

$$1) I_1 = \frac{2h}{3} (f(0) + 4f(2) + f(4)) =$$

$$I_2 = \frac{h}{3} (f(0) + 4f(1) + f(2)) + \frac{h}{3} (f(2) + 4f(3) + f(4))$$

$$A = I_2 + \frac{I_2 - I_1}{2^n - 1} = I_2 + \frac{I_2 - I_1}{16 - 1} = \frac{16}{15} I_2 - \frac{1}{15} I_1$$

$$\frac{16}{15} I_2 = \frac{h}{45} (16f(0) + 64f(1) + 32f(2) + 64f(3) + 16f(4))$$

$$\frac{1}{15} I_1 = \frac{h}{45} (2f(0) + 0f(1) + 8f(2) + 0f(3) + 2f(4))$$

$$A = \frac{h}{45} (14f(0) + 64f(1) + 24f(2) + 64f(3) + 14f(4))$$

$$= \frac{2h}{45} (7f(0) + 32f(1) + 12f(2) + 32f(3) + 7f(4)) \Rightarrow 4^{\text{th}} \text{ order interpolating polynomial } \int_{x_0}^{x_4} f(x) dx$$