

PAC : probability Approximately correct.

> It is a framework for the mathematical analysis of machine learning.

> The goal of PAC : with high probability, the selected hypothesis will have lower error.

> Parameters :  $\epsilon$  &  $\delta$

> With probability at least  $(1 - \delta)$ , a system learn the concept with error at most  $\epsilon$ .

>  $\epsilon$  is upper bound on the error in accuracy (i.e. the hypothesis with error less than  $\epsilon$ ).

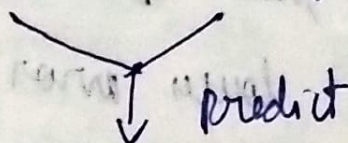
> Accuracy :  $1 - \epsilon$ .



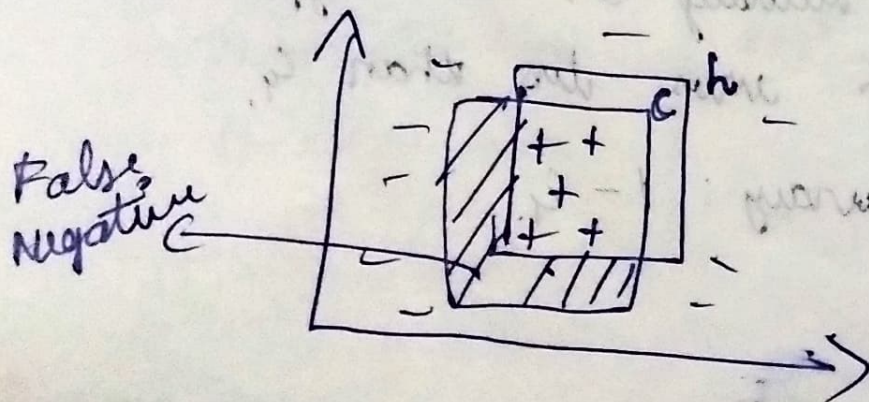
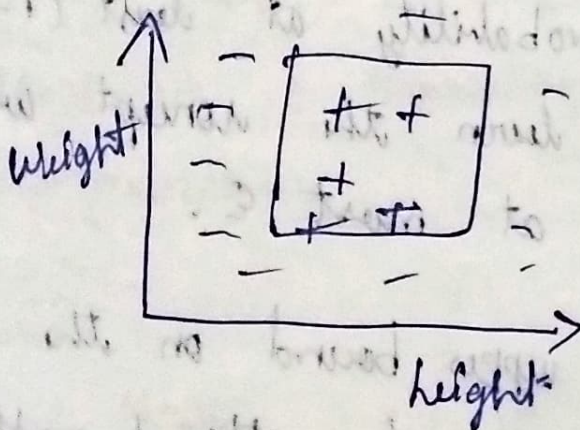
$\delta$  gives the probability of failure in achieving this accuracy  $\delta$ , ( $0 < \delta \leq 1$ ).  
 Confidence :  $1 - \delta$

Eg :

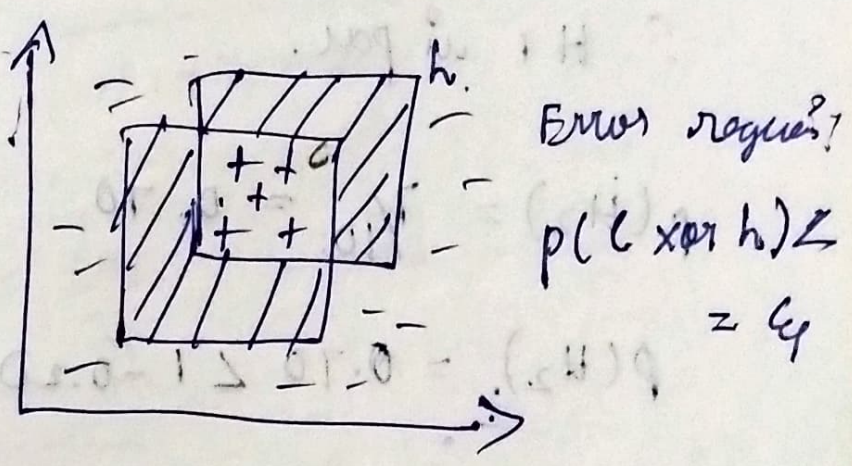
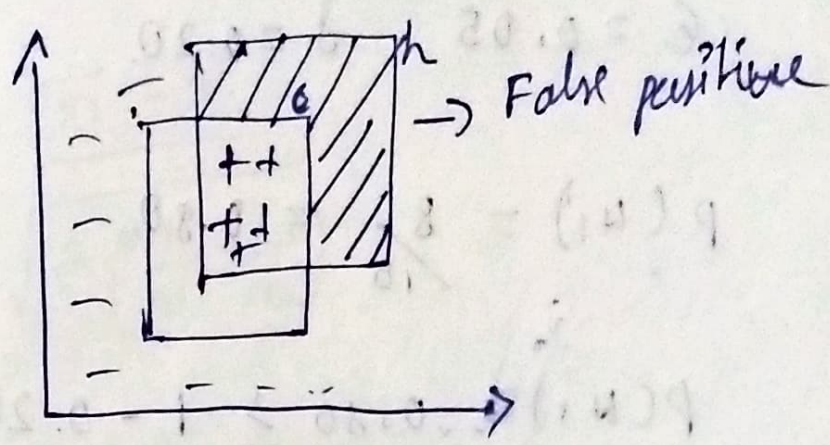
Height & weight



Future  $\rightarrow$  Medium height person as not



ing with Mis  
rect Errors as Early  
ta from Differ



$$p(C \oplus h) \leq \epsilon$$

PAC:

goal:  $p(\text{Error}(C) \leq \epsilon) \geq 1 - \delta$

also:  $p(p(C \oplus h) \leq \epsilon) \geq 1 - \delta$

Eg:

|       | Error( $E_1$ ) |       | ( $E_2$ ) |  |
|-------|----------------|-------|-----------|--|
| 0.04  | 0.04           | 0.04  | 0.043     |  |
|       | 0.03           | 0.035 | 0.03      |  |
| 0.043 | 0.09           | 0.06  | 0.021     |  |
|       | 0.06           | 0.058 |           |  |
|       | 0.025          | 0.55  |           |  |
|       | 0.049          |       |           |  |
|       | 0.023          | 0.045 |           |  |
|       | 0.005          | 0.025 |           |  |



$$\alpha = 0.05 \quad \delta = 0.20$$

$$p(H_1) = \frac{8}{10} = 0.80$$

$$p(H_1) = 0.80 \geq 1 - 0.20$$

$\therefore H_1$  is PAC.

$$p(H_2) = \frac{7}{10} = 0.70$$

$$p(H_2) = 0.70 < 1 - 0.20$$

$\therefore H_2$  is not PAC.