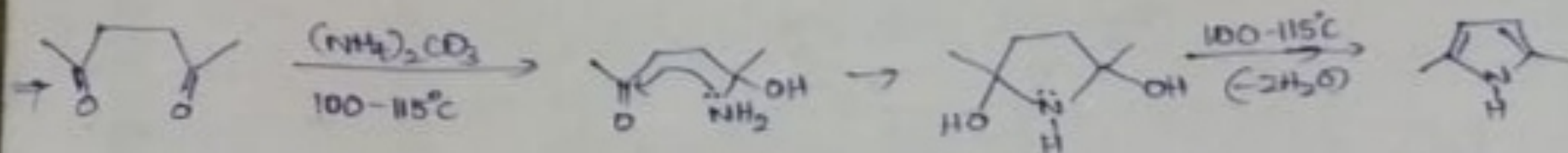
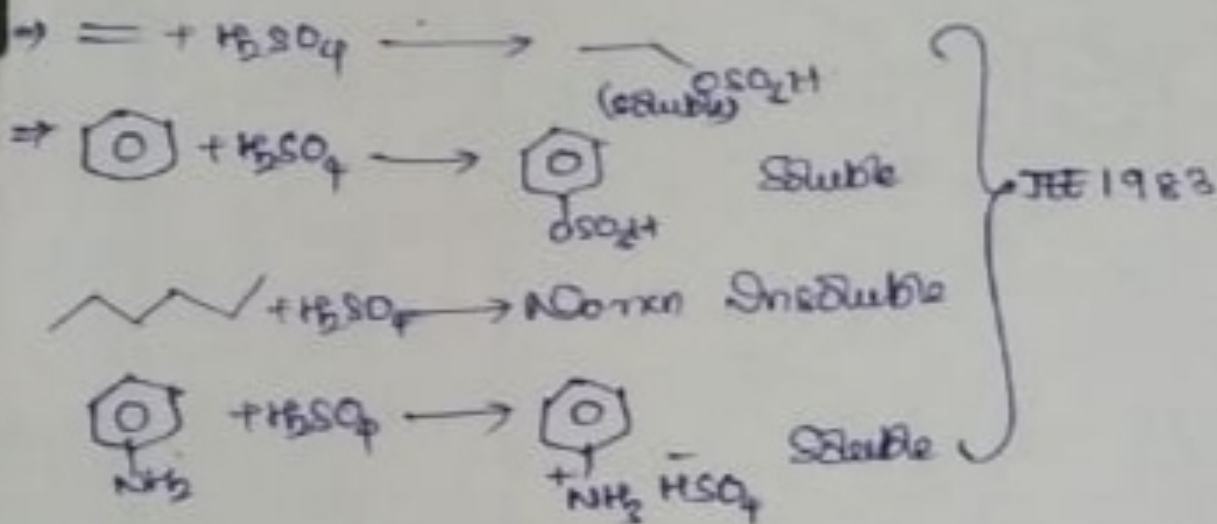


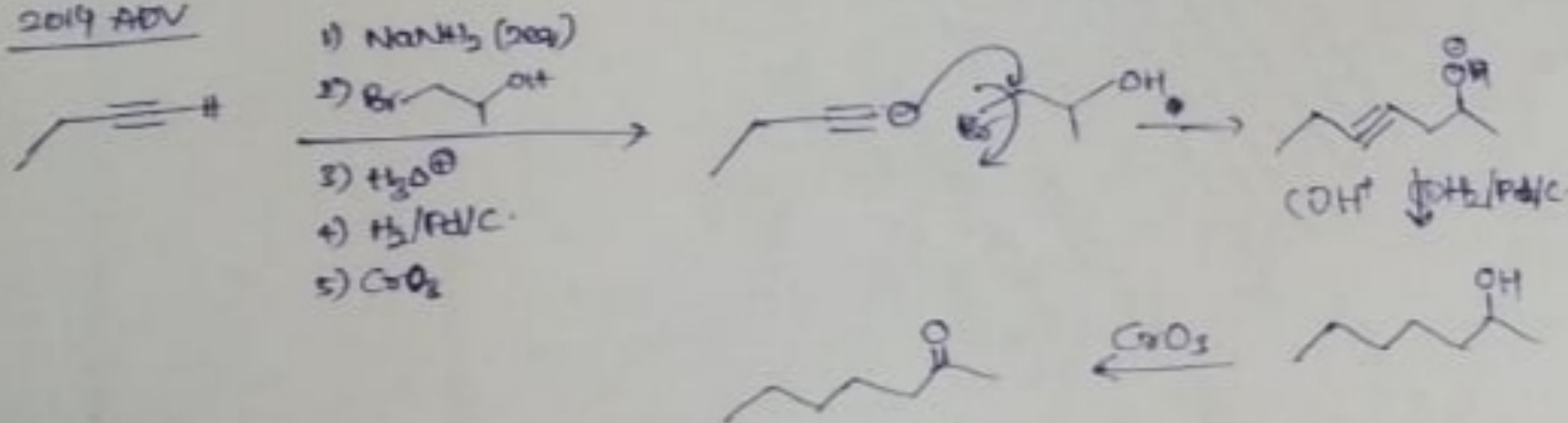
2018 ADV



→ C-C single bond energy is approximately 100 kcal/mol. [2010 JEE]



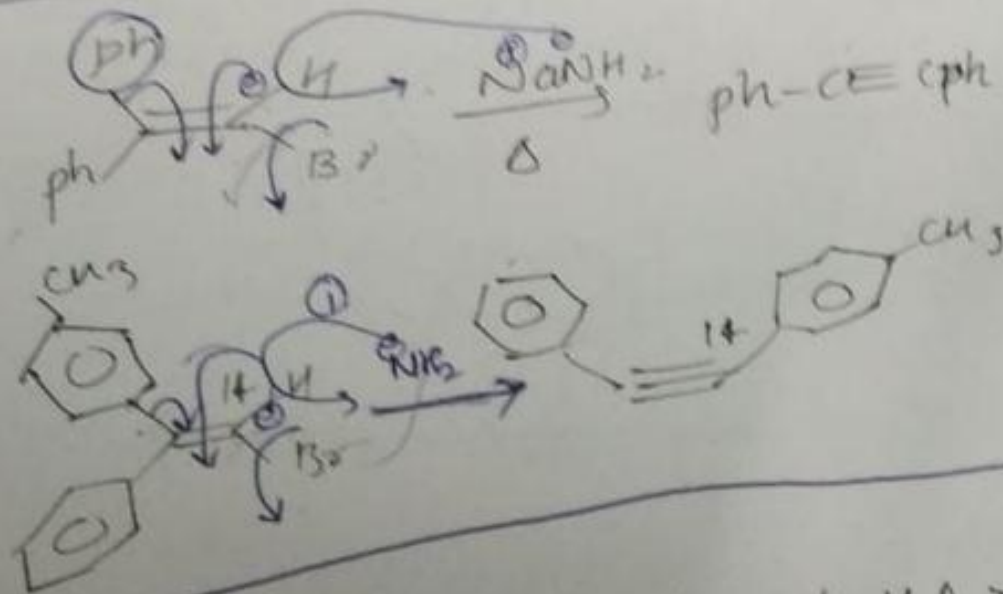
2014 ADV



Mech:  
DPP (21/08/2019)

