

## Minimax Algorithm :

> Minimax is a kind of Backtracking Algorithm.

> It is used in game theory to find the optimal move for a player.

> It is widely used in two player turn - based games.

Eg :

Chess

Tic-Tac-Toe.

In Minimax Two players are called

$\Rightarrow$  Max

$\Rightarrow$  Min

Max  $\rightarrow$  highest Value

Min  $\rightarrow$  Lowest Value.

The Minimax Algorithm proceeds all way down to Terminal node of the tree, then backtrack the tree.



### Algorithm For Min-Max :

$$\text{Minimax}(s) =$$

utility (s) if terminal test (s).

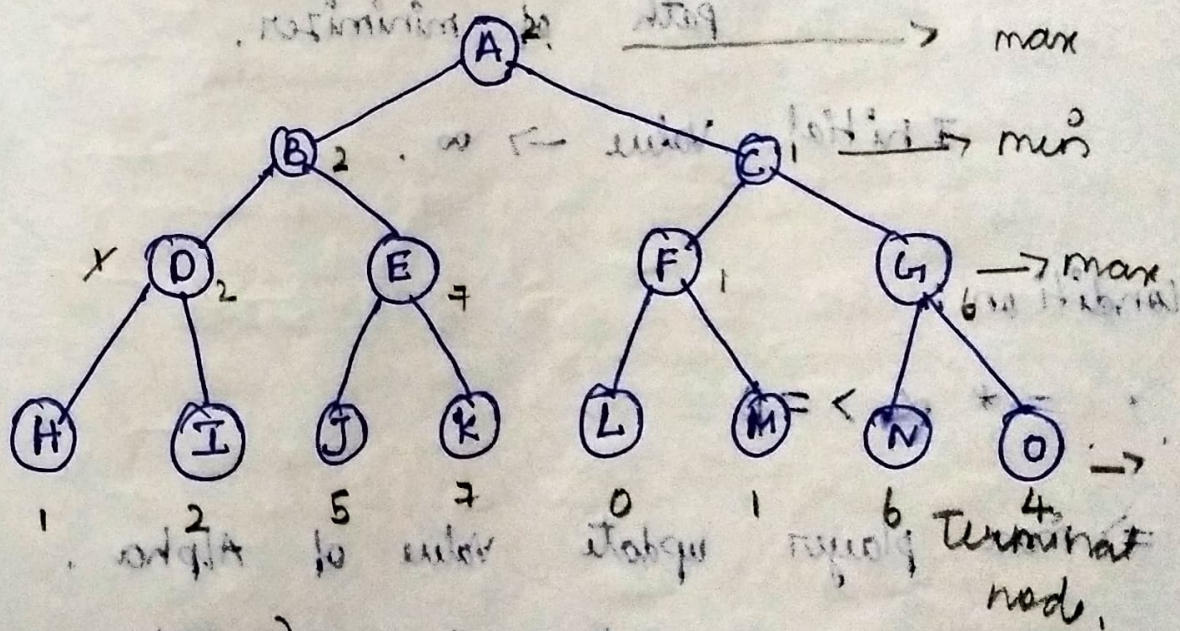
Mark Mark a. e. actions)

$$\min_{\text{player}(s)} \max_a (\text{result}(s, a))$$
$$= \max.$$

Run a  $\in$  action(s)

$$\min_{\max}(\text{result}(s, a)) \text{ if player}(s)$$
$$= \ln n$$

Example - Game tree:

 $\max(-\infty, 1)$ 
$$\max(1, 2) = 2.$$



Alpha beta pruning:

> Alpha Beta pruning is modified version of minimax Algorithm

> This is the technique By which it does not check each node of the game tree.

