
Latency Bound Data Collection from Sparse Sensor Networks using Data MULEs

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A thesis submitted in partial fulfillment of the requirements for the degree of

Master of Technology

to the

Department of Computer Science and Engineering

Indian Institute of Technology Kanpur

August 12, 2014

CERTIFICATE

It is certified that the work contained in this thesis titled “**Latency Bound Data Collection from Sparse Sensor Networks using Data MULEs**” by **Aman Kumar Singh**, has been carried out under our supervision and that this work has not been submitted elsewhere for a degree.

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Abstract

The positive effect of multiple mobile data collectors (or Mobile Ubiquitous LAN Extensions or MULEs) on network lifetime and energy efficiency of a sparse sensor network, when used in data collection from them, is well known. However, the increased latency (due to physical movement of a robot instead of radio communication) may be a problem in some latency sensitive applications. Motivated by this problem, many MULE path scheduling problems in attempts to decrease latency employ multiple MULEs and long range relay nodes for data collection from the sensor network. Most of the work use some kind of network partitioning schemes that do not make use of rendezvous of two MULEs. To overcome this problem, some of these works use long range relay nodes or a common point of origin of the data collection tours of all the employed MULEs. In this thesis we consider latency bound data collection from a sparse sensor network using only MULEs as the means to establish connectivity, and also alleviate the problems mentioned above. The sensors in the field are grouped under planar circular discs of radius equal to their sensing range using disc cover problem. The centers of these discs are called "location nodes". In other words, location nodes define the positions where a MULE comes to gather data from the sensors covered by it. The latency bound, given as an input, determines the bound on the path length of a MULE. Using this bound, we propose a MULE path selection heuristic, which divides the movement and data collection work among multiple MULEs, each of whose data collection tour respects the bound. The tours are chosen in such a way that the MULEs which are supposed to rendezvous for forwarding data, have a definite rendezvous point in the plane to do the same.

Acknowledgement

I would like to express my deepest gratitude towards my thesis supervisors Dr. R.K. Ghosh and Dr. Maitreya Natu. They have guided me, remained very patient and have given valuable suggestions throughout my thesis work. I would like to thank Dr. Vaishali Sadaphal of TCS, TRDDC, Pune for valuable insights into the initial stages of the problem and help in systematizing my approach to the same. I am also indebted to TCS, TRDDC Pune for giving me the opportunity to meet Dr. Natu and Dr. Sadaphal and work with them as a paid intern. Finally, I am in deep gratitude of my family for being a constant source of support and care and taking great pains for it.

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Chapter 1

Introduction

Wireless Sensor Networks consist of a large number of sensor nodes, which are battery-powered, low energy consuming devices. Wireless Sensor Networks (WSNs) are used for applications such as monitoring (e.g., pollution prevention [1], structures and buildings health), event detection (e.g. fire hazard [15]) and target tracking (e.g., surveillance [4]). These devices perform three basic tasks:

- Sample a physical quantity from the surrounding environment
- Process and buffer the acquired data
- Transfer the data through wireless communications to a data collection point called sink node or base station.

The sensors, as soon as deployed on the field, identify their adjacent sensors (neighbours), and are able to form an ad-hoc network. If this network is connected (each sensor is able to send data to another sensor on the field through one or multiple hops), then it is called a dense sensor network. Such a network is used as basic infrastructure for routing sensor-acquired data to the sink node (Base Station) using WSN routing protocols [3]. Occasionally, sink node may send data to all sensor nodes as well.

However, dense networks are seldom realizable in practice. Usually, sensors are spread (air dropped) over a large geographical area resulting in a sparse network. This kind of networks are useful for applications (e.g., environmental monitoring applications [22]) where fine-grained sensing is not required. In sparse sensor networks, islands of sensor sub-networks are formed (WSN islands [25]), which cannot communicate to each other without external help. Data collection from this kind of network, without deploying additional sensors can be done using:

- Long range relay nodes [34]

Long range and high power nodes, whose main purpose is to establish connectivity among such WSN islands, and their connectivity to the base station by relaying/receiving data to/from sensors out of range of the local island. Their placement in a sensor network is a well studied problem.

- Mobile data collectors (MDCs) [8] or Mobile Ubiquitous LAN Extensions (MULEs) [30]:

Controlled mobile robots acting as mobile sinks/Base stations/relay nodes. These can be programmed to tour any set of locations so as to collect data from the sensors at those positions,] and relay the same to base station directly or through another MULE. Since the sensors have to wait for the MULE to arrive in range

1. Sensors may be required to have a battery powered passive wake-up radio device [5], which can be triggered by a nearby MULE. MULE will then be able to collect data from the sensor, and forward the collected data when it is in proximity of the base station (or another MULE assigned to relay to the base station [29]).
2. Sensors wake-up and sleep operation can be controlled at the MAC layer [24] [18]. In this approach, sensors periodically sleep and wakeup to save power. Data transmission occurs only when the MULE is in range, and the sensor is awake.

The MULE approach naturally saves energy of the sensors leading to prolonging network lifetime. The use of MULEs limits sensor communication to one hop only, and relieves sensors from perform aggregation or forwarding of data of other sensors. However, the main disadvantage in this approach is increase in latency of data transfer from sensors to Base Station. This may have negative impact on performance of some applications [11]. This is the reason that the studies on the problems of MULE path optimization and job scheduling are extensive in literature [12].

