

# Blockchains & Cryptocurrencies

## **Mining**



Instructor: Matt Green & Abhishek Jain  
Johns Hopkins University - Spring 2023

\*Some slides based on NBFMG

# Today

- Mining Strategies
- Alternative puzzles (maybe)

# Bitcoin Mining

# Mining Bitcoins in 6 easy steps

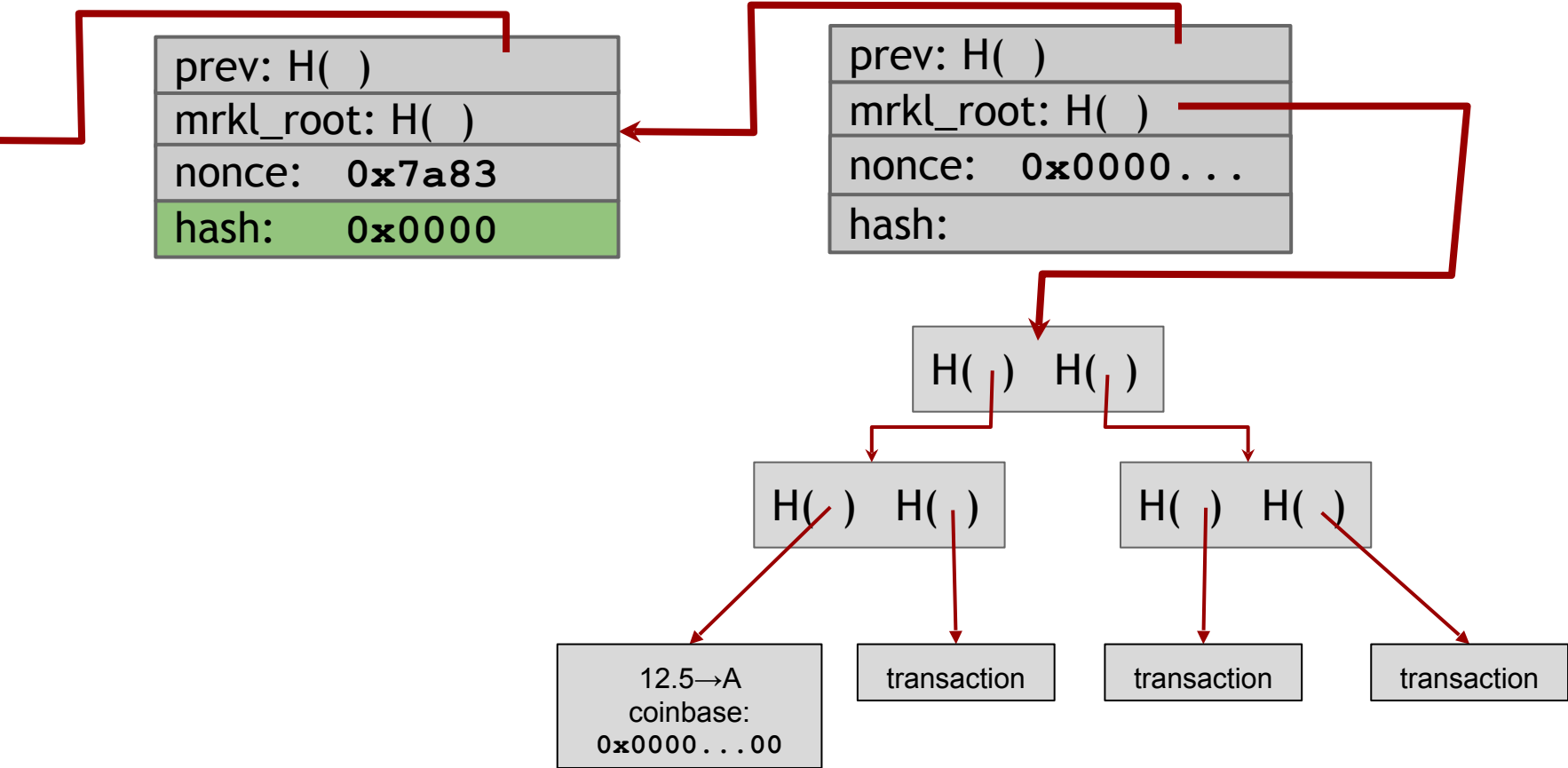
1. Join the network, listen for transactions
  - a. Validate all proposed transactions
2. Listen for new blocks, maintain block chain
  - a. When a new block is proposed, validate it
3. Assemble a new valid block
4. Find the nonce to make your block valid
5. Hope everybody accepts your new block
6. Money!

# Mining Bitcoins in 6 easy steps

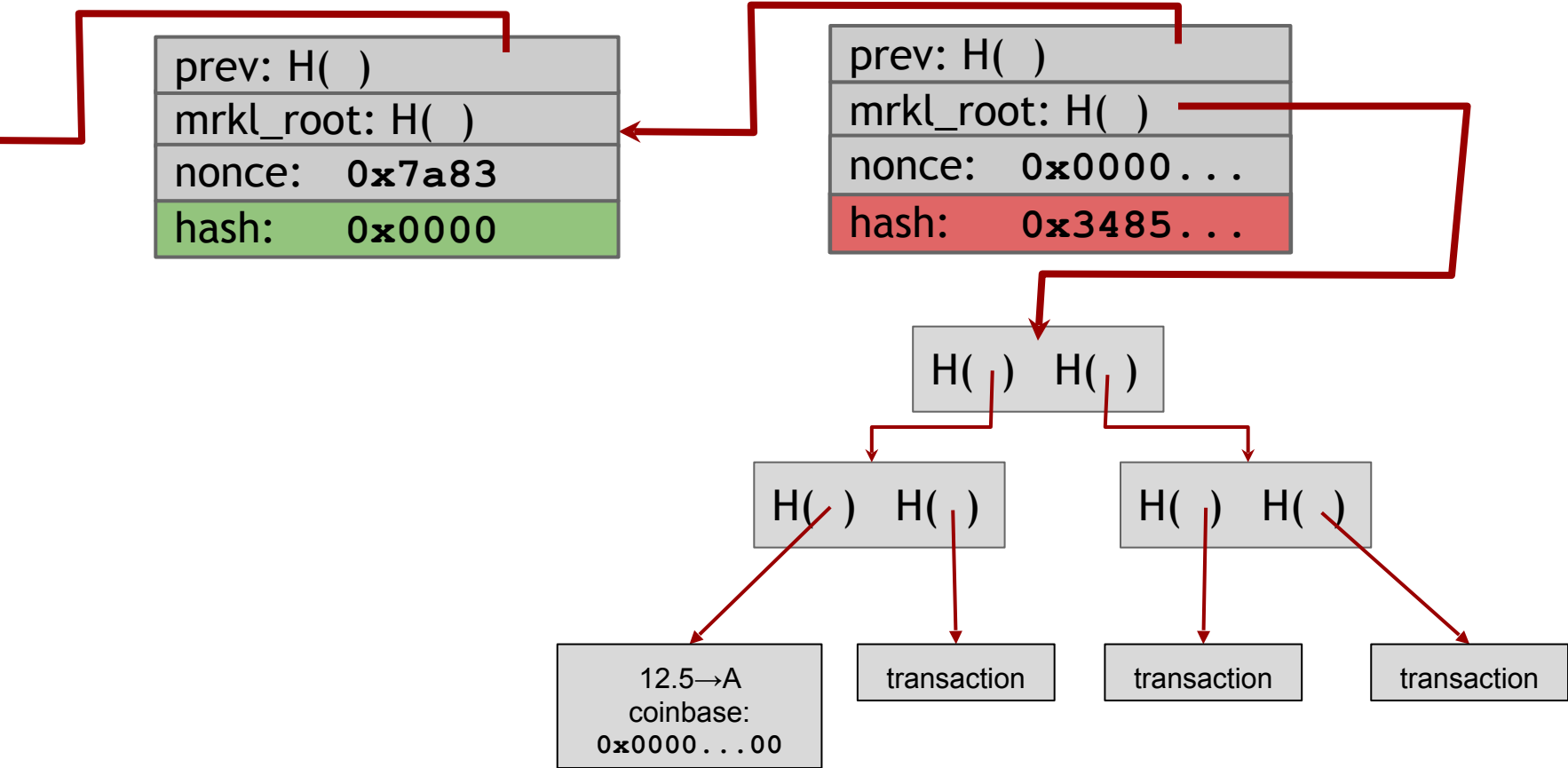
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Useful to  
Bitcoin  
network

