NUMERICAL INTEGRATION EXERCISE

1. The standard normal distribution function is given by:

$$\Phi(z) = \int_{-\infty}^{z} \frac{1}{\sqrt{2\pi}} e^{-x^{2}/2} dx.$$

For probability p within the set of [0,1], the 100p standard normal percentage point is defined as that z_p for which:

$$\Phi(z_p) = p.$$

Using the functions **phi** (**x**) and **Phi** (**z**) in chapter 11 (repeated below), calculate z_p for p = 0.05, 0.95, 0.975, and 0.99. **Hint:** Express the problem as a root-finding problem. That is, use one of the root-finding methods (programs) from chapter 10 and utilize **phi** (**x**) and **Phi** (**z**) as elements in the arguments to that root-finding program from chapter 10.

```
# HERE IS phi(x):
phi <- function(x) return(exp(-x^2/2)/sqrt(2*pi))
# HERE IS Phi(z):
Phi <- function(z) {
   if (z < 0) {
      return(0.5 - simpson_n(phi, z, 0))
   } else {
      return(0.5 + simpson_n(phi, 0, z))
   }
}</pre>
```