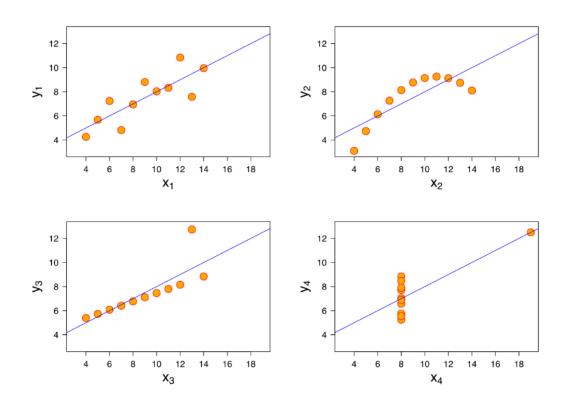
Session Agenda

- Anscombe's Quartet
- Correlation
 - Pearson Product Moment
 - Testing hypotheses
- Simple Linear Regression
 - Basic Facts
 - Example
 - Coding in R
- Model Specification
- Confounding
 - ANOVA
 - Regression
- George E. P. Box Quote
- Review Problems
- Final Exam

Anscombe's Quartet

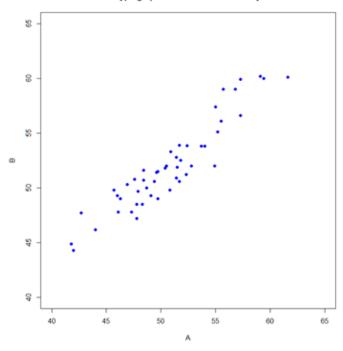
Beware of relying only on simple descriptive statistics!



Property	Value	Accuracy
Mean of x	9	exact
Sample variance of x	11	exact
Mean of y	7.50	to 2 decimal places
Sample variance of y	4.125	plus/minus 0.003
Correlation between x and y	0.816	to 3 decimal places
Linear regression line	y = 3.00 + 0.500x	to 2 and 3 decimal places, respectively
Coefficient of determination of the linear regression	0.67	to 2 decimal places

Testing the Hypothesis of a Zero Correlation

Plot of Typing Speeds for Two Different Keyboards



```
> r <- cor(A,B)

> r

[1] 0.9325682

> n <- length(A)

> T <- r*sqrt((n-2)/(1-r^2))

> T

[1] 17.71045

> qt(0.95, n-2, lower.tail = TRUE)

[1] 1.677927

> pt(T, n-2, lower.tail = FALSE)

[1] 9.863848e-23

> cor.test(A, B, alternative = c("greater"), method = c("pearson"), conf.level = 0.95)
```

Pearson's product-moment correlation

```
data: A and B

t = 17.71, df = 47, p-value < 2.2e-16

alternative hypothesis: true correlation is greater than 0

95 percent confidence interval:
0.8927321 1.00000000

sample estimates:
cor
0.9325682
```

Simple Linear Regression Model

$$y = \beta_0 + \beta_1 x + \varepsilon$$

Where-

y dependent variable,

x independent variable,

 β_0 , β_1 unknown constants

ε random error term.

The method of least squares is used to minimize the sum of squares:

$$S(\beta_0, \beta_1) = \sum_{i=1}^{n} (y_i - \beta_0 - \beta_1 x_i)^2$$

This provides a fitted equation:

$$\hat{y} = b_0 + b_1 x$$

The differences between observed values for y and predicted values are called residuals. Residuals play an important role in diagnosing model adequacy or "model fit".

A basic assumption of simple linear regression is that the random error term has a normal distribution with mean zero and constant variance for all observations. If investigation of the residuals reveals this is not true, the model must be changed.

Simple Linear Regression Estimators

Linear regression model estimators can be expressed in matrix terms. This is what the word "linear" denotes.

