

$$4 \quad A \rightarrow F = f(n) = 3 + 0 = 13$$

$$A \rightarrow B \rightarrow D \rightarrow E = f(n) = 1 + 2 + 5 + 6 = 14$$

$$A \rightarrow B \rightarrow C \rightarrow E = f(n) = 1 + 1 + 3 + 6 = \underline{11}$$

$$5. \quad A \rightarrow F = f(n) = 13 + 0 = 13$$

$$A \rightarrow B \rightarrow D \rightarrow E = f(n) = 1 + 2 + 5 + 6 = 14.$$

$$A \rightarrow B \rightarrow C \rightarrow E \rightarrow F = f(n) = 1 + 1 + 3 + 2 + 0 = \underline{7}.$$

$$5) \quad CV = \frac{100}{100} \times 100 = 100$$

$$4) \quad 100 - 100 = 0$$

$$3) \quad S = \sqrt{\sigma^2}$$

$$\mu p \text{ var}(m)$$

$$2) \quad \sigma^2 = \sum_{i=1}^n (x_i - \bar{x})^2$$

$$\mu p \cdot \mu m(x)$$

$$1) \quad x(n) - x_1$$

$$\mu p \cdot \mu m(n) -$$

A* Search:

> In A* search Algorithm, we use search heuristic $h(n)$ as well as the cost to reach the node $g(n)$. Hence we can combine both costs as following, and this sum is called as a distance number $f(n)$.

> It has combined features of uniform cost search and greedy best-first search.

$$f(n) = g(n) + h(n).$$

where,

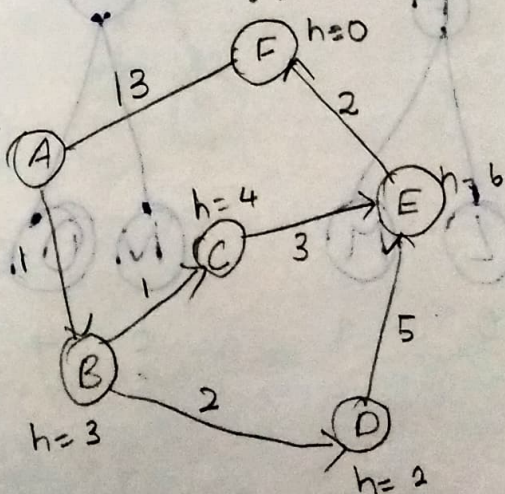
$g(n) \rightarrow$ cost of the path from start node to node n .

$h(n) \rightarrow$ cost of the path from node n to goal state (heuristic function).

Eg

$$F(n) = g(n) + h(n).$$

goal node.



