

1. \mathcal{S}
2. $a \neq 0$
3. $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
4. $X = \{x_1, x_2, \dots, x_n\}$
5. $X = \{x : x \text{ satisfies } \mathcal{P}\}$
6. $-3 \notin E$
7. $\{4, 5, 8\} \subset \{2, 3, 4, 5, 6, 7, 8, 9\}$
8. $\mathbb{N} \subset \mathbb{Z} \subset \mathbb{Q} \subset \mathbb{R} \subset \mathbb{C}$
9. $A \not\subset B$
10. $\bigcup_{i=1}^n A_i = A_1 \cup \dots \cup A_n$
11. $\bigcap_{i=1}^n A_i = A_1 \cap \dots \cap A_n$
12. $A \setminus B = A \cap B' = \{x : x \in A \text{ and } x \notin B\}$
13. $A \xrightarrow{f} B$
14. $f : a \mapsto b$
15. $a_1 \neq a_2$
16. $(f \circ g)(x) = f(g(x)) = f(\sqrt[3]{x}) = (\sqrt[3]{x})^3 = x$
17. $\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} ax + by \\ cx + dy \end{pmatrix}$
18. $\begin{pmatrix} 1 & 2 & 3 \\ \pi(1) & \pi(2) & \pi(3) \end{pmatrix} = \begin{pmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \end{pmatrix}$
19. $g \circ f = id_A$
20. $x \sim y, x \cong y$
21. $psu = qru = qst$
22. $C = QBQ^{-1} = QPAP^{-1}Q^{-1} = (QP)A(QP)^{-1}$
23. $[x] = \{y \in X : y \sim x\}$
24. $r \equiv s \pmod{n}$
25. $A \times D = \emptyset$
26. $f(p/q) = \frac{3p}{3q}$
27. $mn > 0$
28. $|x - y| \leq 4$
29. $a^2 + b^2 \leq c^2 + d^2$

$$30. \binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$31. \gcd(a, b) = ar + bs$$

$$32. 2^{2^5} + 1 = 4,294,967,297$$

$$33. \sqrt[n]{a_1 a_2 \cdots a_n} \leq \frac{1}{n} \sum_{k=1}^n a_k$$

$$34. \lim_{n \rightarrow \infty} f_n / f_{n+1} = (\sqrt{5} - 1)/2$$

$$35. c = 4\,598\,037\,234$$

$$36. \begin{array}{c|cccccccc} \cdot & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 2 & 0 & 2 & 4 & 6 & 0 & 2 & 4 & 6 \\ 3 & 0 & 3 & 6 & 1 & 4 & 7 & 2 & 5 \\ 4 & 0 & 4 & 0 & 4 & 0 & 4 & 0 & 4 \\ 5 & 0 & 5 & 2 & 7 & 4 & 1 & 6 & 3 \\ 6 & 0 & 6 & 4 & 2 & 0 & 6 & 4 & 2 \\ 7 & 0 & 7 & 6 & 5 & 4 & 3 & 2 & 1 \end{array}$$

$$37. \triangle ABC$$

$$38. 120^\circ$$

$$39. \mu_1 \rho_1$$

$$40. \begin{array}{c|cccccc} \circ & \text{id} & \rho_1 & \rho_2 & \mu_1 & \mu_2 & \mu_3 \\ \hline \text{id} & \text{id} & \rho_1 & \rho_2 & \mu_1 & \mu_2 & \mu_3 \\ \rho_1 & \rho_1 & \rho_2 & \text{id} & \mu_3 & \mu_1 & \mu_2 \\ \rho_2 & \rho_2 & \text{id} & \rho_1 & \mu_2 & \mu_3 & \mu_1 \\ \mu_1 & \mu_1 & \mu_2 & \mu_3 & \text{id} & \rho_1 & \rho_2 \\ \mu_2 & \mu_2 & \mu_3 & \mu_1 & \rho_2 & \text{id} & \rho_1 \\ \mu_3 & \mu_3 & \mu_1 & \mu_2 & \rho_1 & \rho_2 & \text{id} \end{array}$$

$$41. \begin{array}{c|ccccc} + & 0 & 1 & 2 & 3 & 4 \\ \hline 0 & 0 & 1 & 2 & 3 & 4 \\ 1 & 1 & 2 & 3 & 4 & 0 \\ 2 & 2 & 3 & 4 & 0 & 1 \\ 3 & 3 & 4 & 0 & 1 & 2 \\ 4 & 4 & 0 & 1 & 2 & 3 \end{array}$$