Differentiate the sum of squares for each parameter.

$$\frac{dS}{d\beta_0} = -2\left[\sum y_i - \beta_0 n - \beta_1 \sum x_i\right]$$

$$\frac{dS}{d\beta_1} = -2\left[\sum x_i y_i - \beta_0 \sum x_i - \beta_1 \sum x_i^2\right]$$

Set equal to zero and form the Normal Equations:

$$\overline{y} = b_0 + b_1 \overline{x}$$

$$\sum x_i y_i / n = b_0 \overline{x} + b_1 \sum x_i^2 / n$$

Express in matrix algebra:

$$\begin{pmatrix} 1 & \overline{x} \\ \overline{x} & \sum x_i^2 / n \end{pmatrix} \begin{pmatrix} b_0 \\ b_1 \end{pmatrix} = \begin{pmatrix} \overline{y} \\ \sum x_i y_i / n \end{pmatrix}$$

Inverting and solving gives the estimators:

$$\begin{pmatrix} b_0 \\ b_1 \end{pmatrix} = \begin{pmatrix} \frac{1}{(\sum x_i^2 / n) - \overline{x}^2} \end{pmatrix} \begin{pmatrix} \sum x_i^2 / n & -\overline{x} \\ -\overline{x} & 1 \end{pmatrix} \begin{pmatrix} \overline{y} \\ \sum x_i y_i / n \end{pmatrix}$$

Some Results

Fundamental Identity—

$$\sum (y - \bar{y})^2 = \sum (\hat{y} - \bar{y})^2 + \sum (y - \hat{y})^2.$$

This states that the total variation about the mean of y equals the total variation of the predicted values of y about the mean of y plus the total variation of the residuals.

Coefficient of Determination—

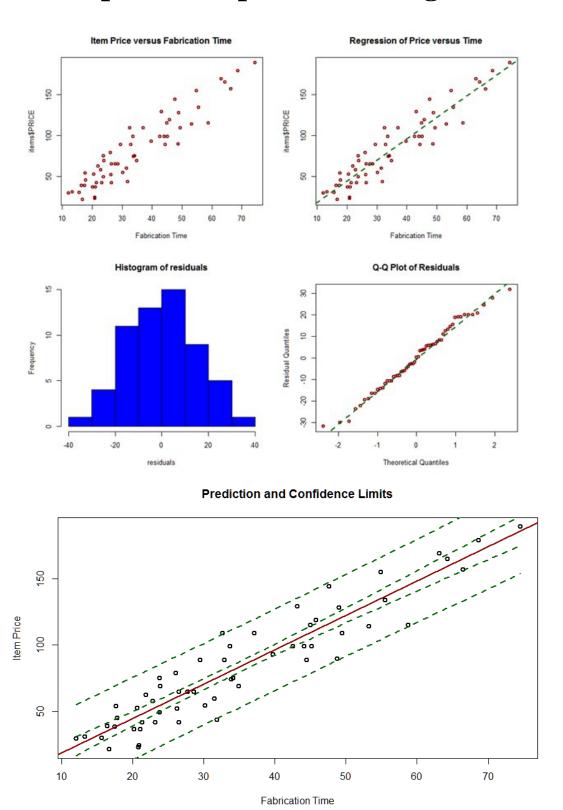
$$r^2 = \frac{\text{explained var intion}}{\text{total var intion}} = \frac{\sum (\hat{y} - \overline{y})^2}{\sum (y - \overline{y})^2}$$

For a simple linear regression model, r^2 is the square of the Pearson Product Moment Correlation Coefficient. For a multiple linear regression model, the coefficient of multiple determination R^2 represents the proportion of variation of the dependent variable accounted for by the independent variables.

Variance of the Random Error Term—

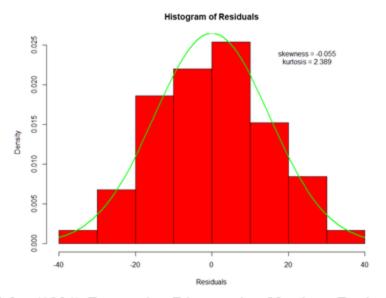
$$\hat{\sigma}^2 = \frac{\sum_{i=1}^n e_i^2}{n-2} = \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n-2}$$

