

Programming for Simulation and MC Methods

Random Variable Generation

Inverse Transform



The Inverse Transform

There is a simple, sometimes useful transformation, known as the *probability* integral transform, that allows us to transform any random variable into a uniform random variable and, more importantly, vice versa. For example, if X has density f and cdf F, then we have the relation

$$F(x) = \int_{-\infty}^{x} f(t) \, \mathrm{d}t,$$

and if we set U = F(X), then U is a random variable distributed from a uniform $\mathcal{U}(0,1)$. This is because

$$P(U \le u) = P[F(X) \le F(x)] = P[F^{-1}(F(X)) \le F^{-1}(F(x))] = P(X \le x),$$

Accept-Reject Method



Accept-Reject Method

Algorithm 1 Accept—Reject Method

- 1. Generate $Y \sim g$, $U \sim \mathcal{U}_{[0,1]}$;
- 2. Accept X = Y if $U \leq f(Y)/Mg(Y)$;
- 3. Return to 1 otherwise.