

I_m could be lagging power factor, however I_{inv} is of leading power

✓ 500hp, 4 pole, 415V motor (L-L), 50Hz squirrel cage IM $\rightarrow S_{rated} = 0.03$ and

$$S_{max} = 0.12 \quad \bar{V}_p = 239.6 \angle 0^\circ$$

$$\bar{I}_m = 535A \quad \bar{I}_m = 535 \angle 14^\circ \checkmark$$

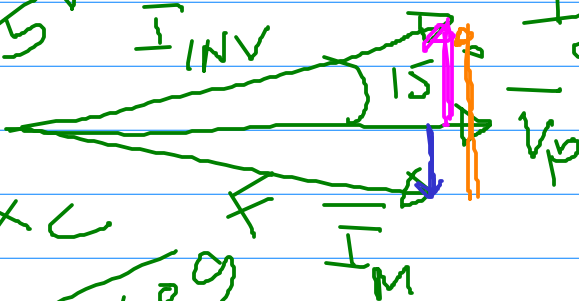
$$\bar{I}_{INV} = ? \angle +15^\circ \checkmark$$

$$535 \cos 14^\circ = I_{INV} \cos 15^\circ \checkmark$$

$$I_{INV} = 537.42A \checkmark$$

$$I_c = 535 \sin 14^\circ + 537.42 \sin 15^\circ$$

$$= 268.52A$$



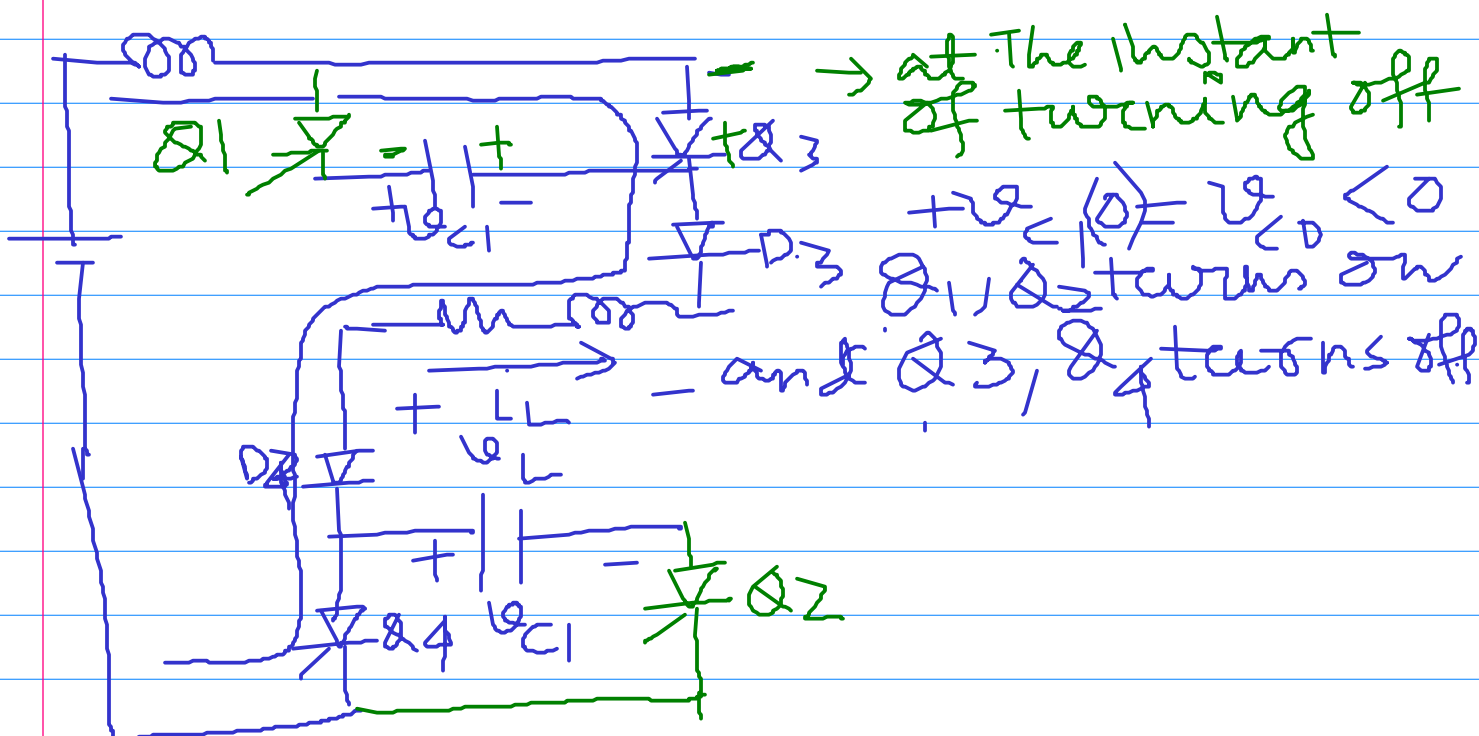
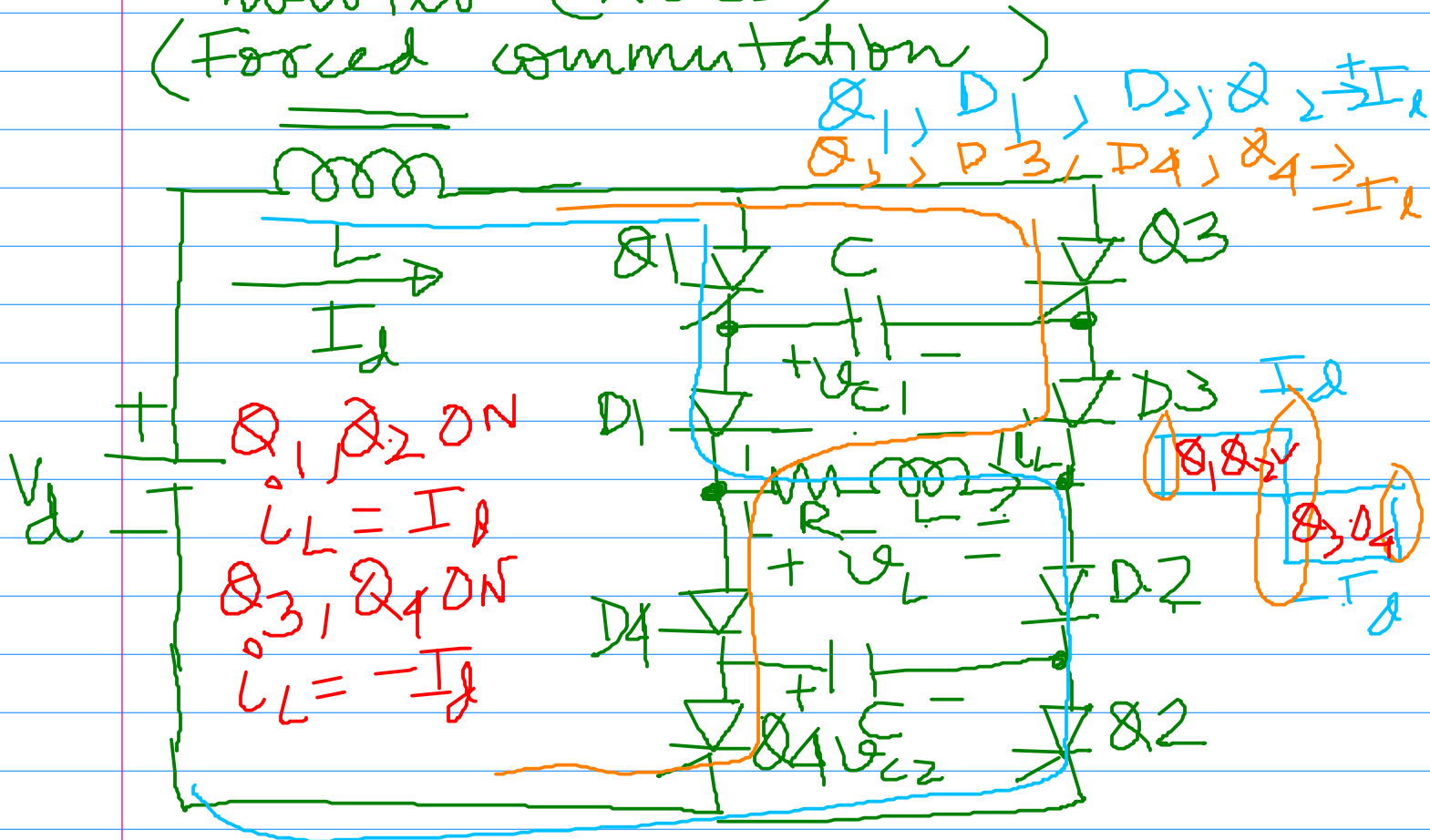
$$\frac{1}{\omega C} = X_C \quad \bar{V}_p = 239.6 \Rightarrow X_C = \frac{239.6}{268.52} = 0.9 \Omega$$

