

Power Apparatus and System Design

Assignment - 3

Submitted By:

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1) The big difference between Power & distribution transformers are:

Power Transformer

- Rated Voltage is 33 kV or more.
- It cannot handle high variation in load.
- Step-up transformers to feed transmission lines from generating stations.
- Built to operate at full load throughout the day.
- Power rating is more than 200 MVA.
- Can be step-up & or step down
- Designed to operate at maximum efficiency at full load.
- It generally has one primary & one secondary winding.
- Generally, primary is connected in star & secondary in delta config.
- flux density is high.

Distribution Transformer

- Rate Voltage is less than 33 kV.
- It handles high load variation.
- Step-Down transformer to feed power to consumer units from distribution lines
- Doesn't work at full load throughout the day and is highly dependent on workload.
- Power rating is less than 200 MVA.
- Only step-down variant available.
- Designed to operate at max efficiency at 60-70% load.
- It has one primary but several secondary windings.
- Generally, primary is connected in Delta but secondary in star.
- flux density is lower.

2) (a) Energy efficiency is a measure of ratio of the instantaneous power output and input for the transformer. All day efficiency is a measure of the ratio of total energy supplied. Note that the supplied energy is the sum of power output & losses.

(b) The power required of my house is 6.385 kVA . Since, most appliances are inductive, for the sake of simplicity, let assume a reasonable power factor of 0.9 .

$$S = \frac{6.385}{0.9} \text{ kVA}, \quad \text{PF} = 0.9$$

$$P = S \times \text{PF} = 6.385 \times 0.9 = 5.7465 \text{ kW}$$

$$Q = \sqrt{S^2 - P^2} = 2.7831 \text{ kVAR.}$$

Let the peak load be applied for my home from 9:30 AM to 2:00 PM.

Let the times be divided into regions, R_i then R_{vi}

→ In R_i , $\text{PF} = \cos\left(\tan^{-1} \frac{Q_i}{P_i}\right) = \cos\left(\tan^{-1} \frac{45}{65}\right) = 0.82$

$$\text{Energy Input } (E_i) = \left[S_i \times \text{PF} + P_{\text{iron-core}} + P_{\text{iron-loss}} \times \left(\frac{S_i}{S}\right)^2 \right] \times t_i$$

$$= \left[65 + 0.4 + 1.35 \times \frac{\sqrt{65^2 + 45^2}}{100} \right] \text{ k}$$

$$= 231.85 \text{ kWh.}$$

$$\text{Energy Output } (E_o) = P_{\text{out}} \times t_i = 65 \text{ kW} \times 2.5 \text{ h} = 227.50 \text{ kWh.}$$

→ In R_{ii} , $P_{loss} = 5.74 \text{ kW}$, $Q = 20.78 \text{ kVAR}$
 $P_{ii} = 85.74 \text{ kW}$, $Q_{ii} = 52.78 \text{ kVAR}$

$$\text{Energy Input } (I_{ii}) = \frac{1}{\eta_{ii}} \left[85.74 + 0.4 + 1.35 \left(\frac{\sqrt{85.74^2 + 52.78^2}}{100} \right) \right]$$

$$= 306.246 \text{ kWh}$$

$$\text{Energy Output } (O_{ii}) = \eta_{ii} \times P_{ii} = 300.09 \text{ kWh}$$

→ In R_{iii} , $P_{iii} = 55.74 \text{ kW}$, $Q_{iii} = 42.78 \text{ kVAR}$.

$$\text{Energy Input } (I_{iii}) = \frac{1}{\eta_{iii}} \left[55.74 + 0.4 + 1.35 \left(\frac{Q_{iii}}{100} \right)^2 \right]$$

$$= 171.265 \text{ kWh}$$

$$\text{Energy Output } (O_{iii}) = \eta_{iii} \times P_{iii}$$

$$= 167.22 \text{ kWh}$$

→ In R_{iv} , $P_{iv} = 41.24 \text{ kW}$, $Q_{iv} = 2.78 + \frac{36}{0.85} \times \sqrt{1-0.85^2}$
 $= 25.09 \text{ kVAR}$.

$$\text{Energy Input } (I_{iv}) = 288.8828 \text{ kWh}$$

$$\text{Output Energy } (O_{iv}) = 281.745 \text{ kWh}$$

→ In R_v , $P_v = 30.74 \text{ kW}$, $Q_v = 2.78 + \frac{25}{0.9} \sqrt{1-0.9^2}$
 $= 14.888 \text{ kVAR}$.

$$\text{Energy Input } (I_v) = 102.70 \text{ kWh}$$

$$\text{Output Energy } (O_v) = 99.905 \text{ kWh}$$

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$$\text{All day efficiency} = \frac{\sum_{k=1}^n O_k}{\sum_{k=1}^n I_k} = 0.9777 \approx \underline{97.8\%}$$