Example of Simple Linear Regression



Linear Regression Example

```
> items <- read.csv(file.path("c:/R401/","pricing.csv"), sep=",")
> require(moments)
> object <-lm(PRICE~TIME, items)
> summary(object)
         Call:
         lm(formula = PRICE \sim TIME, data = items)
          Coefficients:
          Estimate Std. Error t value Pr(>|t|)
          (Intercept) -7.4467 4.8957
                                             -1.521
                                                        0.134
                                            20.154 <2e-16 ***
          TIME
                     2.5942
                                  0.1287
          Residual standard error: 15.19 on 57 degrees of freedom
          Multiple R-squared: 0.8769,
                                                 Adjusted R-squared: 0.8748
         F-statistic: 406.2 on 1 and 57 DF, p-value: < 2.2e-16
> cbind(object$coefficients, confint(object, parm=c(1,2), level= 0.95))
                                     2.5 % 97.5 %
          (Intercept) -7.44667
                                  -17.2502 2.3568
          TIME
                      2.5942
                                    2.3365 2.8520
> x \le seq(from = -40, to = 40, by = 1)
> hist(residuals, col = "red", freq = FALSE, xlab = "Residuals",
    main = "Histogram of Residuals", xlim = c(-40, 40))
> curve(dnom(x, mean = 0, sd = sd(residuals)), col = "green", lwd = 2, add = TRUE)
> text(x = 25, y = 0.024, paste("skewness = ", round(skewness(residuals), digits = 3)))
> text(x = 25, y = 0.023, paste("kurtosis = ", round(kurtosis(residuals), digits = 3)))
```



Fox, John (1991) Regression Diagnostics, Newbury Park, CA: Sage

Bootstrap Applications

```
># Percentile Bootstrap Example
> set.seed(123)
> alpha.boot <- numeric(0)
> beta.boot <- numeric(0)
> for (k in 1:1000) {
+ x <- sample.int(59, size = 59, replace = TRUE)
+ result <- lm(PRICE[x]~TIME[x], items)</p>
+ alpha.boot[k] <- coef(result)[1]
+ beta.boot[k] <- coef(result)[2]
+}
> alpha.coef <- quantile(alpha.boot, c(0.025,0.975))
> beta.coef <- quantile(beta.boot, c(0.025,0.975))
> c(mean(alpha.boot), mean(beta.boot))
        [1] -7.458544 2.593657
> boot.results <-cbind(original,(rbind(alpha.coef, beta.coef)))
> row.names(boot.results) <- c("(Intercept)", "TIME")
> boot.results
                          original
                                              2.5%
                                                           97.5%
        (Intercept) -7.446681 -15.320614 0.6434946
                          2.594250 2.354175 2.8200267
> # Bootstrap Using boot() and the bias-corrected and accelerated method
> bs <- function(formula, data, indices){
+ d <- data[indices,]</p>
+ fit <- lm(formula, data =d)</p>
+ return(coef(fit))
> library(boot)
> set.seed(123)
> results <- boot(data = items, statistic=bs, R=1000, formula=PRICE~TIME)
> bca.intercept <- boot.ci(boot.out=results, type = "bca", index = 1)
> bca.slope <- boot.ci(boot.out=results, type="bca", index = 2)
> bca.coef<-c(bca.intercept[2],bca.slope[2])
> bca.alpha <- c(bca.intercept$bca[4:5])
> bca.beta <- c(bca.slope$bca[4:5])
> comb.bca <-rbind(bca.intercept$bca[4:5], bca.slope$bca[4:5])
> colnames(comb.bca) <- c("2.5%", "97.5%")
> bca.estimates <- cbind(bca.coef, comb.bca)
> rownames(bca.estimates) <- c("(Intercept)", "TIME")
> bca.estimates
                            bca. coef
                                              2.5%
                                                             97.5%
          (Intercept) -7.446681 -15.745730
                                                          0.2645653
                            2.594250 2.346807
                                                          2.8087530
```

The bias-corrected and accelerated method is recommended for general use by Bradley Efron and Robert J. Tibshirani in "An Introduction to the Bootstrap" (CRC Press) Chapter 14 page 188.

Model Specification in Regression Analysis

Multiple linear regression relates a dependent variable to one or more independent variables.

Stages of regression analysis:

- 1. exploratory data analysis,
- 2. model specification,
- 3. estimation of the parameters of the model,
- 4. diagnostic checking and validation,
- 5. interpretation of the parameters.