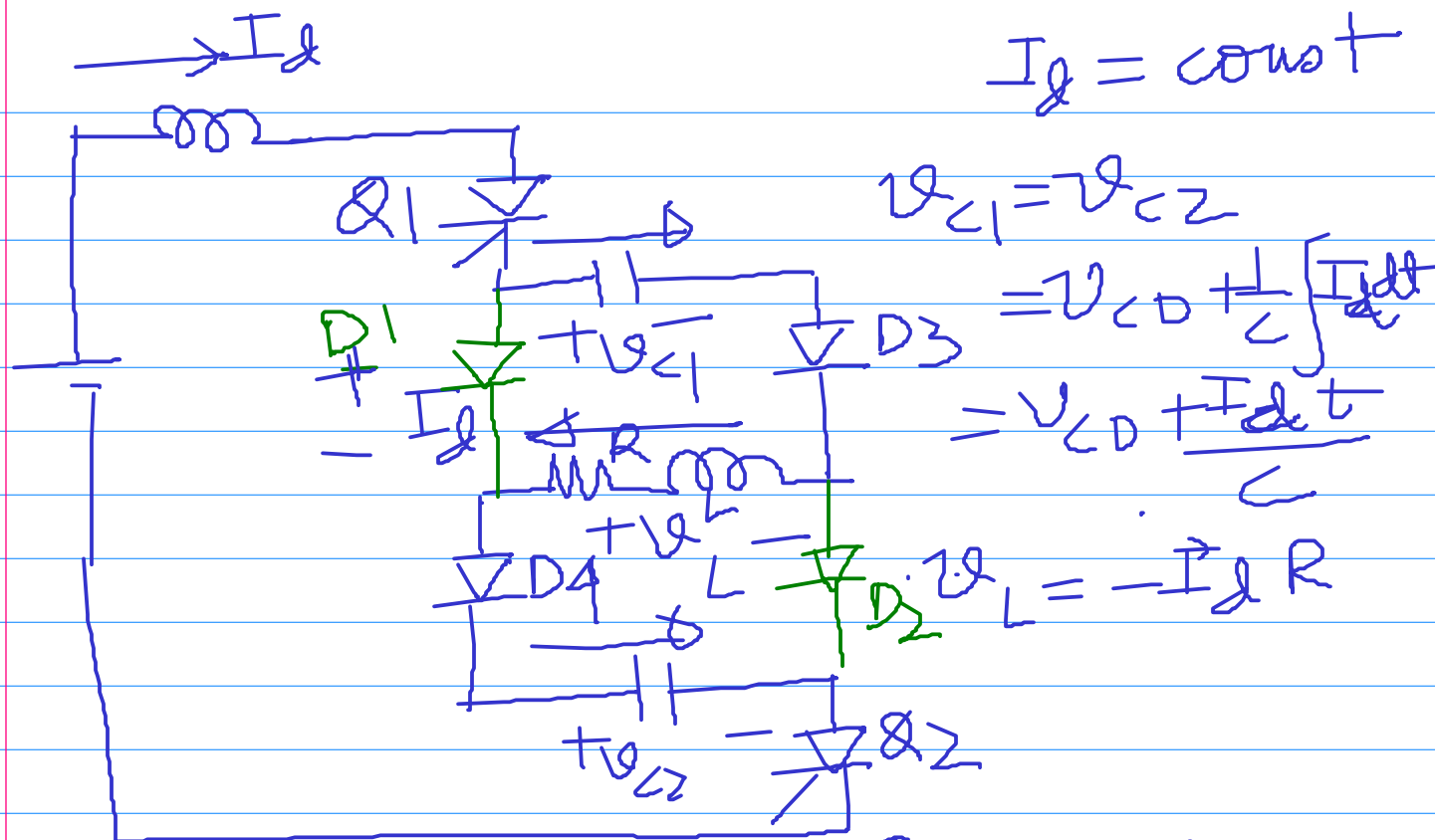
$$X_{CA} = 3 \times 0.9 = 2.7 \Omega$$

$$C_A = \frac{1}{\omega X_{CA}} = \frac{1}{2\pi \times 50 \times 2.7} = 353 \mu F$$

$$C_F = \frac{1}{\omega X_C} = \frac{1}{2\pi \times 50 \times 0.9} = 353 \mu F$$

Auto-sequential-commutated Inverter (ASCI) (Forced commutation)