$$1) A \rightarrow B = f(n) = 1 + 3 = 4$$

$$A \rightarrow F = f(n) = 13 + 0 = 13$$

$$2) A \rightarrow F = f(n) = 13$$

$$A \rightarrow B \rightarrow C = 1 + 1 + 4 = 6$$

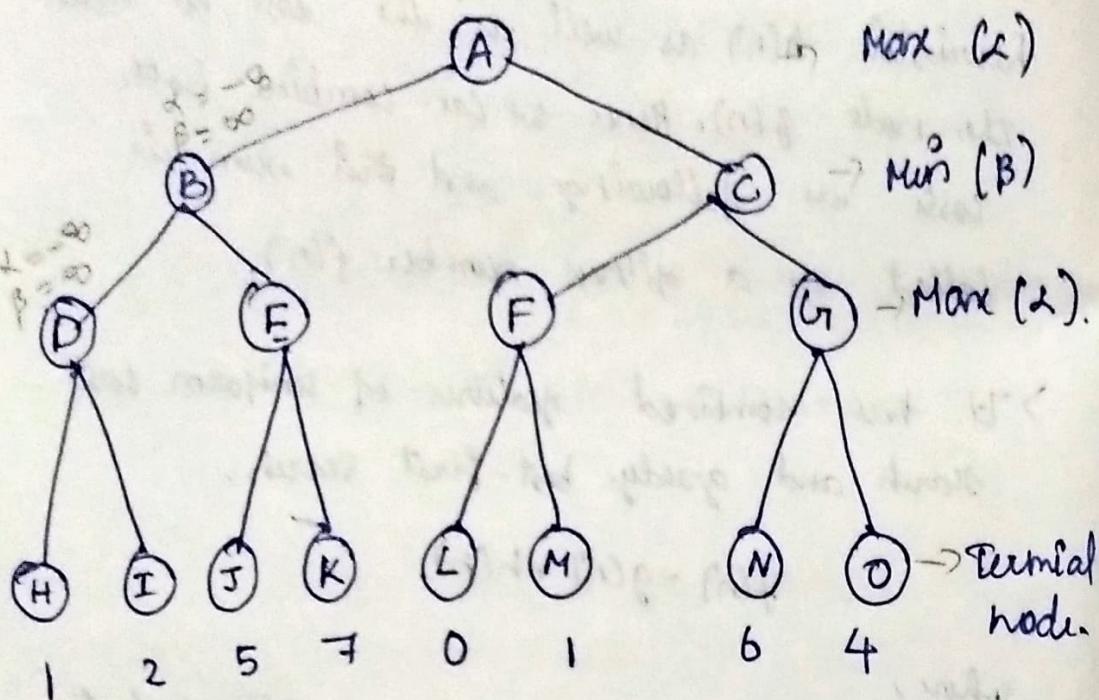
$$A \rightarrow B \rightarrow D = 1 + 2 + 2 = 5$$

$$3) A \rightarrow F = f(n) = 13 + 0 = 13$$

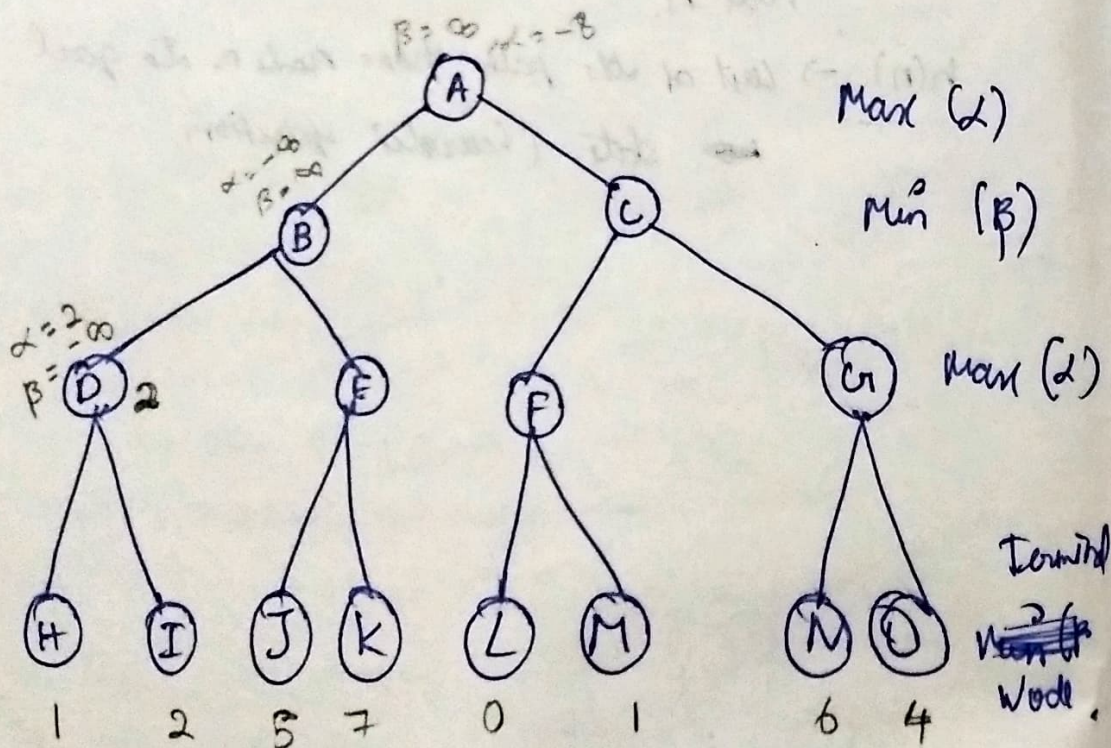
$$A \rightarrow B \rightarrow C = f(n) = 1 + 1 + 4 = 6$$

