

# DAG Query

Input file:            **standard input**  
Output file:          **standard output**  
Time limit:          3 seconds  
Memory limit:        1024 megabytes

This is an interactive problem.

Given a directed acyclic graph (DAG) with  $n$  vertices and  $m$  edges, each edge has an associated weight.

There may be multiple paths between any pair of vertices  $s$  and  $t$ . We define the weight of a path as the product of the weights of all edges along that path. Let  $f(s, t, c)$  denote the sum of the path weights of all distinct paths from  $s$  to  $t$  after multiplying the weight of every edge in the graph by  $c$ . Since the result can be extremely large,  $f(s, t, c)$  is taken modulo 998244353.

Xiao M will inform you of the structure of the DAG in advance (excluding the edge weights).

You may provide parameters  $s$ ,  $t$ , and  $c$ ; the interactor will return the value of  $f(s, t, c)$ . You are allowed to make at most 999 such queries to obtain certain information about the graph. After several query cycles, the interactor will provide a parameter  $k$ , and you need to determine the value of  $f(1, n, k)$ .

## Input

The first line contains two positive integers  $n$  and  $m$  ( $1 \leq n \leq 1000, 1 \leq m \leq 5000$ ), where  $n$  represents the number of vertices in the graph and  $m$  represents the number of edges.

In the following  $m$  lines, each line contains two positive integers  $x$  and  $y$  ( $1 \leq x, y \leq 1000$ ), indicating that there is a directed edge from vertex  $x$  to vertex  $y$  in the graph. It is guaranteed that the graph is a Directed Acyclic Graph (DAG).

## Interaction Protocol

For each query, you need to output in the format `? s t c` ( $1 \leq s, t \leq n, 0 \leq c < 998244353$ ) where  $s, t, c$  are all integers, and the interactor will return the answer of  $f(s, t, c)$ .

When you are confident that the information you have is sufficient to answer the query, output `!`, and the interactor will return a integer parameter  $k$  ( $0 \leq k < 998244353$ ), which means you are asked for the weight of  $f(1, n, k)$ .

You need to output the result of  $f(1, n, k)$ .

After printing a query or the answer, do not forget to output the end of the line and flush the output. Otherwise, you will get the verdict `Idleness Limit Exceeded`. To do this, use:

`fflush(stdout)` or `cout.flush()` in C++; `System.out.flush()` in Java; `flush(output)` in Pascal; `stdout.flush()` in Python; see the documentation for other languages.

## Example

standard input	standard output
3 3	? 1 2 1
1 2	
2 3	? 2 3 1
1 3	
	? 1 3 1
1	
	!
2	
	31488
12	
123	