1.1 Main Contribution of the Work

In this thesis our investigation is centered around study of techniques and heuristics used for the use of MULEs in data collection from sensors. The main contribution of our work is a new heuristic for data collection through MULEs. The usual approach in this direction is to make use of multiple MULEs by partitioning the network into roughly "equal" parts (in terms of TSP

tour time of that partition, together with the time taken to collect data from sensors in that partition), and each partition is assigned to a MULE. Our work takes the latency constraint of the sensor network application as input and computes the number of MULEs required along with their trajectories. We assume MULEs can move freely in the plane of the sensor network, and they have identical, constant speed. The key idea is to create a steiner tree of certain positions on the field, from which MULEs can communicate to sensors, and partition its set of edges into subsets of connected subgraphs, each with approximately same TSP tour time. These approachable positions are called location nodes in the rest of the text, and we also propose a new heuristic for their identification as well.

1.2 Summary of the Work

This thesis has been organized into five chapters including the introductory chapter. In Chapter 2, we first deal with the components of the general problem of data MULE scheduling, and with the aspects that we are concerned, namely, *path selection*. Next, we introduce location nodes, location graphs and propose heuristics to compute them. We also provided justification of our choice of heuristic with performance measures. In Chapter 4, we describe our main heuristic for path selection and also provide pseudocode for the same. In Chapter 5, we present the results of simulation studies conducted to examine the performance the proposed heuristics for data collection using multiple MULEs. Finally, Chapter 6 contains two anticipated directions in which this work may be continued. The first is the addition of capability of MULEs to avoid obstacles, and the second is incorporating optimization of TSP tours for MULEs in the proposed heuristics. A MULE need not travel to exact location of a sensor node in order to collect data. Data transfer can be staged when MULE enters into the communication range of a sensor. So, in the proposed heuristic, it suffices to obtain a TSP tour for a MULEs that passes through communication neighbourhood of sensors instead of exact locations.

Chapter 2

Preliminaries and Subproblems

It is known that controlled MULEs can increase a WSN's lifetime by enabling sensor nodes to save energy. But the problem of energy efficient data collection by MULEs depend on planning optimal paths and job schedules of MULEs. The problems are clubbed together under the Data MULE scheduling problem [32]. In general, achieving the goals of MULEs scheduling problem are hard, and consists of following components:

1. *Path selection*: determines the trajectory the data MULE will follow.
2. *Speed control*: determine how the MULE will change the speed while moving along a trajectory.
3. *Job scheduling*: determines the sensor from which a MULE collects data at each time point

In this thesis our focus is only on path selection of the MULEs.

2.1 Geometric Disc Covering and Location Nodes

In the interest of collecting data from sensors in one hop, we propose to cover the sensor field with circular discs of radius equal to the range of the sensors. The centers of these will be locations where MULEs will pause to collect data from the sensors. For convinience in description, we will refer to these positions as *location nodes*. At a location node, a MULE polls nearby sensors with the same transmission power as sensors, such that sensors that receive the polling messages can upload packets to the MULE within a single hop. Each sensor may be covered by more than one location nodes, but each sensor is associated with only one of

these location nodes for data uploading to the MULE. Our path selection heuristic, proposed in Chapter 4, uses location nodes as the nodes of a graph embedded on the 2D plane, referred to as *location graph*. Underlying assumptions in our approach are: (i) communication region of a sensor is approximated to a circular disc, (ii) all sensor have same communication range, and (ii) the range of the MULE is greater than that of any sensor.

There are two types of geometric disc cover problems:

Geometric minimum disk cover (GMDC) In this problem, a field of nodes is given, and the aim is to cover all the nodes with minimum number of discs (of given radius) possible. The centers of the discs can lie anywhere on the field.

Geometric discreet unit disc cover (GDUDC) In this problem, in addition to a field of nodes, a set of points C is also given. The aim is to determine the smallest subset C' of C , such that the discs placed at the points in C' cover all the nodes in the field.

Though GDUDC was much more extensively explored compared to GMDC, we have used GMDC. Initially, we planned to get an intermediate solution of GMDC through some heuristic/Approximation Scheme, then apply techniques for GDUDC problem for a better solution. Due to our unclear understanding of the algorithm, however, we tried but failed to implement one solution [6] for GDUDC. Therefore, we relied on heuristics for find a disc covering.

Many heuristics and approximation schemes [16], [14] have been proposed for GMDC. Any one of these can be possible candidates. We considered four main heuristics, here referred to as, Johnson's greedy set cover (JGRD), Greedy cover of sorted positions (GRD), Selection of smallest cover (SEL), Hexagonal tiling (HEX), and one approximation scheme know as Shifting strategy (SHFT) and carried out experiments for their efficacy in sample fields.

2.1.1 Preliminaries

For convenience in subsequent description, we introduce certain preliminary notations and concepts. Also, the "point" used here, can be a place holder for "sensor position", "sensor node" and "node" in subsequent description. Let P be the set of points to be covered with discs of radius R , in the square field F . For any two $p_1, p_2 \in P$, there are two $c_1, c_2 \in F$ (called "crosses" for convinience) such that p_1 and p_2 will lie at the boundary of a disc of radius R placed at either c_1 or c_2 . We consider points p_1 and p_2 as covered (barely) by any of the two discs above. For any two points p_1 and p_2 such that distance between p_1 and p_2 is