$$42. a^{-1}(a^{-1})^{-1} = e$$

$$43. g^{-n} = \underbrace{g^{-1} \cdot g^{-1} \cdots g^{-1}}_{n \text{ times}}$$

$$44. \mathbb{Q}^* = \{p/q : p \text{ and } q \text{ are nonzero integers}\}$$

$$45. SL_2(\mathbb{R})$$

$$46. \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} + \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

$$47. \begin{array}{c|cccc} + & (0,0) & (0,1) & (1,0) & (1,1) \\ \hline (0,0) & (0,0) & (0,1) & (1,0) & (1,1) \\ (0,1) & (0,1) & (0,0) & (1,1) & (1,0) \\ (1,0) & (1,0) & (1,1) & (0,0) & (0,1) \\ (1,1) & (1,1) & (1,0) & (0,1) & (0,0) \end{array}$$

$$48. \begin{array}{c|cccc} \circ & a & b & c & d \\ \hline a & a & c & d & a \\ b & b & b & c & d \\ c & c & d & a & b \\ d & d & a & b & c \end{array}$$

$$49. \begin{array}{c|cccc} \circ & a & b & c & d \\ \hline a & a & b & c & d \\ b & b & a & d & c \\ c & c & d & a & b \\ d & d & c & b & a \end{array}$$

$$50. \begin{array}{c|cccc} \circ & a & b & c & d \\ \hline a & a & b & c & d \\ b & b & c & d & a \\ c & c & d & a & b \\ d & d & a & b & c \end{array}$$

$$51. \begin{array}{c|cccc} \circ & a & b & c & d \\ \hline a & a & b & c & d \\ b & b & a & c & d \\ c & c & b & a & d \\ d & d & d & b & c \end{array}$$

$$52. \begin{array}{c|cccc} \cdot & 1 & 5 & 7 & 11 \\ \hline 1 & 1 & 5 & 7 & 11 \\ 5 & 5 & 1 & 11 & 7 \\ 7 & 7 & 11 & 1 & 5 \\ 11 & 11 & 7 & 5 & 1 \end{array}$$

$$53. \begin{pmatrix} 1 & x & y \\ 0 & 1 & z \\ 0 & 0 & 1 \end{pmatrix}$$

$$54. \begin{pmatrix} 1 & x & y \\ 0 & 1 & z \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & x' & y' \\ 0 & 1 & z' \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & x+x' & y+y'+xz' \\ 0 & 1 & z+z' \\ 0 & 0 & 1 \end{pmatrix}$$

$$55. \sigma = \begin{pmatrix} 1 & 2 & \cdots & n \\ a_1 & a_2 & \cdots & a_n \end{pmatrix}$$

$$56. H_2 = \{\text{id}, \rho_1, \rho_2\}$$

$$57. \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

$$58. G = \{a + b\sqrt{2} : a, b \in \mathbb{Q} \text{ and } a \text{ and } b \text{ are not both zero}\}$$

$$59. H = \left\{ \begin{pmatrix} a & b \\ c & d \end{pmatrix} : a + d = 0 \right\}$$

$$60. (d_1, d_2, \dots, d_{10}) \cdot (10, 9, \dots, 1) \equiv 0 \pmod{11}$$

$$61. \ 6.00000 + 0.00000i$$

$$62. \ \langle a \rangle = \{a^k : k \in \mathbb{Z}\}$$

$$63. \ z^{-1} = \frac{a-bi}{a^2+b^2}$$

$$64. \ \overline{z} = a-bi$$

$$65. \ z = \operatorname{cis}\left(\frac{2k\pi}{n}\right)$$

$$66. \ *$$

$$67. \ A = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \quad \text{and} \quad B = \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}$$

$$68. \ \begin{array}{c|cccc} \circ & \text{id} & \sigma & \tau & \mu \\ \hline \text{id} & \text{id} & \sigma & \tau & \mu \\ \sigma & \sigma & \text{id} & \mu & \tau \\ \tau & \tau & \mu & \text{id} & \sigma \\ \mu & \mu & \tau & \sigma & \text{id} \end{array}$$