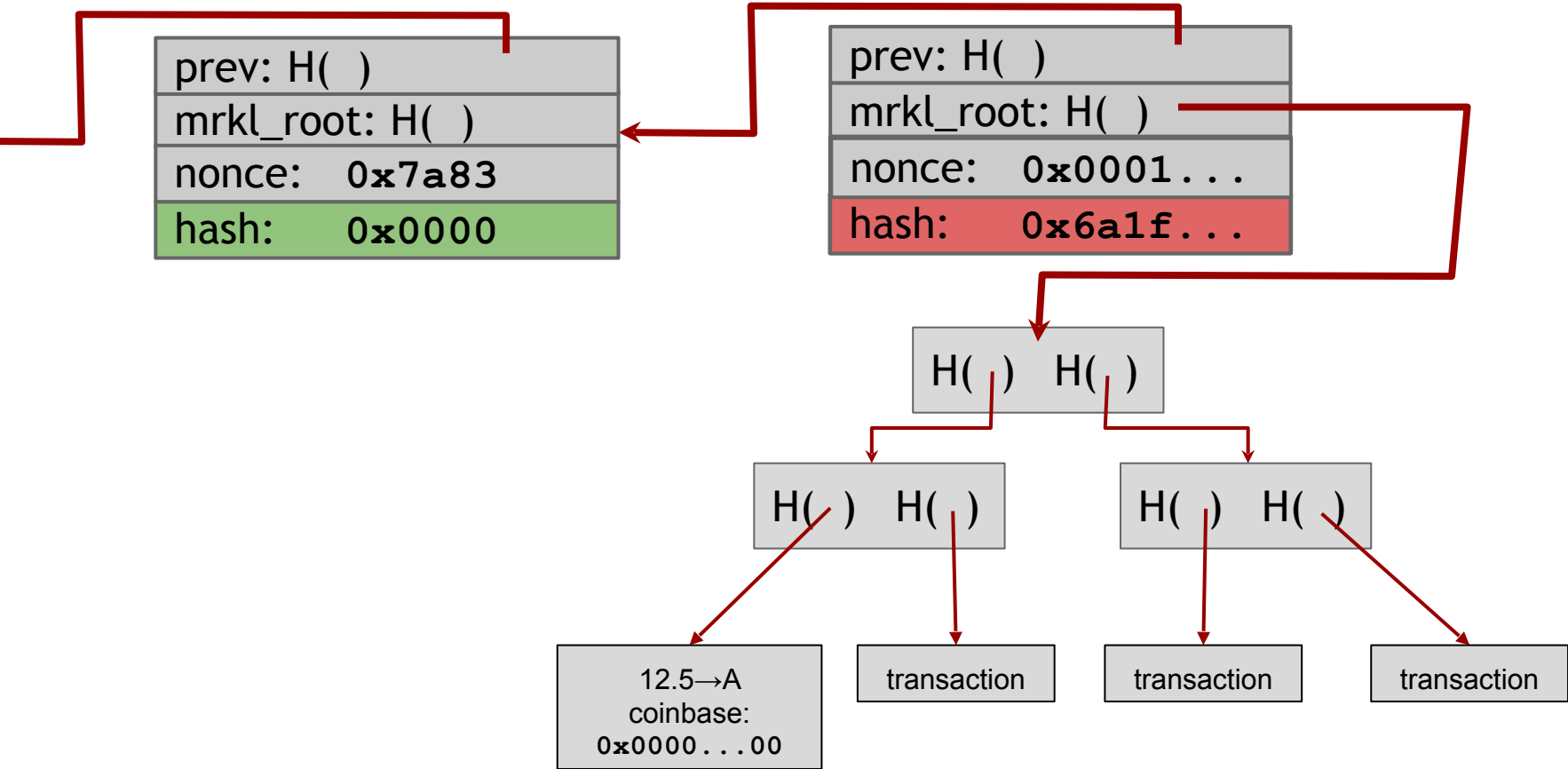
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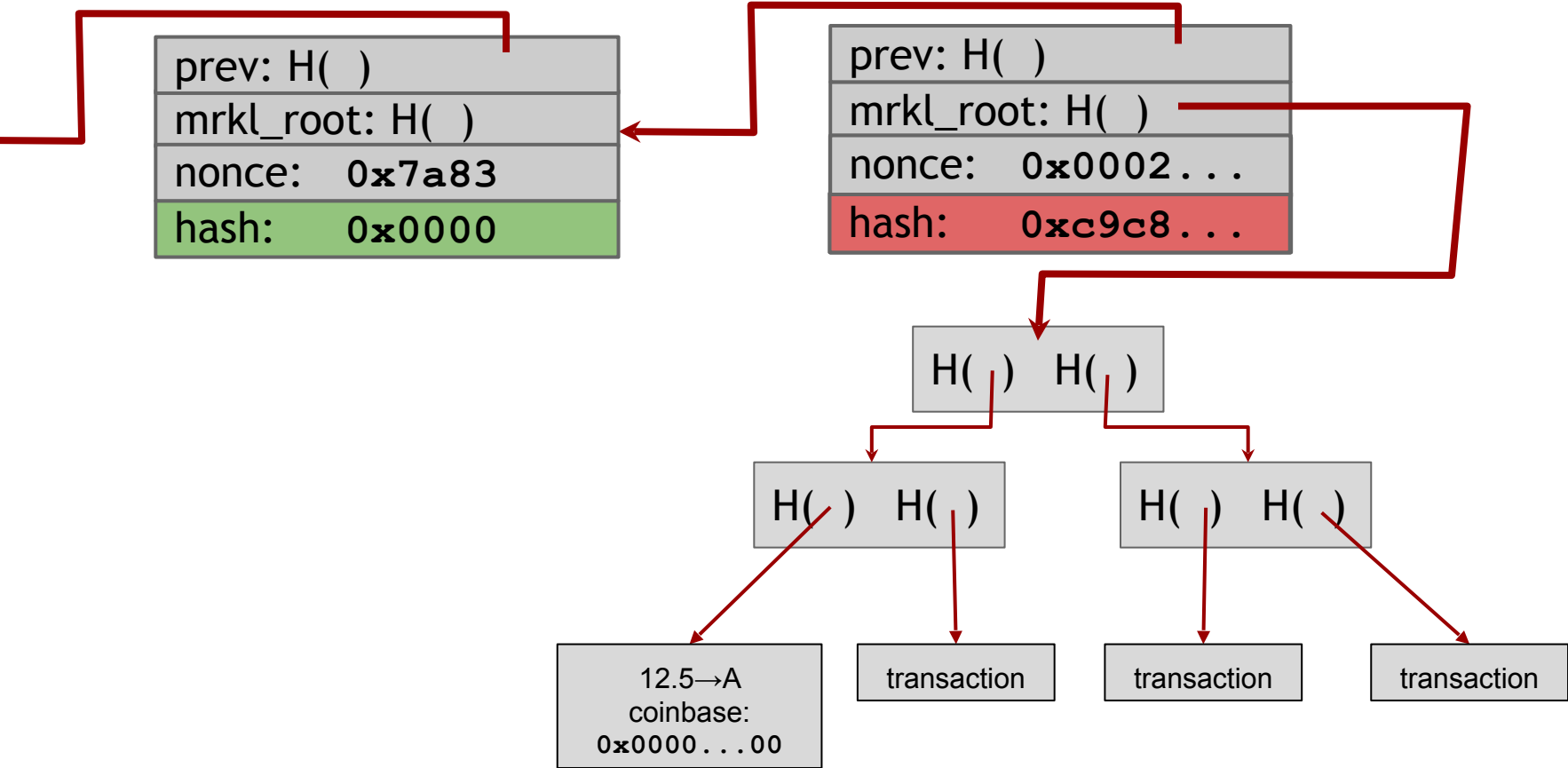


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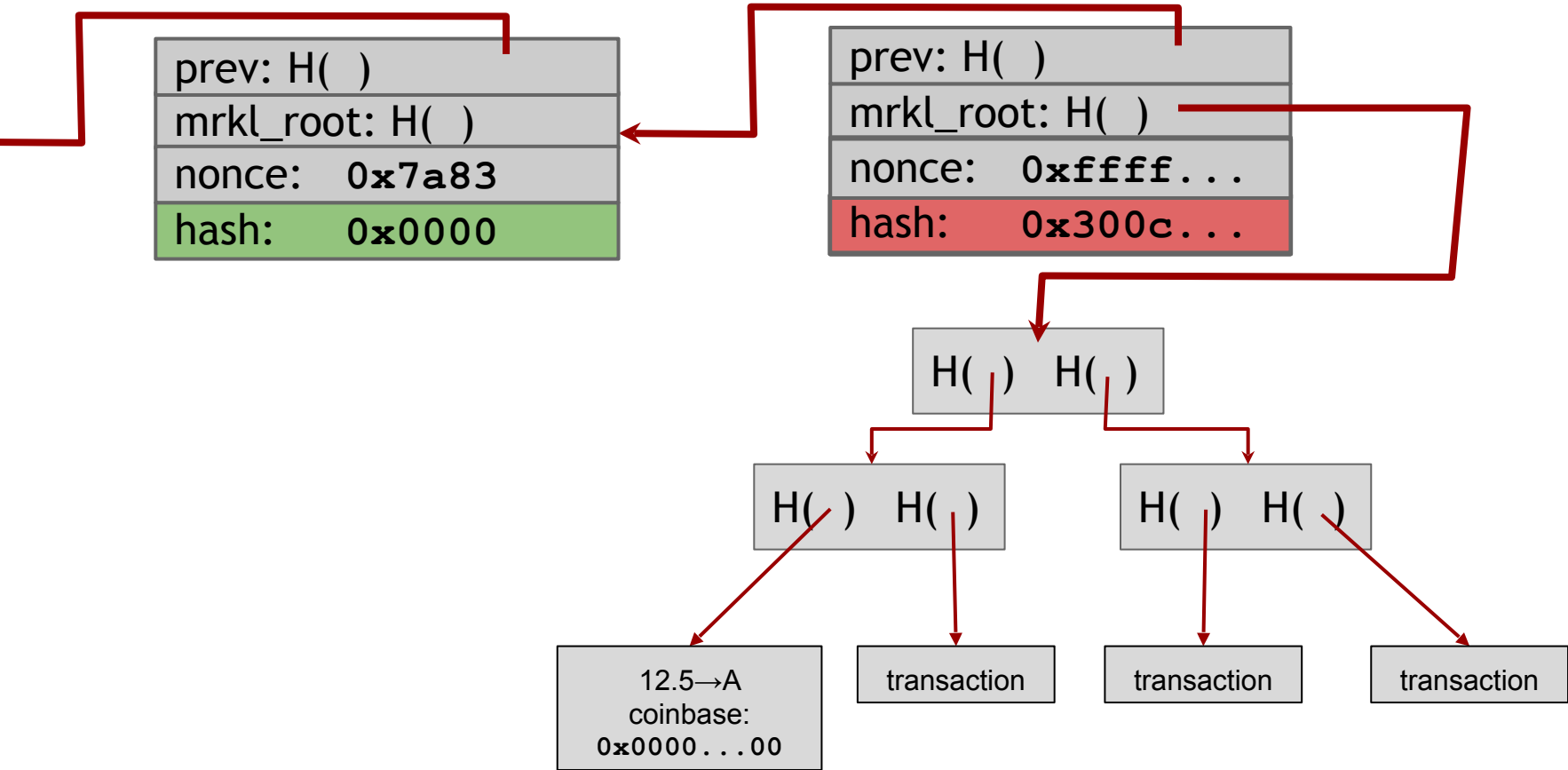