Let's say this mode ends at $t = t_1$ when D_1, D_2 becomes forward biased

$0 = V_{c0} + \frac{I_d t_1}{C} + I_d R$

$$\overbrace{\quad \quad \quad}^{V_c}$$

$$V_c = -I_d R \text{ at } t = t_1$$

$$-V_{c0} = V_c(t=0)$$

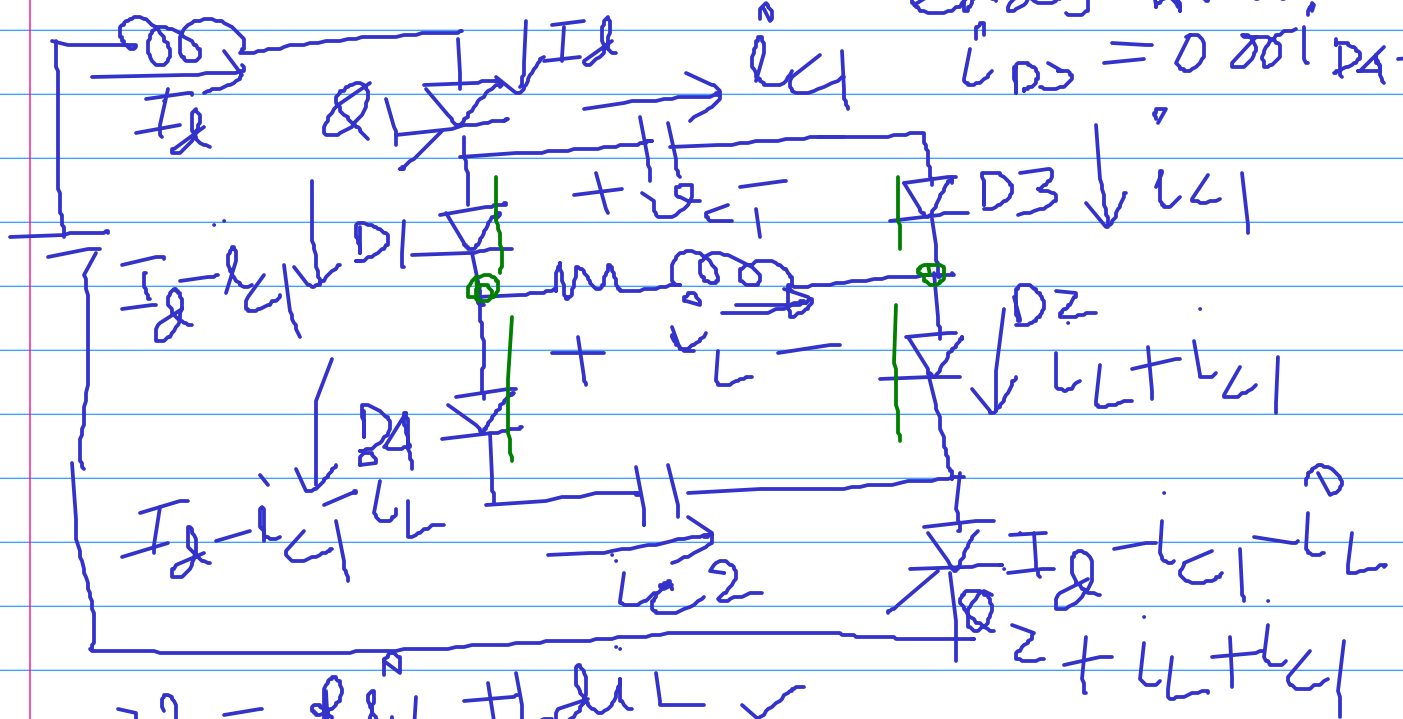
$$-I_d R = V_c(t = t_1)$$

$$C \frac{dV_c}{dt} = i_c \quad \frac{C \times [-I_d R + V_{c0}]}{t_1} = -I_d$$

Let's assume V_{c0} is known

$$t_1 = \frac{20 \times 10^{-6} \times [-256 + 3286]}{594} = 51 \mu\text{sec}$$

This mode ends when $i_{D3} = 0$ or $i_{D4} = 0$



$$v_L = v_C = R_L i_L + L \frac{di_L}{dt}$$

$$\frac{di_L}{dt} = \frac{v_C - R_L i_L}{L} = I_d - i_{L1} - i_L$$