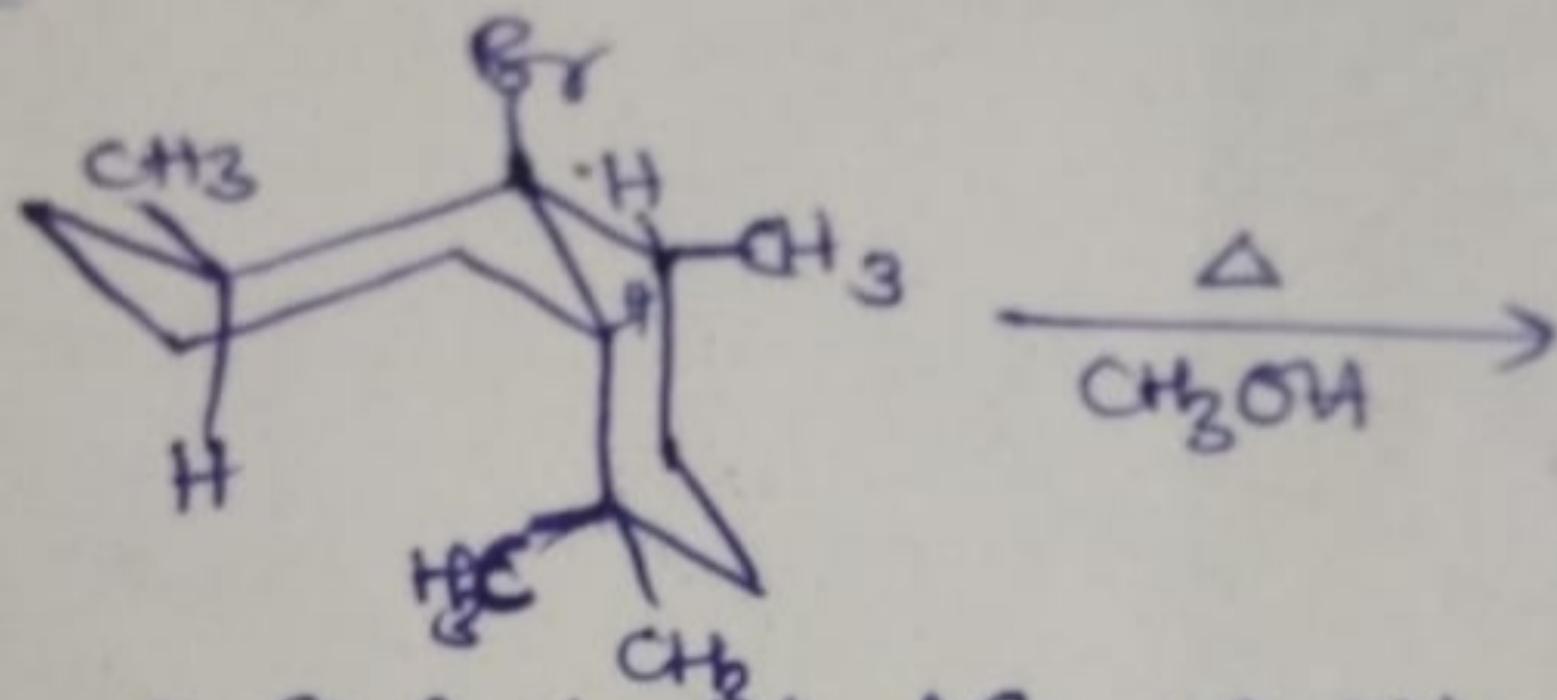
Anti  
Group  
Migration

Vinyl c<sup>+</sup> intermediate



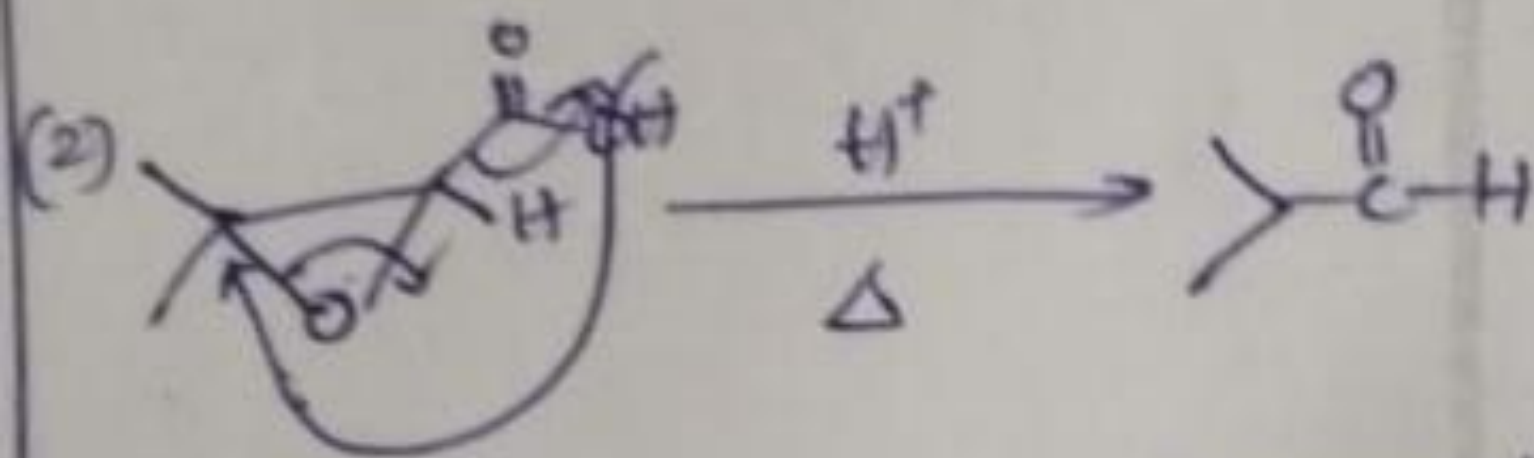
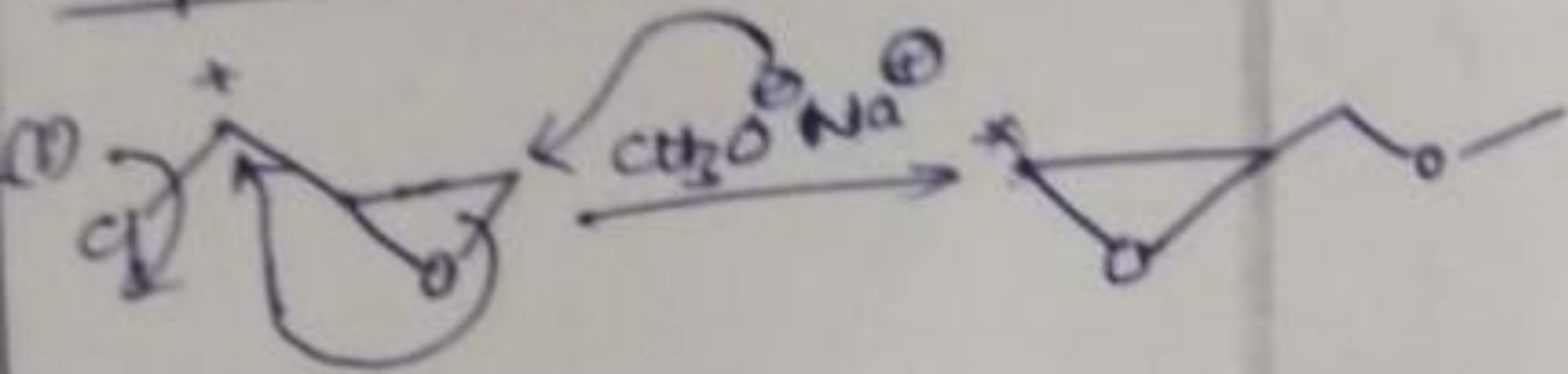
k. H. A > pKa ≡

NOTE:

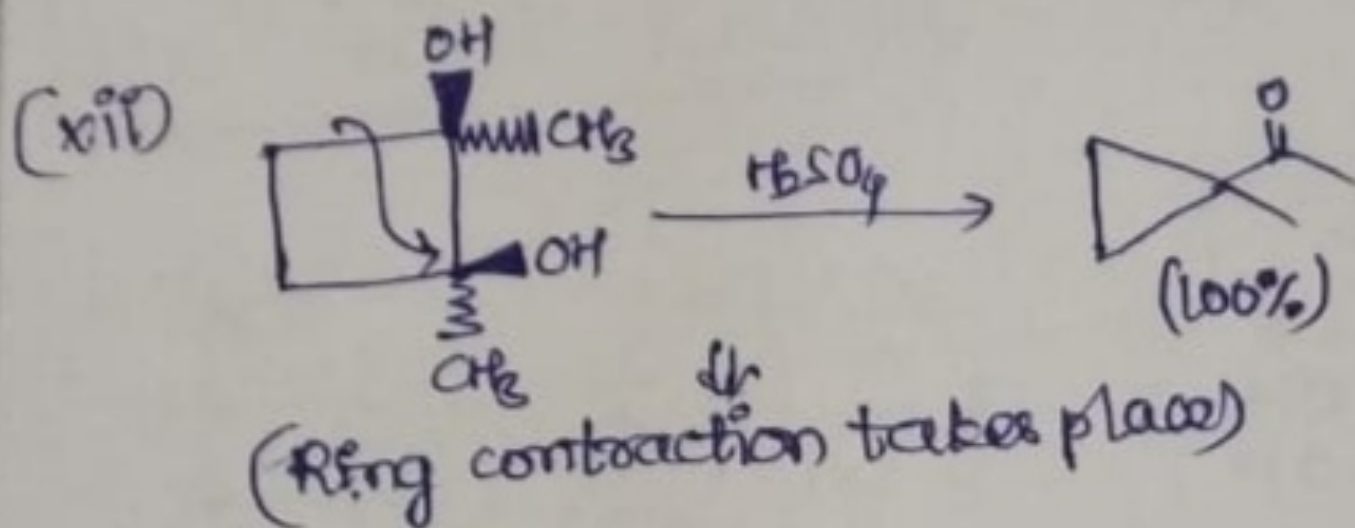
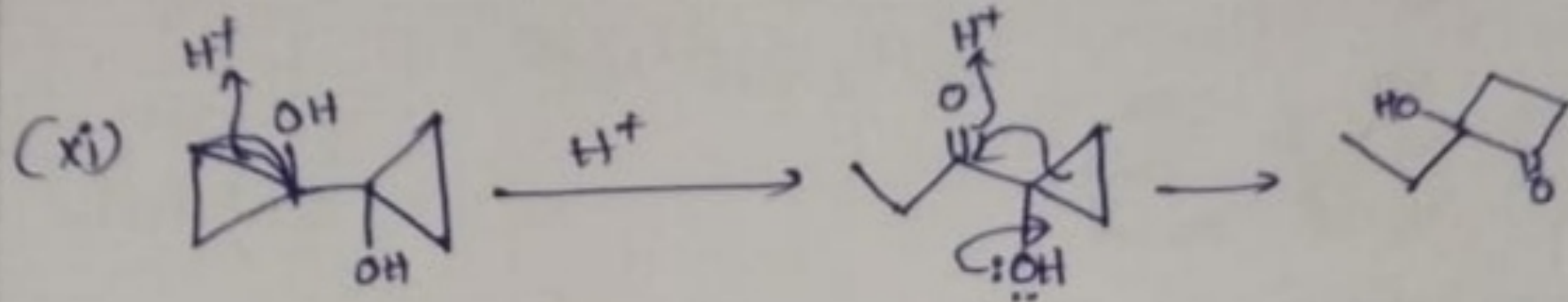


As it is heated in MeOH, ionisation takes place to form  $C^+$ . Then there are 3  $\beta$ -H which form alkene.

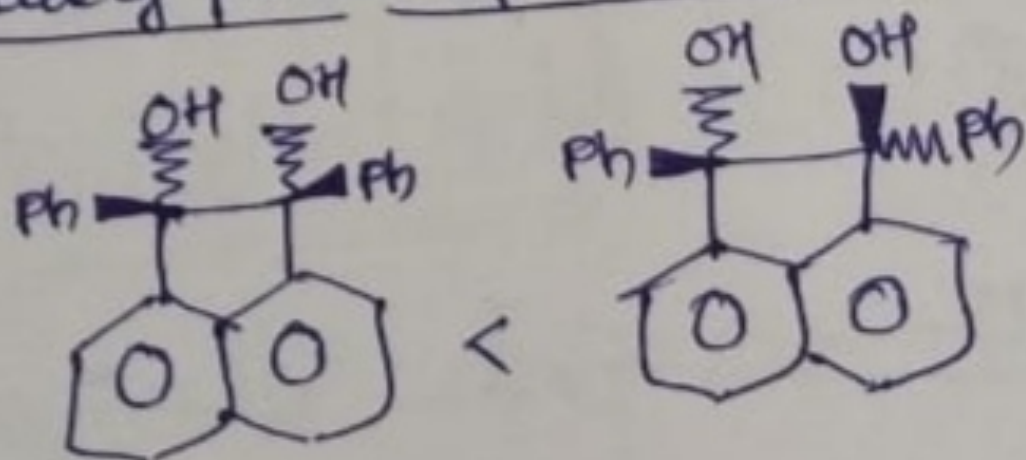
Propose Mech:



→ During cleavage of epoxide in basic medium, if any LG is there  $\text{O}^-$  reattaches & forms ring again