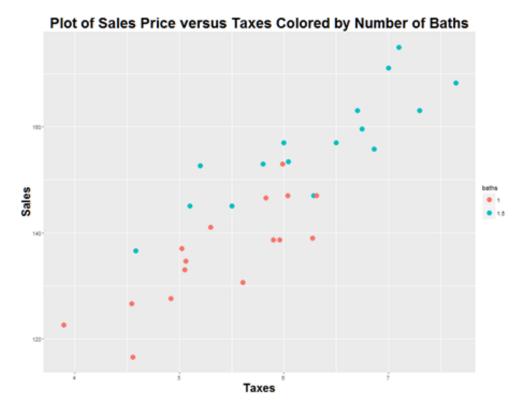
EDA, theoretical considerations and prior experience contribute to model specification.

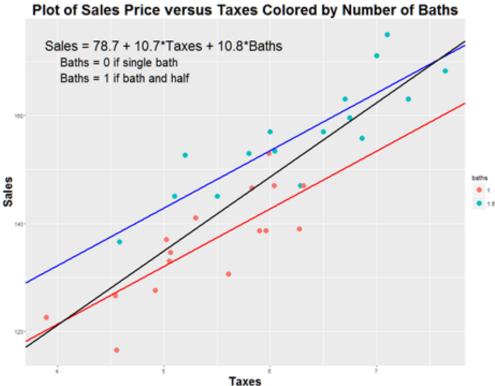
Model Specification Questions:

- Are the right independent variables included in the model?
- Are unnecessary variables excluded from the model?
- Are the variables expressed in proper functional form?

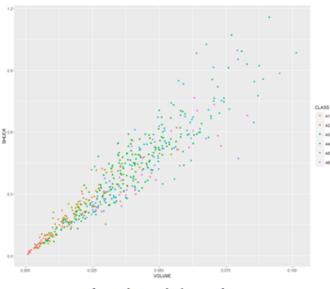
Specification errors can lead to problems of estimation, interpretation and erroneous prediction.

Model Specification and Dummy Variables

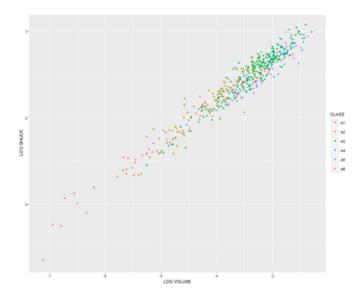




Transformations



 $Shuck \cong k * Volume$



 $\log(Shuck) \cong c + m * \log(Volume)$

http://kenbenoit.net/assets/courses/ME104/logmodels2.pdf

Abalone Regression Analysis

> model <- lm(L SHUCK ~ L VOLUME + CLASS + TYPE, data = mydata) > summary(model)

Call:

 $lm(formula = L SHUCK \sim L VOLUME + CLASS + TYPE, data = mydata)$

Residuals:

1Q Median Min 3Q -0.270634 -0.054287 0.000159 0.055986 0.309718

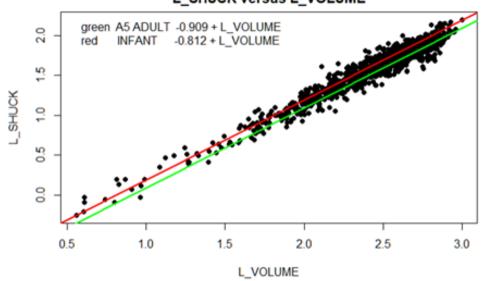
Coefficients:

Estimate Std. Error t value Pr(>|t|) (Intercept) -0.817512 0.019040 -42.936 < 2e-16 *** L VOLUME 0.999303 0.010262 97.377 < 2e-16 *** CLASSA2 -0.018005 0.011005 -1.636 0.102124 CLASSA3 -0.047310 0.012474 -3.793 0.000158 *** CLASSA4 -0.075782 0.014056 -5.391 8.67e-08 *** CLASSA5 -0.117119 0.014131 -8.288 3.56e-16 *** TYPEADULT 0.021093 0.007688 2.744 0.006180 ** Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1

Residual standard error: 0.08297 on 1029 degrees of freedom Multiple R-squared: 0.9504, Adjusted R-squared: 0.9501

