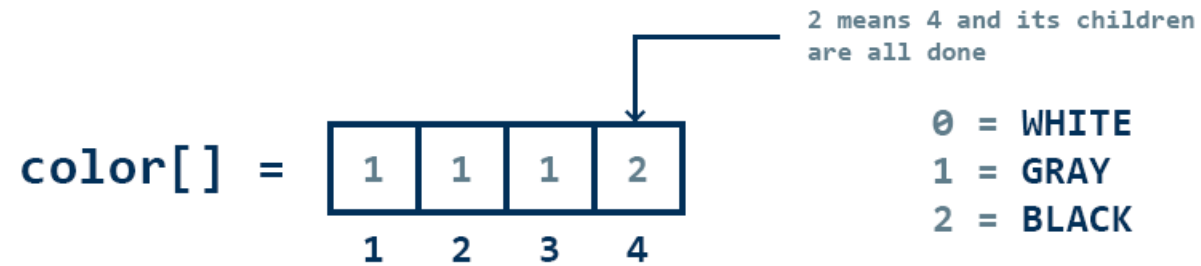
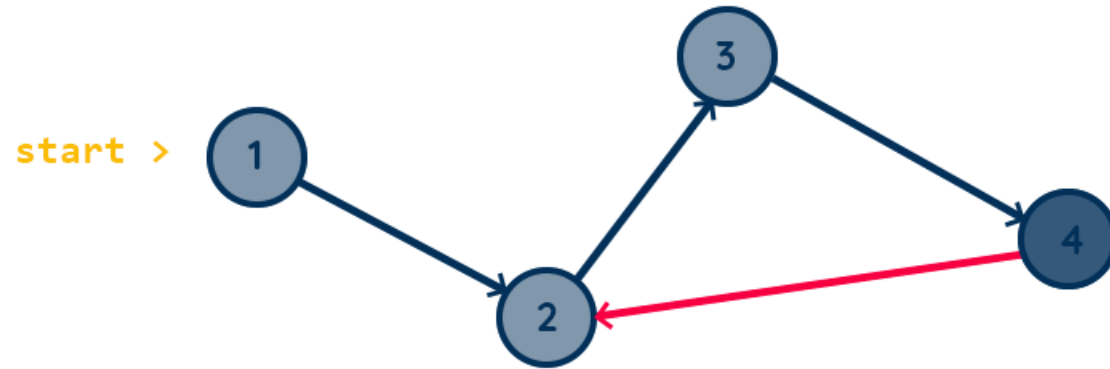


color[] =

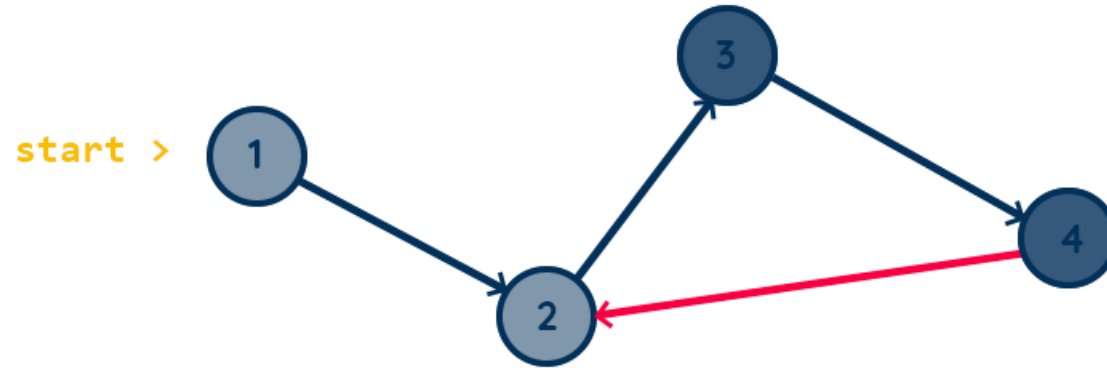
1	1	1	2
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding



Cycle Finding

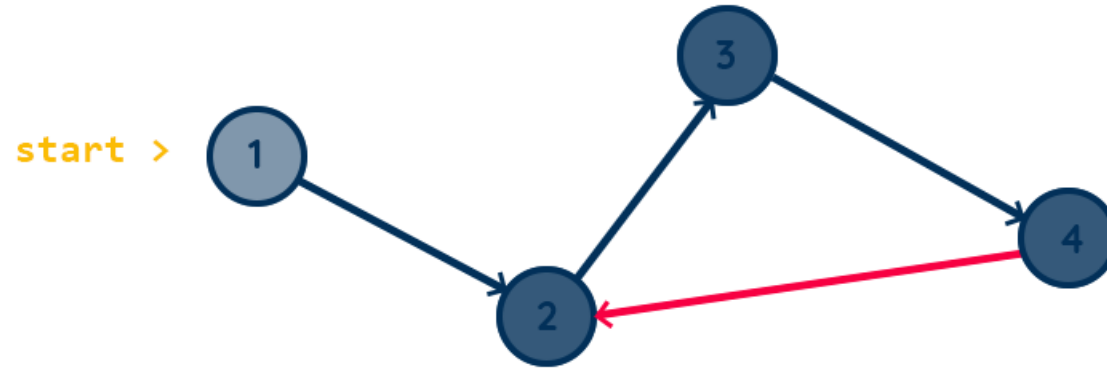


color[] =

1	1	2	2
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

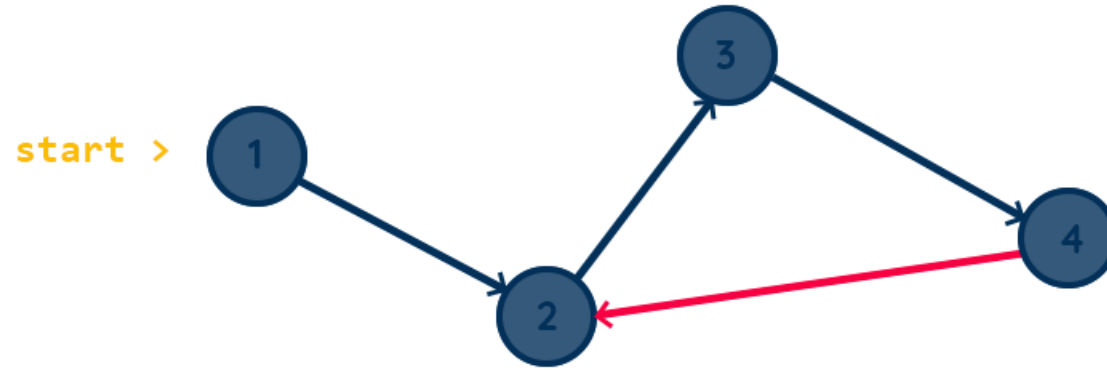


color[] =

1	2	2	2
1	2	3	4

0 = WHITE
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Cycle Finding

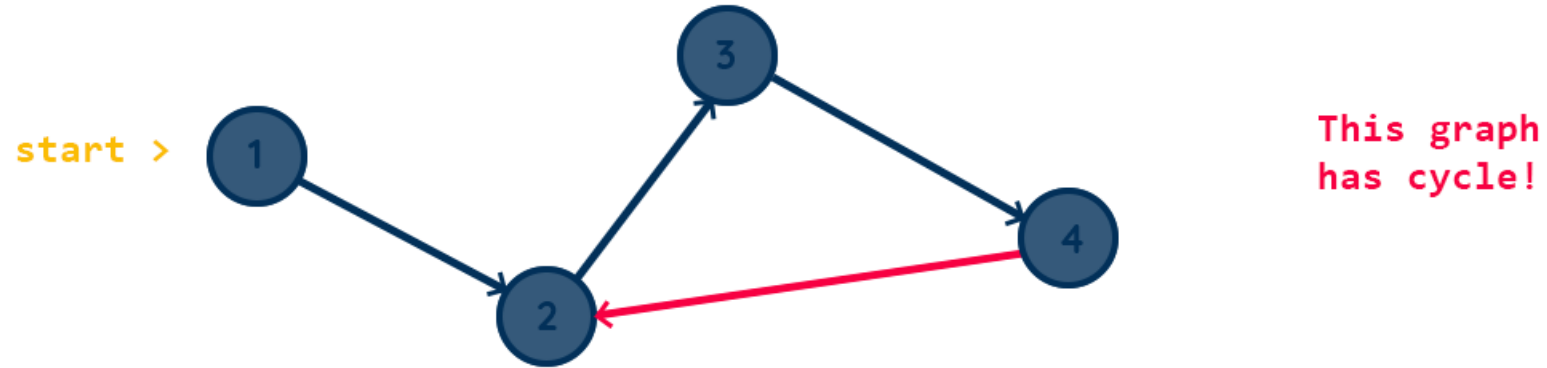


color[] =

2	2	2	2
1	2	3	4

0 = WHITE
1 = GRAY
2 = BLACK

Cycle Finding

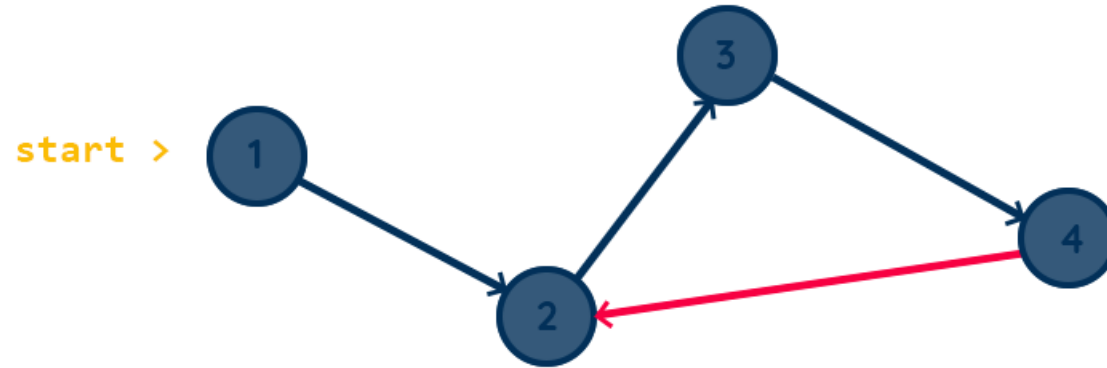


color[] =

2	2	2	2
1	2	3	4

0 = WHITE
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Cycle Finding



This graph
has cycle!

Topological Sorting
is not possible

color[] =

2	2	2	2
1	2	3	4

0 = WHITE
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