$$69. \ \sigma = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 6 & 3 & 5 & 1 & 4 & 2 & 7 \end{pmatrix} = (162354)$$

$$70. \ \tau = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 1 & 4 & 2 & 3 & 5 & 6 \end{pmatrix} = (243)$$

$$71. \ \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 2 & 4 & 1 & 3 & 6 & 5 \end{pmatrix} = (1243)(56)$$

$$72. \ 1 \mapsto 3, \quad 3 \mapsto 5, \quad 5 \mapsto 2, \quad 2 \mapsto 1$$

$$73. \ (16)(253) = (16)(23)(25) = (16)(45)(23)(45)(25)$$

$$74. \ \lambda_\sigma : A_n \rightarrow B_n$$

$$75. \ \text{id}, \frac{360^\circ}{n}, 2 \cdot \frac{360^\circ}{n}, \dots, (n-1) \cdot \frac{360^\circ}{n}$$

$$76. \ D_n = \{1, r, r^2, \dots, r^{n-1}, s, sr, sr^2, \dots, sr^{n-1}\}$$

$$77. \ Z(G) = \{g \in G : gx = xg \text{ for all } x \in G\}$$

$$78. \ \mathcal{O}_{x,\sigma} = \{y : x \sim y\}$$

$$79. \ \phi : \mathcal{L}_H \rightarrow \mathcal{R}_H$$

$$80. \ [G:K] = \frac{|G|}{|K|} = \frac{|G|}{|H|} \cdot \frac{|H|}{|K|} = [G:H][H:K]$$

$$81. \ (1), (123), (132), (243), (243)^{-1} = (234), (142), (142)^{-1} = (124)$$

$$82. \ p \nmid a$$

$$83. \ \phi(n) = n \left(1 - \frac{1}{p_1}\right) \left(1 - \frac{1}{p_2}\right) \cdots \left(1 - \frac{1}{p_k}\right)$$

$$84. \ \mathbf{b} = (2, 2)^{\mathfrak{t}}$$

$$85. \ A = 00, B = 02, \dots, Z = 25$$

$$86. \ 169^{191} \bmod 667 = 25$$

$$87. y^D = x^{km+1} = x^{kn} = (1 + tq)x = x + tq(rp) = x + trn = x \bmod n$$

$$88. n = 3551, E = 629, x = 31$$

$$89. 2^{15-1} \equiv 2^{14} \equiv 4 \pmod{15}$$

$$90. (x_1, x_2, \dots, x_n) \mapsto (x_1, x_2, \dots, x_n, x_1, x_2, \dots, x_n, x_1, x_2, \dots, x_n)$$

$$91. (0.999)^{10,000} \approx 0.00005$$

$$92. \binom{n}{k} q^k p^{n-k}$$

$$93. \binom{n}{1} qp^{n-1} = 500(0.005)(0.995)^{499} \approx 0.204$$

$$94. \binom{n}{2} q^2 p^{n-2} = \frac{500 \cdot 499}{2} (0.005)^2 (0.995)^{498} \approx 0.257$$

$$95. H \in \mathbb{M}_{m \times n}(\mathbb{Z}_2)$$

$$96. H\mathbf{x} = \mathbf{0}$$

$$97. \text{Null}(H)$$

$$98. \begin{pmatrix} a_{11} & a_{12} & \cdots & a_{1,n-m} \\ a_{21} & a_{22} & \cdots & a_{2,n-m} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{m,n-m} \end{pmatrix}$$

$$99. G = \left(\frac{I_{n-m}}{A} \right)$$

$$100. G = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix}$$

$$101. \mathbf{x} = (x_1, x_2, x_3, x_4, x_5, x_6)$$

$$102. \begin{pmatrix} 000000 & 001101 & 010110 & 011011 \\ 100011 & 101110 & 110101 & 111000 \end{pmatrix}.$$

$$103. \delta_{ij} = \begin{cases} 1 & i = j \\ 0 & i \neq j \end{cases}$$

$$104. \begin{pmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$$

$$105. H\mathbf{x} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, H\mathbf{y} = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, H\mathbf{z} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

$$106. \begin{pmatrix} 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 \end{pmatrix}$$

$$107. G = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \\ 0 & 1 \\ 1 & 1 \end{pmatrix}$$