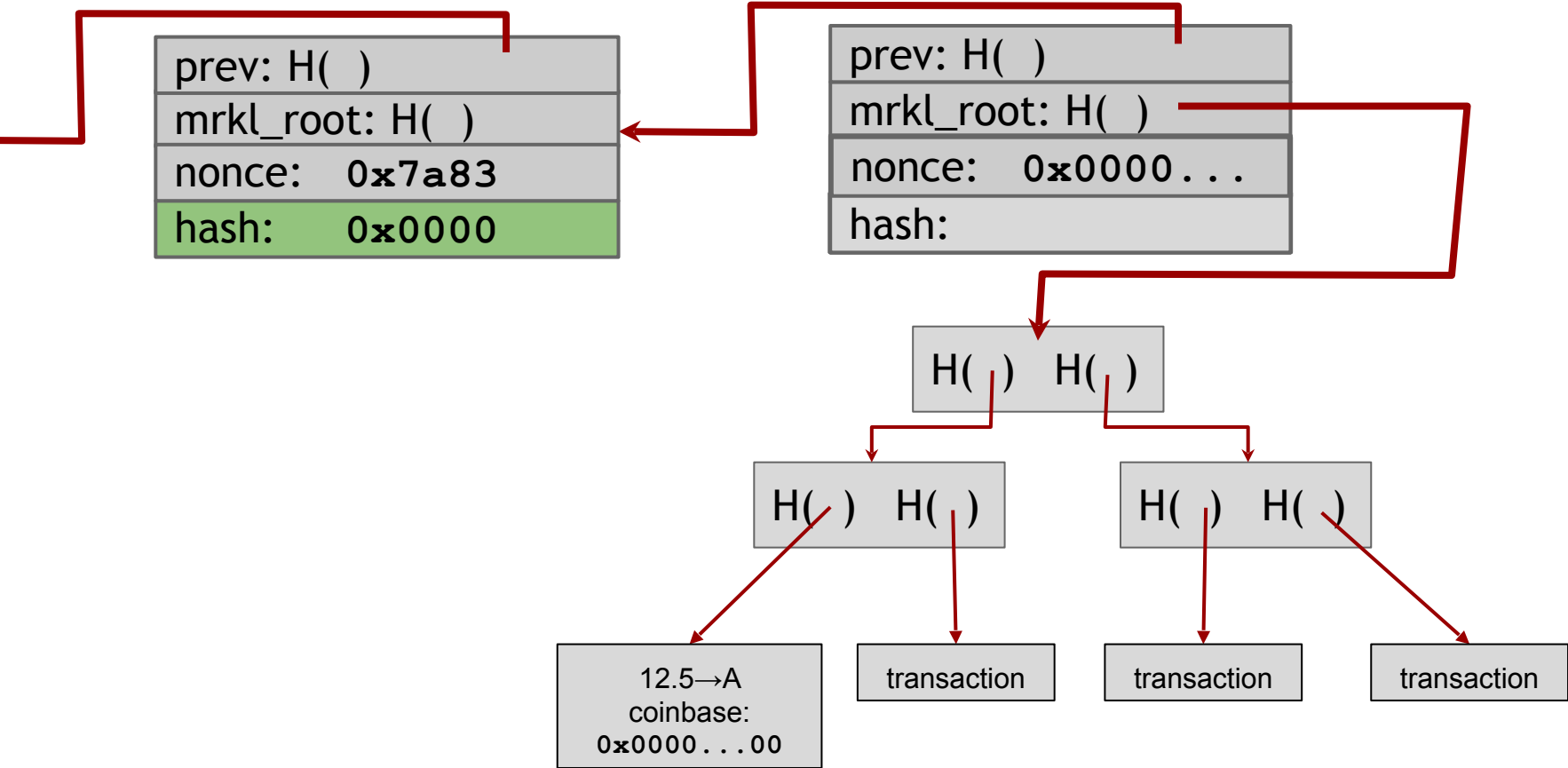
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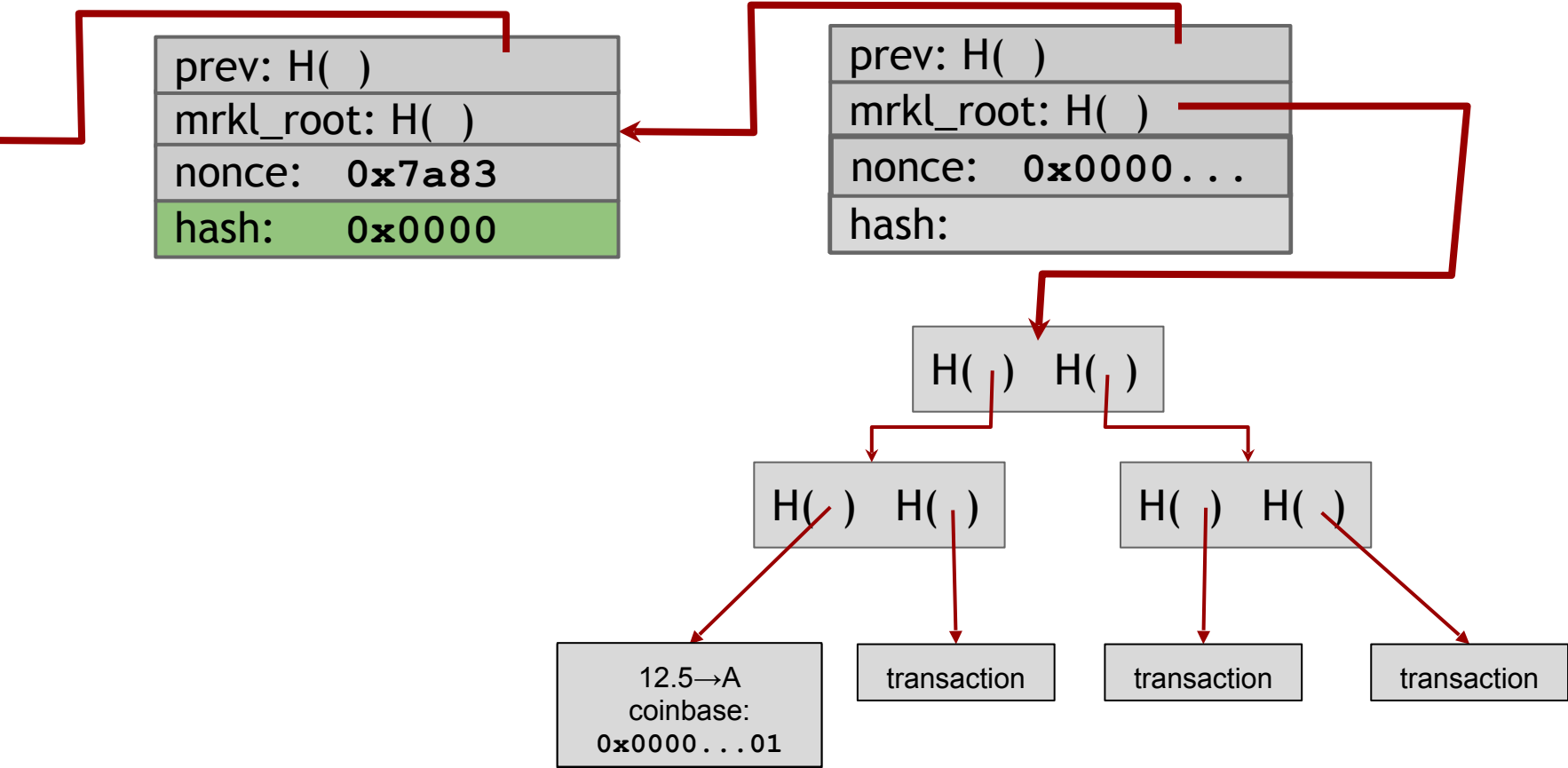
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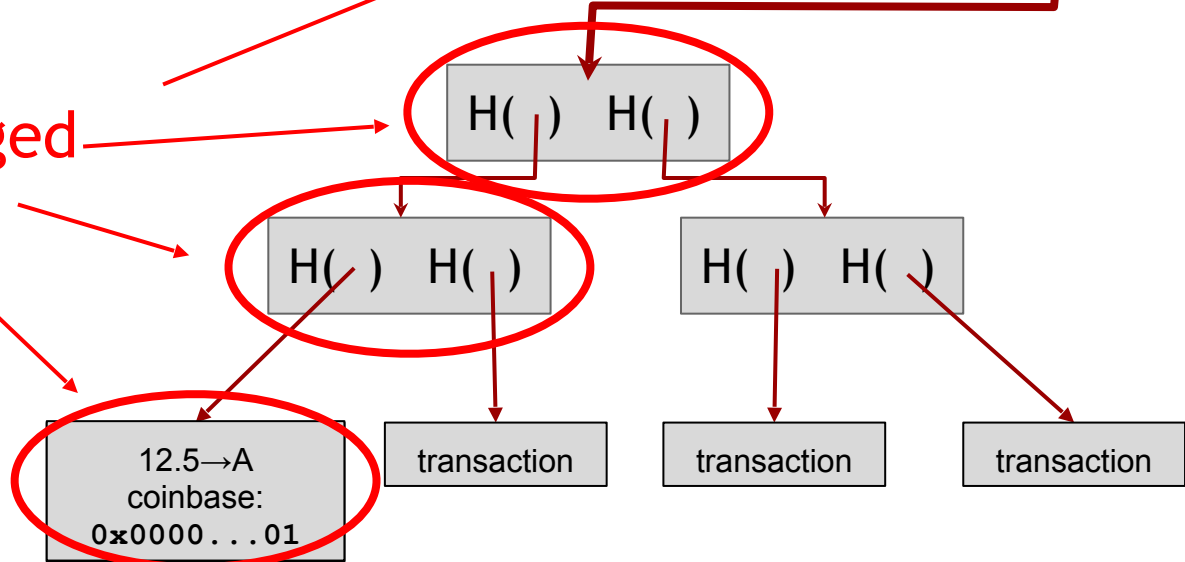


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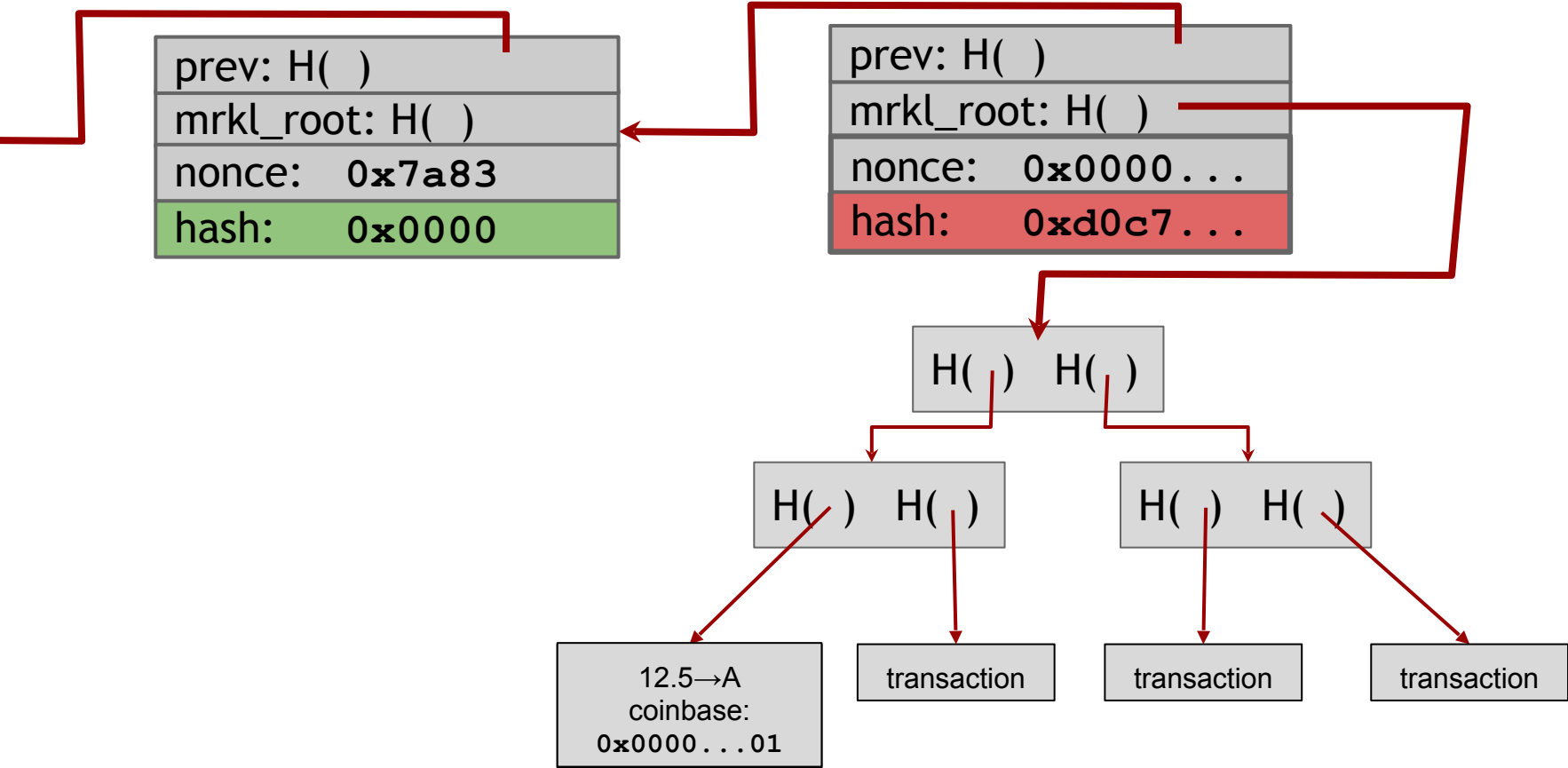
prev: H( )
mrkl_root: H( )
nonce: 0x7a83
hash: 0x0000

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hash:

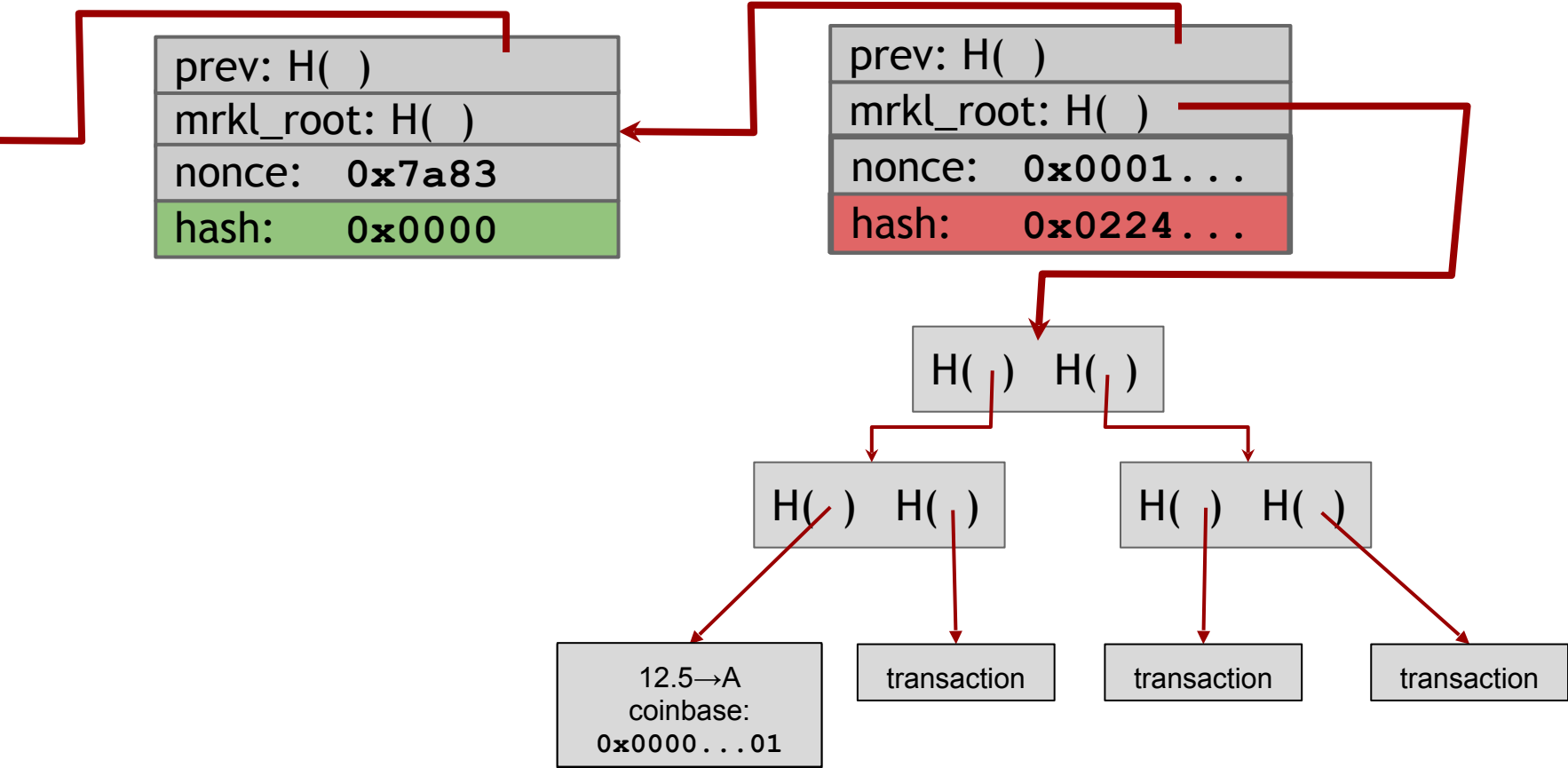
All changed



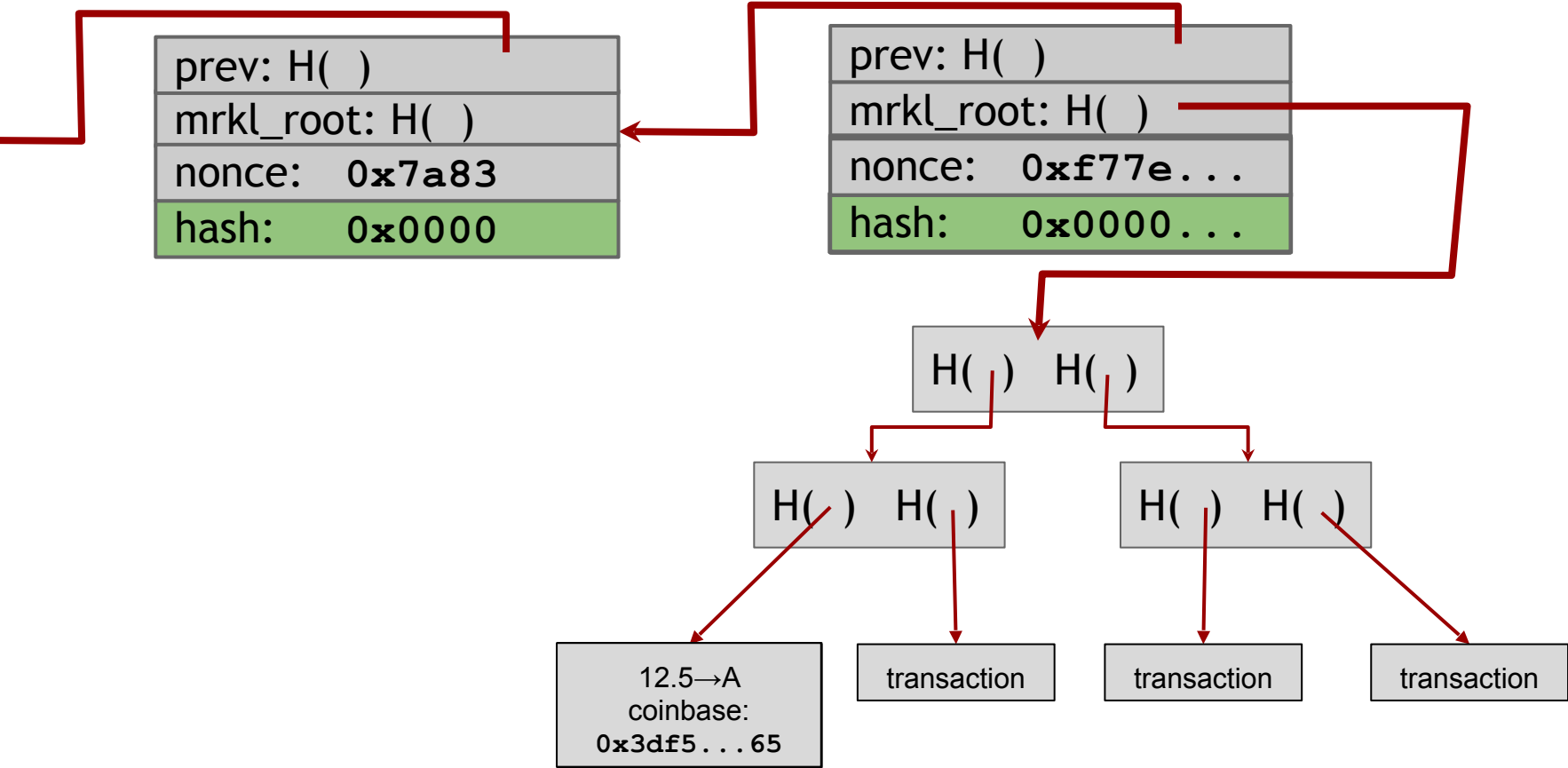
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# Finding a valid block





# CPU mining (numbers from 2014)

```
while (1){  
    HDR[kNoncePos]++;  
    IF (SHA256(SHA256(HDR)) < (65535 << 208) / DIFFICULTY)  
        return;  
}
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Throughput on a high-end PC = 10-20 MHz  $\approx 2^{24}$

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Throughput on a high-end PC = 10-20 MHz  $\approx 2^{24}$

**139,461 years to find a block!**

# Evolution of mining



CPU



GPU



FPGA



ASIC

# Evolution of mining



CPU



GPU



FPGA



ASIC

Huge energy consumption (in 2017, annual rate nearly as high as Denmark)!

# The future

- Can small miners stay in the game?
- Would we be better off without ASICs?
- Should we implement consensus without proofs of work?

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**Motivation for Altcoins**

Mining pools



# Economics of being a small miner

- In 2014, expected revenue:  $\approx \$1,000/\text{month}$
- High probability ( $\sim 50\%$ ) of not mining a block within a year

# Mining pools

- **Goal:** pool participants all attempt to mine a block with the same coinbase recipient
  - send money to key owned by pool manager
- Distribute revenues to members based on how much work they have performed
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How do we know how much work members perform?

# Mining shares

Idea: prove work with “near-valid blocks” (shares)