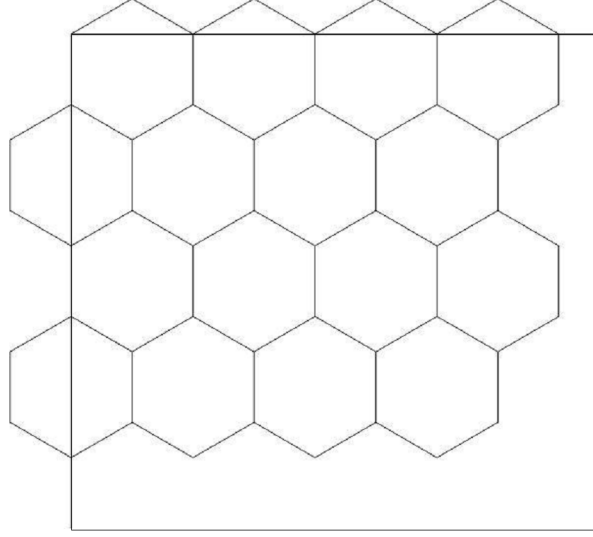


Figure 2.1: Hexagonal tiling

less than $2R$, there exist two crosses c_1 and c_2 (c_1 and c_2 are said to "involve" p_1 and p_2 for convinience). Let C be the set of all possible crosses in the field F .

A set S of disc centres such that they cover all the points in the field F is called a solution of the GMDC problem in the field F . Let S_1 be such a solution. Then there exists a solution $S_2 \subset C$ such that $|S_1| = |S_2|$.

2.1.2 Heuristics and the Approximation Scheme

We focused on implementing four heuristics and one approximation scheme to obtain covering sensor fields. We provide a synopsis of these techniques before discussing the results.

OPT This is an algorithm for the optimum solution, which uses brute-force to search for the minimum set cover in order to find the optimum solution. At first we create a table of the information regarding which cross (refer section 2.1.1) covers which of the sensors. These crosses act like the subsets of the set of all sensors containing the sensors they cover. Next, we find the minimum set cover using brute-force. Needless to say, the running time of this algorithm blows up very fast.

HEX In this heuristic [23], the sensor field is initially tiled with regular hexagons of sides equal to the radius of the discs to be used (see, figure 2.1). A sensor is said to be covered by a hexagon, if it is closer to its center than the center of any other hexagon.

JGRD This is originally a set cover heuristic [10]. Consider the set P as the target set to be achieved from the union of smaller subsets, and the discs centered at the crosses in C represent the subsets of points covered by them. Our problem of MGDC then becomes a set cover problem. The reference [10] gives a greedy heuristic for this.

GRD We have designed this heuristic. Let the list of all sensor positions in the given field of sensor nodes be L . First sort L according to their (x, y) position co-ordinates (first by x co-ordinate and then by y co-ordinate). Starting from the first sensor node p in the list, pick the disc which covers maximum number of uncovered sensor nodes and covers p too. To do this, compute all the crosses in C which involve p (refer 2.1.1 for "crosses" and "involving a node"). Place a disc of radius R at each of the crosses, and choose the cross whose disc covers the most number of points. Choose the next uncovered sensor in L and repeat the covering procedure, until all sensors are covered.

SHFT The shifting strategy is derived from [16]. This algorithm takes two input parameters: l (shifting parameter, chosen later) and D (diameter of discs to be used for covering). Let the field be a square of length W . First we divide the field into vertical strips of width $l \times D$, as shown in figure 2.2. We do disc cover on these vertical strips (explained later) individually (treating them as separate fields. The union of the solutions of all the vertical strips is clearly a solution to the problem. This solution is assigned to *current_solution*. Now, the whole partition of strips is shifted horizontally, away from the origin, by the amount of D (as shown in figure 2.3). Again, all the strips are covered with discs (to be explained later how), and the union of the solutions of these shifted vertical strips another solution, assigned to *new_solution*. If the size of *new_solution* (the number of discs in the solution) is less than the size of *current_solution*, the current solution now becomes *new_solution*. We continue shifting the partition and measuring the solutions thus generated $l - 1$ times.

To cover a strip of width w , we again apply the shifting strategy. We divide the strip into squares of side w (and maybe a remainder rectangle, in case W leaves a remainder upon dividing with w). To cover this square (of size $w \times w$) with discs of diameter D , we use the strategy OPT described above. The shifting of this partition is done by the amount D just like in the original field, and the smallest solution is chosen. The shifting parameter l depends on the time constraint one has regarding the running time of this algorithm. It is chosen in such a way that the problem size in each square (of size $w \times w$) is small enough for the OPT

to run in required time constraint.