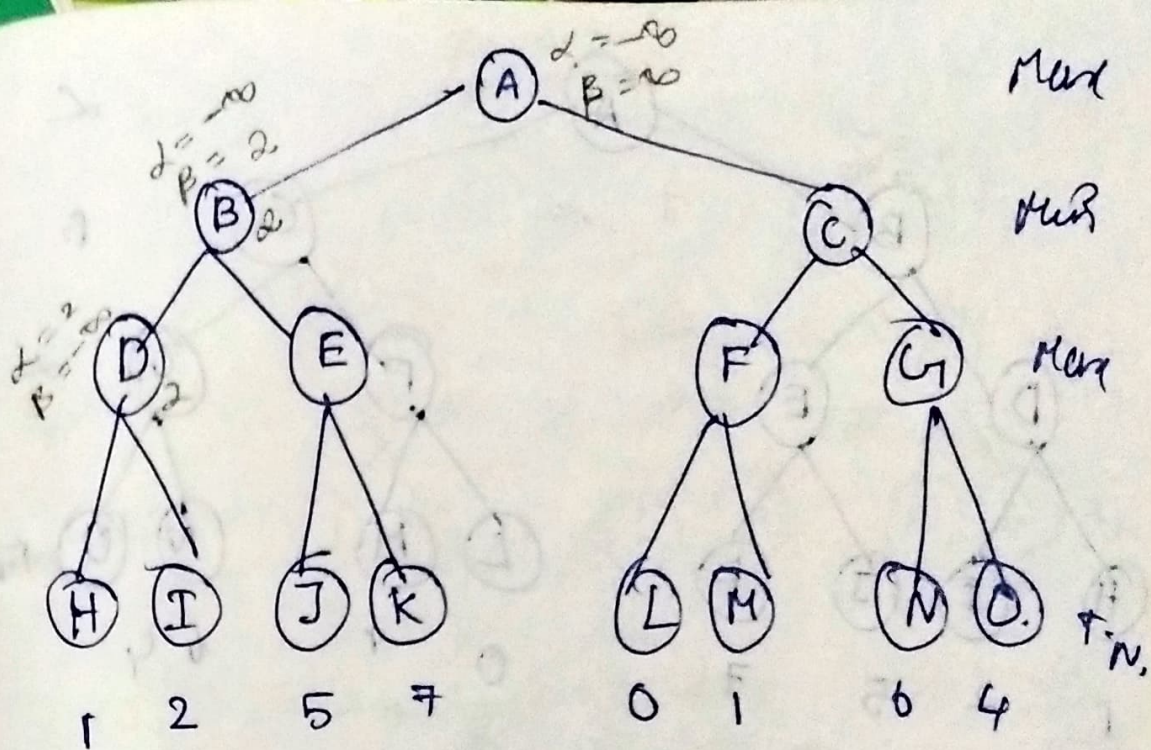
$$A \rightarrow B \rightarrow D \rightarrow F = 8 + 6 = 14$$

Alpha Beta Pruning:

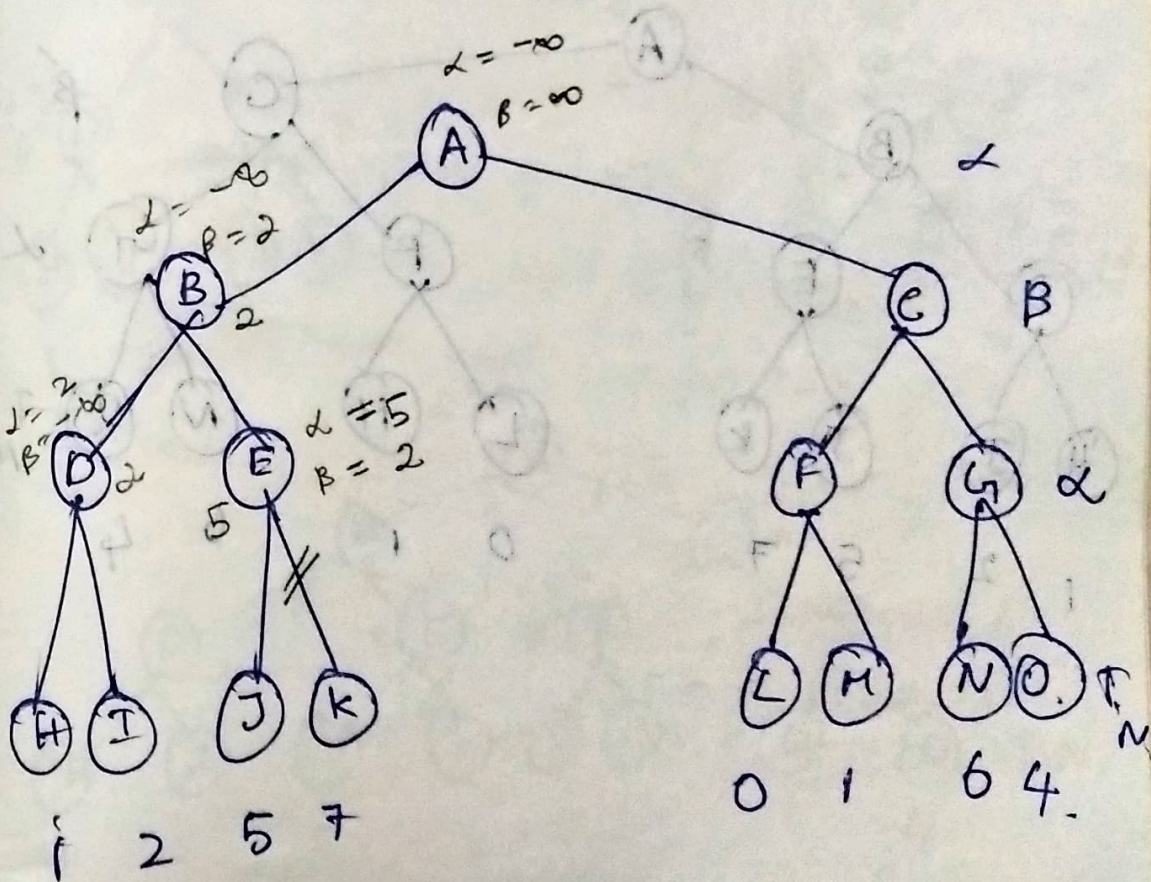


$$(-\infty, 1) = \alpha = 1, (1, 2) = \alpha = 2, \beta = \infty$$