$$v_{C1} = v_{C2}$$

$$i_{L2} + i_L = I_d - i_{L1}$$

$$C \frac{dv_{C1}}{dt} + C \frac{dv_{C2}}{dt} = I_d - i_L$$

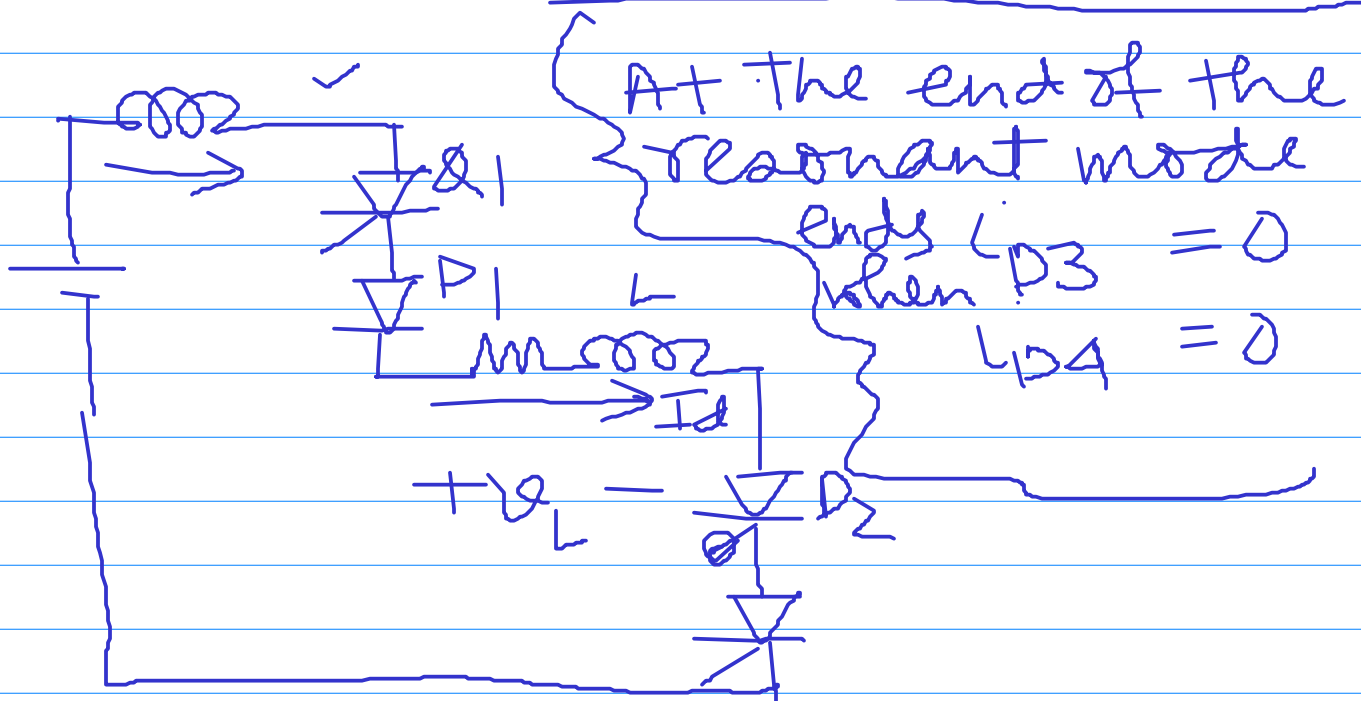
$$2C \frac{dv_C}{dt} = I_d - i_L$$

$$2C \frac{d^2 v_C}{dt^2} = \frac{di_L}{dt} = \frac{I_d - v_C - R_L i_L}{L}$$

$$\begin{aligned}
 2LC \frac{d^2 v_L}{dt^2} + v_L &= R \hat{i}_L \\
 &= R (I_d - 2\hat{i}_L) \\
 &= RI_d - 2RC \frac{dv_L}{dt}
 \end{aligned}$$

$$2LC \frac{d^2 v_L}{dt^2} + 2RC \frac{dv_L}{dt} + v_L = RI_d$$

$$v_L(t) = RI_d + e^{-\delta t} (A \sin \omega t + B \cos \omega t)$$



$$2LC \frac{d^2 v_L}{dt^2} + 2RC \frac{dv_L}{dt} + v_L = RI_d$$

$$v_L(0) = -I_d R$$

$$2i_L = I_d - \dot{i}_L$$

$$2 \frac{dv_L}{dt} = I_d - \dot{i}_L$$

$$2 \frac{dv_L}{dt}(0) = I_d - \dot{i}_L(0)$$

$$= 2I_d \rightarrow \dot{i}_L(0) = -I_d$$

$$\frac{dv_L}{dt}(0) = \frac{I_d}{C}$$

$$v_L(t) = I_d R + e^{-\delta t} (A \sin \omega t + B \cos \omega t)$$

$$\delta = \frac{R}{2L} \quad \omega = \sqrt{\omega_0^2 - \delta^2}$$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$

$$v_L(0) = I_d R + B \Rightarrow B = v_L(0) - I_d R$$

$$= -I_d R - I_d R$$

$$= -2I_d R$$

$$\frac{dv_L}{dt} = e^{-\delta t} (-\delta) A \sin \omega t + e^{-\delta t} A \omega \cos \omega t$$