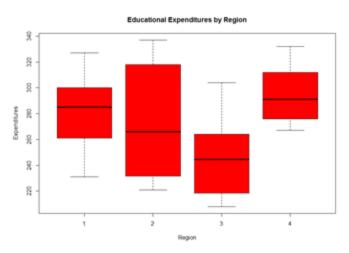
F-statistic: 3287 on 6 and 1029 DF, p-value: < 2.2e-16





Model Specification

Annual educational expenditure data are collected each of the fifty states. The states are grouped according to geographic region. It is of interest to find if regional differences can be detected. The initial analysis is a one-way ANOVA of Y = Per capita expenditure on education versus region (1, 2, 3, 4).



```
> result <- aov(Y~region, data=schools)
> summary(result)
            Df Sum Sq Mean Sq F value Pr(>F)
                         5823
                                5.454 0.00271 **
             3 17469
region
Residuals
            46 49111
                         1068
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> aggregate(Y~region, data = schools, mean)
  region
1
       1 280.6667
2
       2 273.8333
3
       3 246.8125
       4 294.5385
> TukeyHSD(result)
 Tukey multiple comparisons of means
    95% family-wise confidence level
Fit: aov(formula = Y ~ region, data = schools)
$region
          diff
                     lwr
                               upr
2-1 -6.833333 -45.23834 31.571669 0.9643719
3-1 -33.854167 -70.14348 2.435150 0.0754499
4-1 13.871795 -23.89485 51.638443 0.7619900
3-2 -27.020833 -60.28054 6.238875 0.1482733
4-2 20.705128 -14.16052 55.570776 0.3982160
4-3 47.725962 15.20545 80.246473 0.0016539
```

Model Development

Now consider the analysis if covariates are included in a multiple linear regression analysis. They are:

```
X1 = Per capita income
```

X2 = Number of residents per thousand under 18 years of age

X3 = Number of residents per thousand living in urban areas

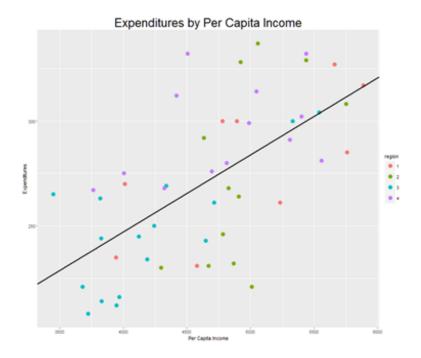
Revised analysis includes both continuous and categorical predictors.

```
> rs <- lm(Y~X1+X2+X3+region, data=schools)</pre>
> summary(rs)
Call:
lm(formula = Y \sim X1 + X2 + X3 + region, data = schools)
Residuals:
   Min
            10 Median
                            3Q
                                  Max
-58.324 -18.336 -2.848
                        19.900
                                66.752
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -44.48314 112.25760 -0.396 0.69387
                        0.01071 3.285 0.00203 **
X1
             0.03518
X2
             0.43372
                        0.27782
                                 1.561 0.12582
             0.02158
                        0.04000 0.539 0.59243
X3
region2
            -9.26738
                       12.50284 -0.741 0.46259
           -11.07212 12.50480 -0.885 0.38085
region3
region4
           10.30383 13.04614 0.790 0.43398
               0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
Residual standard error: 26.91 on 43 degrees of freedom
Multiple R-squared: 0.5324,
                              Adjusted R-squared:
F-statistic: 8.161 on 6 and 43 DF, p-value: 6.463e-06
```

Region is no longer a predictive factor. X1 emerges.