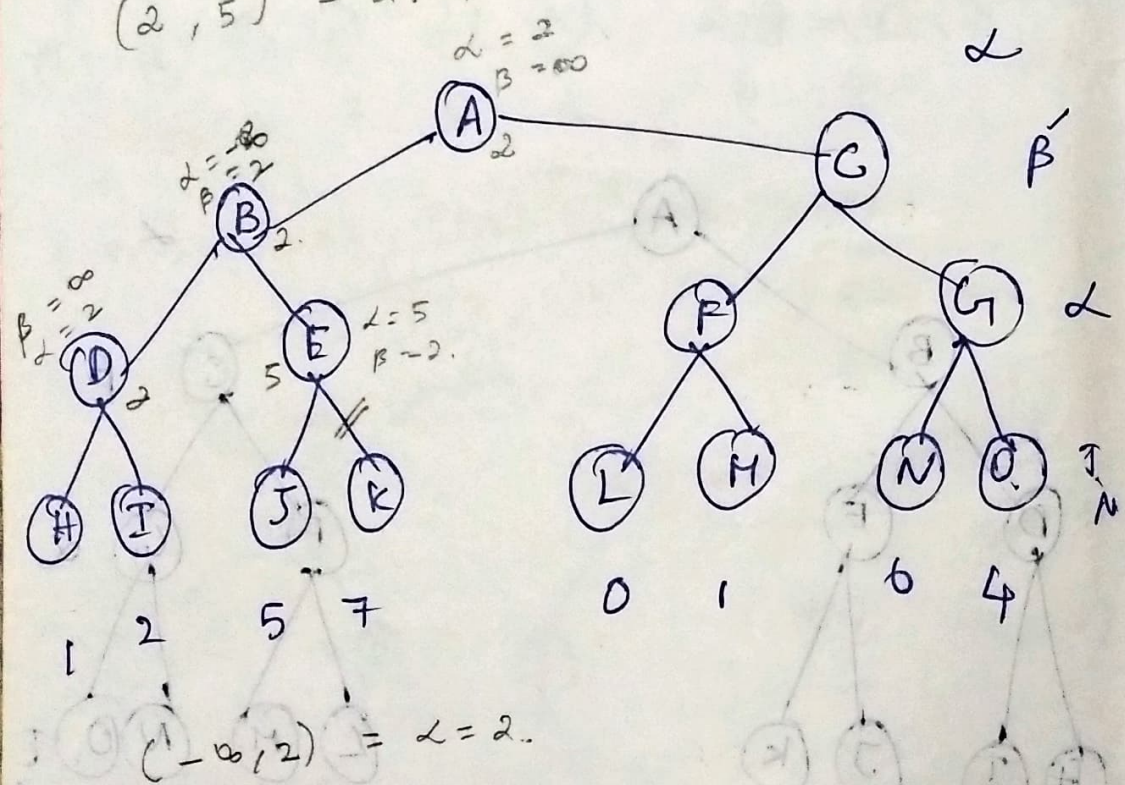
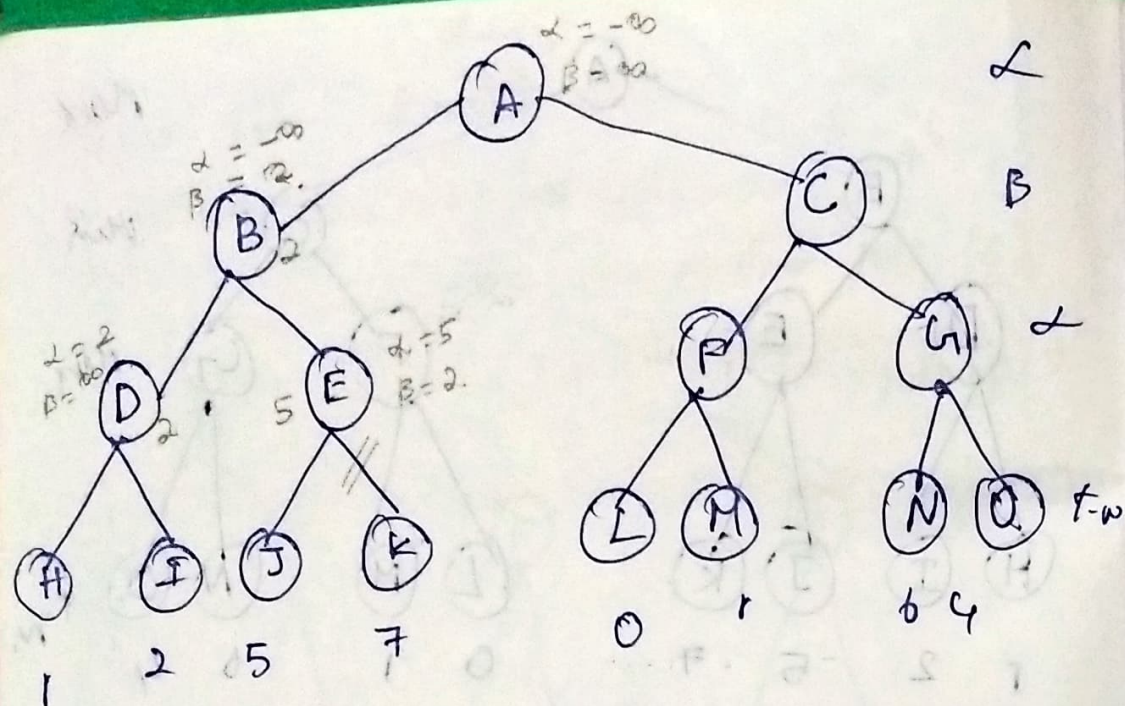
$$(-\infty, 2) = \beta = 2$$