$$108. C^\perp = \{\mathbf{x} \in \mathbb{Z}_2^n : \mathbf{x} \cdot \mathbf{y} = 0 \text{ for all } \mathbf{y} \in C\}$$

$$109. 2^k \left(\binom{n}{0} + \binom{n}{1} + \binom{n}{2} + \cdots + \binom{n}{\frac{d-1}{2}} \right) = 2^n$$

$$110. \phi(a \cdot b) = \phi(a) \circ \phi(b)$$

$$111. G \cong H$$

$$112. \begin{array}{c|ccc} + & 0 & 1 & 2 \\ \hline 0 & 0 & 1 & 2 \\ 1 & 1 & 2 & 0 \\ 2 & 2 & 0 & 1 \end{array}$$

$$113. \prod_{i=1}^n G_i = G_1 \times G_2 \times \cdots \times G_n$$

$$114. \prod G_i$$

$$115. \underbrace{(a,b) + (a,b) + \cdots + (a,b)}_{mn/d \text{ times}} = (0,0)$$

$$116. \mathbb{Z}_{p_1^{e_1}} \times \cdots \times \mathbb{Z}_{p_k^{e_k}}$$

$$117. a * b = a + b + ab$$

$$118. A = \begin{pmatrix} \omega & 0 \\ 0 & \omega^{-1} \end{pmatrix} \quad \text{and} \quad B = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

$$119. \begin{pmatrix} \pm 1 & k \\ 0 & 1 \end{pmatrix}$$

$$120. \operatorname{Inn}(G) = \operatorname{Aut}(G)$$

$$121. g \mapsto \rho_g$$

$$122. G \times H \cong \overline{G} \times \overline{H}$$

$$123. \langle m \rangle \cap \langle n \rangle = \langle l \rangle$$

$$124. \{z^i y^j \mid 0 \leq i < p, 0 \leq j < 2\}$$

$$125. \begin{array}{c|cc} & N & (12)N \\ \hline N & N & (12)N \\ (12)N & (12)N & N \end{array}$$

126.
$$\begin{array}{c|ccc} + & 0+3\mathbb{Z} & 1+3\mathbb{Z} & 2+3\mathbb{Z} \\ \hline 0+3\mathbb{Z} & 0+3\mathbb{Z} & 1+3\mathbb{Z} & 2+3\mathbb{Z} \\ 1+3\mathbb{Z} & 1+3\mathbb{Z} & 2+3\mathbb{Z} & 0+3\mathbb{Z} \\ 2+3\mathbb{Z} & 2+3\mathbb{Z} & 0+3\mathbb{Z} & 1+3\mathbb{Z} \end{array}$$
127. $[(ij)(ak)][ija]^2[(ij)(ak)]^{-1} = (ijk)$
128. $\sigma^{-1}(a_1a_2a_4)\sigma(a_1a_2a_4)^{-1} \in N$
129. $(a_1a_2a_4)\sigma(a_1a_2a_4)^{-1} \in N$
130. $\ker \phi = SL_2(\mathbb{R})$
131. $\eta(g_1K) = \psi(g_1) = \psi(g_1)\psi(k) = \psi(g_1k) = \psi(g_2) = \eta(g_2K)$
132. $\mathbb{Z}/\ker \phi = \mathbb{Z}/m\mathbb{Z} \cong G$
133. $(hn)^{-1} = n^{-1}h^{-1} = h^{-1}(hn^{-1}h^{-1})$
134. $G \rightarrow G/N \rightarrow \frac{G/N}{H/N}$
135. $\begin{pmatrix} 3/5 & -4/5 \\ 4/5 & 3/5 \end{pmatrix}, \quad \begin{pmatrix} 1/2 & -\sqrt{3}/2 \\ \sqrt{3}/2 & 1/2 \end{pmatrix}, \quad \begin{pmatrix} -1/\sqrt{2} & 0 & 1/\sqrt{2} \\ 1/\sqrt{6} & -2/\sqrt{6} & 1/\sqrt{6} \\ 1/\sqrt{3} & 1/\sqrt{3} & 1/\sqrt{3} \end{pmatrix}$
136. $\|\mathbf{x}\| = \sqrt{\langle \mathbf{x}, \mathbf{x} \rangle} = \sqrt{x_1^2 + \cdots + x_n^2}$
137. $\langle A\mathbf{x}, A\mathbf{y} \rangle = \langle \mathbf{x}, \mathbf{y} \rangle$
138. $(2) \Rightarrow (3)$
139. $\langle \mathbf{x}, \mathbf{y} \rangle = \frac{1}{2} [\|\mathbf{x} + \mathbf{y}\|^2 - \|\mathbf{x}\|^2 - \|\mathbf{y}\|^2]$
140. $T_\phi = \begin{pmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} = \begin{pmatrix} \cos \phi & \sin \phi \\ \sin \phi & -\cos \phi \end{pmatrix}$
141. $\begin{pmatrix} 4/\sqrt{5} & 0 & 3/\sqrt{5} \\ -3/\sqrt{5} & 0 & 4/\sqrt{5} \\ 0 & -1 & 0 \end{pmatrix}$
142. $E(n) = \{(A, \mathbf{x}) : A \in O(n) \text{ and } \mathbf{x} \in \mathbb{R}^n\}$
143. $G = H_n \supset H_{n-1} \supset \cdots \supset H_1 \supset H_0 = \{e\}$
144. $\mathbb{Z}_{p_1^{\alpha_1}} \times \cdots \times \mathbb{Z}_{p_n^{\alpha_n}}$
145. $\{g_i \in G : i \in I\}$
146. $g^{-1} = (g_{i_1}^{k_1} \cdots g_{i_n}^{k_n})^{-1} = (g_{i_n}^{-k_n} \cdots g_{i_1}^{-k_1})$
147. $(gh)^{p_i^t} = g^{p_i^t} h^{p_i^t} = 1 \cdot 1 = 1$
148. $|g| = p_1^{\beta_1} p_2^{\beta_2} \cdots p_k^{\beta_k}$
149. $g = g^{a_1 b_1 + \cdots + a_k b_k} = g^{a_1 b_1} \cdots g^{a_k b_k}$
150. $g^{(a_i b_i) p_i^{\beta_i}} = g^{b_i |g|} = e$
151. $G^{(0)} = G \supset G^{(1)} \supset G^{(2)} \supset \cdots$