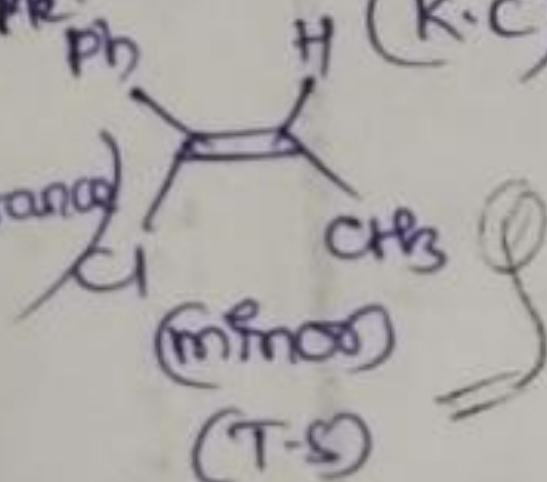
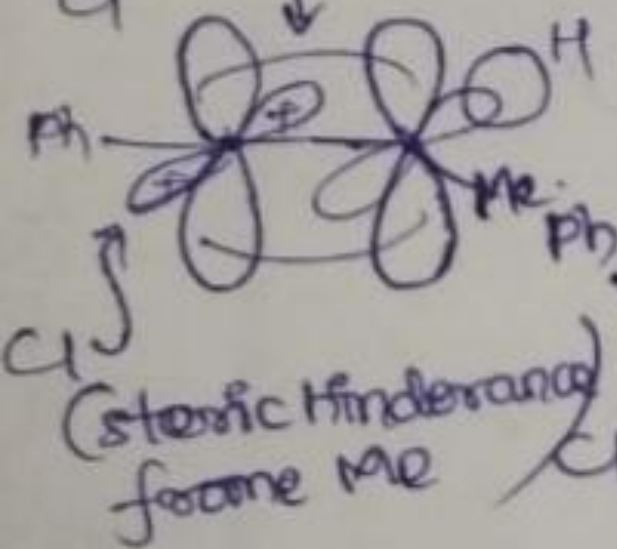
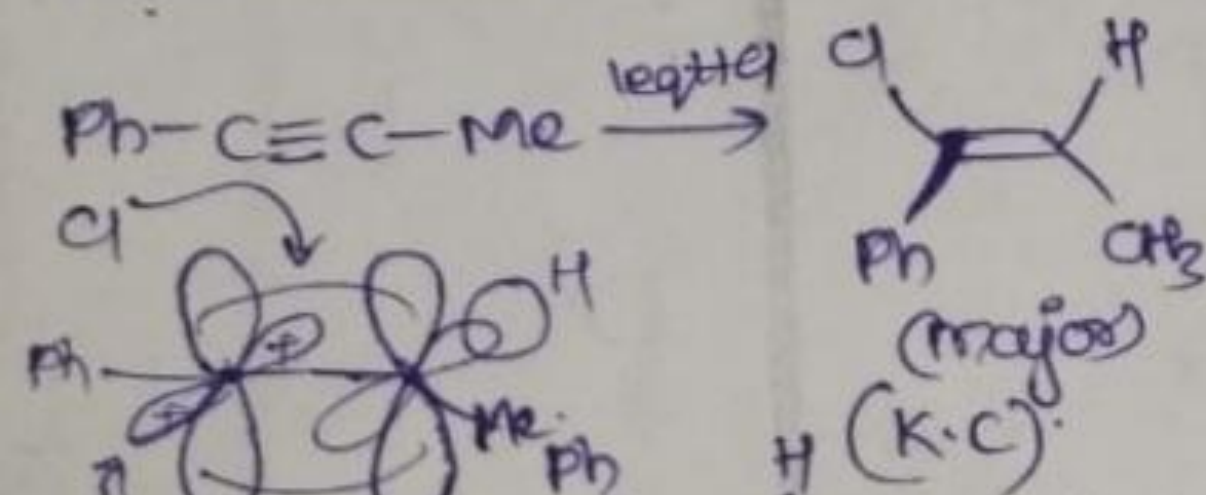
Rate of pinacol Spinacone





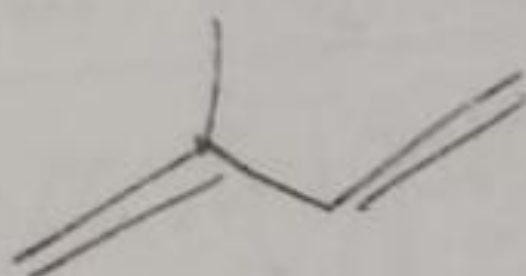
(Then Given in all std Books).

2020-IIT

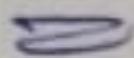
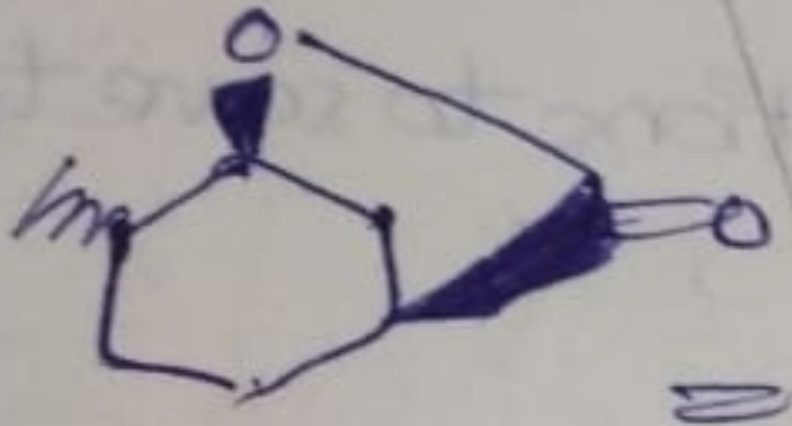


(more stable synor  
when HCl is in excess)

BY

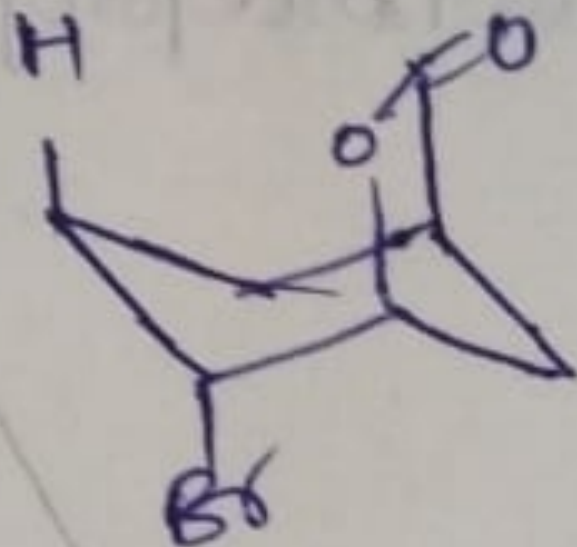


B6

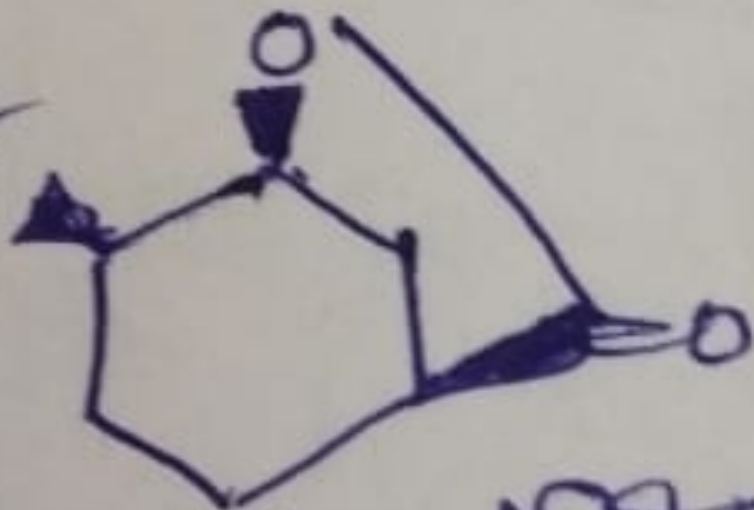


Antielimination  
occurs

H



B6

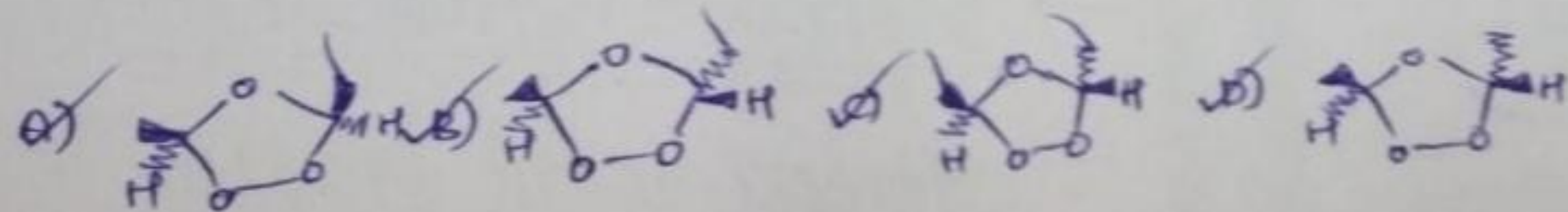
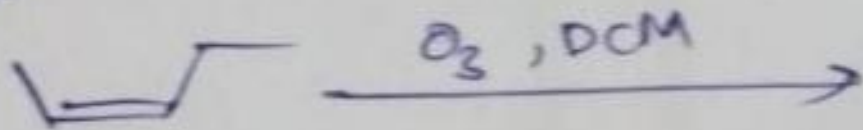


B6



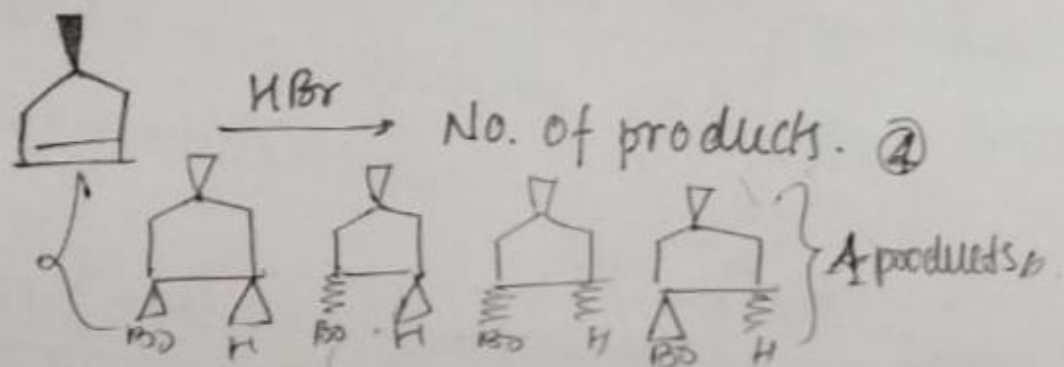
Not possible

Q: Products formed

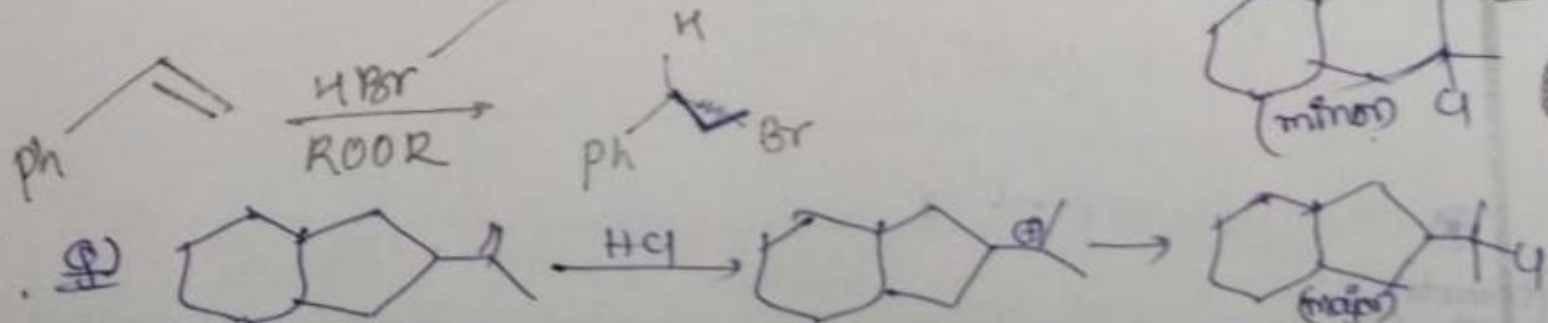




Q



Q



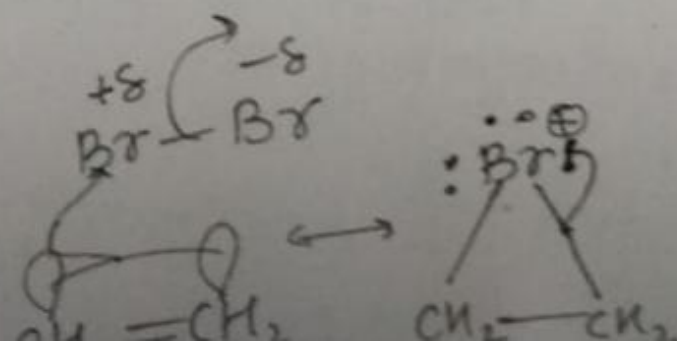
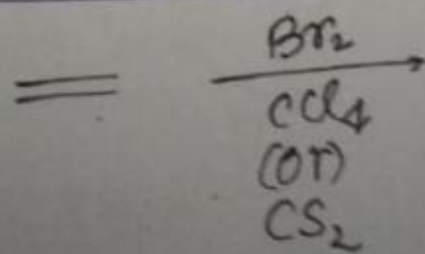
2019 MAINS  
2-Jan-S-II

