# Adversarial Robustness and Anomaly Detection for Financial ML Models

#### Introduction

In financial systems, defending against adversarial inputs and detecting out-ofdistribution (OOD) anomalies is crucial. Adversarial attacks can craft subtle perturbations to evade detection, while OOD anomalies represent rare, unexpected market behaviors (e.g., fraud, flash crashes).

### Algorithm Overview

Mahalanobis Distance: Measures distance to the in-distribution mean under estimated covariance, highlighting deviations.

$$D_M(x) = \sqrt{(x-\mu)^{\top} \Sigma^{-1} (x-\mu)}$$

Autoencoder Reconstruction Error: Trains to minimize self-reconstruction loss; large error indicates anomaly.

$$E(x) = ||x - \hat{x}||^2$$

**Ensemble Score:** Combines Mahalanobis and autoencoder signals to improve detection across linear and non-linear structures.

## Thresholding

Uses Extreme Value Theory (EVT) to model score tails and determine principled thresholds rather than arbitrary percentiles, providing statistical rigor.

#### Robustness Tests

Includes bootstrap confidence intervals on AUC metrics and adversarial perturbation tests (FGSM) to evaluate model resilience.

## Conclusion

This module provides a comprehensive and theoretically sound framework to secure financial ML models against unexpected and adversarially crafted anomalies.