152. $Z_3 \rtimes Z_4$
153. $\phi(ab) = gabg^{-1} = gag^{-1}gbg^{-1} = \phi(a)\phi(b)$
154. $\sum_{y \in \mathcal{O}_x} |G_y| = |\mathcal{O}_x| \cdot |G_x|$
155. $|\widetilde{X}_{(13)(24)}| = 2^2 = 4$
156. $|\mathcal{S}| = |\text{orbit of } P| = [G : N(P)]$
157. $q \not\equiv 1 \pmod{p}$
158. $p \nmid \binom{p^k m}{p^k}$
159. 44\,352\,000
160. $\begin{pmatrix} \alpha & \beta \\ -\bar{\beta} & \bar{\alpha} \end{pmatrix}$
161. $(a_1 + b_1 \mathbf{i} + c_1 \mathbf{j} + d_1 \mathbf{k})(a_2 + b_2 \mathbf{i} + c_2 \mathbf{j} + d_2 \mathbf{k}) = \alpha + \beta \mathbf{i} + \gamma \mathbf{j} + \delta \mathbf{k}$
162. $T = \left\{ \begin{pmatrix} a & b \\ 0 & c \end{pmatrix} : a, b, c \in \mathbb{R} \right\}$
163. $A = \begin{pmatrix} a & b \\ 0 & c \end{pmatrix} \quad \text{and} \quad B = \begin{pmatrix} a' & b' \\ 0 & c' \end{pmatrix}$
164. $F = \left\{ \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 \\ 1 & 1 \end{pmatrix}, \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix} \right\}$
165. $\frac{a}{a^2-2b^2} + \frac{-b}{a^2-2b^2}\sqrt{2}$
166. $R/I \cong \frac{R/J}{I/J}$
167. $\left\{ \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}, \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix}, \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 \\ 1 & 1 \end{pmatrix}, \right\}$
168. $f(x) = \sum_{i=0}^n a_i x^i = a_0 + a_1 x + a_2 x^2 + \cdots + a_n x^n$
169. $c_i = \sum_{k=0}^i a_k b_{i-k} = a_0 b_i + a_1 b_{i-1} + \cdots + a_{i-1} b_1 + a_i b_0$
170. $p(x) = \frac{b_0}{c_0} + \frac{b_1}{c_1}x + \cdots + \frac{b_n}{c_n}x^n$
171. $p(x) = \alpha(x)\beta(x) = \frac{c_1c_2}{d_1d_2}\alpha_1(x)\beta_1(x) = \frac{c}{d}\alpha_1(x)\beta_1(x)$
172. $\omega^i \sqrt[3]{-\frac{q}{2} + \sqrt{\frac{p^3}{27} + \frac{q^2}{4}}} + \omega^{2i} \sqrt[3]{-\frac{q}{2} - \sqrt{\frac{p^3}{27} + \frac{q^2}{4}}}$
173. $D[x]$
174. $c_{r+s} = a_0 b_{r+s} + a_1 b_{r+s-1} + \cdots + a_{r+s-1} b_1 + a_{r+s} b_0$
175. $O \preceq \cdots \preceq b_3 \preceq b_2 \preceq b_1 \preceq b$