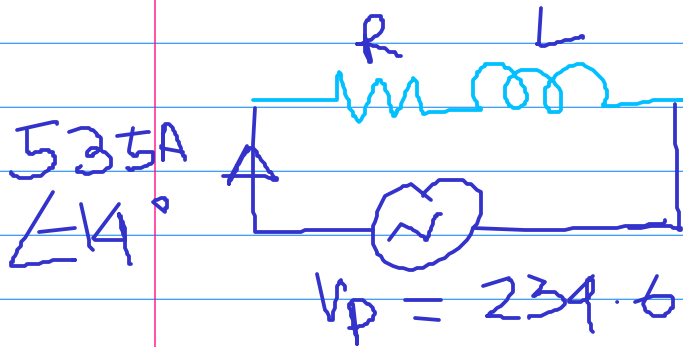
$$+ e^{-\delta t} (-\delta) B \cos \omega t + e^{-\delta t} B \omega (-\sin \omega t)$$

$$\frac{dv_L}{dt}(t=0) = A\omega - B\delta$$

$$A = \frac{I_d}{C} + \frac{(-2I_d R \times \frac{R}{2L})}{\omega}$$

$$A = \frac{I_d}{\omega} \left[\frac{1}{C} - \frac{R^2}{L} \right]$$

Q3, Q4 → outgoing thyristors



$$\frac{4I_d}{\pi} = 535\sqrt{2}$$

$$I_d = 594 \text{ A}$$

$$|Z| = \frac{239.6}{535} = 4478$$

$$\phi = \frac{R}{\omega L}$$

$$= \frac{0.4344}{2 \times 345^\circ} = 628.32$$

$$\frac{\omega L}{R} = \tan 14^\circ$$

$$\omega L = 0.1086 \Omega$$

$$L = \frac{0.1086}{2\pi \times 50}$$

$$= 345.7 \mu\text{H}$$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$

$$C = 10 \mu\text{F}$$

$$= \frac{1}{\sqrt{345.7 \mu\text{H} \times 10 \mu\text{F}}} = 17007.9$$

$$\omega = \sqrt{\omega_0^2 - \phi^2} = 16996$$

$$B = -2I_d R = -2 \times 594 \times 4344 = -516$$

$$A = \frac{I_d}{\omega} - I_d \frac{R^2}{L} = 3475.86$$

$$I_d R = 594 \times 4344 = 258$$

Swing to 2 integral $-628t$

$$V_C(t) = 258 + e^{-628t} (3475 \sin \omega t - 516 \cos \omega t)$$

$$V_C(t_2) = V_{C0}$$

$$i_L(t_2) = I_d$$

$$i_L(t) = I_d - 2C \frac{dV_C}{dt}$$

$$\frac{dV_C(t)}{dt} = e^{-628t} [3475\omega \cos \omega t + 516\omega \sin \omega t] - 628 e^{-628t} [3475 \sin \omega t - 516 \cos \omega t]$$

$$i_L(t) = I_d - 20 \times 10^{-6} e^{-628t} \{ 3475\omega \cos \omega t + 516\omega \sin \omega t + 3475 \times 628 \sin \omega t - 516 \times 628 \cos \omega t \}$$

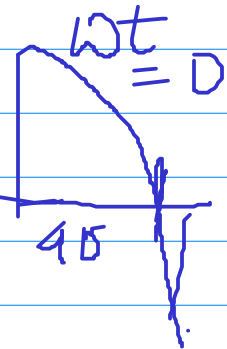
At what value of t_2 , $i_L(t_2) = I_d$

$$i_L(t) = I_d - 20 \times 10^{-6} e^{-628t} \{ 58765 \cos \omega t + 10956 \sin \omega t \}$$

$$\omega t_2 = 120^\circ \Rightarrow \frac{2\pi}{3}$$

$$t_2 = \frac{2\pi}{3 \times 16996} = 123.2 \mu s$$

$$\frac{20 \text{ mSec}}{10 \text{ mSec}} = 123.2 \mu$$



$$v_c(t_2) = 258 + e^{-628 \times 123 \times 10^{-6}} \left\{ 34750 \sin 120^\circ - 516 \cos 120^\circ \right\}$$

$$= 258 + 9256 \times 3268$$

$$= \underline{\underline{3286 \text{ V}}} = V_{CD}$$

