Neutron Activation

Lab course protocol

Group 3

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21/03/2025

Advanced lab course in astronomy Eberhard Karls Universität Tübingen

WiSe 2024/25

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1 Introduction

In this experiment, natural samples of silver and indium are activated using slow (thermal) neutrons from an AmBe (Americium-Beryllium) source. This process, known as *neutron activation*, results in the formation of radioactive isotopes through neutron capture.

The decay of these isotopes is tracked using Geiger-Müller counters, enabling the determination of their decay curves, half-lives, and initial activities. This technique, called *Neutron Activation Analysis (NAA)* - is a powerful, non-destructive method widely used in material analysis and nuclear research.

2 Theory

2.1 Radioactivity: α , β , and γ Decay

Radioactive decay is the spontaneous transformation of an unstable atomic nucleus into a more stable one, accompanied by the emission of particles or electromagnetic radiation:

- α -decay: Emission of a helium nucleus (${}_{2}^{4}$ He), typical for heavy nuclei with a proton surplus. It has a short range (usually only a few *centimetres* in air) and is easily shielded.
- β -decay: These type of decays are a result of the weak interaction (weak nuclear force). β -decays have two subtypes:
 - $-\beta^-$: A neutron transforms into a proton, emitting an electron and an antineutrino:

$$n \rightarrow p + e^- + \bar{\nu}_e$$

 $-\beta^{+}$: A proton becomes a neutron, emitting a positron and a neutrino:

$$p \to n + e^+ + \nu_e$$

• γ -emission: The nucleus transitions from an excited to a lower energy state, emitting a high-energy photon:

$$_{Z}^{A}X^{\ast }\rightarrow _{Z}^{A}X+\gamma$$

Most of the time, these high energy photons interact with matter in three ways - photo effect, Compton effect and pair production.

2.2 Activity

The activity A(t) of a radioactive sample is the number of decays per unit time:

$$A(t) = \lambda N(t) = \lambda N_0 e^{-\lambda t}$$

where:

- λ is the decay constant,
- N(t) is the number of undecayed nuclei at time t, and N_0 is the initial number of nuclei.
- A is measured in **Becquerel** (Bq), where 1 Bq = 1 decay/s.

The half-life $t_{1/2}$ (i.e, the time after which exactly half of the initial activity remains) is given by:

$$t_{1/2} = \frac{\ln 2}{\lambda}$$

2.3 Differential Equations for Decay and Activation

For pure radioactive decay without any kind of external input:

$$\frac{dN}{dt} = -\lambda N$$

When new radioactive nuclei are being produced (e.g., during activation), the equation becomes:

$$\frac{dN}{dt} = -\lambda N + P$$

where P is the **production rate**. Solving this gives the time-dependent activity:

$$A(t_a) = A_S \left(1 - e^{-\lambda t_a} \right)$$

with $A_S = \sigma \Phi n$ as the saturation activity, and t_a being the activation time.

2.4 Saturation Activity

The saturation activity A_S is the maximum activity that can be reached under continuous irradiation:

$$A_S = \sigma \Phi n$$

It is approached asymptotically as $t_a \to \infty$. This value depends on:

- σ : Neutron capture cross-section,
- Φ: Neutron flux,
- n: Number of target atoms in the irradiated sample.

2.5 Creation of Free Neutrons

Free neutrons are not stable in nature (mean lifetime ~ 886 s) and must be produced via nuclear reactions. In this experiment, a (α, \mathbf{n}) reaction in an AmBe source is used:

$$^{9}\text{Be} + \alpha \rightarrow ^{12}\text{C} + n$$

Here, ²⁴¹Am emits α particles, which interact with ⁹Be to release neutrons. The resulting fast neutrons are slowed down (moderated) using paraffin to become *thermal neutrons* ($E \approx 0.025 \text{ eV}$), which are highly effective in neutron capture reactions.

An example of neutron capture (an (n, γ) reaction) relevant to this experiment:

$$Ag^{107,109} + n \rightarrow Ag^{108,110*} \rightarrow Ag^{108,110} + \gamma$$

These reactions result in radioactive isotopes whose decay can then be studied.

3 Experiments

3.1 Description of the Experimental Procedure

The experiment is divided into several parts, starting with detector calibration and background measurement, followed by the activation and decay analysis of silver and indium samples. The following steps summarize the procedure:

1. Calibration of the Geiger-Müller counters:

- A ⁶⁰Co source is generally placed next to the detector for calibration. However in our case, we have chosen a sample of Thorium.
- The voltage applied to the GM tubes is varied incrementally, and the corresponding count rates are recorded using a scaler.
- A voltage vs. count rate plot is created to identify the plateau region.
- The working voltage is chosen within the first third of the plateau to ensure stable operation.

2. Measurement of the background radiation:

- With no active source or sample present, a 60-minute background measurement is taken. We have taken a 45-minute measurement.
- Data is recorded in intervals of $\Delta t = 60$ s using the Cassylab software. For our experiment, we have used a 5 minute interval.