176. $a \not\leq c$

177. $a = a \wedge b = a \wedge (a_1 \vee \cdots \vee a_n) = (a \wedge a_1) \vee \cdots \vee (a \wedge a_n)$

178. $(a \wedge b') \vee (a' \wedge b) = O \Rightarrow a \vee b = (a \vee a) \vee b = a \vee (a \vee b) = a \vee [I \wedge (a \vee b)] =$
 $a \vee [(a \vee a') \wedge (a \vee b)] = [a \vee (a \wedge b')] \vee [a \vee (a' \wedge b)] = a \vee [(a \wedge b') \vee (a' \wedge b)] =$
 $a \vee 0 = a$

179. $u + v = (u_1, \dots, u_n) + (v_1, \dots, v_n) = (u_1 + v_1, \dots, u_n + v_n)$

180. $u + v = (\alpha_1 + \beta_1)v_1 + (\alpha_2 + \beta_2)v_2 + \cdots + (\alpha_n + \beta_n)v_n$

181. $v_k = -\frac{\alpha_1}{\alpha_k}v_1 - \cdots - \frac{\alpha_{k-1}}{\alpha_k}v_{k-1} - \frac{\alpha_{k+1}}{\alpha_k}v_{k+1} - \cdots - \frac{\alpha_n}{\alpha_k}v_n$

182. $E = \mathbb{Z}_2[x]/\langle x^2 + x + 1 \rangle$

183.

$+$	0	1	α	$1 + \alpha$
0	0	1	α	$1 + \alpha$
1	1	0	$1 + \alpha$	α
α	α	$1 + \alpha$	0	1
$1 + \alpha$	$1 + \alpha$	α	1	0

184.

\cdot	0	1	α	$1 + \alpha$
0	0	0	0	0
1	0	1	α	$1 + \alpha$
α	0	α	$1 + \alpha$	1
$1 + \alpha$	0	$1 + \alpha$	1	α

185. $\{1, \sqrt[6]{5}i, \sqrt[3]{5}, (\sqrt[3]{5})^2, (\sqrt[6]{5})^5i, (\sqrt[6]{5})^7i = 5\sqrt[6]{5}i \text{ or } \sqrt[6]{5}i\}$

186. $0 = f(\beta) = f\left(\frac{p(\alpha)}{q(\alpha)}\right) = a_0 + a_1\left(\frac{p(\alpha)}{q(\alpha)}\right) + \cdots + a_n\left(\frac{p(\alpha)}{q(\alpha)}\right)^n$

187. $(a+b)^p = \sum_{k=0}^p \binom{p}{k} a^k b^{p-k}$

188. $(a+b)^{p^{n+1}} = ((a+b)^p)^{p^n} = (a^p + b^p)^{p^n} = (a^p)^{p^n} + (b^p)^{p^n} = a^{p^{n+1}} + b^{p^{n+1}}$

189. $G_1 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad \text{and} \quad G_2 = \begin{pmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix}$

190.

$(000) \mapsto (000000)$	$(100) \mapsto (100100)$
$(001) \mapsto (001001)$	$(101) \mapsto (101101)$
$(010) \mapsto (010010)$	$(110) \mapsto (110110)$
$(011) \mapsto (011011)$	$(111) \mapsto (111111).$

191.