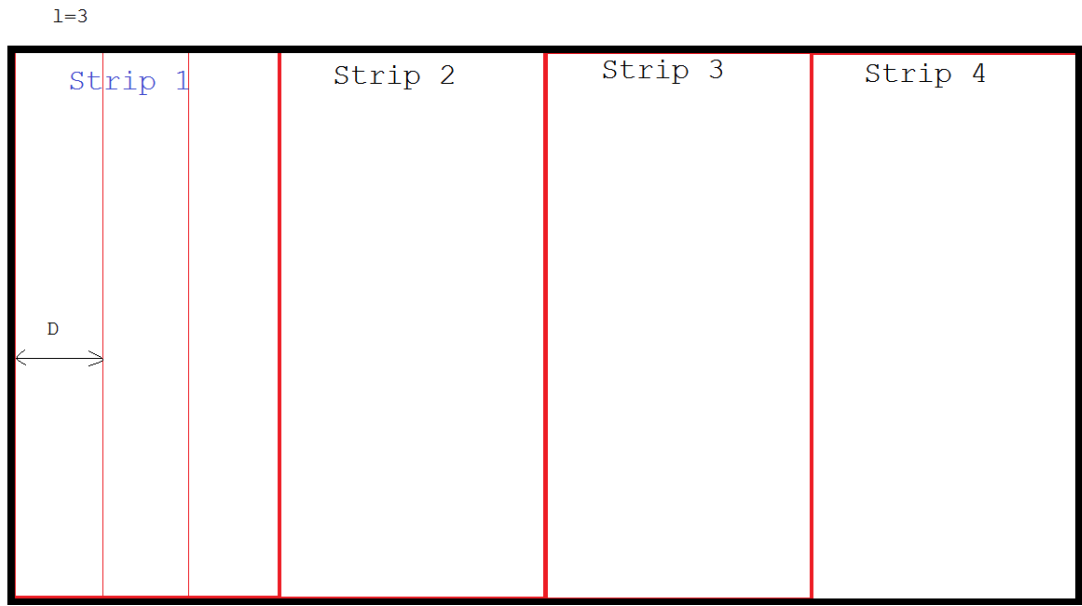


Figure 2.2: Original division of the field into vertical strips. l is 3 here.

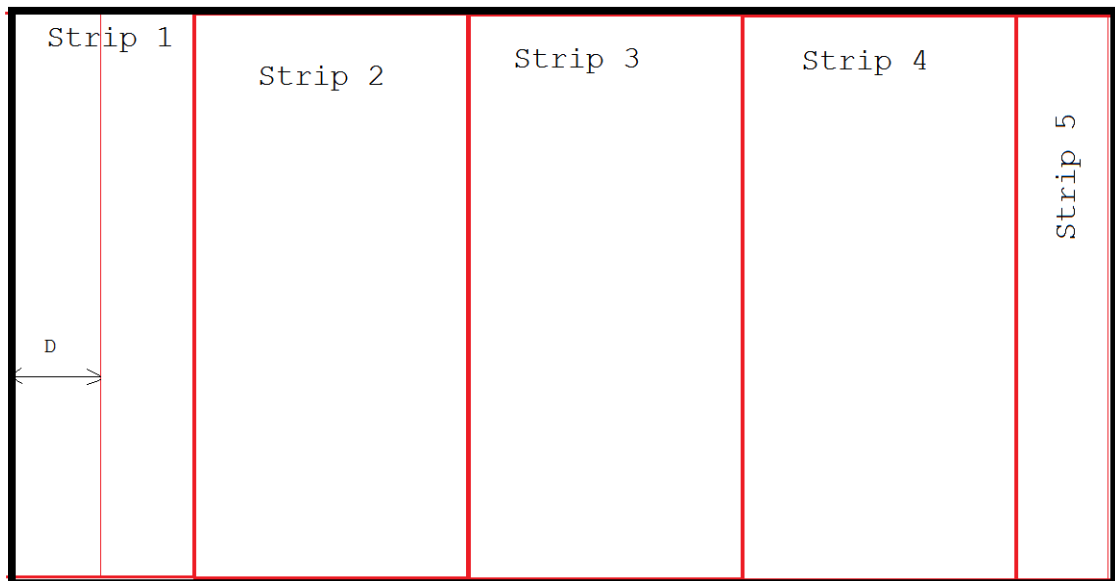


Figure 2.3: After the shift right by the amount D

SEL For any sensor s , let C_s be the set of crosses (refer the subsection 2.1.1) covering it. Pick the cross which covers the least number of sensors. Keep iterating on the remaining uncovered sensors, until all the sensors are covered.

RND Randomly pick crosses until all the sensors are covered. This not a good heuristic, but we have include it just for sake of comparision with other heuristics.

Table 2.1: Pros and cons of the heuristics implemented

Heuristic	Pro	Con
JGRD	–	$O(n^3)$ memory usage
GRD	Performs the best among the tested heuristics	$O(n^3 \log(n))$ Running time
SEL	Linear running time	$O(n^3)$ memory usage
SHFT	Controllable approximation ratio	Large running time
HEX	Linear memory requirement and Linear running time	Performed worse than RND

2.1.3 Results of testing the heuristics' performance

The above heuristics and the approximation scheme were tested on a $1000\text{m} \times 1000\text{m}$ field with discs of radius 50m. The number of sensors are increased from 50 to 100 in steps of 10. As we can see, GRD performed the best. Therefore we chose GRD for our implementation.