Q

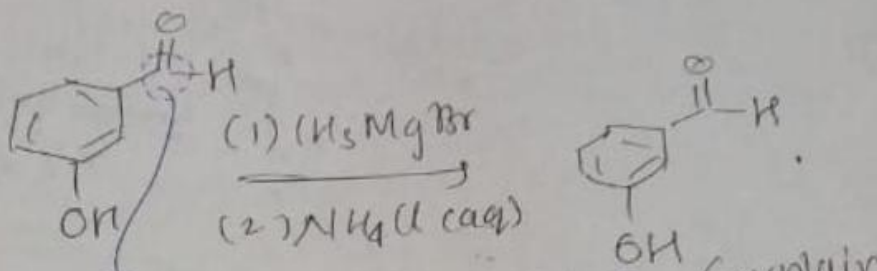
Not much ring expansion bcoz  $^{\oplus}$  is  $3^{\circ}$ .



Addition of  $X_2$



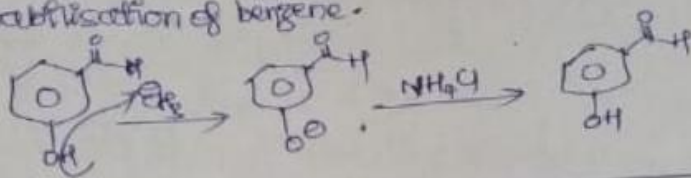
Q4)



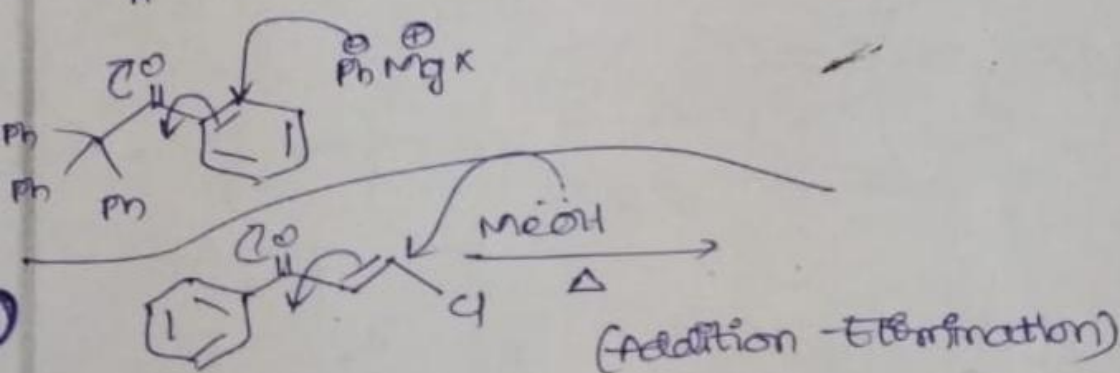
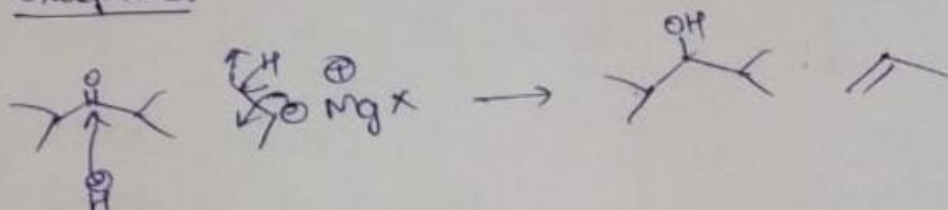
Explanation: This is not enough electrophilic force of resonance stabilisation of benzene.

(explain)

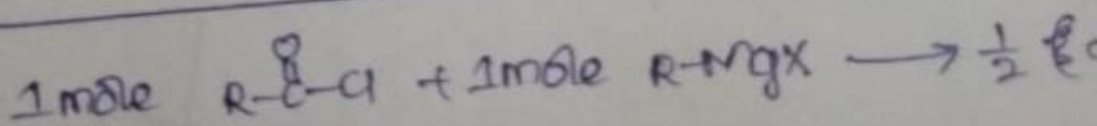
Q5



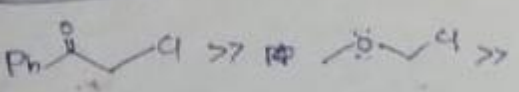
Exceptions:



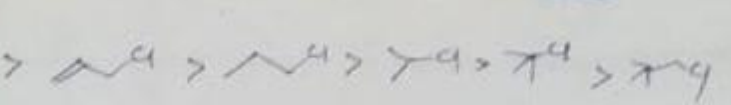
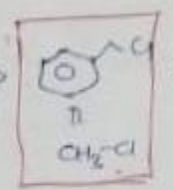
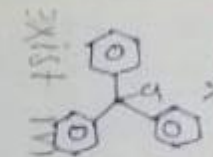
During cleavage of Epoxide in if any leaving group is there - and forms ring again.



SN2 reaction

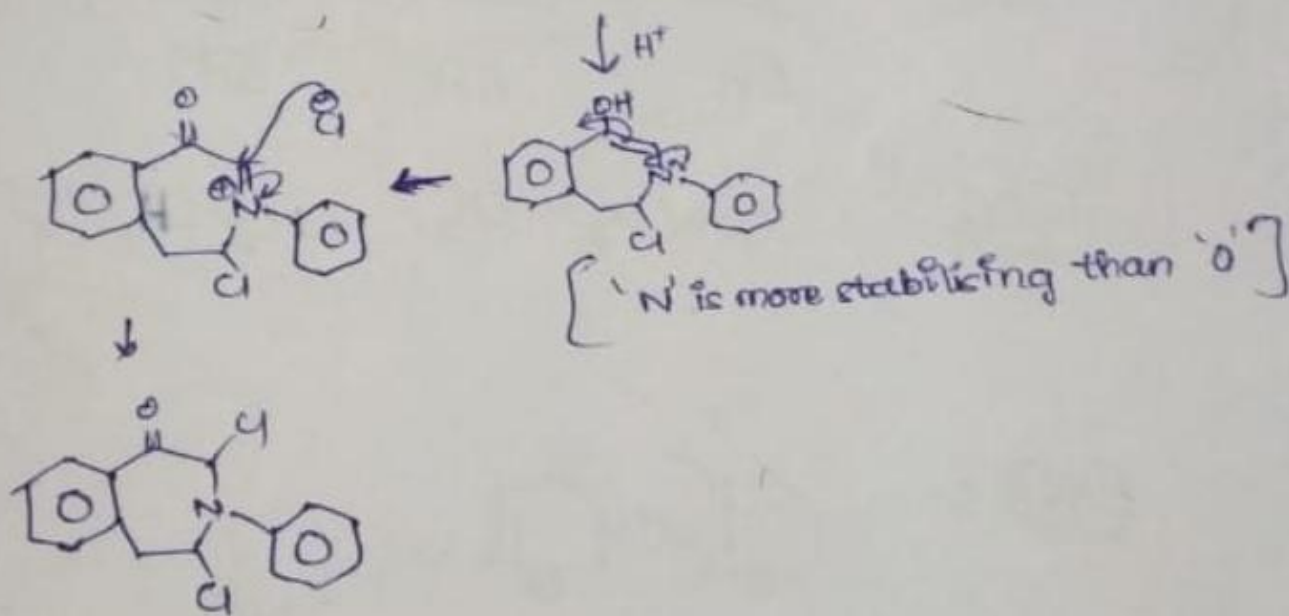
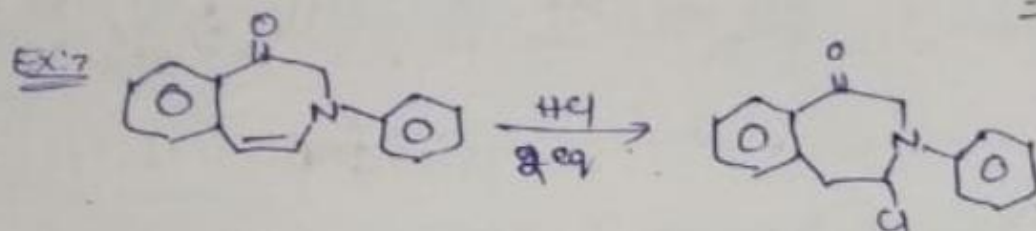
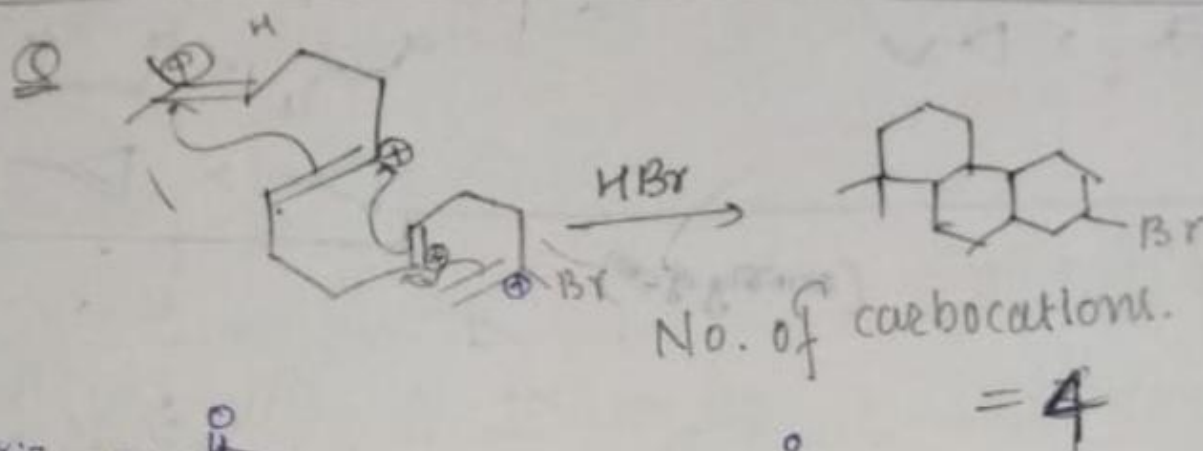
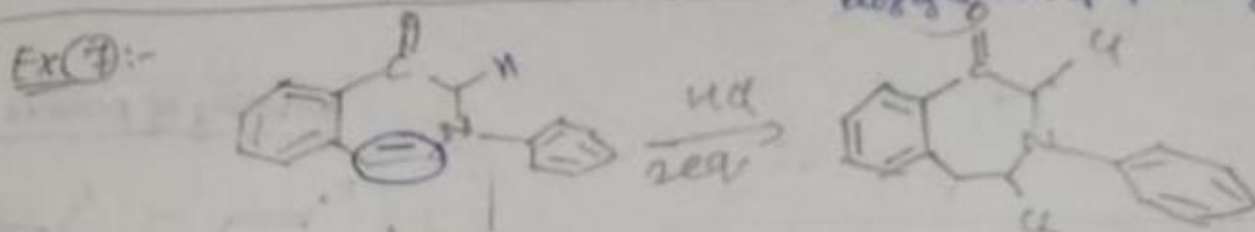
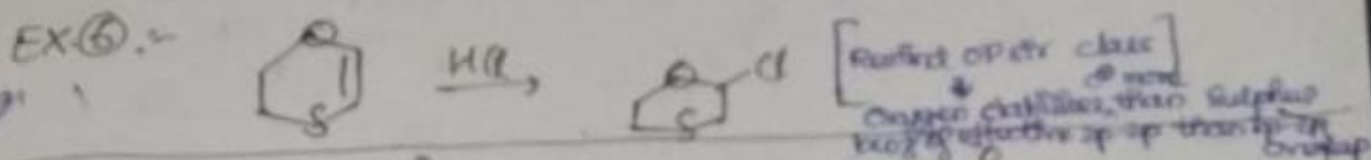
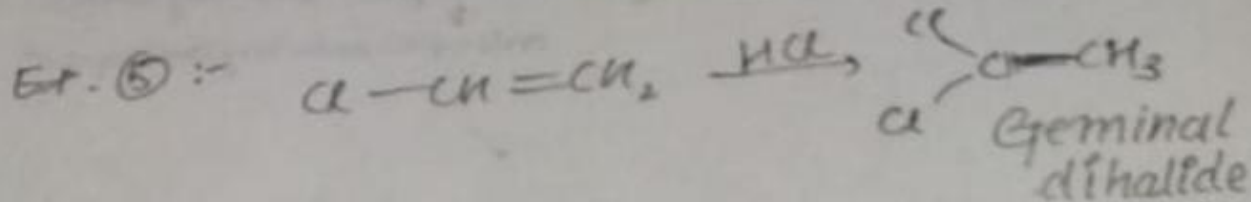