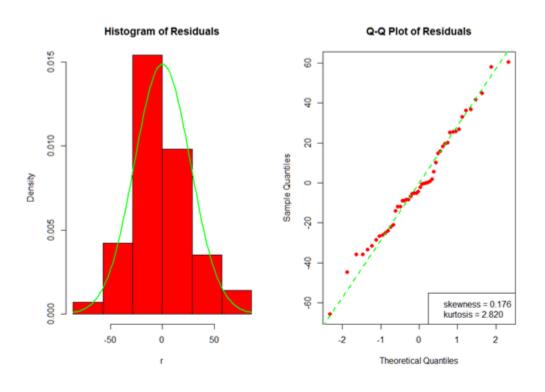
Subsequent Analysis

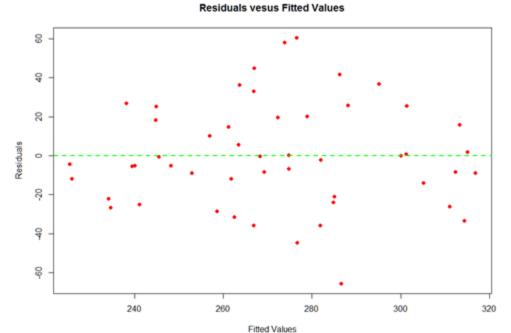
```
> rs <- lm(Y~X1, data=schools)</pre>
> summary(rs)
Call:
lm(formula = Y \sim X1, data = schools)
Residuals:
   Min
            1Q Median
                             3Q
                                   Max
-63.340 -25.969 0.338 22.230 66.333
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.001e+02 3.026e+01 3.309 0.00178 **
            3.676e-02 6.419e-03 5.726 6.55e-07 ***
               0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
Residual standard error: 28.71 on 48 degrees of freedom
Multiple R-squared: 0.4059, Adjusted R-squared: 0.3935
F-statistic: 32.79 on 1 and 48 DF, p-value: 6.552e-07
```

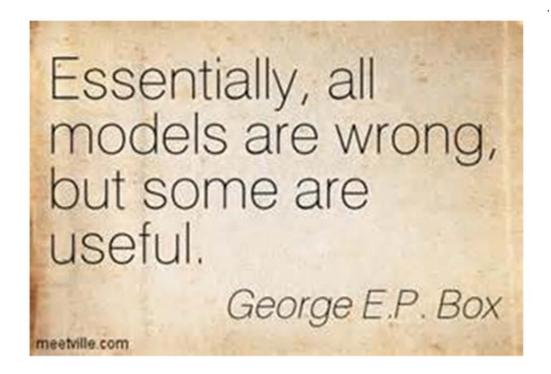


Subsequent regression analysis on X1, X2 and X3 indicates X1 and X2 should be retained as predictors in a multiple linear regression model.

Model Diagnostics (X1 and X2 predictors)







George Edward Pelham Box FRS

(18 October 1919 – 28 March 2013) was a statistician, who worked in the areas of quality control, time-series analysis, design of experiments, and Bayesian inference. He has been called "one of the great statistical minds of the 20th century".

- Statistics, as a science, is not algorithmic or deterministic. Data are rarely perfect. Judgment is necessary in the application of statistical methods to arrive at valid, useful conclusions.
- A model for data must be discarded or revised if it does not adequately fit the data and is misleading. This may lead to insights and progress.
- When faced with judgment calls, make the choice that best facilitates understanding the world as it is. It is fine to consider alternative models in the process of drawing conclusions.

Selected Review Problems

Use Bayes' Theorem to find the indicated probability with the following table.

	Approve of mayor	Do not approve of mayor
Republican	8	17
Democrat	18	13
Independent	7	37

One of the 100 test subjects is selected at random. Given that the person selected approves of the mayor, what is the probability they vote Democrat?

$$\frac{18/100}{(18/31)(31/100) + (8/25)(25/100) + (7/44)(44/100)} = 18/33 = 0.545$$

Suppose there are three married couples: A, B and C: couple A, both partners approve of the mayor, couple B, both partners no not approve of the mayor, and couple C, one partner approves of the mayor and the other partner does not approve of the mayor.

Pick one couple at random and partner at random. If the selected partner does not approve of the mayor, what is the probability the other partner approves of the mayor?

Solution by enumeration: Couple A is out of consideration. Only couples B and C could result in the initial selection mentioned. However only couple C has an unselected partner who approves of the mayor. Thus, based on the stated sampling condition, there are three ways the first partner could be picked. Couple B partner 1, Couple B partner 2 or Couple C partner 1 (partner 2 has the opposite opinion). Thus the conditional probability is 1 out of 3 possibilities or 1/3.

By Bayes theorem: (1/2)(1/3) / (0(1/3) + 1(1/3) + (1/2)(1/3)) = (1/2) / (1 + 1/2) = 1/3.

Solve the problem.