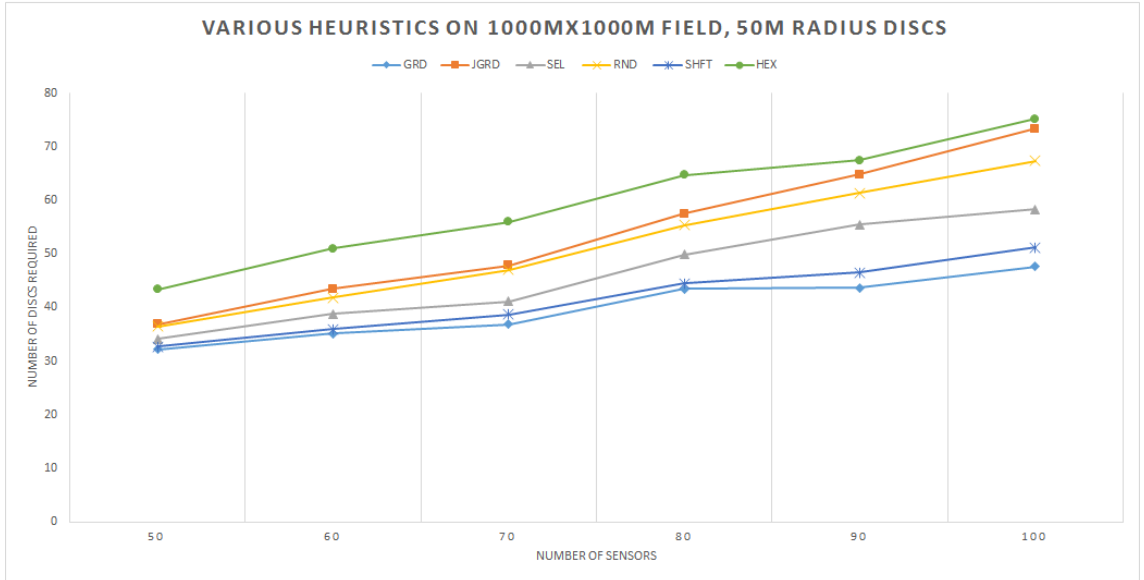


Figure 2.4: Results of testing above heuristics and the approximation scheme on a $1000\text{m} \times 1000\text{m}$ field

2.2 Euclidean minimum steiner trees

Definition (Euclidean minimum Steiner Tree problem). Given a set P of points in a 2-D plane as input, the output is a network of line segments connecting all of the points in S , with the smallest total (Euclidean) length.

The line segments making the Steiner Tree need just be incident on the points in S . This implies that the algorithm is free to use additional points from the plane, if necessary, to produce the smallest total length network. The additional points are called *Steiner points*.

For computing Steiner tress, we use the exact solution finder software GeoSteiner [35] [36] [39]. Following figures show a disc cover of 100 sensors in a $1000\text{m} \times 1000\text{m}$ field with discs of radius 50m, and the Steiner trree of the disc centers thus computed.

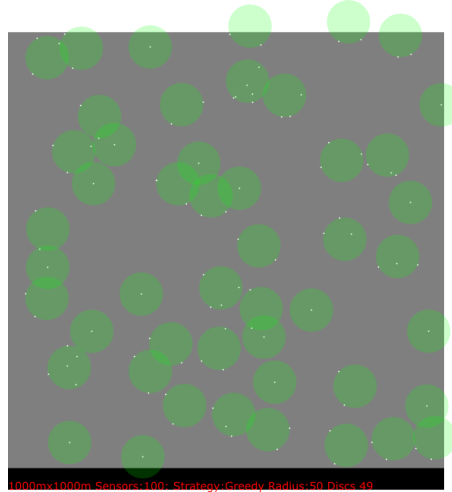


Figure 2.5: 50m radius disc cover of 100 sensors in 1000×1000 field

The white dots are sensor positions

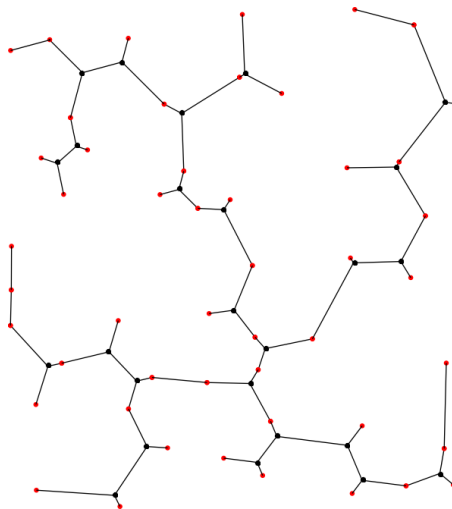


Figure 2.6: The Steiner tree of disc centers of figure 2.5

The black dots are Steiner points and the red dots are disc centers

Chapter 3

Related Works

Most notable related work is [19]. Their goal is to find the trajectories of k MULEs to collect data from the N wireless sensor nodes deployed on 2-D Euclidean space such that the data collection latency (the length of the longest trajectory among k trajectories) is minimized. They consider two cases:

Case 1: Each MULE is connected to the sink only from their original positions (base stations).

Case 2: Each MULE is connected to the sink directly at any time from any location.

Intuitively, it may be better to utilize MULE to MULE communication too for data transfer, which is absent in their approach but essential to our approach. They solve the problem by formulating k -traveling salesperson problem with neighborhood (k -TSPN) and k -rooted path cover problem with neighborhood (k -PCPN) problems. Their algorithm has a constant factor approximation, however, as they say in section 5 of their paper, this algorithm itself is based on another approximation algorithm [13], which is a very complicated rounding-based algorithm and difficult to use. Therefore, they propose heuristics to solve it.

A similar problem of covering a set of points in a plane using multiple robots [7] also seemed promising, but, we were unable to accomodate the additional constraints listed above (they use Clique cover problem [17], which has its own application in data collection algorithms for dense sensor networks).

Another related work [21] is on SenCars [20] (a MULE). Their algorithm takes as input m : the number of SenCars, the sensor network (sensor node positions in the field) and a set of polling points P (positions from where the SenCar can stop and communicate with sensors around it). Their aim is to divide the set of polling points P into subsets P_1, P_2, \dots, P_m , each

of which have approximately equal weight. The weight of a subset of polling points is the sum of operation times of a SenCar at each polling point (The time that a SenCar will take to collect data from the sensors covered by that polling point, which is directly proportional to the number of sensors covered by it), plus the time it will take the SenCar to visit each polling point in this partition. They show an integer linear programming formulation of the problem, and also provide a heuristic.