add carbon.



(viii) Nature of medium

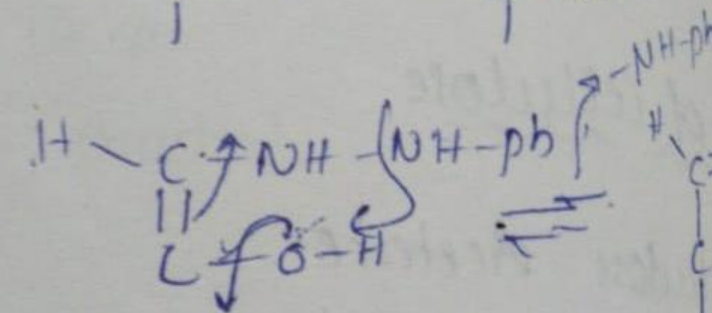
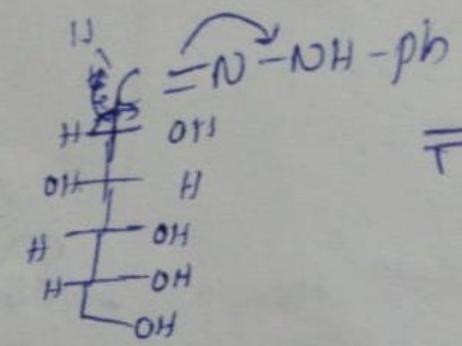
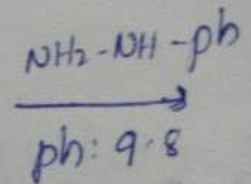
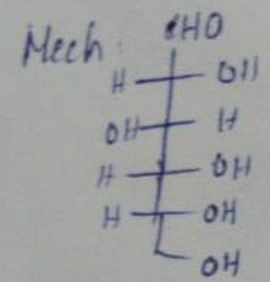
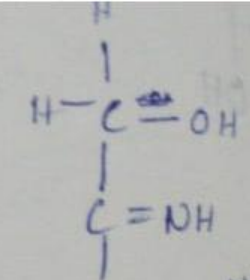
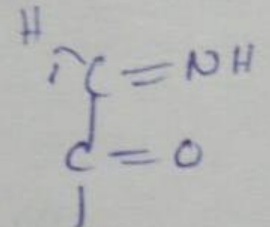
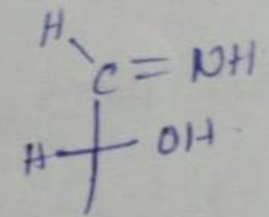
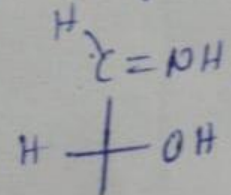
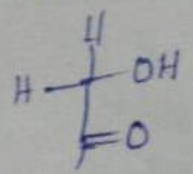
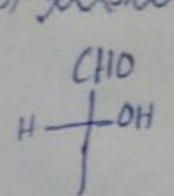
PATH	Reactants	Transition state	Change in transition state relatively starting reactants	How an increase in solvent polarity affects the rate
SN <sup>1</sup>	R-X	$R^{\oplus} \cdots X^{\ominus}$	separation of unlike charges (increases).	large increase in rate of rxn.
SN <sup>1</sup>	R-X <sup>+</sup>	$R^{\oplus} \cdots X^{\oplus}$	Dispersal of charge	small decrease.
SN <sup>2</sup>	R-X + Y <sup>-</sup>	$Y^{\ominus} \cdots R \cdots X^{\ominus}$	Dispersal of charge	small decrease
SN <sup>2</sup>	R-X + Y	$Y^{\oplus} \cdots R \cdots X^{\ominus}$	separation of unlike charge	large increase
SN <sup>2</sup>	R-X <sup>+</sup> + Y <sup>-</sup>	$Y^{\ominus} \cdots R \cdots X^{\oplus}$	Dispersal of charge	large decrease
SN <sup>2</sup>	R-X <sup>+</sup> + Y	$Y^{\oplus} \cdots R \cdots X^{\oplus}$	Dispersal of charge	small decrease.





shows this test

3) Osazone: (Yellow, yet Orange, Red solid) (250 m.p.)



\* Glucose, Mannose, Fructose forms same osazone (✓)

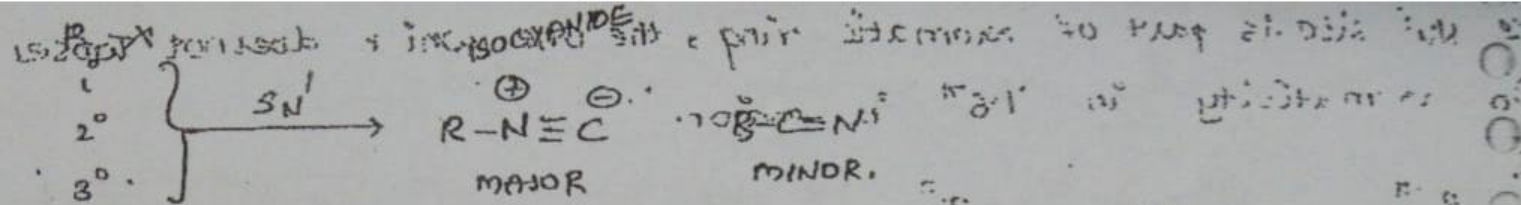
\* Glucose & Galactose forms different osazones

\* Arabinose & Ribose forms

Net reaction

[24]



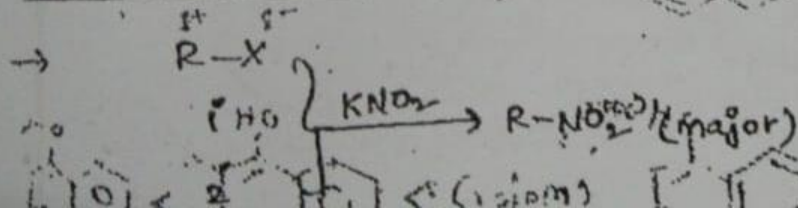


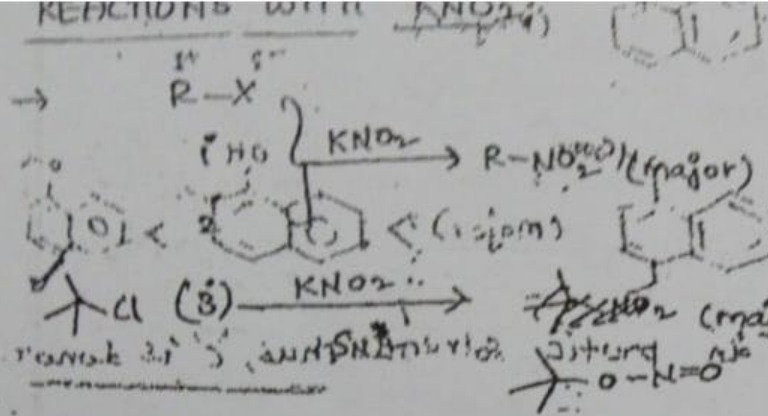
## HSAB PRINCIPLE (Hard soft acid-base)

$\rightarrow$  { Hard acid, Hard Base } are more stable. Others all are least stable.  
{ Soft acid, Soft Base. }

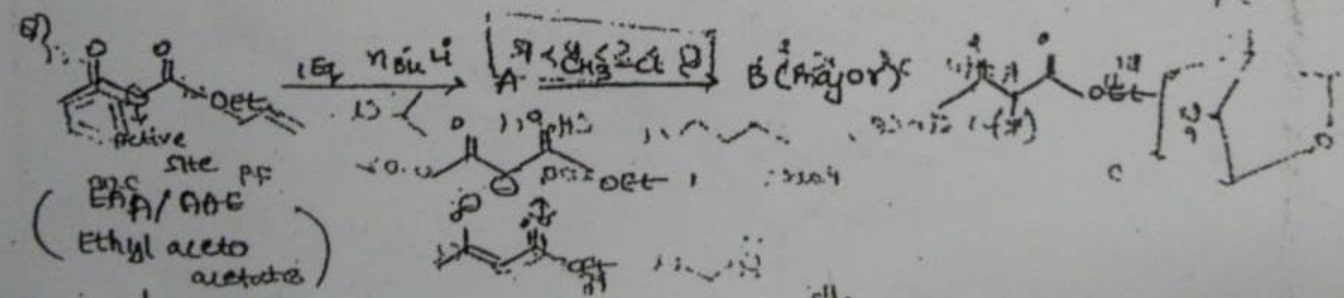
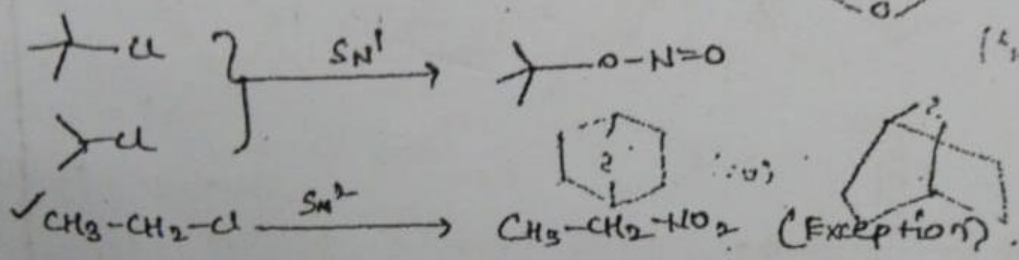
$\rightarrow$  HB: more (HARD) EN DONOR. HS: less (SOFT) EN DONOR.  
HA:  $S_N1$  Carbo cation. SA:  $S_N2$  Carbo cation.