3. Preparation of the samples:

- Natural silver and indium metal samples are used.
- Samples are handled only with pliers and inserted into the neutron source using aluminum rods.
- Care is taken to avoid contact with the rod ends that are inserted into the source, due to their own activation.

4. Activating and measuring the decay of silver:

- The silver sample is irradiated for various activation times: 5 s, 10 s, 20 s, 30 s, 45 s, 60 s, 90 s, 2 min, 5 min, and 15 min.
- After irradiation, the sample is quickly transferred to the detector setup.
- Decay measurements are conducted for 400 s total duration, with a counting interval of $\Delta t = 5$ s.
- The time offset between the end of irradiation and start of measurement is recorded with a stopwatch for later correction.

5. Activating and measuring the decay of indium:

- The indium sample is irradiated and then measured in the same manner as the silver sample.
- Decay is recorded using the parameters: 30 minutes total, with $\Delta t = 5$ s intervals.
- The activation time and timing offset are recorded.

3.2 Sketch and Description of the Neutron Source

The neutron source used is a moderated Americium-Beryllium (AmBe) source embedded within a layered shielding structure:

- The source emits α particles from ²⁴¹Am, which interact with beryllium to release neutrons via the (α, n) reaction.
- It is housed inside a cube of paraffin (edge length: 150 cm), with inner solid paraffin and outer layers made of borated paraffin bricks.
- A 1 cm thick lead shield surrounds the source to block γ radiation.
- The sample holder is inserted into slits at the back of the assembly, which have direct line-of-sight to the neutron source.

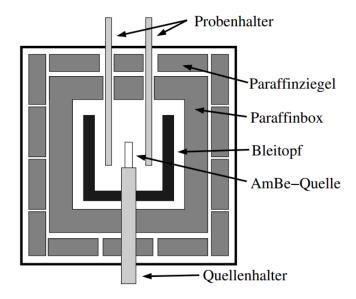


Figure 1: AmBe source setup (Schematic).

3.3 Sketch and Working Principle of the Detector

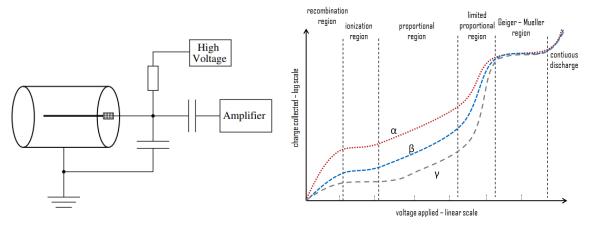
In this experiment, a Geiger-Müller (GM) counter is used to detect the radiation emitted by the activated silver and indium samples. The GM counter is a type of gaseous ionization detector, consisting of a cylindrical tube filled with a noble gas at low pressure and a central wire anode. When ionizing radiation enters the detector through a thin mica window, it ionizes the gas, creating electron-ion pairs.

Due to the high voltage applied across the electrodes, these primary electrons are rapidly accelerated, gaining enough energy to cause further ionization — resulting in an *avalanche* of secondary electrons. This avalanche produces a measurable current pulse, which is counted as a detection event.

In the *Geiger-Müller (plateau) region*, the size of the output pulse is independent of the energy of the incoming radiation, allowing only particle counting, not energy discrimination. To prevent continuous discharge, the tube includes a *quenching gas* that limits the avalanche.

While GM counters cannot differentiate between types or energies of radiation, they are extremely useful for measuring decay rates and background radiation due to their simplicity and sensitivity.

In this experiment, two GM tubes are used, and the operating voltage is chosen from the plateau region of the tube's characteristic curve, ensuring a stable response.



(a) Working principle of a Geiger-Müller (b) I-V characteristic curve of a GM counting counter tube (Source: [Pow25])

Figure 2: Schematic diagram of a Geiger-Müller counter and its I-V characteristic curve. The plateau region is used in this experiment for stable operation.

3.4 Capture and Decay Reactions of Relevant Isotopes

• Silver Activation (natural silver contains ¹⁰⁷Ag and ¹⁰⁹Ag):

$$^{107} \mathrm{Ag} + n \to ^{108} \mathrm{Ag}^* \to ^{108} \mathrm{Ag} + \gamma \quad (\mathrm{T}_{1/2} \approx 2.4 \, \mathrm{min})$$

 $^{109} \mathrm{Ag} + n \to ^{110} \mathrm{Ag}^* \to ^{110} \mathrm{Ag} + \gamma \quad (\mathrm{T}_{1/2} \approx 24 \, \mathrm{s})$

• Indium Activation (natural indium is mostly ¹¹⁵In):

$$^{115}{\rm In} + n \rightarrow ^{116}{\rm In}^* \rightarrow ^{116}{\rm In} + \gamma \quad ({\rm T}_{1/2} \approx 54\,{\rm min})$$

• These reactions produce radioactive isotopes that decay via β^- emission, and their decay rates are measured in this experiment.

Branching Ratios

In general, radioactive isotopes can decay via multiple channels, each with a characteristic probability known as the *branching ratio*. These ratios quantify the likelihood of a nucleus decaying through a particular path relative to all possible decay modes.