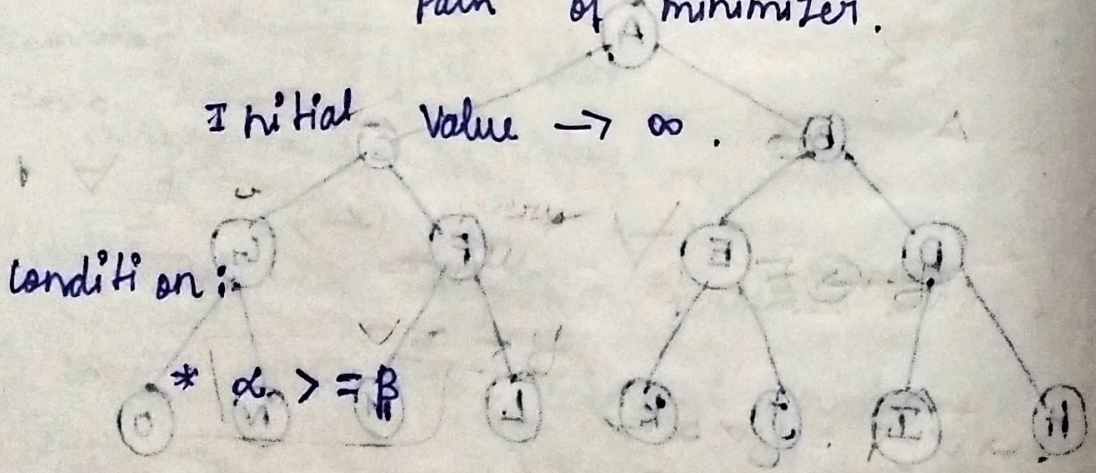
>  $\alpha$ - $\beta$  pruning is the pruning (cutting down) of useless branches in decision trees.

Parameters:

Alpha ( $\alpha$ )  $\Rightarrow$  highest value choice along path of maximizer.

Initial value  $\rightarrow -\infty$

Beta ( $\beta$ )  $\Rightarrow$  Lowest value choice along path of minimizer.