## REACTIONS WITH $KNO_2$



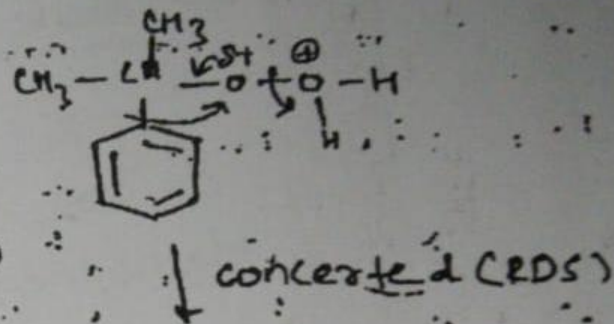
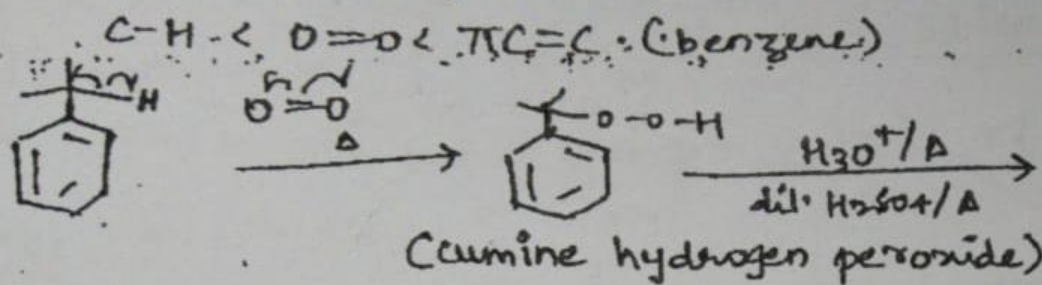


$\text{AgNO}_2$ :

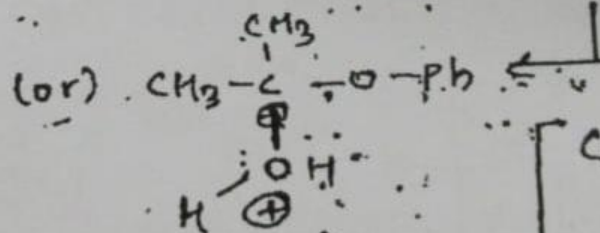
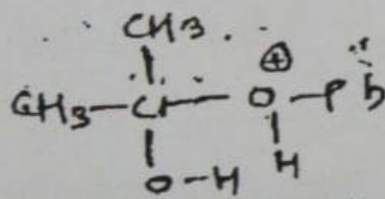


at high temp. free radical mechanism takes place.

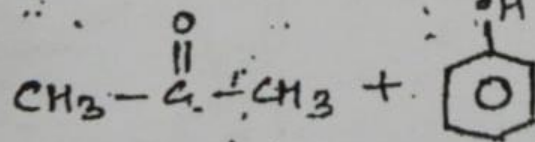
weaker bonds gets dissociated.



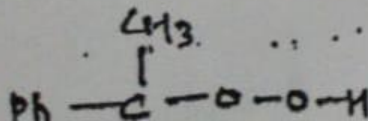
(migratory aptitude migrates from carbon to electron deficient oxygen)



Cummine Hydroperoxide rearrangement

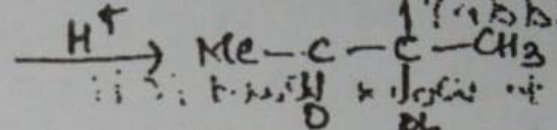
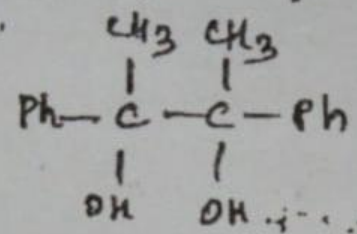
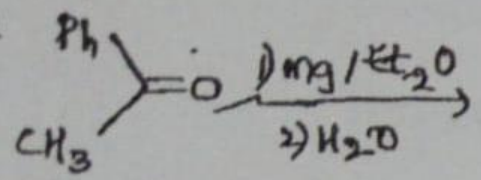


(equally formed)



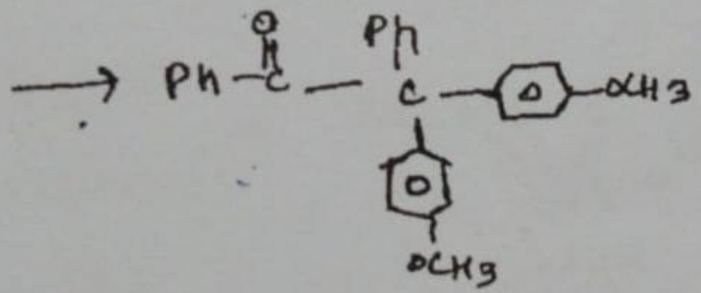
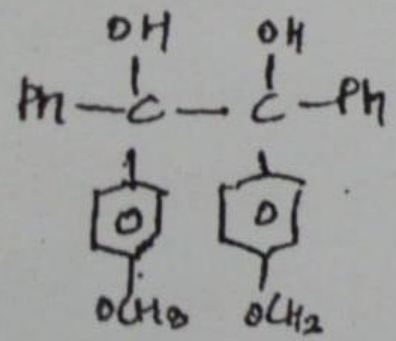


NPS Step is (ii).

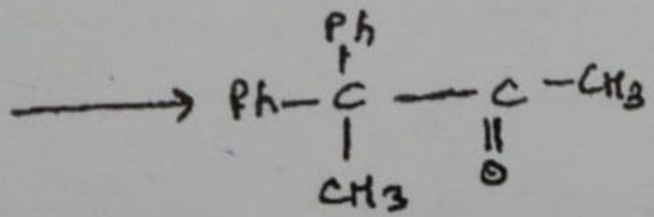
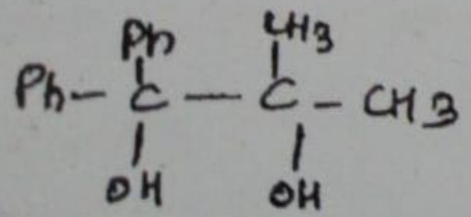


Migratory order:  $(-\text{Ph} > -\text{H} > \text{R})$

$(-\text{CH}_3 > -\text{CH}_2 > -\text{CH}_3)$



→ Among phenyl donating groups are faster than wdc.



2017-18

400 (M)

In case (i)  
(i) If  $\text{Z}$  is 'H'  $\Rightarrow$  product is imine ( $>=NH$ )

(ii) If  $\text{Z}$  is 'R'

**NOTE**  $\rightarrow NaBH_4$  reduces imine to corresponding amine.

(ii) if  $\text{Z}$  is 'R'  $\Rightarrow$  product is N-alkyl imine ( $>=N-R$ )

(iii) if  $\text{Z}$  is 'Ar'  $\Rightarrow >=N-Ar$  (N-aryl imine).

**NOTE** :-

Schiff's reagent :- Generally carbonyl compound (best aromatic aldehyde) reacts with, generally primary amine (best aromatic 1<sup>o</sup> amine) to give N-alkyl or N-aryl imine known as Schiff's base, which is p (pink in color) which when passed through  $SO_2$  gas becomes colourless sol<sup>n</sup>, commonly known as Schiff's reagent or pararosaniline or rosaniline hydrochloride sol<sup>n</sup>.

Use :- To detect aldehydes only.

Observation :- becomes coloured (generally magenta)

Exception :- Acetone shows Schiff's test.

(iv) If  $\text{Z} = NH_2 \Rightarrow$  Hydrazine  $\Rightarrow$  Hydrazone Base, Alkane +  $N_2 \uparrow$

(v) If  $\text{Z} = -NH-Ph \Rightarrow$  Phenyl Hydrazine  $\Rightarrow$  phenyl Hydrazone

(vi) If  $\text{Z} = -NH-\text{C}_6\text{H}_3(NO_2)_2 \Rightarrow$  2,4-Dinitrophenyl-Hydrazine  $\Rightarrow$  2,4-Dinitrophenyl Hydrazone

Other names

\* (2,4-DNP)

\* Brady's reagent

\* Bohr's reagent

Use :- Used to detect carbonyl comp<sup>nd</sup>s. (All will give this test)

Observation :- Gives either red, yellow (or) orange colored solid.

(vii) If  $\text{Z} = -NH-\overset{\overset{O}{\parallel}}{C}-NH_2 \Rightarrow$  semicarbazide  $\Rightarrow$  semicarbazone

**NOTE** :- Like hydrazine semicarbazone also gives alkane upon rxn with alkali, also known ~~also known~~ as Wolf-Kühner reduction.

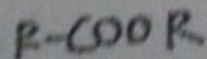
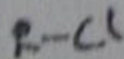
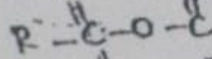
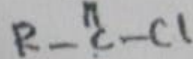


# GRIGNARD REAGENT:

## ORDER OF REACTIVITY:

Active ester  $\rightarrow$  Carbonyl Comp  $\rightarrow$  Acid chlorides  $\rightarrow$  anhydride

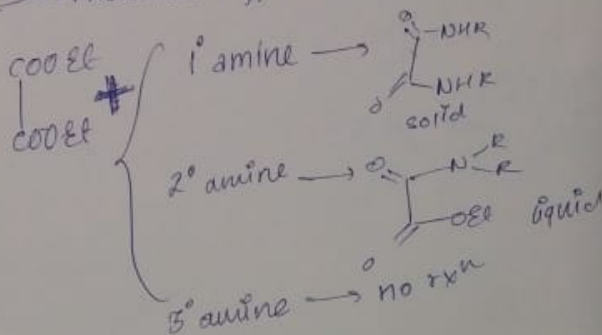
Esters  $\rightarrow$  Alkyl halides.