A drawback in any graph partitioning approach is that the TSP evaluation of a partition (the length of tour that the SenCar handling that partition will have to take), does not take into account the rendezvous of two neighbouring MULEs (MULEs covering neighbouring partitions). Here, the authors simply assume that each SenCar can forward the gathered data to te neighbouring SenCars when they move close enough. It is a reasonable assumption in a relatively denser sensor network (where MULEs' tours can be close enough to communicate to each other) because MULEs transfer data at high speed and they aggregate data before transmitting. This facilitates a SenCar to transfer/recieve required data within the brief contact time. But in the case of a sparse sensor network containing sensor islands, each with similar weights, this approach may lead to isolated partitions as the islands may be far away. This will lead to the situation where a SenCar cannot communicate with any other SenCar, because its tour never gets close enough to another SenCar's tour. Our approach ensures connectivity through ensuring MULE rendezvous at some point in the plane.

Reference [28] is a connectivity restoration algorithm for a sparse sensor network. Its authors use both stationary Relay Nodes (RN) and Mobile data collectors, or mobile relay nodes (similar to MULEs) to restore connectivity in a set of sensor islands as their sensor network. They call each island a partition. Although RNs are best for providing stable link from cluster to the sink, there is only a limited number of stationary RNs they can use. For each partition they choose a representative sensor node, which has the responsibility to collect and store the data from its partition. For these representative nodes, they compute the Steiner tree, for the determination of positions of relay nodes. Since stationary RNs are preferable to MDC's, initially all the relay nodes are mobile (i.e. are MDCs). Each of them visits a subset of representative nodes under bounded latency L . One by one they start connecting each partition to the sink through relay nodes, and at each step they check whether the remaining MDCs are still able to cover the remaining clusters under the bound latency.

Another work that uses Steiner tree to plan MULE path is [37]. Their work is applicable only on dense sensor networks, because they use RPs (rendezvous points) situated at steiner points to collect and buffer data from nodes farther away from the bases station for the MULE to visit and collect later. Ofcourse this means they have to be in range of their adjacent snesor in the Steiner tree, which can not be guaranted in a sparse WSN.

Chapter 4

Path selection

Our approach to a better heuristic is driven by the concept of location graph and using the same for construction of low latency tours of the MULEs in data collection phase. The two critical subproblems encountered in this context are: (i) Euclidean Minimum Steiner Tree (EMST), and (ii) Euclidean Travelling Salesman Problem (ETSP). The EMST problem has already been introduced in chapter 2. We will briefly restate these here for sake of completeness and convenience in description of our heuristic.

Definition (Euclidean Travelling Salesman Problem). *Given a set of n 2D points in a plane find a minimum weight length tour of all the points, visiting every point exactly once.*

We use Christofides algorithm [9] as the approximation heuristic for computing TSP route of a set of points.

Definition (Euclidean minimum Steiner Tree problem). *Given a set P of points in a 2-D plane as input, the output is a network of line segments connecting all of the points in S , with the smallest total (Euclidean) length.*

The line segments making the Steiner Tree need just be incident on the points in S . This implies that the algorithm is free to use additional points from the plane, if necessary, to produce the smallest total length network. The additional points are called *Steiner Points*.

The location nodes (the nodes in location graph) computed earlier, form the set P , and the EMST is generated using the set P , and is called the location graph T . The pseudo code for the heuristic which appear later in section 4.1.1 uses the EMST as input. The choice of EMST as data structure over MST is guided by the fact that the weight (weight here means total of lengths of all the edges in a graph) of EMST is always atmost the weight of the MST,

and we use the weight of a tree as an approximation of the weight of the TSP tour of its vertices.

The TSP time unit is the time taken by a MULE to visit all points on EMST. The cost of ETSP on a set is atmost twice the cost of the EMST on it. Therefore, it should be reasonable to use the Steiner tree traversal as a guide for partitioning. Furthermore, in the case where the field also includes obstacles, Steiner trees lend themselves naturally to cover all the points due the properties of Steiner points [40] as explained in section 2.2 of Chapter 2. Though we plan not to cover the obstacle avoidance case, we briefly sketch the underlying ideas in Chapter 6.

4.1 Path Selection Heuristic

The aim of path selection heuristic is to find a minimum partitioning of the set of location nodes of a location graph by addition of extra Steiner points such that following conditions are satisfied.

- Each of the subsets has a TSP tour length (in units of time) less than a per-specified value L , and for any two sets S_i and S_j , $S_i \cap S_j \leq 1$.
- Let V be the set of all subsets S_i . Let E be the set of pairs of subsets (S_i, S_j) such that $S_i \cap S_j = 1$. Then the graph $G(V, E)$ should be a connected graph.

It assumed that the time a MULE spends in a network while collecting data consists of three main components: (i) travelling from one location node to another t_{TSP} (ii) Talking to sensors belonging to a location node t_{LS} , called MULE's pause time, at a location node (iii) Talking to other MULEs/Base station t_{MBS} .

We assume that MULE to MULE data transfer times are shorter due to two reasons, namely, (i) MULEs may use data aggregation while sending data to fellow a MULE or BS, and (ii) MULEs being relative expensive and more robust than sensor node, typically have higher bandwidth for inter MULE data transfer. This is the reason, we ignore the contribution of t_{MBS} . The component t_{LS} for each location node can be given as an input (observed before running the heuristic, by simply sending one MULE on a tour of all the location nodes in the field to measure and record such times beforehand), or computed using sensor parameters, such as: Sensor data throughput (SDT , effective data rate, after taking into account the overhead introduced due to protocol headers) and Sensor data sampling rate (SSR , data sampling rate of the sensor, the speed of data acquisition of the sensor from its environment in bytes/sec).