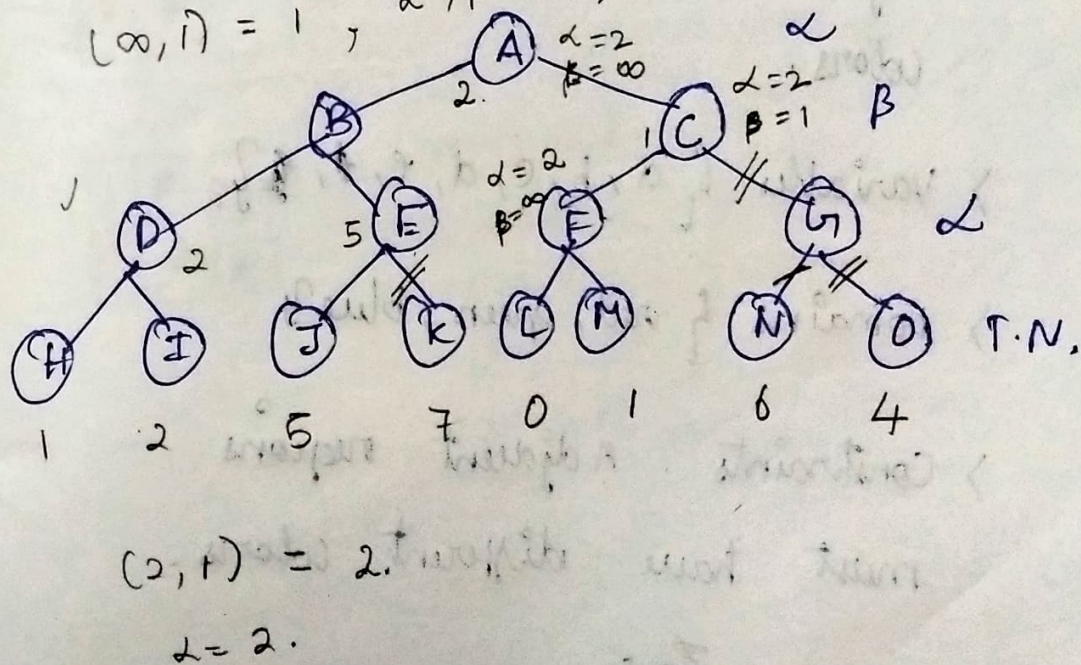
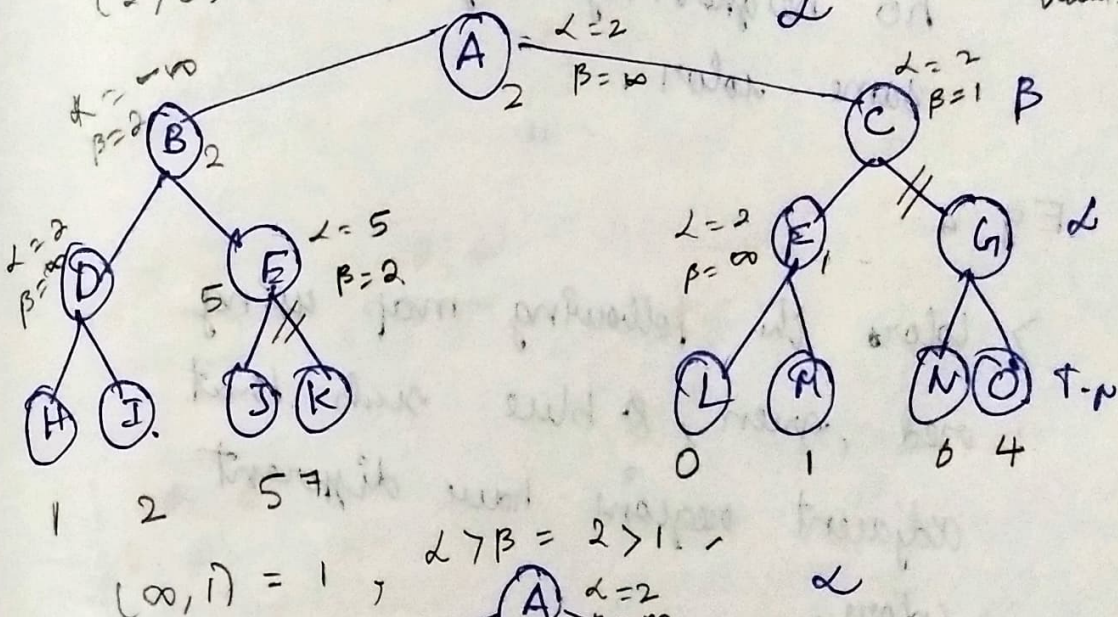
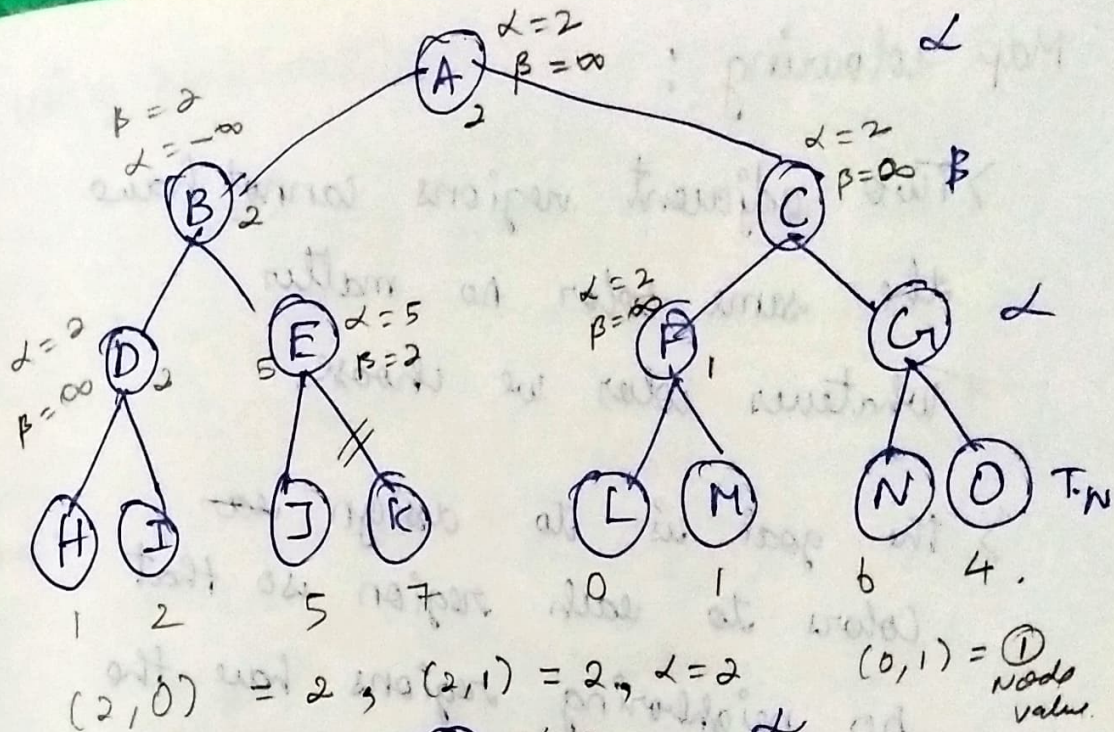