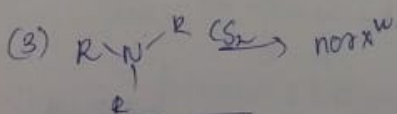
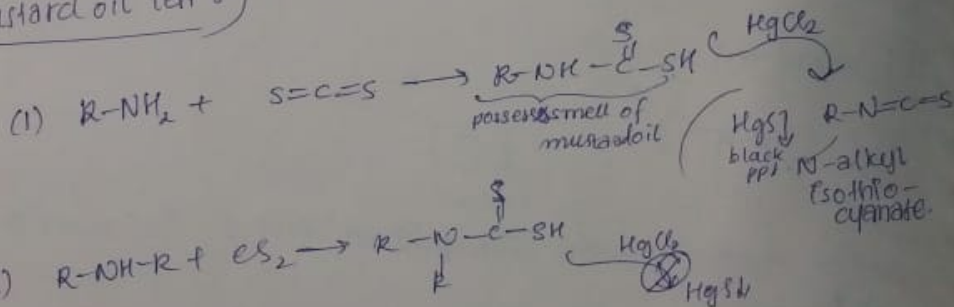
(c) 3° amine

Doesn't form white solid, no rxn occurs.

Rxn with diethyl oxalate No known as Hoffmann's method.



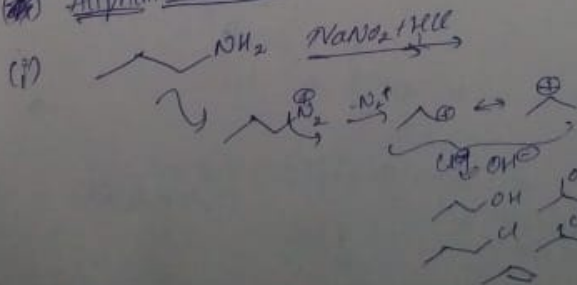
Hoffmann's mustard oil test:



Rxn with nitrous acid

Imp. for Advanced

(A) Aliphatic-1-amine

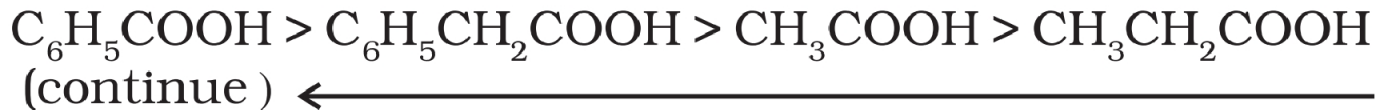


Here alcohols are major products.

The effect of the following groups in increasing acidity order is

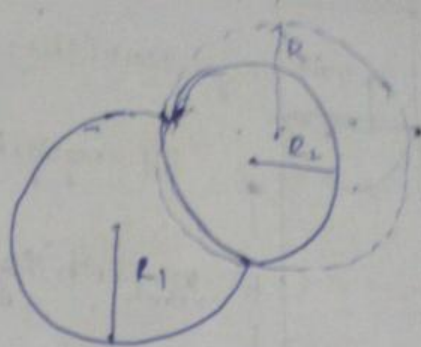
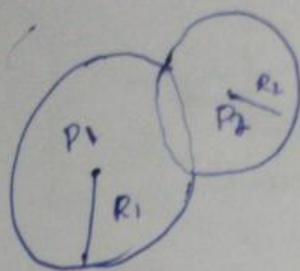


Thus, the following acids are arranged in order of increasing acidity (based on  $\text{pK}_a$  values):



Direct attachment of groups such as phenyl or vinyl to the carboxylic

Double bubble



$$P_0 \quad \Delta P = P_1 - P_0 = \frac{4T}{R_1}$$

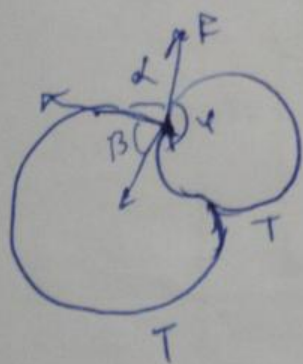
$$\Delta P = P_2 - P_0 = \frac{4T}{R_2}$$

$$\Delta P = P_1 - P_2 = \frac{4T}{R}$$

$$\frac{4T}{R_1} - \frac{4T}{R_2} = \frac{4T}{R}$$

$$\frac{1}{R_1} - \frac{1}{R_2} = \frac{1}{R}$$

$$R = \frac{R_1 R_2}{R_1 - R_2}$$

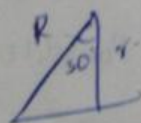
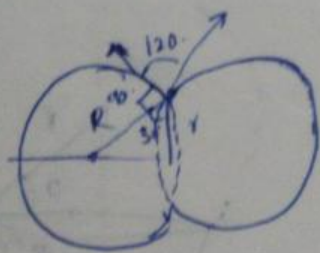


$$\alpha = \beta = \gamma = 120^\circ$$

Because particles is in equilibrium under equal forces.

$$R_1 = R_2$$

$$R = \frac{R_1 R_2}{R_1 - R_2} \approx \infty$$

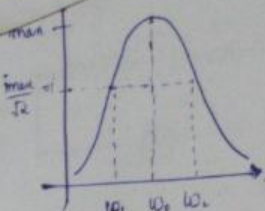


$$\cos 30^\circ = \frac{R_1}{R}$$

$$R = \frac{R_1}{\cos 30^\circ}$$



$\omega_1$  and  $\omega_2$  are frequencies related to half of max power.



Band width of circuit

$$\omega_0 = \frac{1}{\sqrt{LC}}$$

$$\omega L - \frac{1}{\omega C} = \pm R$$

$$\omega^2 LC - 1 = \pm \omega RC$$

$$\omega^2 LC \mp \omega RC - 1 = 0$$

$$\omega = \frac{\pm RC \pm \sqrt{C^2 R^2 + 4LC}}{2LC}$$

$$\left\{ \begin{aligned} \omega_1 &= \frac{-RC \pm \sqrt{C^2 R^2 + 4LC}}{2LC} \\ \omega_2 &= \frac{\sqrt{C^2 R^2 + 4LC} + RC}{2LC} \end{aligned} \right\}$$

$\omega_2 - \omega_1 = \text{band width of circuit}$

$$= \frac{2RC}{2LC} = \frac{R}{L}$$

$$Q_{\text{factor}} = \frac{\text{band width}}{\text{Resonance angular frequency}}$$

(Resonant angular frequency)

Band width

$$= \frac{\omega_2 - \omega_1}{\omega_0}$$

$$= \frac{\frac{1}{\sqrt{LC}}}{\frac{R}{L}} = \frac{1}{R} \cdot \frac{L}{\sqrt{LC}}$$

$$Q_{\text{factor}} = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$Q_{\text{factor}} = \frac{\text{Voltage across inductor or capacitor}}{\text{Net voltage}}$$

$$= \left( \frac{V_L}{V_{\text{net}}} \text{ or } \frac{V_C}{V_{\text{net}}} \right)$$

$$= \left( \frac{V_L}{R} \text{ or } \frac{V_C}{R} \right)$$

$$= \frac{1}{\omega RC} \text{ or } \frac{\omega L}{R} = \frac{1}{R} \sqrt{\frac{L}{C}} \text{ or } \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$Q_{\text{factor}} = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$i_0 = \frac{V_0}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$\frac{i_{\text{max}}}{2} = \frac{V_0}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$\frac{V_0}{\sqrt{2} R} = \frac{V_0}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$(X_L - X_C)^2 + R^2 = 2R^2$$

$$(X_L - X_C)^2 = R^2$$

$$X_L - X_C = \pm R$$



$$w_{\perp e} = \frac{k \lambda}{d} (\sin \alpha + \sin \beta) \rightarrow E_{\perp}$$

$$= \frac{k \lambda}{d} (\cos \beta - \cos \alpha) \rightarrow E_{\parallel}$$

$$loop = \frac{2k \lambda}{R} \sin\left(\frac{\alpha}{2}\right)$$



## Gamma function

$$\Gamma(n) = \int_0^{\infty} e^{-x} \cdot x^{n-1} dx$$

### properties

$$1) \Gamma(n+1) = n\Gamma(n)$$

$$2) \Gamma(n+1) = n!$$

$$3) \Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$$

$$4) \Gamma(1) = 1$$

$$\int_0^{\pi/2} \frac{\sin^m x \cdot \cos^n x}{2} dx = \frac{\Gamma\left(\frac{m+1}{2}\right) \Gamma\left(\frac{n+1}{2}\right)}{2 \Gamma\left(\frac{m+n+2}{2}\right)}$$

### Wallis's formula

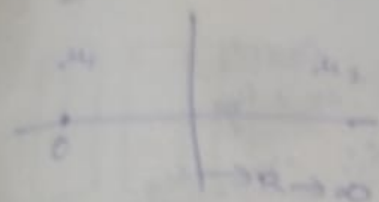
$$\int_0^{\pi/2} \sin^n x \cdot dx = \frac{n-1}{n} \cdot \frac{n-3}{n-2} \cdot \frac{n-5}{n-4} \dots \rightarrow \text{If } n \text{ is even}$$

$$= \frac{n-1}{n} \cdot \frac{n-3}{n-2} \cdot \frac{n-5}{n-4} \dots \frac{1}{2} \cdot 1, \text{ if } n \text{ is odd}$$

$$(2) \int_0^{\pi/2} \sin^6 x \cdot dx = \int_0^{\pi/2} \sin^4 x \cdot \cos^2 x \cdot dx$$

$$\begin{aligned} &= \frac{\Gamma\left(\frac{6+1}{2}\right) \Gamma\left(\frac{0+1}{2}\right)}{2 \Gamma\left(\frac{6+2}{2}\right)} = \frac{\Gamma\left(\frac{7}{2}\right) \Gamma\left(\frac{1}{2}\right)}{2 \Gamma(4)} = \frac{\frac{5}{2} \Gamma\left(\frac{5}{2}\right) \cdot \sqrt{\pi}}{2 \times 3!} \\ &= \frac{\frac{5}{2} \cdot \frac{3}{2} \cdot \frac{1}{2} \Gamma\left(\frac{1}{2}\right) \cdot \sqrt{\pi}}{2 \times 6} = \frac{12 \cdot \sqrt{\pi}}{5 \times 3 \times 12} = \frac{96}{15 \times 12} = \frac{15\pi}{96} \end{aligned}$$

## Refraction of Plane Surfaces



$$\frac{\mu_2}{v} = \frac{\mu_1}{u}$$

Consider a pool of water containing water to a depth 'h' if an observer views the base of the pool along a normal to the free surface then find the depth as observed by him.

