MAT 1204 - DIFFERENTIAL EQUATION I

Assignment 2

Answer ALL questions and submit solutions for 1[i,iii,v]; 2[i,ii,iv], 3[i, ii, iv]; 4[i, ii, v,vi] on or bevore 22nd, May, 2023.

1. Solve each of the following differential equations:

i.
$$(D^2 - 8D + 15)y = 0$$

ii.
$$(D^2 + 4D + 5)y = 0$$

iii.
$$(D^8 + 6D^6 - 32D^2)y = 0$$

iv.
$$(D^4 - 4D^3 + 8D^2 - 8D + 4)y = 0$$

v.
$$(D^3 + D^2 + 4D + 4)y = 0$$
 if $y(0) = 0, y'(0) = 0, y''(0) = -5$.

2. Solve the following differential equations:

i.
$$(D^2 + 6D + 9) y = 5e^{3x}$$

ii.
$$(D^2 - 6D + 9) y = 6e^{3x} + 7e^{-2x} - 2$$

iii.
$$(D^3 + 3D^2 + 3D + 1) y = e^{-x}$$

iv.
$$(D-1)^3 y = 16e^{3x}$$

v.
$$(D^2 - D - 6)$$
 $y = e^x \cosh 2x$.

3. Solve the following differential equations:

i.
$$(D^2 - 4D + 4) y = x^3 e^{2x}$$

ii.
$$(D^2 - 5D + 6) y = e^x \cos 2x$$

iii.
$$(D^2 + 5D + 6) y = e^{-2x} \sec^2 x (1 + \tan x)$$

iv.
$$(D^2 - 6D + 13) y = 8e^{3x} \sin 4x + 2^x$$

4. Solve the following differential equation:

i.
$$(D^2 + 2D + 1) y = 2x + x^2$$

ii.
$$(D^3 - 2D + 4) y = x^4 + 3x^2 - 5x + 2$$

iii.
$$(D^3 + 3D^2 + 2D)y = x^2$$

iv.
$$(D^2 - 2D + 1)y = x \sin x$$

v.
$$(D^2 - 2D + 1) y = xe^x \sin x$$

vi.
$$(D^2 + 9) y = \sec 3x$$

vii.
$$(D^3 + D^2 - D - 1) y = \cos 2x$$