- 6) True or False: In a hypothesis test, an increase in a will cause a decrease in the power of the test provided the sample size is kept fixed.
 A) True
 B) False
- 3,132
- 7) True or False: In a hypothesis test regarding a population mean, the probability of a type II error, β, depends on the true value of the population mean.
 - A) False B) True
- (6) is False and (7) is true.

The systolic blood pressures of the patients at a hospital are normally distributed with a mean of 138 mm Hg and a standard deviation of 13.5 mm Hg. Find the two blood pressures having these properties: The mean is midway between them and 90% of all blood pressures are between them.

We are looking for an interval that is symmetric with the mean in the middle. To have 90% of the blood pressures between them, 95% of the readings must be to the left of the upper bound, and 5% to the left of the lower bound.

```
> gnorm(0.95, 138, 13.5, lower.tail = TRUE)
[1] 160.2055
> gnorm(0.05, 138, 13.5, lower.tail = TRUE)
[1] 115.7945
```

Construct the indicated confidence interval for the difference between population proportions $p_1 - p_2$. Assume that the samples are independent and that they have been randomly selected.

```
x_1 = 15, n_1 = 50 and x_2 = 23, n_2 = 60; Construct a 90% confidence interval for the difference between population proportions p_1 - p_2.
```

```
A) -0.232 < p<sub>1</sub> - p<sub>2</sub> < 0.065 B) 0.477 < p<sub>1</sub> - p<sub>2</sub> < 0.122 C) 0.123 < p<sub>1</sub> - p<sub>2</sub> < 0.477 D) 0.151 < p<sub>1</sub> - p<sub>2</sub> < 0.449
```

```
> x <- c(15, 35)

> y <- g(23, 37)

> M <- rbind(x,y)

> prop_test(M, alternative = c("two_sided"), conf_level = 0.90, correct = FALSE)
```

2-sample test for equality of proportions without continuity correction

```
data: M
X-squared = 0.8376, df = 1, p-value = 0.3601
alternative hypothesis: two sided
90 percent confidence interval:
-0.23173354, 0.06506688
sample estimates:
grop 1 prop 2
0.3000000 0.3833333
```

A researcher was interested in comparing the amount of time spent watching television by women and by men. Independent simple random samples of 14 women and 17 men were se lected, and each person was asked how many hours he or she had watched television during the previous week. Assume the population variances are equal so that the sample variances can be pooled.

	Women	Men
Sample average	11.4 hr	16.8 hr
Standard deviation	4.1 hr	4.7 hc
Sample size	14	17

Use a 0.05 significance level to test the claim that the mean amount of time spent watching television by women is smaller than the mean amount of time spent watching television by men. Use the tradition method of hypothesis testing.

For this problem, a one-sided test is required. The alternative will be framed as a positive.

```
> s1.2 <- 4.1\(\text{1\text{1}}\)2

> s2.2 <- 4.7\(\text{2}\)2

> n1 <- 14

> n2 <- 17

> pool <- sqrt((s1.2\(\text{n1}\)-1)+s2.2\(\text{n2}\)-1))/(n1+n2-2))

> den <- pool\(\text{sqrt}(1/n1+1/n2)\)

> x1 <- 11.4

> x2 <- 16.8

> t <- (x2-x1)/den

> t

[1] 3.369099

> pt(t,29,lower.tail=FALSE)

[1] 0.001073162

> qt(0.95,29,lower.tail=TRUE)

[1] 1.699127
```

Use the given data to find the equation of the regression line. Round the final values to three significant digits, if necessary.

```
15) \frac{x \mid 6 \mid 8 \mid 20 \mid 28 \mid 36}{y \mid 2 \mid 4 \mid 13 \mid 20 \mid 30}

A) y = -2.79 + 0.897x

B) y = -2.79 + 0.950x

C) y = -3.79 + 0.801x

D) y = -3.79 + 0.897x

> x < -c(6, 8, 20, 28, 36)

> y < -c(2, 4, 13, 20, 30)

> lm(y = x)

Call: lm(formula = y \sim x)

Coefficients: (Intercept) x
```

-3, 7900

0.8975

16) For the data below, determine the value of the linear correlation coefficient r between y and x^2 .

```
> x <- c(1.2, 2.7, 4.4, 6.6, 9.5)
> y <- c(1.6, 4.7, 9.9, 24.5, 39.0)
> x <- x^2
> cor(x, y, method = c("pearson"))
[1] 0.9902759
```

18) In studying the occurrence of genetic characteristics, the following sample data were obtained. At the 0.05 significance level, test the claim that the characteristics occur with the same frequency.