```
4AA087F0A52ED2093FA816E53B9B6317F9B8C1227A61F9481AFED67301F2E3FB
D3E51477DCAB108750A5BC9093F6510759CC880BB171A5B77FB4A34ACA27DEDD
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9C20B06B01A0136F192BD48E0F372A4B9E6BA6ABC36F02FCED22FD9780026A8F
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D3E51477DCAB108750A5BC9093F6510759CC880BB171A5B77FB4A34ACA27DEDD
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9C20B06B01A0136F192BD48E0F372A4B9E6BA6ABC36F02FCED22FD9780026A8F
```

# Mining pools

Pool manager



# Mining pools

Pool manager

Hey folks! Here's  
our next block to  
work on





# Mining pools

Pool manager

prev:	H( )
mrkl_root:	H( )
nonce:	
hash:	



# Mining pools

## Pool manager

prev:	H( )	
mrkl_root:	H( )	coinbase: 6.25 → pool
nonce:		
hash:		



# Mining pools

Pool manager



# Mining pools

Pool manager

0x000000000000a877902e...

0x0000000000001e8709ce...

0x000000000000490c6b00...

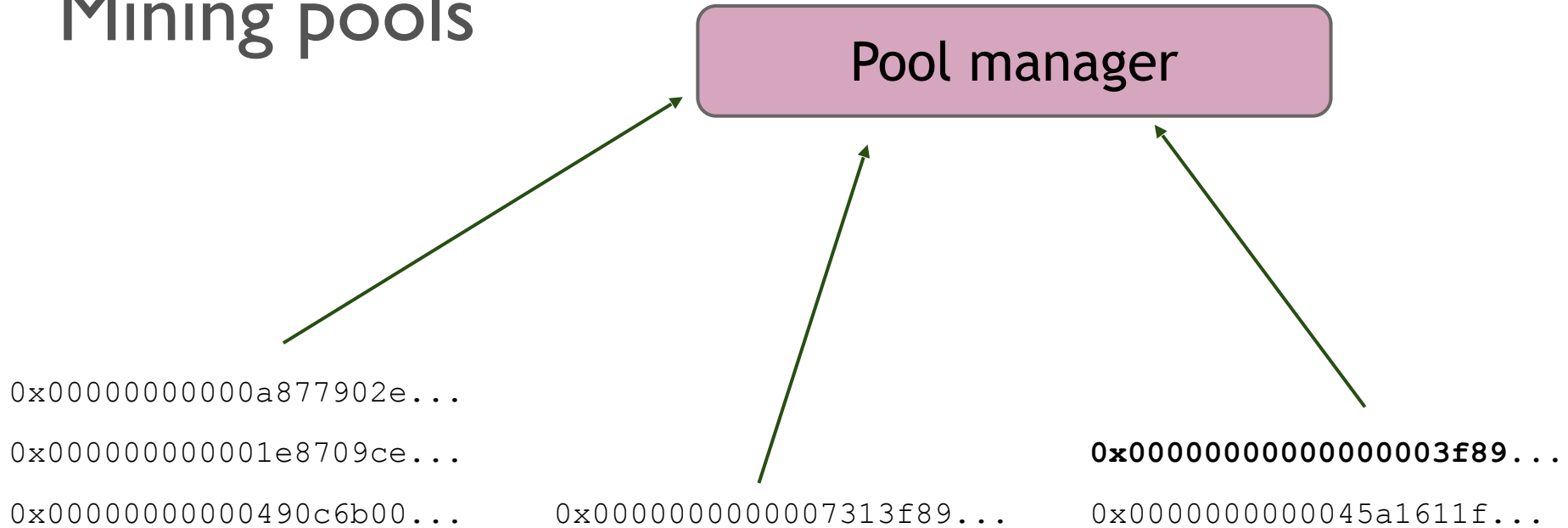
0x00000000000007313f89...

**0x000000000000000003f89...**

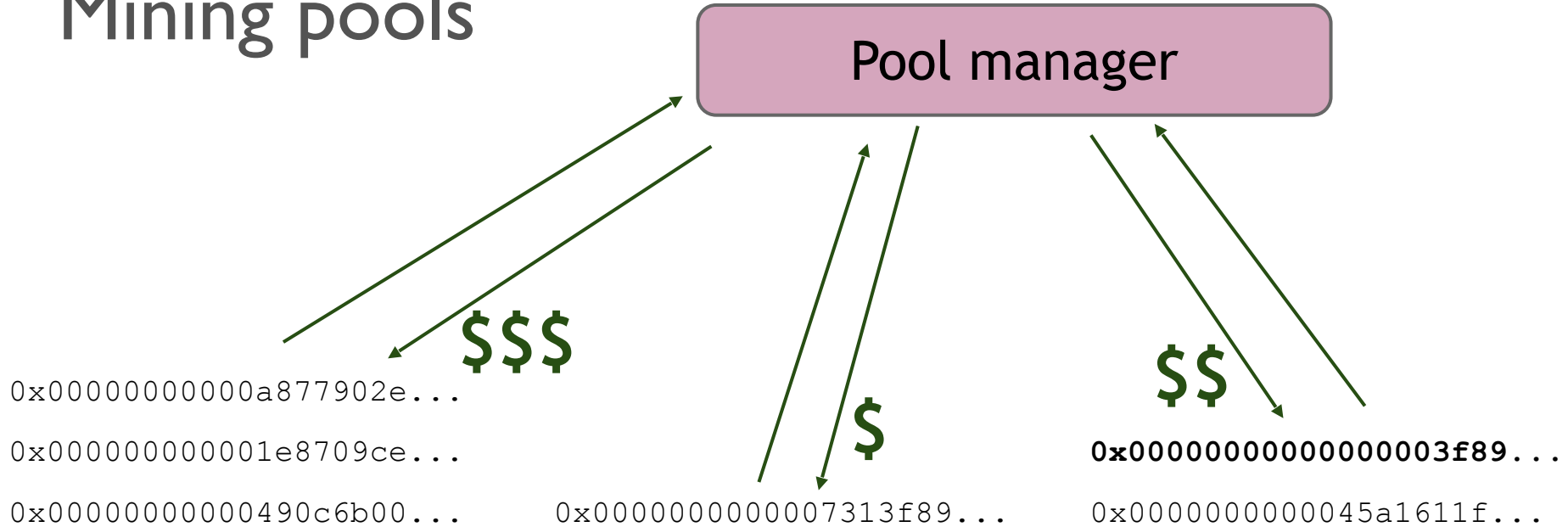
0x00000000000045a1611f...



# Mining pools



# Mining pools



# Mining pool history

- First pools appear in late-2010
  - Back in the GPU era!
- By 2014: around 90% of mining pool-based
- June 2014: GHash.io exceeds 50% (!)

# Are mining pools a good thing?

- Pros

- Make mining more predictable
- Allow small miners to participate
- More miners using updated validation software

- Cons

- Lead to centralization
- Discourage miners from running full nodes

Question: Can we prevent pools?



# Mining strategies

# Game-theoretic analysis of mining

Several strategic decisions

- Which transactions to include in a block
  - Default: any above minimum transaction fee
- Which block to mine on top of
  - Default: longest valid chain
- How to choose between colliding blocks
  - Default: first block heard
- When to announce new blocks
  - Default: immediately after finding them

# Game-theoretic analysis of mining

Assume you control  $0 < a < 1$  of mining power

Can you profit from a non-default strategy?

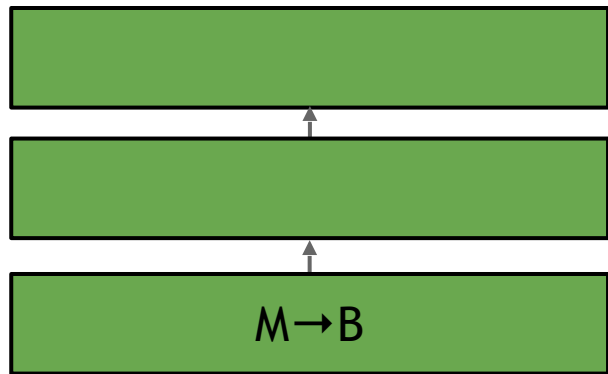
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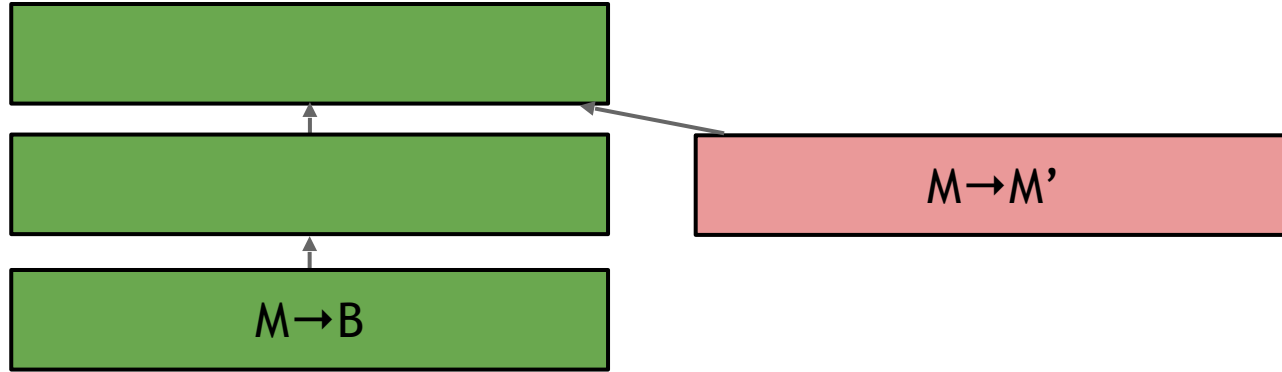
Can you profit from a non-default strategy?

**For some  $\alpha$ , YES!**

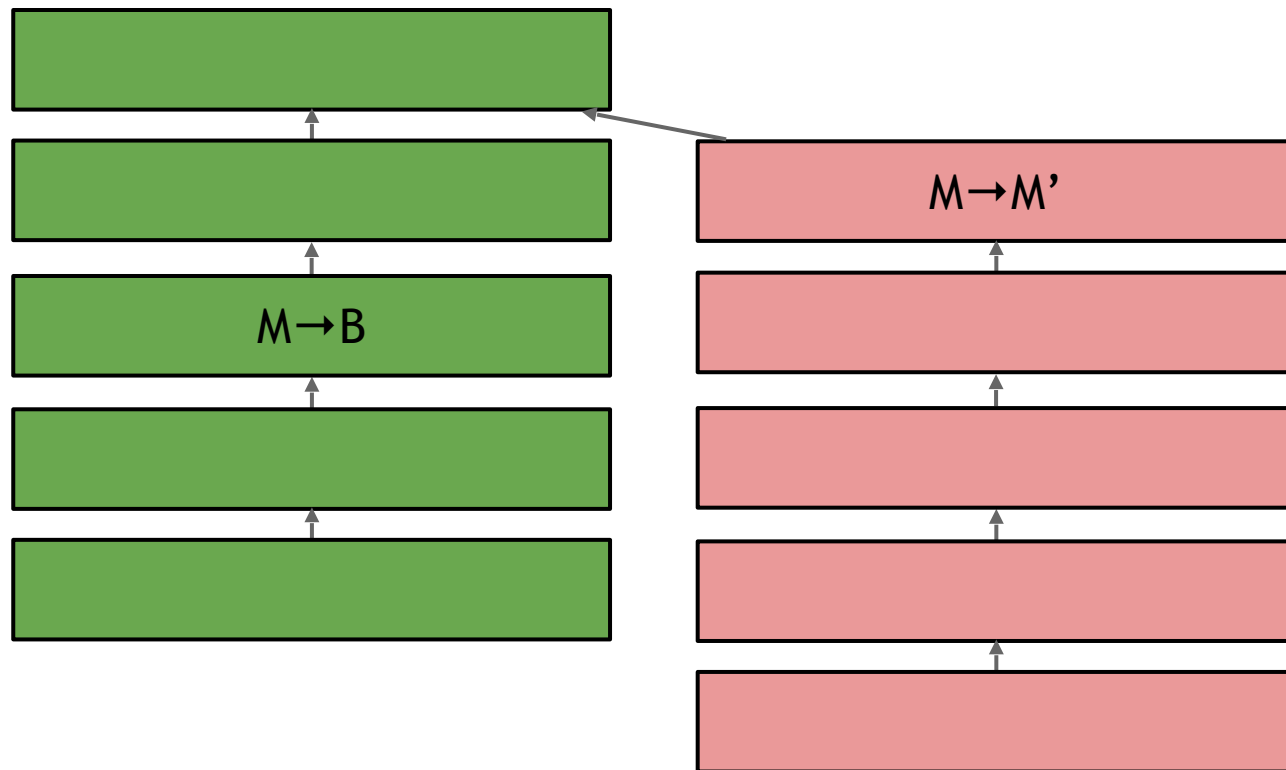
# Forking attacks



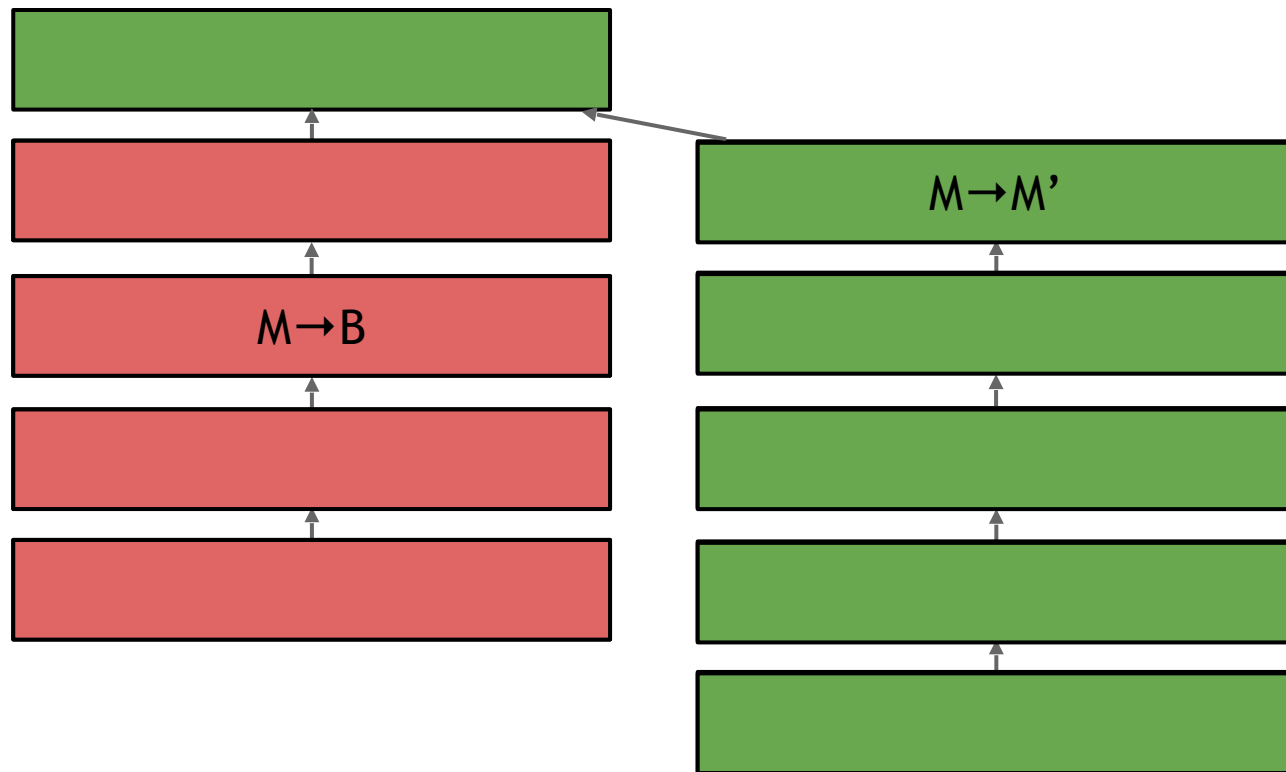
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- Certainly possible if  $\alpha > 0.5$ 
  - may be possible with less
- Attack is detectable
- Might be reversed
- Might crash exchange rate

# PoW 51% Attack Cost

<https://www.crypto51.app/>

This is a collection of coins and the theoretical cost of a 51% attack on each network.

[Learn More](#)

[⚡ Tip](#)

Name	Symbol	Market Cap	Algorithm	Hash Rate	1h Attack Cost	NiceHash-able
<a href="#">Bitcoin</a>	BTC	\$212.07 B	SHA-256	158,092 PH/s	\$641,748	0%
<a href="#">Ethereum</a>	ETH	\$43.26 B	Ethash	240 TH/s	\$272,454	3%
<a href="#">BitcoinCashABC</a>	BCH	\$4.70 B	SHA-256	2,947 PH/s	\$12,117	16%
<a href="#">Litecoin</a>	LTC	\$3.29 B	Scrypt	272 TH/s	\$20,709	5%
<a href="#">Zcash</a>	ZEC	\$707.21 M	Equihash	7 GH/s	\$13,521	3%
<a href="#">Dash</a>	DASH	\$686.48 M	X11	6 PH/s	\$2,070	3%
<a href="#">EthereumClassic</a>	ETC	\$625.51 M	Ethash	4 TH/s	\$4,075	231%
<a href="#">BitcoinGold</a>	BTG	\$138.61 M	Zhash	766 KH/s	\$287	71%