$(000) \mapsto (000000)$	$(100) \mapsto (111100)$
$(001) \mapsto (001111)$	$(101) \mapsto (110011)$
$(010) \mapsto (011110)$	$(110) \mapsto (100010)$
$(011) \mapsto (010001)$	$(111) \mapsto (101101).$

$$192. \ G = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$193. \ G = \begin{pmatrix} g_0 & 0 & \cdots & 0 \\ g_1 & g_0 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ g_{n-k} & g_{n-k-1} & \cdots & g_0 \\ 0 & g_{n-k} & \cdots & g_1 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & g_{n-k} \end{pmatrix}$$

$$194. \ H = \begin{pmatrix} 0 & \cdots & 0 & 0 & h_k & \cdots & h_0 \\ 0 & \cdots & 0 & h_k & \cdots & h_0 & 0 \\ \cdots & \cdots & \cdots & \cdots & \cdots & \cdots & \cdots \\ h_k & \cdots & h_0 & 0 & 0 & \cdots & 0 \end{pmatrix}$$

$$195. \ \det \begin{pmatrix} 1 & 1 & \cdots & 1 \\ \alpha_1 & \alpha_2 & \cdots & \alpha_n \\ \alpha_1^2 & \alpha_2^2 & \cdots & \alpha_n^2 \\ \vdots & \vdots & \ddots & \vdots \\ \alpha_1^{n-1} & \alpha_2^{n-1} & \cdots & \alpha_n^{n-1} \end{pmatrix} = \prod_{1 \leq j < i \leq n} (\alpha_i - \alpha_j)$$

$$196. \ p(x) = \det \begin{pmatrix} 1 & 1 & \cdots & 1 & 1 \\ \alpha_1 & \alpha_2 & \cdots & \alpha_{n-1} & x \\ \alpha_1^2 & \alpha_2^2 & \cdots & \alpha_{n-1}^2 & x^2 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \alpha_1^{n-1} & \alpha_2^{n-1} & \cdots & \alpha_{n-1}^{n-1} & x^{n-1} \end{pmatrix}$$

$$197. \ \beta = (-1)^{n+n} \det \begin{pmatrix} 1 & 1 & \cdots & 1 \\ \alpha_1 & \alpha_2 & \cdots & \alpha_{n-1} \\ \alpha_1^2 & \alpha_2^2 & \cdots & \alpha_{n-1}^2 \\ \vdots & \vdots & \ddots & \vdots \\ \alpha_1^{n-2} & \alpha_2^{n-2} & \cdots & \alpha_{n-1}^{n-2} \end{pmatrix}$$

$$198. \ \beta = (-1)^{n+n} \prod_{1 \leq j < i \leq n-1} (\alpha_i - \alpha_j)$$

$$199. \ \begin{pmatrix} (\omega^{i_0})^r & (\omega^{i_1})^r & \cdots & (\omega^{i_{s-1}})^r \\ (\omega^{i_0})^{r+1} & (\omega^{i_1})^{r+1} & \cdots & (\omega^{i_{s-1}})^{r+1} \\ \vdots & \vdots & \ddots & \vdots \\ (\omega^{i_0})^{r+s-1} & (\omega^{i_1})^{r+s-1} & \cdots & (\omega^{i_{s-1}})^{r+s-1} \end{pmatrix}$$

$$200. \ H = \begin{pmatrix} 1 & \omega & \omega^2 & \cdots & \omega^{n-1} \\ 1 & \omega^2 & \omega^4 & \cdots & \omega^{(n-1)(2)} \\ 1 & \omega^3 & \omega^6 & \cdots & \omega^{(n-1)(3)} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & \omega^{2r} & \omega^{4r} & \cdots & \omega^{(n-1)(2r)} \end{pmatrix}$$

$$201. \ H\mathbf{x} = \begin{pmatrix} a_0 + a_1\omega + \cdots + a_{n-1}\omega^{n-1} \\ a_0 + a_1\omega^2 + \cdots + a_{n-1}(\omega^2)^{n-1} \\ \vdots \\ a_0 + a_1\omega^{2^r} + \cdots + a_{n-1}(\omega^{2^r})^{n-1} \end{pmatrix} = \begin{pmatrix} f(\omega) \\ f(\omega^2) \\ \vdots \\ f(\omega^{2^r}) \end{pmatrix} = 0$$