$$(-\infty, 5) = \alpha = 5$$

$$\alpha > \beta$$

$$5 > 2$$





Map colouring :

- > Two adjacent regions cannot have the same color no matter whatever color we choose.
- > The goal is to assign ~~sa~~ colors to each region so that no neighboring regions have the same color.

Eg. a

- > Color the following map using red, green, & blue such that adjacent regions have different colors.

> Variables $\{a, b, c, d, e, f, g\}$

> Domains $\{red, green, blue\}$

> Constraints : Adjacent regions must have different colors.

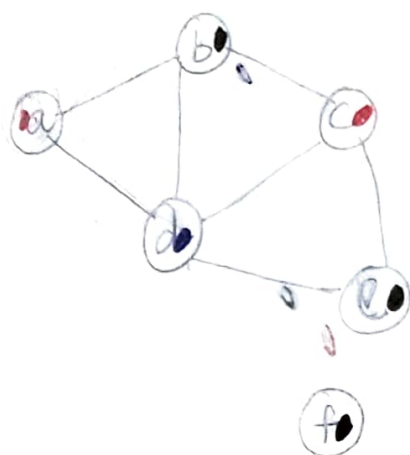
eg: $a \neq b$



a \rightarrow red
b \rightarrow blue
c \rightarrow black
d \rightarrow red.
e \rightarrow Blue.