4.1.1 Heuristic

The overall strategy is to create an EMST of the location nodes and then divide this tree into subgraphs, using the tree edges as the guide. Each subgraph's set of nodes will be covered by one MULE (henceforth, this set of nodes will be called a subtour). The term "weight" is equivalent to "time interval" in this algorithm, and is measured in seconds. An edge of the tree is said to have weight equal to its length divided by the speed of the MULE (time taken by the MULE to cover that edge). The weight of a location node is equal to the time a MULE has to wait there for data collection (called pause time). It depends on the latency bound and the number of sensor nodes covered by that location node. Steiner points have zero weight. The weight of the TSP tour of a set of nodes is equal to the smallest amount of time it takes for a travelling salesman to visit each node exactly once.

Consider any euclidean spanning tree of a set of 2D points in a plane (none of the points have any weight). Clearly, one way to visit all points would be to start from the root, and visit the nodes in the depth first search order, always travelling along the edges. This would take time equal to twice the weight of the tree (each edge travelled twice, once for going from parent to child, and once for coming back to the parent from the child). Thus, the optimal travelling salesman tour must be bounded by twice the weight of the tree.

Now consider the case, when the points have weights too (i.e. the travelling salesman has to wait at the point for a time equal to its weight). Then, the TSP approximation needs to be modified just by adding the total weight of all points in the tree.

Given any tree T , we start from the given root node $root$. $root$ then becomes the current node $curr$. Then following steps of Prim's algorithm [27], we first mark $curr$ as visited, then we insert all the incident edges of the current node with unvisited nodes to the min-heap $edgeHeap$. Computation of a tour for a MULE consists of two stages coded in two inner while loops.

Note: Since we use a $3/2$ approximation algorithm [9] for computing the TSP tour of a subtour, the bound that we will use in the implementation will be actually $3 \times$ weight of the tree. In general, if an x approximation algorithm for euclidean TSP is used, then the bound for TSP weight used should be $2 \times x \times$ weight of the tree.

Now we describe the algorithm. Let $boundary$ be a set of nodes of the steiner tree, initially containing any one node from the Steiner tree. The algorithm picks any one node from the $boundary$ and calls it $root$. The algorithm then computes a connected subgraph of the Steiner

tree (containing that root node) with bounded TSP time. The nodes of this subgraph form a subtour, covered by one MULE. The boundary nodes of a subgraph are those nodes of the steiner tree (regardless of whether they are location nodes or Steiner points), which belong to the subgraph, and do not have all their adjacent nodes in the subgraph. All the boundary nodes from this subgraph are inserted into *boundary*, and the algorithm is called again. This continues until all the nodes are part of exactly one subtour.

Preliminaries

Some data structures and inputs used in the pseudocode are as follows. T is the Steiner tree of the location nodes, given as input to the algorithm. ASP is the average sensor pause time, calculated using L (latency bound), SDT (sensor data throughput) and SSR (sensor data sampling rate). These three are given as input to the algorithm. The map w , taken as input by the algorithm, is the map from the nodes in the Steiner tree T to the number of sensors they cover. Each location nodes will have a non zero entry in the map w , whereas all the Steiner points will have zero entry in the map. For instance, for a node v , $w[v]$ is the number of sensors covered by v . $edgeHeap$ is a min-heap of the pairs $(tWeight, edge)$, where $edge$ is a pair of nodes (v_1, v_2) , and $tWeight = 3 \times weight_of_edge(v_1, v_2) + ASP \times w[v_1]$. The ordering in the min-heap is according to its first argument $tWeight$. To push an edge into the heap $edgeHeap$ means to calculate the $tWeight$ of the edge, then inserting the pair $(tWeight, edge)$ in the heap.

Computation of subtours

Computation of subtours begins from the picking of a node from the set *boundary*. This node will be called *root* for this subtour. Before the computation of the subtour, we mark *root* as visited, and for all nodes v adjacent to *root*, we push the edges $(v, root)$ into $edgeHeap$.

The subtour is computed in two stages. In the first stage, represented by the first inner while loop, *currSet* contains the nodes currently included in the subtour being computed. *currT* is the upper bound of the TSP tour of the nodes in *currSet*; it is updated every time we insert a node into *currSet*. Before popping a pair $(tWeight, edge)$ from $edgeHeap$, we first check for the condition, whether $currT + tWeight$ is greater than L ; if it is, first stage ends here, and we break from the while loop. Otherwise, we pop the pair $(tWeight, (v_1, v_2))$ from $edgeHeap$, all the edges incident to v_1 which have unvisited end nodes are inserted into

the heap, $v1$ is inserted to $currSet$, and $currT += tWeight$.

We keep popping edges from $edgeHeap$ until either $edgeHeap$ becomes empty or, adding any more nodes to $currSet$, leads to $currT$, our current estimate of the weight of the TSP tour of $currSet$, becoming greater than L , our given latency bound. By this time, we are sure that the TSP tour of the nodes in $currSet$ will not exceed L .

Observe that any Steiner point whose all adjacent nodes belong to same subtour is useless. Because, such a Steiner point neither serves as a connecting node between different subtours, nor represents a location node. So, such a Steiner point should be eliminated from the subtour. The function *cleanTour* is used on $currT$ for this purpose, and the first stage ends here.

In the beginning of the second stage, although we are sure that the TSP tour of the nodes in $currSet$ will not exceed L , but the actual weight of the TSP tour of the nodes in $currSet$ might be low enough to add still more nodes into $currSet$. For testing whether this is possible or not, first we compute the actual weight of the TSP tour of $currSet$. Then, before adding a node to $currSet$, we test whether its inclusion will make $currT$ exceed L or not. If yes, then $currSet$ is the final subtour for this MULE. Otherwise, the second stage repeats.