Sol:  $\frac{\mu}{v} = \frac{1}{H} \Rightarrow H_{\text{app}} = \frac{H_{\text{real}}}{\mu}$

Note: the observed depth =  $H_{\text{app}}$  = apparent depth

the actual depth =  $H_{\text{real}}$  = real depth



Find

- Distance of the ~~image~~ bird as seen by the fish from it
- Dist of the fish as seen by the bird from it

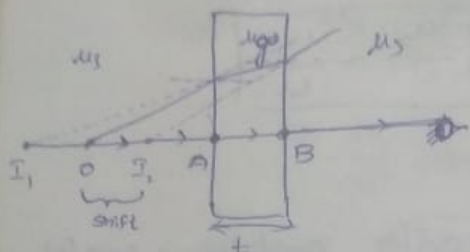
Sol: i)  $\frac{4}{3v} = \frac{1}{-40} \Rightarrow v = \frac{-160}{3}$

$$d = \frac{160}{3} + 60 = \frac{340}{3} \text{ cm}$$

ii)  $\frac{1}{v} = \frac{4}{180} \Rightarrow v = \frac{180}{4} = 45 \text{ cm}$

$$d = 85 \text{ cm}$$

# Refraction through parallel sided glass slab



Case-1

$$\mu_s \neq \mu_g$$

$$S_i: \frac{\mu_g}{-A I_1} = \frac{\mu_s}{-A O}$$

$$\Rightarrow A I_1 = A O \cdot \frac{\mu_g}{\mu_s} \quad \text{--- (1)}$$

$$S_i: B I_1 = A I_1 + A B$$

$$B I_1 = \frac{\mu_g}{\mu_s} A O + t$$

$$\frac{\mu_s}{B I_2} = \frac{\mu_g}{B I_1} \Rightarrow B I_2 = \frac{\mu_s}{\mu_g} \cdot B I_1 = A O + \frac{\mu_s}{\mu_g} \cdot t$$

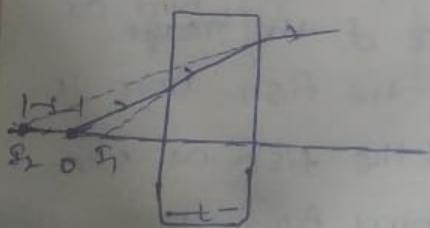
$$A I_2 = B I_2 - A B = A O + \left[ \frac{\mu_s}{\mu_g} t - t \right]$$

$$\Rightarrow A O - A I_2 = t \left[ 1 - \frac{\mu_s}{\mu_g} \right]$$

$$\frac{\mu_g}{\mu_s} = \mu_{rel}$$

$$= t \left[ 1 - \frac{1}{\mu_{rel}} \right]$$

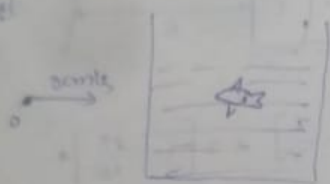
Case-II



$$s = t \left[ 1 - \frac{1}{\mu_{rel}} \right]$$

$$\mu_r = \frac{\mu_g}{\mu_s}$$

Q Figure shows a cubical container filled with water. A fish is moving towards one of the walls with a speed of 4 cm/s and an observer also moves towards the wall at a speed of 3 cm/s. Find  
 i) Speed of 'o' seen by fish  
 ii) Speed of 'f' seen by 'o'



i)  $v_{f/o}$

$$\frac{u_2}{v} = \frac{u_1}{u}$$

$$\frac{u_1}{v_{f/o}} = \frac{4}{3 \times 4}$$

$$\Rightarrow v_{f/o} = -\frac{4}{3} \times 4$$

$$\Delta x_{f/o} = x_o + v_f$$

$$= x_o + \frac{3}{4} x_f$$

by differentiating

$$\vec{v}_{f/o} = -3 + \frac{3}{4}(-4)$$

$$= -6 \text{ cm/s}$$

ii)  $\vec{v}_{o/f}$

$$\frac{u_2}{v} = \frac{u_1}{u} \Rightarrow \frac{4}{3v_o} = \frac{1}{4} \Rightarrow v_o = \frac{4}{3} \times 4$$

$$\Delta x_{o/f} = x_f + v_o = x_f + \frac{4}{3} x_o$$

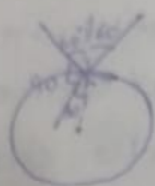
by diff

$$\Rightarrow \vec{v}_{o/f} = -4 + \frac{4}{3}(-3) = -8 \text{ cm/s}$$

Q How much water should be filled in a container of height 21 cm so that it will appear half filled when viewed along normal to water surface ( $\mu_w = \frac{4}{3}$ )



Q A light ray incident on the point on the surface of the glass sphere of  $\mu = \sqrt{3}$  at an angle of incidence  $60^\circ$ . It is reflected and refracted into the farther surface of sphere. Find angle between reflected & refracted ray.



$$\frac{\sqrt{3}}{2 \sin r} = \sqrt{3} \Rightarrow r = 30^\circ$$

$$\Rightarrow \text{angle} = 90^\circ$$

Q A ray of light travels from a liquid of  $\mu_1$  into air. If incident beam is rotating at angular speed  $\omega$  then what is the angular speed of refracted beam at the instant the angle of incidence is  $30^\circ$  [ $\mu = \sqrt{2}$ ] [ $\omega = \frac{1}{\sqrt{6}} \text{ rad/sec}$ ]

$$\mu_1 \sin i = \mu_2 \sin r$$

$$\mu_1 \cos i \cdot \frac{di}{dt} = \mu_2 \cos r \cdot \frac{dr}{dt}$$

$$\frac{dr}{dt} = \frac{\sqrt{2} \times \frac{1}{\sqrt{6}} \times \sqrt{2}}{\sqrt{2} \times \frac{1}{\sqrt{2}}}$$

$$= \frac{1}{\sqrt{2}}$$

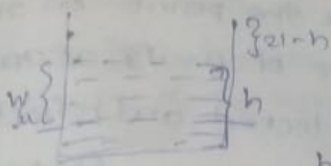
$$\mu = \frac{\sin i}{\sin r}$$

$$\sin r = \frac{1}{\sqrt{2}}$$

$$\cos r = \sqrt{1 - \frac{1}{2}}$$

$$= \frac{1}{\sqrt{2}}$$

$$\frac{\sqrt{2}}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$



$$\frac{h}{w} = 21 - h$$

$$\Rightarrow \frac{3}{4}h = 21 - h \Rightarrow h = 12 \text{ cm}$$

Q A small obj is kept at centre of bottom of cylindrical beaker of diameter 6cm and height 10cm filled completely with water ( $\mu = \frac{4}{3}$ ) consider the light ray from the obj leaving the beaker through a corner. If this ray and the ray along the axis of beaker is used to locate the image. Find the apparent depth in this case



$$\sin i = \frac{3}{x}$$

$$\tan i = \frac{3}{10} \text{ (if } 3 \text{ )}$$

$$\tan r = \frac{3}{10}$$

1 did wrong

$$\frac{4}{3} = \frac{\sin i}{\sin r}$$

$$\mu = \frac{16}{3}$$

$$\frac{4}{3} = \frac{3}{10 \sin r} \Rightarrow \sin r = \frac{9}{20}$$

$$\frac{4}{3} = \frac{\sin r \times 5}{3}$$

$$r = 53$$

$$\tan 53 = \frac{3}{4}$$

$$\frac{4}{3} = \frac{3}{10} \Rightarrow \mu = \frac{9}{4} = 2.25$$

$+1$  AC  
 $+3$  A  
 $+1$  -80

20) AA  
 30) ABC  
 30) - AC

$$\frac{T_1}{T_2} = \frac{120}{10} \quad (2x)$$

on the  
 at angle  
 refracted  
 Find angle

A parallel beam of width  $l$  is incident from air on to a boundary in air and water. find the width of the refracted beam ( $\mu = \frac{4}{3}$ )



$t$  - remaining same

$$\frac{1}{\sqrt{2} \sin r} = \frac{4}{3}$$

$$\sin r = \frac{3}{4\sqrt{2}}$$

$$\cos r = \sqrt{1 - \frac{9}{32}}$$

$$= \frac{\sqrt{23}}{4\sqrt{2}} = \frac{t}{AB}$$

$$\Rightarrow AB = \frac{4\sqrt{2}}{\sqrt{23}} \cdot t$$

$$\cos r \cdot \frac{1}{\sqrt{2}} = \frac{t}{AB}$$

$$AB = t\sqrt{2}$$

$$\frac{t \cdot \frac{1}{\sqrt{2}}}{\frac{1}{\sqrt{23}}} = t \cdot \sqrt{2}$$

$$t' = \frac{t\sqrt{23}}{6}$$

of  $R=1$   
 at constant  
 of  
 angle of  
 and/sec?

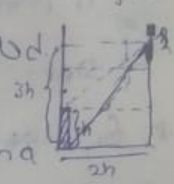
$$\frac{9m}{5m}$$

$$r = \frac{1}{2\sqrt{2}}$$

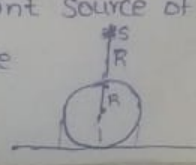
$$\sqrt{1 - \frac{1}{8}}$$

$$\frac{1}{2\sqrt{2}}$$

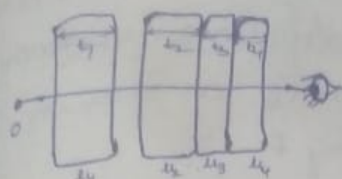
An observer can see through a pin hole, the top end of the thin rod of height  $h$ . When the beaker is filled with a liquid of height  $2h$ , he cannot see lower end of the rod.



An opaque sphere of radius  $R$  lies on a horizontal plane on the perpendicular to through the point of contact there is a point source of light at a dist.  $R$  above the sphere.



- i) find the area of shadow on the plane.  $3\pi R^2$
- ii) A transparent liquid of  $\mu = \sqrt{3}$  is filled above the plane such that sphere is just covered with liquid. find the new area of shadow formed.

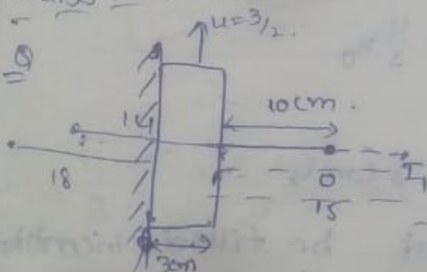


$$S = \sum_{i=1}^N l_i \left(1 - \frac{1}{\mu_{r_i}}\right)$$

Note: Even if slabs are kept in contact with each other. We can use the formula shift directly by assuming negligible thickness of the air

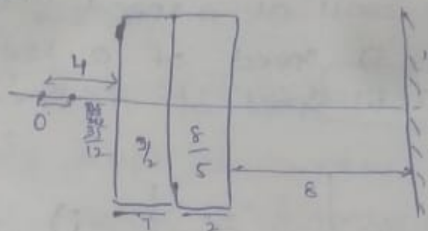
surrounding to be present b/w the two

slabs



Q Find the location of the final image w.r.t to obj.'s initial location

Sol



$$S = 1 \left[1 - \frac{2}{3}\right] + 2 \left[1 - \frac{2.5}{4}\right]$$

$$= 1 \cdot \frac{1}{3} + \frac{3}{4} = \frac{13}{12}$$

$$S = 2 \left[1 - \frac{5}{8}\right] + 1 \left[1 - \frac{2}{5}\right]$$

$$= \frac{3}{4} + \frac{1}{5} = \frac{19}{20}$$

$$S = 2.8 + \frac{1}{2} = \frac{5.7}{2}$$

$$= \frac{33.4}{12}$$

Note: Even

$$\frac{3}{2v} = \frac{1}{-15}$$

$$v = -15 \text{ cm}$$

$$\frac{1}{v} = \frac{3}{-2 \times 21}$$

$$\text{dis} = 24 \text{ cm}$$