# What can a “51% attacker” do?

Steal coins from existing address? 

Suppress some transactions?

- From the block chain 
- From the P2P network 

Change the block reward? 

Destroy confidence in Bitcoin?  

# Selfish Mining

---

(Block-Withholding Attack)

**Majority is not Enough:  
Bitcoin Mining is Vulnerable\***

Ittay Eyal and Emin Bilen Sirer

Department of Computer Science, Cornell University  
ittay.eyal@cornell.edu, egs@systems.cs.cornell.edu

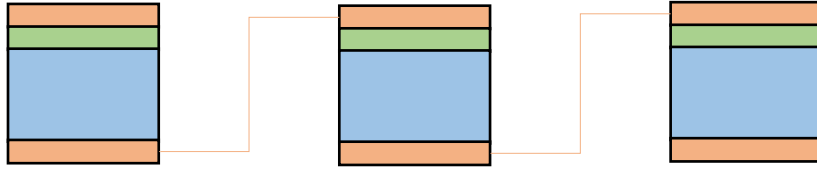
# Selfish Mining Strategy (aka block withholding)

- Form a pool.
- Secretly mine blocks. Don't announce blocks right away. Try to get ahead!
- Announce as and when necessary to maintain lead, or to avoid falling behind

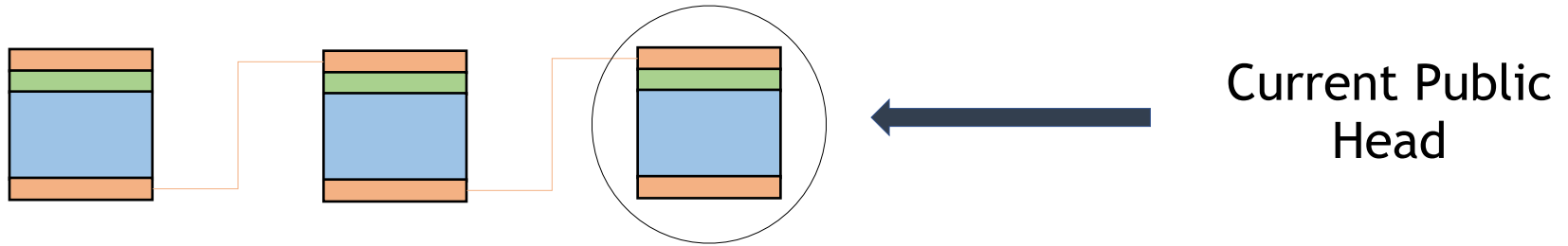




# Public Chain

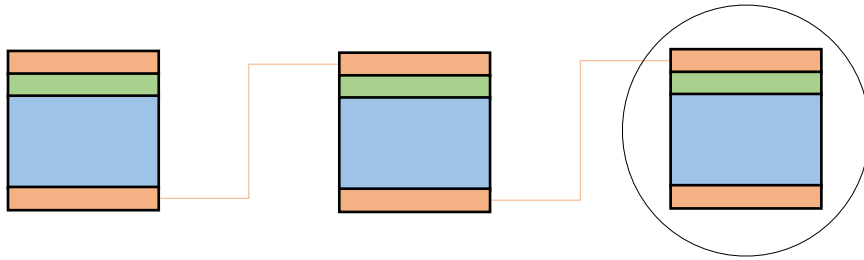


# Public Chain



# Public Chain

- The honest miners and the selfish miner pool start mining at the current public head.



Honest Miners

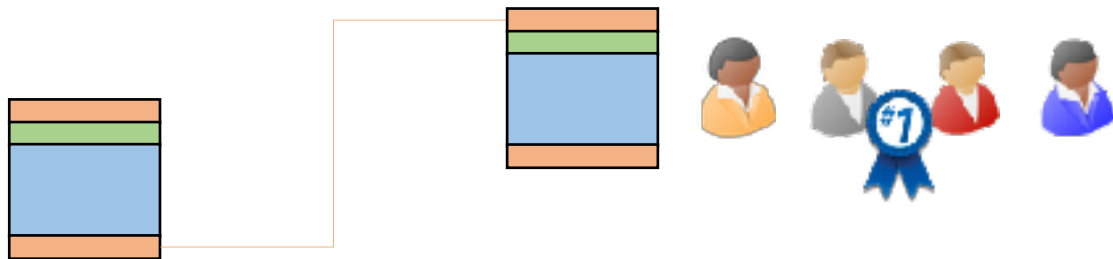


Selfish Miner Pool

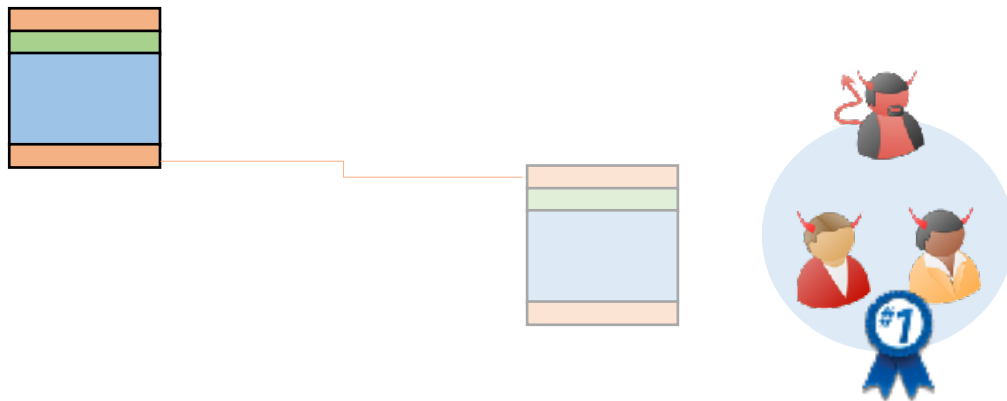


Case a

Honest miners find a new block first.



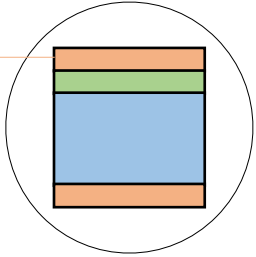
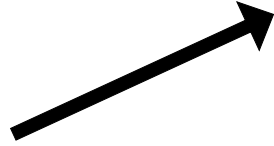
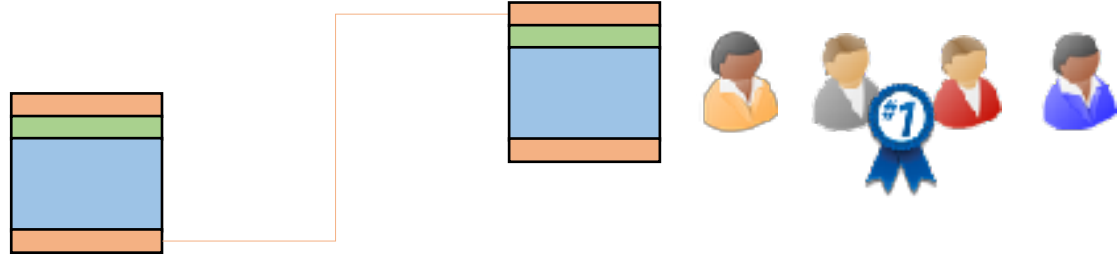
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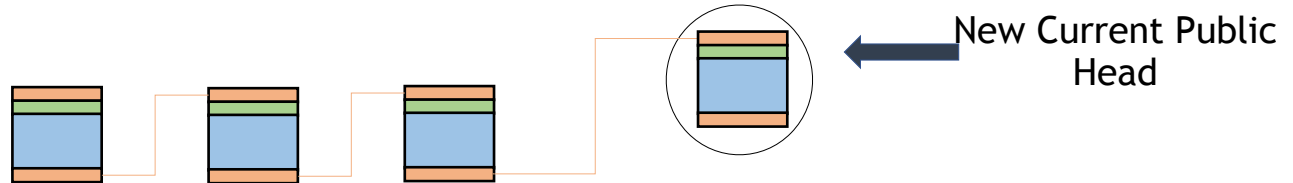
Case b

Case a

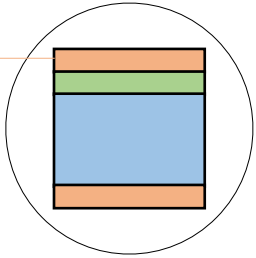
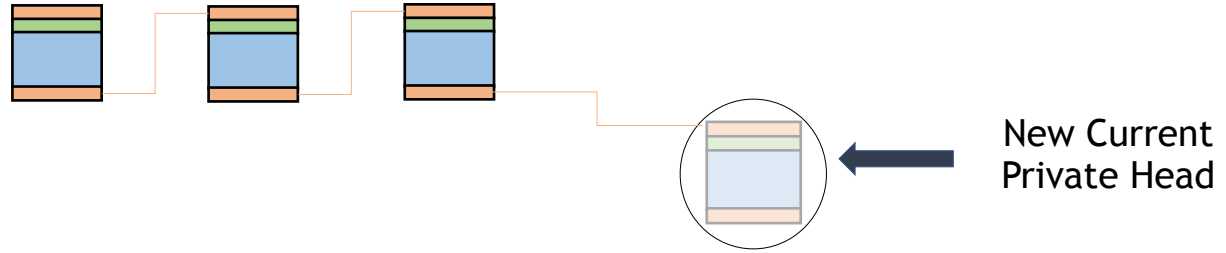
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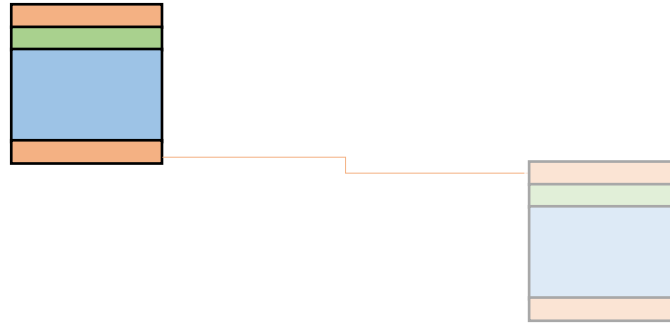
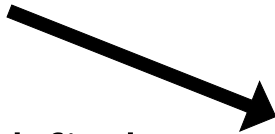
Selfish miner pool adopts the main branch and starts mining on the new current public head.



Selfish pool keeps this branch private, and starts mining on this private branch.

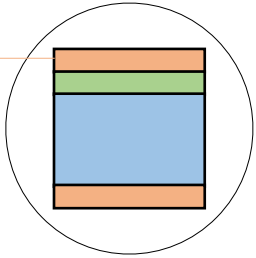
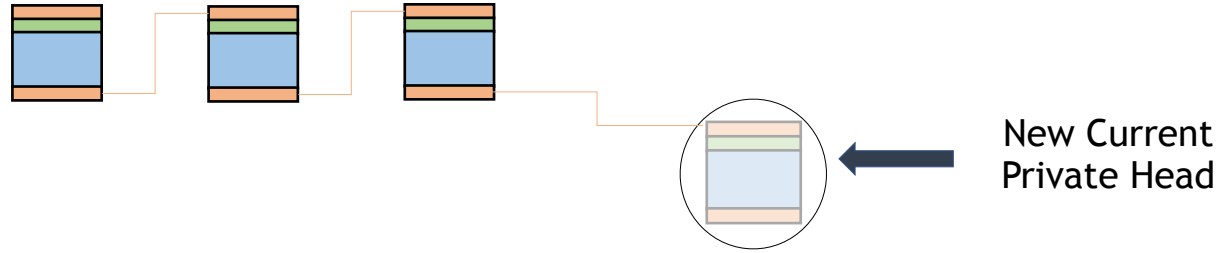


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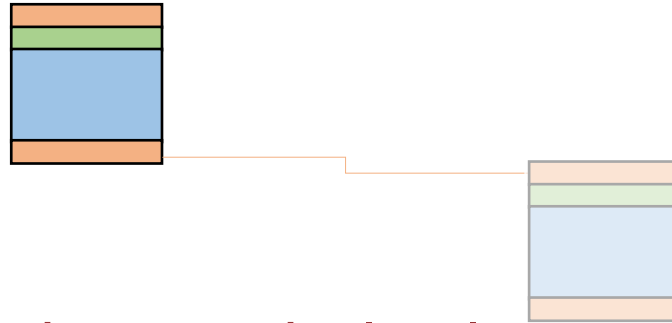
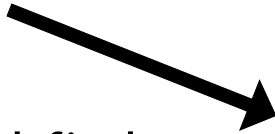


Case b

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Case b

Let's look at case b closely.

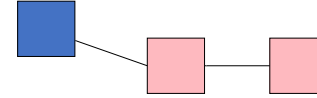
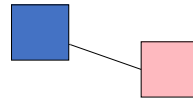
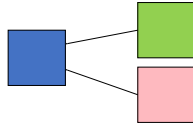






Honest miners discover a new block on the public branch.

Case 1

Case 2

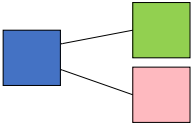
Selfish pool finds a second block.



-  Public Head
-  Block mined by honest miners
-  Block mined by selfish pool and kept private
-  Block mined by selfish pool and made public



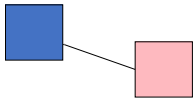
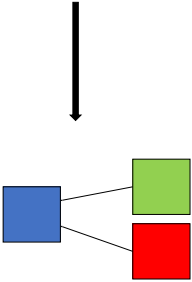
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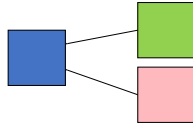
The selfish pool publishes its private branch.



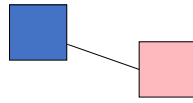
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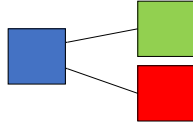
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Case 2

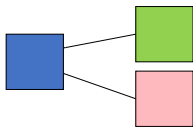


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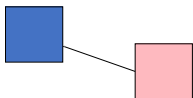


- There are 2 competing chains of the same length now.
- The selfish pool mines to extend its branch.
- Honest miners choose to mine on either branch.

Honest miners discover a new block on the public head.



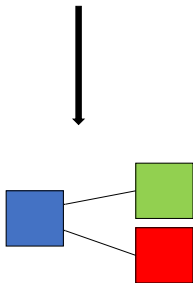
Case 1



Case 2



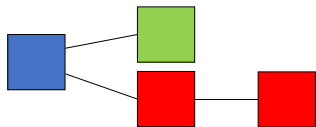
The selfish pool publishes its private branch.



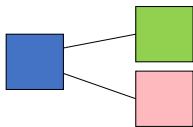
