T-Test

- mean of two samples or to compare a sample mean to a known population mean.
- Of It is used when the population standard deviation is unknown and the sample size is small.
- 10 There are three main type of t-test ____

A one sample t-test

the one sample t-test is used to compare the mean ob a single sample to a unown population moan. Here our Null hypothesis be stated that there is no significant different difference between the sample mean and the population mean.

O Ascumption ?

Normality (ii) Independence (the observation of sample must be independent (iii) Random sampling (iv) Ununown population std.

(a) suppose a manufacturer claims that the average Weight of their new chocolate bars is 50 grams, we nightly doubt that and Want to check this so we drew out a sample of 25 chocolate bars and measured their Weight, the sample mean came out to be 49.7 gm. and the sample so was 1-2 gm. Consider the significance level to be 0.05.

Mull Hypothesis (Ho): there is no signiBicanco dir Beronce het Ween

A Verage Weight OF chocolate bar is 50 gm.

4. = 50

Alternative Hypothesis (Ha): 450

We have population mean (1) = 50, sample mean $(\bar{x}) = 49.7$ cample 5.0 (6) = 1.2 N = 25

Now, We need to Bind the T-statistic

Hele

T- statistic =
$$\frac{49-7-50}{25}$$
 = -1.25

10 Now, We are going to find out the p-value.

As our p-value > signi bicance level (0.05)

-then we can't reject our Null hypothesis.

B Independent Wo-sample t-tost o

The independent two sample t-test is hypothesis states that there is no significance difference between the means of two samples.

It is also known as unpaired t-test.

(D) Assumption

- 1) Independence of observations 2) Normality 3) Equal Variance (+wo sample must be independent) (Homoscedasticity)
- 1 Random Sampling
- Suppose a Wobsite owner claims that there is no difference in the average time spend on their website between desutop and mobile users. To test this claim, we collect data for 30 desutop users and 30 mobile users regarding the time spend on the website in minutes. The sample statistics are as following

destatop users = [12,15, 18,16,20, 17, 14,22, 19,21,23,18,25,17,16,24,
20, 19, 22, 18, 15, 14, 23, 16, 12,21, 19,17, 20,14]

Mobile users = $\begin{bmatrix} 10, 12, 14, 13, 14, 15, 11, 17, 14, 16, 18, 14, 20, 15, 14, 19, 16, 15, 17, 14, 12, 11, 18, 15, 10, 16, 15, 13, 16, 11 \end{bmatrix}$

and desktop &D = 9.5 and Mobile &D = 2.7.

O First let construct our null hypothesis as Well as alternative

nypothesis

Null hypothesis (Ho): There is Decytop User Mean = Mobile user Mean

Alternative hypothesis (Ha): Desytop user mean = Mobile user Mean

we need to Bindout t-statistic. + he Bormula ob T-statistic be.

$$t = \frac{\text{First sample mean}}{\frac{51^2}{n_1} + \frac{52^{\frac{1}{2}}}{n_2}}$$

where
$$S_1 = \text{First sample SD}$$
 $n_1 = \text{Birst sample size}$
 $S_2 = \text{Second sample SD}$
 $n_2 = \text{Second sample Size}$

Here t-statistic =
$$\frac{18.5 - 14.3}{\sqrt{\frac{3.5^2}{30} + \frac{2.7^2}{30}}} = \frac{4.2}{0.81} = 5.20$$

Now, degree of Breedom =
$$(n_1-1) + (n_2-1)$$

= 29+29

this t-statistic and dB (58) We have p-value = Retire Now, Corrosponding = 2. 7 X1006



- so, clearly p-value < level ob significance (0.05)
- so, Null hypothesis canbe rejected.
- so, the average time spend on deskdom and average time spend on mobile are different (proved)

Pair-2 sample + test of

A paired two sample t-test, also known as a dependent or paired samples t-test, is a statistical test used to compare the means of two related or dependent groups.

Assum ptions

- O paired observations @ Normality @ Independence ob pairs (Fach pair ob observations should be independent).
- (4) Let's assume that a Bitness center is evaluating the ebbectiveness of a new 8-week weight loss program. They enroll 15 participants in the program and measure their weights before and abter the program.

The goal is to test whether the new weight loss program leads to a significante reduction in the participant weights.