Q2) (a) Load sharing in transformers is on the basis of Z_{eq} . It is very similar to current sharing in parallel resistor branch.
 Let S_n be load taken by branch n , & S_{rn} be its rated load. Z_{eqn} its Z_{eq} .

$$S_A = \frac{(Z_{eqB} \parallel Z_{eqC} \parallel Z_{eqD}) \times S}{(Z_{eqB} \parallel Z_{eqC} \parallel Z_{eqD}) + Z_{eqA}} = 115.7 \text{ kVA}$$

$$S_B = \frac{(Z_{eqA} \parallel Z_{eqC} \parallel Z_{eqD}) \times S}{(Z_{eqA} \parallel Z_{eqC} \parallel Z_{eqD}) + Z_{eqB}} = 231.6 \text{ kVA}$$

$$S_C = 286.497 \text{ kVA} \quad \left. \begin{array}{l} \text{Similarly calculated} \\ \text{as above} \end{array} \right\}$$

$$S_D = 366.406 \text{ kVA}$$

Clearly, A & B are overloaded. Since $S_A > S_{RA}$, $S_B > S_{RB}$
 for A $0.3924 / (0.3924 + 1.3) \times S_{new} < 200$ & $0.2875 \times S_{new} < 100$

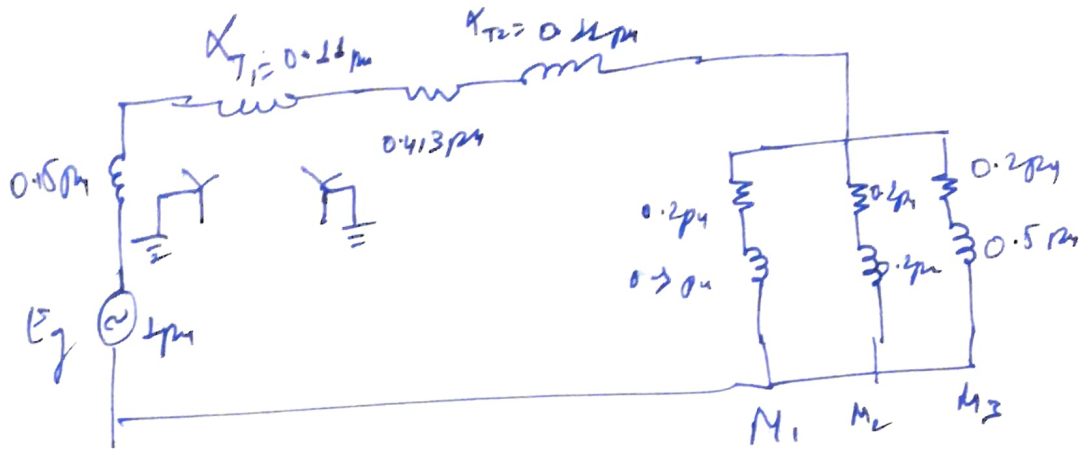
(b) $S_{new} < 844.28$ & $S_{new} < 795.23 \text{ kVA}$

$\therefore S_{new}$ must be 795.23 kVA for no overloading

\therefore B, C & D would be underloaded.

(c) It is not possible for B, C & D to operate at their rated kVA as doing so would overload A & B as shown in (b).

4) (a)



$$\text{Net efficiency } (E) = E_{T1} \times E_{T2} \\ = 0.97 \times 0.97 = 0.941$$

$$\therefore \text{Total losses} = \text{full load power} \times (1 - E) \\ = 100 \text{ MVA} \times (1 - 0.941) \\ = 5.91 \text{ MW}$$

(b)

At 70% full load power = 70 MVA.

$$\text{So losses} = 70 \times (1 - 0.941) \\ = 4.13 \text{ MVA} = \text{const loss}$$

$$\text{So, } \eta = \frac{70}{70 + 0.7^2 \times 4.13 + 4.13} \approx 91.9\%$$

(c)

Another for 97% efficiency

$$\text{At full load, losses} = 100 \times (1 - 0.97^2) = 8.7329 \text{ MW}$$

$$\text{At 70% load, losses} = 0.7 \times 8.7329 = 6.1129 \text{ MW}$$

$$\text{for full load efficiency} = 0.97^2 = 0.941 \\ \text{i.e., } 94.1\%$$

$$\text{for 70% load} = \frac{3 \times 70}{2 \times 70 + 3 \times 0.7^2 \times 4.13 + 3 \times 4.13} = 91.9\%$$

(d)

We see the transformers when operated at 60-70% load give maximum efficiency and then distribution transformer is preferred also the demand is not all throughout the day. In b & c the situation relates with distribution transfer characteristics.