This is a Chi-square goodness-of-fit test. The counts are expected to be equal under the null hypothesis. This expectation is 38 which needed to be compared against the observed counts.

```
> obs <- c(28, 30, 45, 48, 38, 39)
> ec <- rep(sum(obs)/6, times = 6)
> diff <- sum((obs - ec)^2/ec)
> diff
[1] 8.263158
> pchisq(diff, df = 5, lower.tail = FALSE)
[1] 0.1423164
> qchisq(0.95, df = 5, lower.tail = TRUE)
[1] 11.0705
```

20) Fill in the missing entries in the following partially completed one-way ANOVA table.

Source	df	SS	MS=SS/df	F-statistic
Treatment	3			11.16
Error		13.72	0.686	
Total				

Error degrees of freedom = 13.72/0.686 = 20. Total degrees of freedom = 3 + 20 = 23

Treatment MS =
$$11.16(.686) = 7.656$$
. Treatment SS = $7.656(3) = 22.97$

Total SS =
$$13.72 + 22.97 = 36.69$$

Some Sync Session Learning Points

- Essentially all models are wrong, but some are useful.
- It is perfectly proper to use both classical and robust methods routinely and only worry when they differ enough to matter.
- The Pearson Correlation Coefficient is intended to measure the association between two normally distributed random variables.
- Simple linear regression involves estimating two parameters in the equation and the variance of the error term.
- In simple linear regression, r² equals the square of the Pearson Correlation Coefficient.
- r² is the ratio of explained variation to total variation.
- Linear regression requires the normal equations to be amenable to linear algebra. It must be possible to isolate the coefficients.
- Multiple linear regression is not limited to straight line relationships. Polynomials may qualify.
- Model specification involves answering three questions:
 - o Are the right variables included?
 - o Are unnecessary variables excluded?
 - Are the variables in proper functional form?

Final Exam Topics

- Probability
 - Calculations using probability
 - Bayes' Theorem
 - Means and variances for probability distributions
- Hypothesis Testing
 - Type I and Type II Errors
 - Correlation
 - t tests
 - one sample
 - two sample
- Confidence Interval Construction
- One-way AOV
 - F test
 - o p-values
- Linear Regression

The test is two hours, proctored, with open book and open notes. There are ten multiple choice or true/false questions. No preview of the exam is available. Review questions are available in module ten. Excel, R or any comparable calculator application may be used. The course site, WileyPlus, electronic files, hardcopy and e-readers for kindles may be used. Cloud storage of files is allowed.

Only one computer screen is allowed. Portable devices such as kindles and iPads are not allowed unless special arrangements are made. No navigation from the testing site to the internet for browsing is allowed.

Examity Specifications

Standard Rules	
Alone in room	
Clear Desk and Area	
Connected to a powersource	
No phones or headphones	
No dual monitors	
No leaving seat	
No talking	
Webcam, speakers, and microphone must remain on throughout the test.	
The proctor must be able to see you for the duration of the test.	
Additional Rules	
Handheld calculator	
Scrap paper	
Open book	
Drink on desk	
Online Calculator	

Special Instructions	
No browsing of the internet is allowed.	0
No separate portable devices such as Kindles or iPads, which provide internet access, are permitted during the exam. Other than the above, this is an open resource exam.	0
All resources located on the test taker's personal computer are permitted. Students may access any printed materials, text books, printed notes, personal computer files and the Canvas course site which includes use of WileyPlus. Documents can be in any format such as .pdf, .docx or .html.	0
Use of eBook readers is permitted during the exam provided the reader is resident on the student's personal computer.	0
This exam requires computation. MS Excel, R, RStudio or any calculator application which does not require internet access is permitted. Handheld calculators, such as a TI 84, Casio or comparable, are also acceptable.	0

Examity has been instructed that this is an open book exam meaning "open resource". All resources located on the test taker's personal computer, external file storage as with the cloud, and printed materials are permitted.

Final Exam and Proctoring

