

Sorting Customer Orders

- Sorting Algorithms:

Bubble Sort:

- Description: Repeatedly steps through the list, compares adjacent elements, and swaps them if they are in the wrong order. This process is repeated until the list is sorted.
- Time Complexity:

Best Case: $O(n)$ (when the list is already sorted)

Average Case: $O(n^2)$

Worst Case: $O(n^2)$

Insertion Sort:

Description: Builds the sorted array one element at a time by repeatedly picking the next element and inserting it into the correct position in the already sorted part.

- Time Complexity:

Best Case: $O(n)$ (when the list is already sorted)

Average Case: $O(n^2)$

Worst Case: $O(n^2)$

Quick Sort:

- Description: Selects a 'pivot' element and partitions the array into two sub-arrays, according to whether they are less than or greater than the pivot. The sub-arrays are then sorted recursively.

- Time Complexity:

Best Case: $O(n \log n)$

Average Case: $O(n \log n)$

Worst Case: $O(n^2)$ (when the smallest or largest element is always chosen as the pivot)

Merge Sort:

- Description: Divides the array into halves, recursively sorts them, and then merges the sorted halves to produce the final sorted array.
- Time Complexity:
 - Best Case: $O(n \log n)$
 - Average Case: $O(n \log n)$
 - Worst Case: $O(n \log n)$
- Time Complexity Comparison:

Bubble Sort:

- Best Case: $O(n)$
- Average Case: $O(n^2)$
- Worst Case: $O(n^2)$

Quick Sort:

- Best Case: $O(n \log n)$
 - Average Case: $O(n \log n)$
 - Worst Case: $O(n^2)$
- Why Quick Sort is Generally Preferred Over Bubble Sort:

Efficiency: Quick Sort is significantly more efficient on average than Bubble Sort due to its $O(n \log n)$ average time complexity compared to $O(n^2)$ for Bubble Sort.

Performance: Quick Sort performs well on large datasets and is typically faster in practice due to fewer comparisons and swaps.

Divide and Conquer: Quick Sort uses a divide-and-conquer approach, which is more scalable and adaptable to various types of data.

Memory Usage: Quick Sort is an in-place sorting algorithm, meaning it requires a small amount of additional memory space compared to other sorting algorithms like Merge Sort.