Case 1

Selfish pool mines a second block and publishes it.

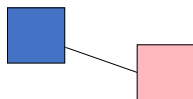
Revenue = 2



Honest miners discover a new block on the public head.



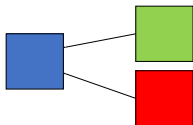
Case 1



Case 2



The selfish pool publishes its private branch.

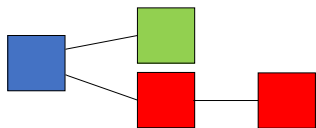


Case 1

Case 2

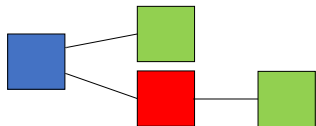


Revenue = 2

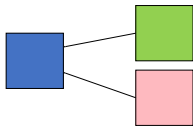


Honest miners mine a block after the pool's revealed block.

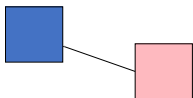
Revenue = 1



Honest miners discover a new block on the public head.



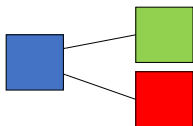
Case 1



Case 2



The selfish pool publishes its private branch.



Case 1

Case 2

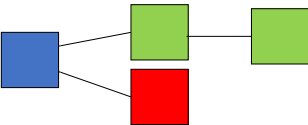
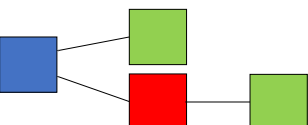
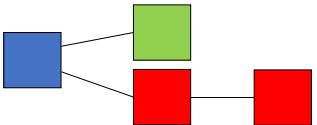
Case 3

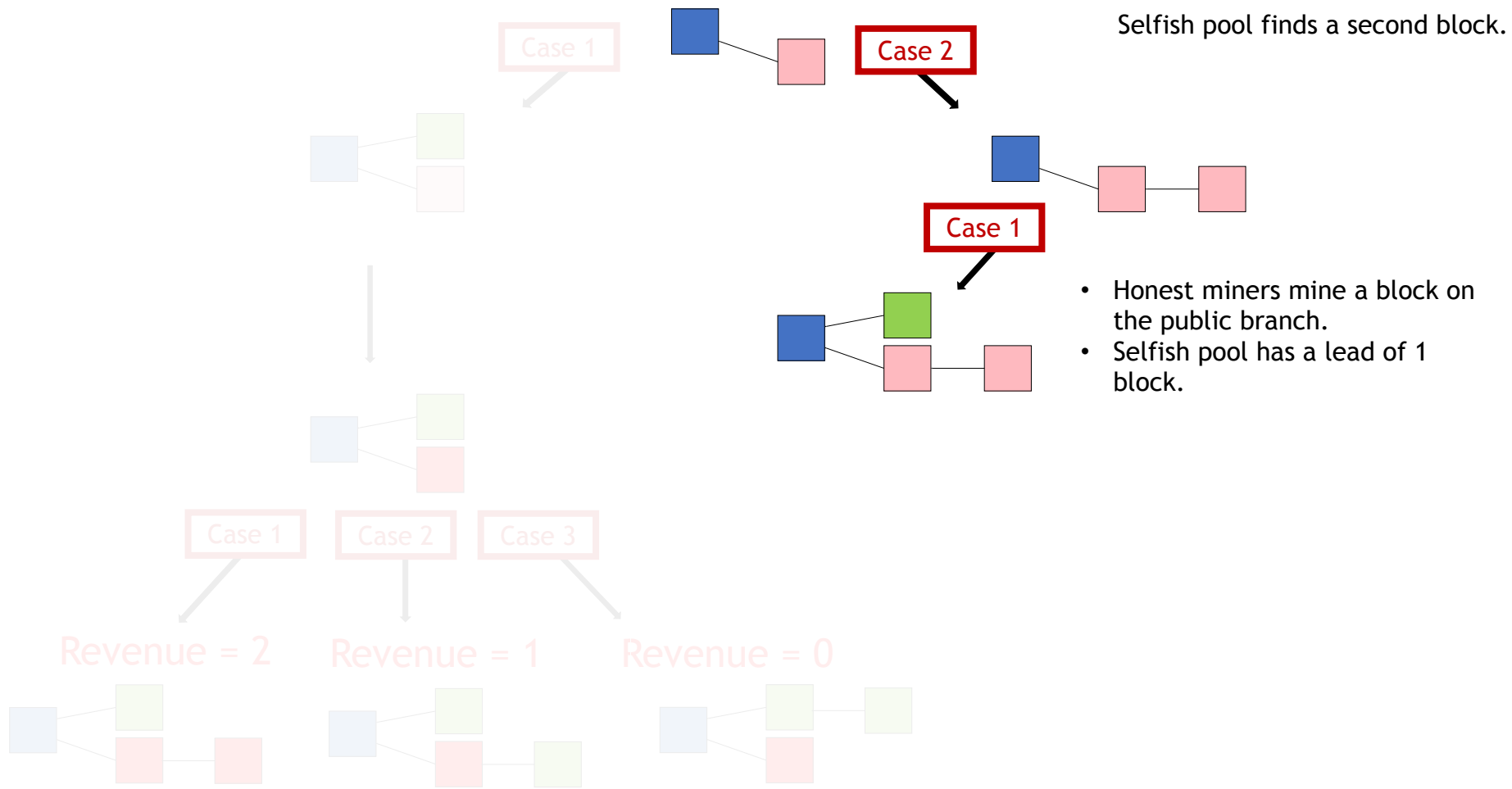
Honest miners mine a block after their own block.

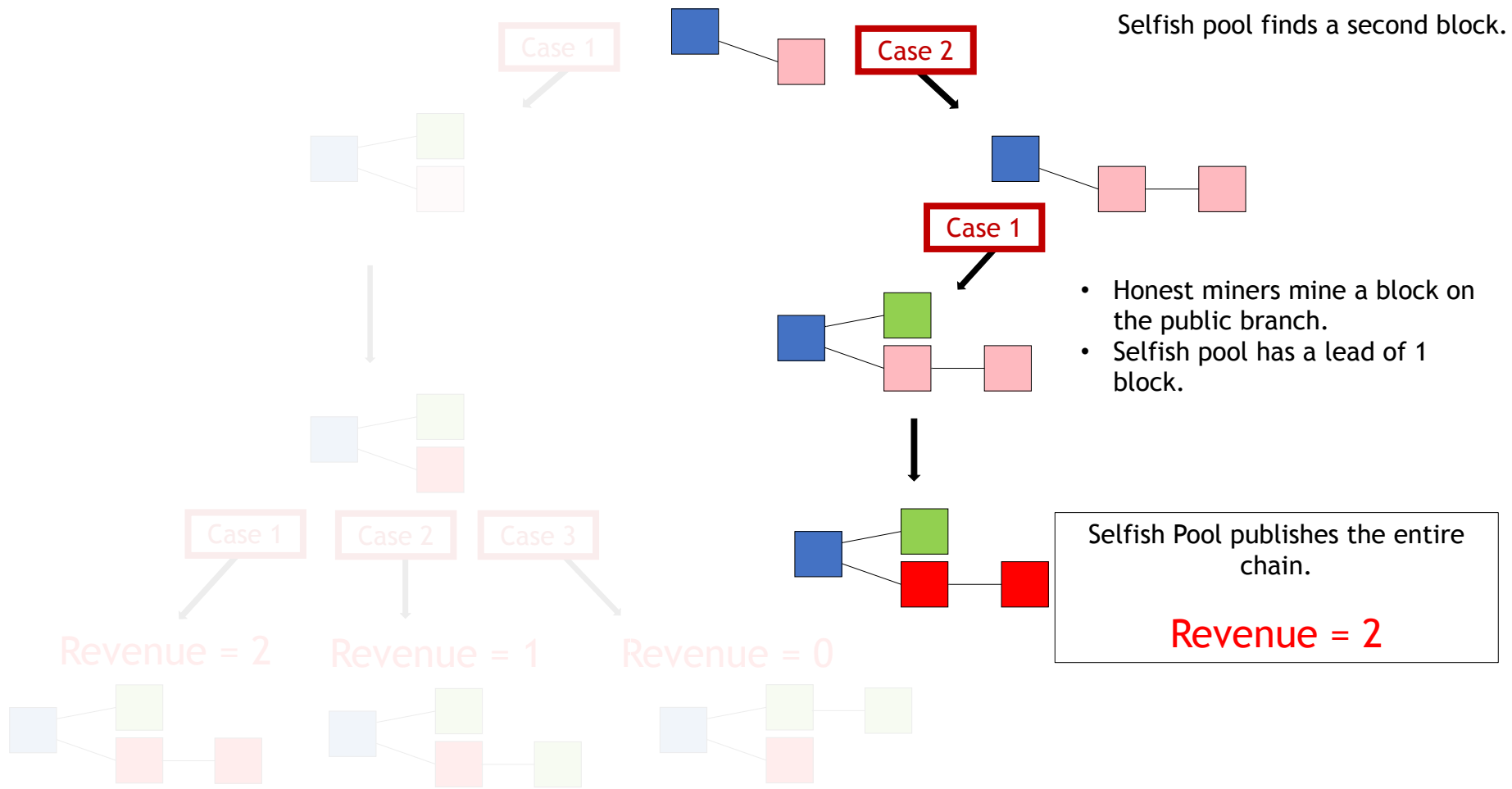
Revenue = 0

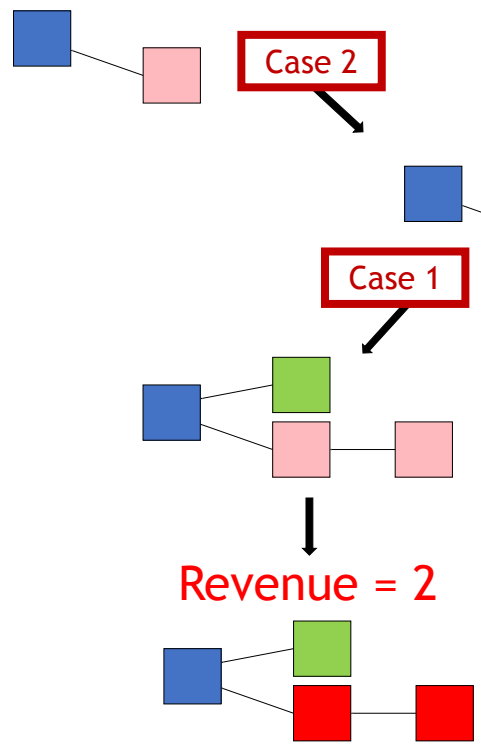
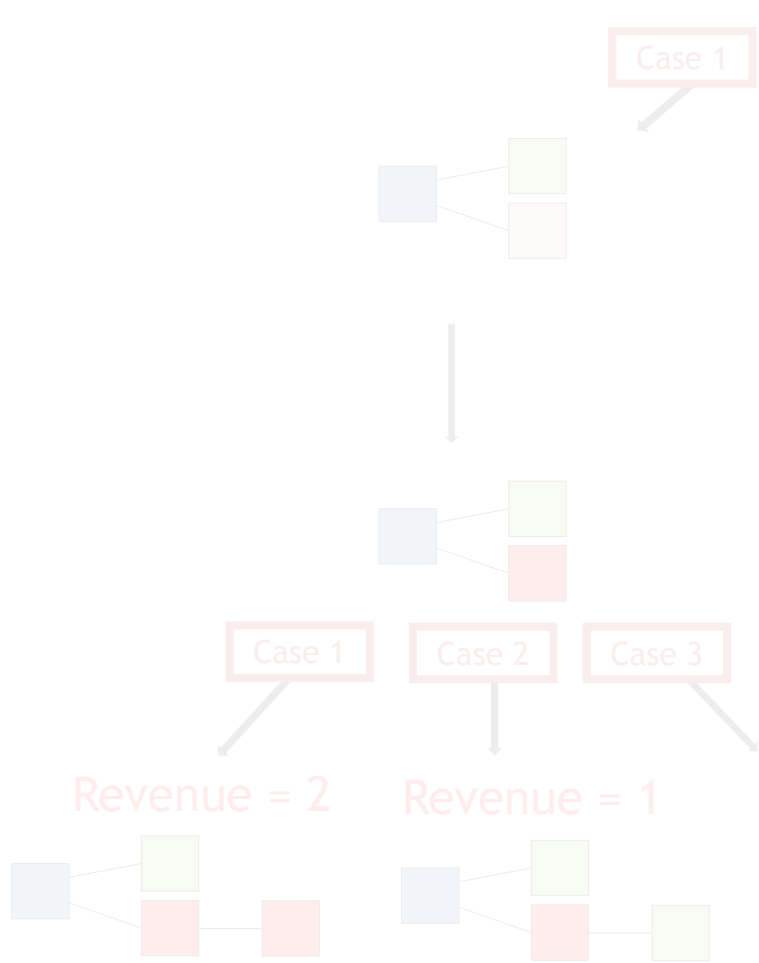
Revenue = 2

Revenue = 1









Selfish pool finds a second block.

- Selfish pool mines a block on their private chain
- Selfish pool gets a lead of >2 blocks.

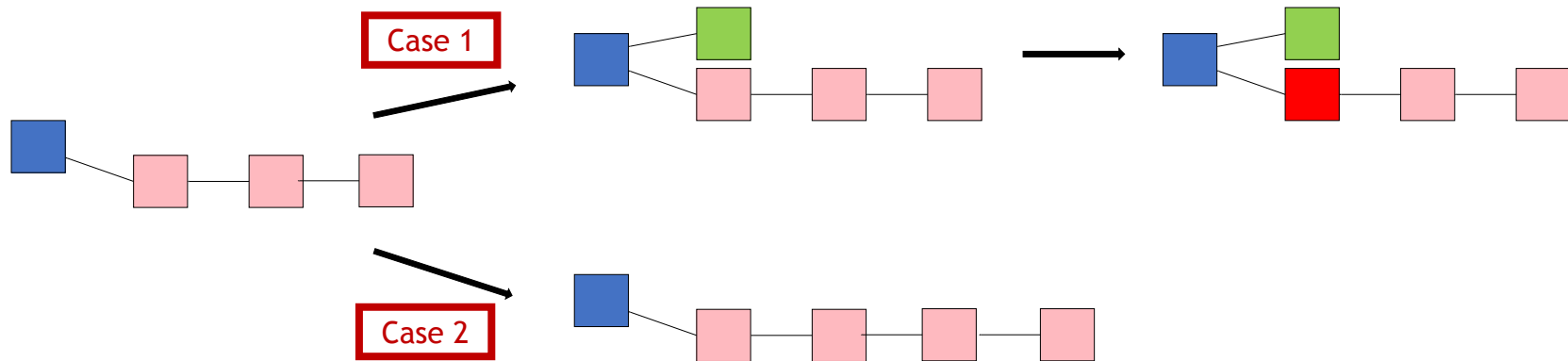


# Selfish Pool gets a lead of $>2$ blocks

- Selfish pool continues to mine on its private branch.
- For each subsequent block mined by an honest party, it publishes one block from its private chain.
- Tries to maintain a lead of 2 blocks for as long as possible.
- If the lead reduces to 1, it publishes its private branch.

Earns revenue for all its blocks.

# Selfish Pool gets a lead of $>2$ blocks



If the selfish pool is in minority, then with a very high probability this lead will eventually reduce to one block.

# Analysis

- Set of miners in the system :  $1, \dots, n$
- Miner  $i$  has mining power:  $m_i$

$$\sum_{i=1}^n m_i = 1$$

- Let the total mining power of selfish pool be:  $\alpha$
- Mining power of others:  $(1 - \alpha)$
- Ratio of honest miners that choose to mine on pool's block:  $\gamma$
- Ratio of honest miners that choose to mine on the other block :  $(1 - \gamma)$

# Analysis: Revenue Rate (Ideal Case)

- Revenue rate of each agent is the revenue earned by it for each block mined in the system.
- Let **revenue rate** of selfish pool be:  $r_{pool}$
- Let total **revenue rate** of others be:  $r_{others}$
- Revenue rate should be proportional to the mining power.

$$r_{pool} \propto \alpha$$

- Ideally,  $r_{pool} + r_{others} = 1$

# Analysis: Revenue Rate (Selfish Mining)

- Since selfish mining causes intentional branching in the blockchain, several mined blocks are not included in the blockchain.
- Total block generation rate drops.
- As a result,  $r_{pool} + r_{others} < 1$

# Analysis: Revenue Rate Ratio

- Actual revenue rate of each agent is the revenue rate ratio.
- Revenue rate ratio of an agent is defined as the ratio of its blocks out of the total blocks added to the main chain

$$R_{pool} = \frac{r_{pool}}{r_{pool} + r_{others}} = \frac{\alpha(1 - \alpha^2)(4\alpha + \gamma(1 - 2\alpha)) - \alpha^3}{1 - \alpha(1 + (2 - \alpha)\alpha)}$$

- Assuming honest majority,

$$0 \leq \alpha \leq \frac{1}{2}$$

- Selfish miners earn more revenue than their mining power if,

$$R_{pool} > \alpha$$