Bebore the program -

[80, 92, 75, 68, 85, 78, 73, 90, 70, 88, 76, 84, 82, 77, 91]

ABter the program -

[78, 93, 81, 67, 88, 76, 74, 91, 60, 88, 77, 81, 80, 79, 88]

Mall hypothesis: (Ha): Mean | before = Moan | ABter

Alternative hypothesis (Ha): Mean | before > Mean | aBter

bosically it is $\frac{\overline{X}_{dirb}}{S \cdot D_{dirb}}$

so, here t-statistic should be ____

-0.0667

= -0.0667

= -0.108

× - 0.11

so, we see that

P-Value > level ob signi Bicance

(0.05)

So, We cannot reject our null happothesis.

so, We have not enough excidence

mean & after program.

to say that mean of be Bord is less than

(Xdigg = Mean of the difference

Columns of before and after)

Means Birst We calculate the

difference of before columns and

After column then we calculate

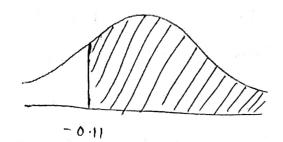
the mean of that me new edumn.

Some and siphiff = Siphoff that

New column

1 Here _

Attack word to the		
Before	ABter	Colcumn
80		
92	₹ 8	1 min 2 232 1
75	93	1 12 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
5.1168	81	
85	88	a g
78	76	2
73	74	-1.2
90 70	91	-1
& 8	6 9	•1
₹6	88	0
84	77	-1
8 Q 7 7	81	3
91	80	2
	** 9	- 2 2
	ing and an experience of the second	3



we got p-Value = 0.5424

co, p-Value > levol of significance (0.05)

so, We can't reject our null hypothesis, so that mean We havenote enough evedance to prove that the mean average of sweight before program is greater than the mean average of weight program. (Proved)

(common Senario Where paired t-test is used)

(D) Match or correlated group (2) Before and After studies problems

One simple or single simple t test:

Let we have the titanic dataset and we are assuming that average age of the passengers would be 35,whereas some of us claim that it would be less than 35. So we are going to do the t-test for this problem statement.

Answer:

```
so our null hypothesis (Ho): Average age of the passenger is 35 alternative hypothesis(Ha): Average age is less than 35
```

```
In [1]:
```

```
import pandas as pd
import numpy as np
import seaborn as sns
import scipy.stats as stat
```

```
In [2]:
```

```
df=sns.load_dataset("titanic")
```

```
In [37]:
```

```
df["age"].isnull().sum()
```

Out[37]:

177

```
In [38]:
```

```
pop=df["age"].dropna()
```

```
In [39]:
```

```
pop.isnull().sum()
```

Out[39]:

0

let suppose we have taken 25 sample from the population.

```
In [40]:
```

```
sample=pop.sample(25).values
```

```
In [41]:
sample
Out[41]:
array([40., 42., 19., 37., 30., 29., 2., 22., 26.,
           , 22. , 15. , 10. , 51. , 31. , 43.
                                                     , 19. , 4.
      27.
            , 32. , 0.42, 21. , 38. , 35. , 31.
now we have to test the assumptions
In [42]:
#checking for the normality
from scipy.stats import shapiro
In [43]:
result=shapiro(sample)
p_value=result[1]
if p_value>0.05:
   print("our sample is normally distributed.")
   print("our sample isn't normally distributed.")
our sample is normally distributed.
In [44]:
pop_mean=35
In [45]:
from scipy.stats import ttest_1samp
In [46]:
result=ttest_1samp(sample,pop_mean)
p_value=result[1]/2 # as it is left-tailed test
if p value>0.05:
   print("Our null hypothesis is true.Average age of the passenger is 35 yr")
else:
   print("we reject our null hypothesis and Average age is less than 35 yr")
we reject our null hypothesis and Average age is less than 35 yr
In [47]:
result
Out[47]:
Ttest_1sampResult(statistic=-3.157360962130363, pvalue=0.00425752320269086
2)
```

```
In [49]:
```

```
# checking our test with the population dataset
df["age"].mean()
```

Out[49]:

29.69911764705882

Independent 2 sample t-test:

now we are claiming that the average age of male and average age for female would be similar.for this we are going to do the t-test.

Answer

null hypothesis(Ho): average age of male is similar to the average age of female

alternative hypothesis(Ha):average age of male is not similar to average age of female.there is significant difference between them.