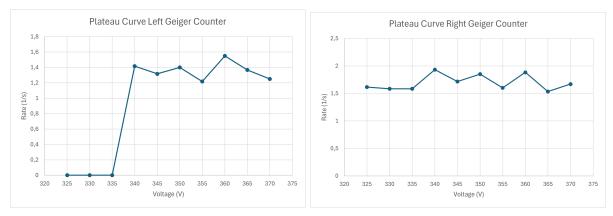
In this experiment, however, the activation products (108 Ag, 110 Ag, and 116 In) **decay predominantly via a single** β^- **decay mode**. As a result, only the main decay channel is considered in the analysis, and branching ratios are not treated separately in the data evaluation. Nevertheless, they are implicitly reflected in the total measured activity.

4 Analysis

4.1 Plateau Curve and Operating Voltage

To determine a suitable operating voltage for the Geiger-Müller counters, the count rate was measured as a function of applied voltage using a ⁶⁰Co calibration source. The resulting plateau curves for both the left and right detectors are shown in Figure. (Add reference)

The plateau region corresponds to the range where the count rate remains approximately constant despite increasing voltage, indicating stable detector operation. Based on the curves, a voltage of 325 V was selected, lying within the first third of the plateau. This ensures reliable detection while minimizing the risk of continuous discharge or excessive dead time.



- (a) Plateau Curve for left Geiger Counter
- (b) Plateau Curve for Right Geiger Counter

Figure 3: Plateau Curves

4.2 Background

In order to find the correct half life and initial activities, we need to substract the background radiation in the lab. We measured this using the geiger counters for 45 minutes with an interval of 5 minutes.

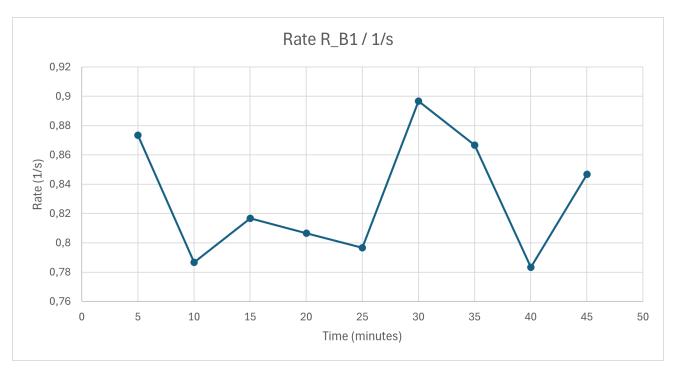


Figure 4: Background Radiation Measured using both of the geiger counters

On average we found the background radiation to be 0.83 counts/second. This is subtracted from the next measurements.

4.3 Silver Decay Curves

4.4 Indium Decay Curves

The Indium sample was activated over a period of 3-4 hours. The time taken for the sample to travel from the neutron source to the counter was 18 seconds.

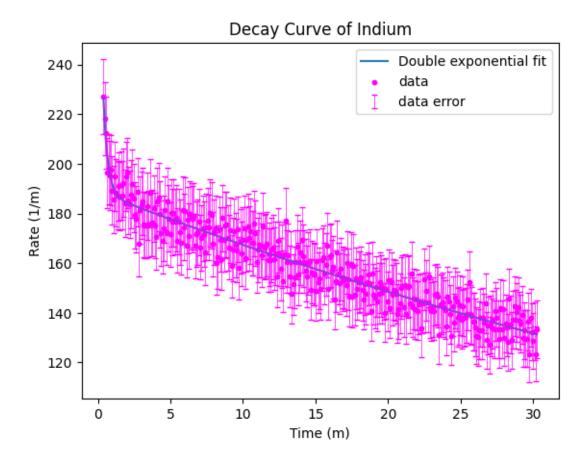


Figure 5: Activity of Activated Indium Sample over time. The data points are fitted with a double exponential curve

The decay curve obtained in figure 5 is fitted with a double exponential curve of the form $a_1e^{b_1x} + a_2e^{b_2x}$. This fits the two different decays happening in the sample. ¹¹⁶In decays largely by β^- decay with a half life of 14.10 seconds[Jaea] and ¹¹⁷In also decays by β^- with a half life of 43.2 minutes[Jaeb].

With the double exponential fitting we found decay contants $\lambda_1 = 3.21 \ min^{-1}$ and $\lambda_2 = 0.0119 \ min^{-1}$ which imply half lives of 12.93 seconds and 57.8 minutes. These values are relatively close to the actual half lives we expect. For Indium, we found an initial activity of 321 counts/minute.

The observed half lives fit the expected values relatively well, with some errors being present due to errors in handling the experiment and impurities in the material.

5 Conclusions

We initally found the plateau region of the geiger coutners and set it to 360 V for our experiments. We observed the background counts for 45 minutes, giving us an activity of 0.83 counts/second.

For silver, we found We were unable to find ...

For the Indium sample we obtained the decay curve and fitted it with a double exponential function to obtain half lives of two decays happening in the sample. The observed values of half life were relatively close to their theoretical counterparts.

References

- [Jaea] Andreas Jaeck. *Indium-116 isotopic data and properties*. en. URL: https://chemlin.org/isotope/indium-116.
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