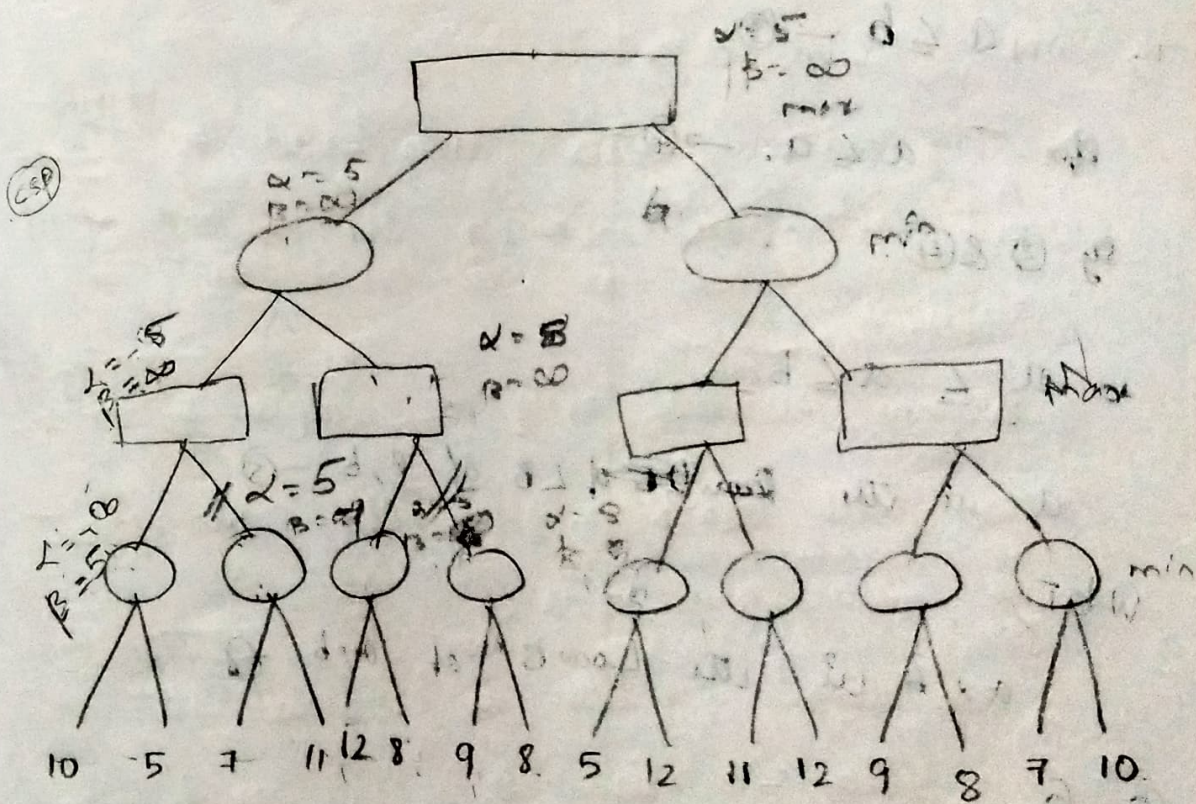
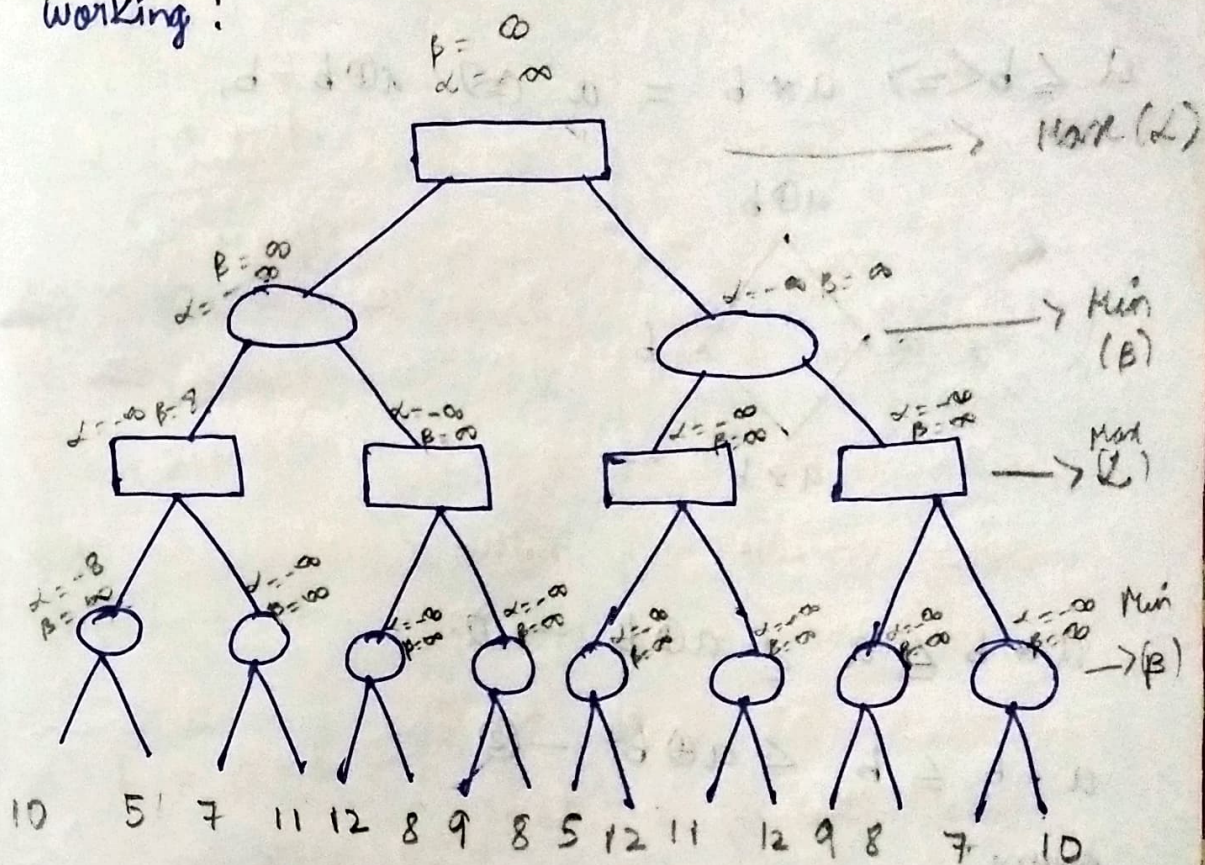


$\Rightarrow$  max player update value of Alpha.

$\Rightarrow$  min player update value of Beta.



working :



$(-\infty, 5)$

5, 7

$(5, 8)$