In [50]:

```
male_age=df[df["sex"]=='male']["age"]
female_age=df[df["sex"]=='female']["age"]
```

In [51]:

```
pop_male_age=male_age.dropna()
pop_female_age=female_age.dropna()
```

In [52]:

```
sample_male=pop_male_age.sample(25).values
sample_female=pop_female_age.sample(25).values
```

In [53]:

```
sample_male
```

Out[53]:

```
array([11. , 74. , 18. , 1. , 65. , 45. , 19. , 38. , 22. , 31. , 7. , 4. , 44. , 28. , 40.5 , 21. , 36. , 34. , 0.42, 33. , 50. , 70.5 , 70. , 32. , 18. ])
```

```
In [54]:
sample female
Out[54]:
array([14., 30., 7., 18., 16., 40., 49., 38., 43., 38., 45., 29., 45.,
       36., 4., 35., 41., 29., 51., 22., 19., 17., 30., 54., 21.])
checking for assumptions
In [55]:
#normality check:
In [56]:
l={"sample_male":sample_male, "sample_female":sample_female}
for i in 1:
   result=shapiro(l[i])
   p_value=result[1]
   if p_value>0.05:
        print(f"{i} is normally distributed")
   else:
        print(f"{i} isn't normally distributed")
sample_male is normally distributed
sample_female is normally distributed
In [57]:
# variance test
In [58]:
result=stat.levene(sample_male,sample_female)
if result[1]>0.05:
   print("these two sample columns have equal variance")
else:
   print("variance of these two columns are not equal")
these two sample columns have equal variance
testing the t-test:
In [62]:
result=stat.ttest_ind(sample_male,sample_female)
if result[1]>0.05:
```

we can't reject our null hypothesis so average age of male is similar to a verage age of female

else:

print("we can't reject our null hypothesis so average age of male is similar to aver

print("average age of male is not similar to average age of female.there is signific

pair two sample t test:

Let's assume that a fitness center is evaluating the effectiveness of a new 8-week weight loss program. They enroll 15 participants in the program and measure their weights before and after the program. The goal is to test whether the new weight loss program leads to a significant reduction in the participants' weight. Before the program: [80, 92, 75, 68, 85, 78, 73, 90, 70, 88, 76, 84, 82, 77, 91] After the program: [78, 93, 81, 67, 88, 76, 74, 91, 69, 88, 77, 81, 80, 79, 88] Significance level $(\alpha) = 0.05$

answer:

so we have data of weight Before the program: [80, 92, 75, 68, 85, 78, 73, 90, 70, 88, 76, 84, 82, 77, 91] and After the program: [78, 93, 81, 67, 88, 76, 74, 91, 69, 88, 77, 81, 80, 79, 88]

now our null hypothesis(Ho):mean(before)=mean(after)

alternative hypothesis(Ha):mean(before)>mean(after)

now we need to test our assumptions :

```
In [64]:
```

```
# checking the normality of the different columns of these two columns column_before=np.array([80, 92, 75, 68, 85, 78, 73, 90, 70, 88, 76, 84, 82, 77, 91]) column_after=np.array([78, 93, 81, 67, 88, 76, 74, 91, 69, 88, 77, 81, 80, 79, 88])
```

```
In [65]:
```

```
diff_column=column_before-column_after
```

In [66]:

```
diff_column
```

Out[66]:

```
array([2, -1, -6, 1, -3, 2, -1, -1, 1, 0, -1, 3, 2, -2, 3])
```

In [71]:

```
result=shapiro(diff_column)
p_value=result[1]
if p_value>0.05:
    print("normally distributed")
else:
    print("not normally distreibuted")
```

now we need to find out the t-statistic.

In []:

```
In [72]:
t_statistic=diff_column.mean()/(diff_column.std()/np.sqrt(15))
In [73]:
t_statistic
Out[73]:
-0.10850778933039285
this the right-tailed test. now we need to find out the p value with respect to t statistic
In [76]:
p_value=stat.t.sf(t_statistic,14)
In [77]:
if p_value>0.05:
    print("we can't reject our null hypothesis and mean(before)=mean(after)")
    print("we reject our null hypothesis and (Ha):mean(before)>mean(after)")
we can't reject our null hypothesis and mean(before)=mean(after)
```