- For a given  $\gamma$ , a selfish miners pool of size  $\alpha$  earns more revenue than its relative size for,

$$\frac{1 - \gamma}{3 - 2\gamma} \leq \alpha \leq \frac{1}{2}$$

$$\frac{1 - \gamma}{3 - 2\gamma} \leq \alpha \leq \frac{1}{2}$$

- Honest miners always mine on the pool's branch

$$\text{For } \gamma = 1, \quad 0 \leq \alpha \leq \frac{1}{2}$$

- Honest miners randomly choose which branch to mine on

$$\text{For } \gamma = \frac{1}{2}, \quad \frac{1}{4} \leq \alpha \leq \frac{1}{2}$$

- Honest miners never mine on the pool's branch

$$\text{For } \gamma = 0, \quad \frac{1}{3} \leq \alpha \leq \frac{1}{2}$$



# Problem with Bitcoin Protocol

- In case of multiple branches of the same length:
  - A miner mines and propagates only the first branch it received.
- There is no measure to guarantee a low  $\gamma$ .
- Sybil attack combined with selfish mining can lead to  $\gamma \approx 1$ .
  - In this case, a selfish pool of any size would earn more revenue than its mining power.
  - Rational miners will join the selfish pool.
  - The selfish pool would increase towards majority.

# Solution: A simple change in the Bitcoin Protocol

- In case a miner encounters multiple branches of the same length:
  - He should propagate all the branches it receives.
  - He should choose which one to mine on uniformly at random.
- This change would yield  $\gamma = \frac{1}{2}$ .
- This change is backward compatible.

# Selfish-mining attacks

- Surprising departure from previous assumptions
- Not yet observed in practice!
- Plausible reason: selfish-mining is detectable, could lead to a crash in exchange rates for Bitcoin

# Punitive forking

- Suppose you want to blacklist transactions from address **X**
  - Freeze an individual's money forever
- Extreme strategy: announce that you will refuse to mine on any chain with a transaction from **X**

# Punitive forking

- Suppose you want to blacklist transactions from address  $X$ 
  - Freeze an individual's money forever
- Extreme strategy: announce that you will refuse to mine on any chain with a transaction from  $X$

With  $\alpha < 0.5$ , you'll soon fall behind the network

# Feather-forking strategy

- To blacklist transactions from  $X$ , announce that you will refuse to mine directly on any block with a transaction from  $X$ 
  - but you'll concede after  $n$  confirming blocks
- Chance of pruning an offending block, when  $n=1$ , is  $\alpha^2$

# Response to feather forking

- For other miners, including a transaction from X induces an  $\alpha^2$  chance of losing a block
- Might be safer to join in on the blacklist
- Can enforce a blacklist with  **$\alpha < 0.5!$**

# Response to feather forking

- For other miners, including a transaction from X induces an  $\alpha^2$  chance of losing a block
- Might be safer to join in on the blacklist
- Can enforce a blacklist with  **$\alpha < 0.5!$**

Success depends on convincing other miners you'll fork



# Feather-forking: what is it good for?

- Freezing individual bitcoin owners
  - ransom/extortion
  - law enforcement?
- Enforcing a minimum transaction fee
  - Current transaction fees are low (about 2% of revenue)
  - But may become significant when mining reward becomes low

# Summary

- Miners are free to implement any strategy
- Very little non-default behavior in the wild
- Game-theoretic analysis necessary
- Recent works in this direction. See, e.g.:  
[Badertscher-Garay-Maurer-Tshudi-Zikas,  
EUROCRYPT'18]