Constraint Graph:

nodes are variables, arcs are constraints.



have a set
of variables
and a set
of constraints
between them

Constraint Satisfaction Problem:

> constraint programming or constraint solving is about finding values for variables such that they satisfy a constraint (conditions).

> $CSP = \{V, D, C\}$.

Variables = $V = \{v_1, \dots, v_n\}$

Domain = $D = \{D_1, \dots, D_n\}$

Constraints = $C = \{C_1, \dots, C_K\}$.

> Eg:

> crossword puzzle

> crypt-Arithmetic problem

> Map colouring problem.

Domain:

Discrete
Finite

(Finite)

Finite

Type of constraint in CSP:

Unary

Binary

Linear

Non-Linear

TO

Variables: T, O, G, U

+ GO

Domains: 0-9

OUT

2 1
8 1

1 0 2

T = 2

O = 1

G = 8

U = 0

S E N D

+ M O R E

M O N E Y

9 5 6 7

+ 1 0 8 5

1 0 6 5 2

S = 9

M = 1

E = 5

N = 0

R = 6

D = 8

Y = 7

2

$$E + 0 = N.$$

0 or 1

+

carry can be 0 or 1.

$$0 \Rightarrow \cancel{0} + E + \cancel{0} = N.$$

$$E \neq N$$

$$1 \Rightarrow 1 + E + \cancel{0} = N.$$

$$\Rightarrow 1 + E = N. \quad \text{--- (1)}$$

$$N + R = E +$$

carry can be 0 or 1.

$$0 \Rightarrow \cancel{0} + N + R = E$$

$$N + R = E + 10$$

$$1 + \cancel{E} + R = \cancel{E} + 10.$$

$$R \neq 9$$

$$1 \Rightarrow 1 + N + R = E + 10.$$

$$1 + 1 + \cancel{E} + R = \cancel{E} + 10$$

$$R = 8. \checkmark$$

$$\therefore E + 10.$$

Why Means

the carry

of the

$$E + 0 = 1.$$

so we add

10 to the

E.]

$$D + E = Y + 10$$

$$E = 7. \Rightarrow$$

$$E + 0 = N.$$

$$1 + 7 = N.$$

↓
carry $N \neq 8 \therefore \boxed{K=8}$

$$D = 7, E = 6.$$

$$D + E = Y + 10.$$

$$7 + 6 = Y + 10.$$

$$13 = Y + 10.$$

$$Y = 3, X,$$

$$E + 0 = N.$$

$$6 + 0 = N.$$

$$7 \neq N.$$

$$\boxed{D=7}$$

$$D = 7, E = 5.$$

$$E + 0 = N.$$

$$5 + 0 = N.$$

$$1 + 5 = 6.$$

$$N = 6, \nearrow$$

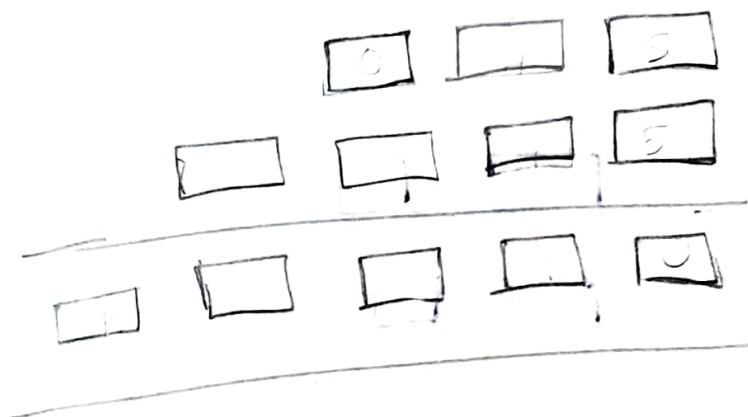
$$5 + 6 = 11 \times$$

$$5 + 7 = 12 \checkmark$$

$$6 + 7 = 13 \checkmark$$

EAT
+ THAT

APPLE


$$T \cap E = \emptyset$$

100

$$f \cdot g = h.$$
$$14 = 2$$