The edge records still left in the Heap, after completion of one full iteration of the second inner while loop, form the boundary of the nodes in $currSet$. These nodes are pushed in the *boundary*, from where the next *root* for the next MULE's subtour computation is chosen.

Pseudocode

Algorithm 1 Dividing the set nodes with weights of a given Steiner tree into subsets of bounded TSP time

function GREEDYSTEINER(A Steiner tree T of location in a plane, An array w of the number of sensors under a location node, Starting vertex $root$, desired upper bound on latency L)
 ▷ this function returns S: Set of tours, each with touring time $\leq L$
 Set S
 $N \leftarrow$ number of vertices in T
 $hApprox \leftarrow 3.0$
 $MSPEED \leftarrow$ speed of the MULE used
 $SDT \leftarrow$ sensor data throughput
 $SSR \leftarrow$ sensor data sampling rate
 $ASP \leftarrow \frac{(L \times SSR)}{SDT}$ (average sensor pause time for one sensor)
 $queue$ *boundary*.push($root$)
 $bool$ *visited*[N]
 $vertex$ *curr*

```

for  $i \leftarrow 1, N$  do
     $visited[i] \leftarrow false$ 
end for
while 1 do
    if  $boundary.empty()$  then
        break
    end if
     $currT \leftarrow 0.0$ 
     $cycleWeight \leftarrow 0.0$ 
     $Min\_heap\ edgeHeap$ 
     $curr \leftarrow root$ 
     $Set\ currSet, tempSet$ 
     $visited[curr] \leftarrow true$ 
     $Set\ U \leftarrow$  all unvisited vertices adjacent to  $cur$ 
    for all vertex  $v$  in  $U$  do
         $edgeHeap.push((hApprox \times dist(v, curr)) + (ASP \times w[curr]), (v, curr))$ 
    end for
     $currSet.insert(curr)$ 
    while  $\neg edgeHeap.empty()$  do
         $nextWeight \leftarrow edgeHeap.top().first$ 
         $currT \leftarrow currT + nextWeight$ 
        if  $currT \geq hApprox \times L$  then break
        end if
         $curr \leftarrow edgeHeap.top().second.first$ 
         $currSet.insert(curr)$ 
         $visited[curr] \leftarrow true$ 
         $edgeHeap.pop()$ 
         $U.clear()$ 
         $U \leftarrow$  all unvisited vertices adjacent to  $cur$ 
        for all vertex  $v$  in  $U$  do
             $edgeHeap.push((hApprox \times dist(v, curr)) + (ASP \times w[curr]), (v, curr))$ 
        end for
    end while
     $cleanTour(currSet)$ 
     $Tour\ currTour$ 
     $tempSet \leftarrow currSet$ 
     $cycleWeight, currTour \leftarrow TSPCircuit(tempSet)$ 
    for all sensor  $s$  in  $currTour$  do  $cycleWeight \leftarrow cycleWeight + ASP * w[s]$ 
    end for
    while  $\neg edgeHeap.empty()$  and  $cycleWeight < L$  do
         $curr \leftarrow edgeHeap.top().second.first$ 
         $tempSet.insert(curr);$ 
         $cleanTour(tempSet)$ 
         $cycleWeight, currTour \leftarrow TSPCircuit(tempSet)$ 

```

```

for all sensor  $s$  in  $currTour$  do  $cycleWeight \leftarrow cycleWeight + ASP * w[s]$ 
end for
if  $cycleWeight > L$  then
    break
end if
 $currSet.insert(curr)$ ;
 $visited[curr] \leftarrow true$ 
 $edgeHeap.pop()$ 
 $U.clear()$ 
 $U \leftarrow$  all unvisited vertices adjacent to  $cur$ 
for all vertex  $v$  in  $U$  do
     $edgeHeap.push((hApprox \times dist(v, curr)) + (ASP \times w[curr]), (v, curr))$ 
end for
end while
 $S.insert(currTour)$ 
while  $\neg heap.empty()$  do
     $edge\ e = edgeHeap.top().second$ ;
     $boundary.push(e.second)$ ;
     $edgeHeap.pop()$ ;
end while
if  $boundary.empty()$  then
    return false
end if
end while
end function
function CLEANTOUR( $vSet$  : the set of vertices in the current tour)  $\triangleright$  Delete all Steiner
vertices from  $vSet$ , whose all adjacent verices are in  $vSet$  itself.
end function

```

Chapter 5

Results and Conclusions

We use [33] for sensor specification. The sensors are ZigBee temperature sensors, collecting data at one reading per second. In [33], the authors have used 12 bits for one temperature reading. Therefore, our *SSR* (sensor data sampling rate) is expected to be 1.25 byte/second. The *SDT* (sensor data throughput) is taken to be 13.4 kbps [26]. The MULEs' speed is taken to be 10m/s [31]. The sensor positions are chosen randomly in a field of 1000m \times 1000m, and the sensor range is 50m. Note that Zigbee sensor ranges can lie between 10m to 100m.

5.1 Simulation results

We now present simulation results of our heuristic applied on the following 6 cases:

- Field size: All Cases: 1000m \times 1000m
- Sensor Range: All cases: 50 m
- Number of sensors: Case 1: 50, Case 2: 60, Case 3: 70, Case 4: 80, Case 5: 90, Case 6: 100

For each of the above cases we generate 6 random distributions of the sensors, and apply our heuristic on each of them with latency bound of 100 seconds, increasing in steps of 100s until only one MULE is adequate to cover the whole field. The graph "Number of MULEs required vs Required latency bound" for a case is the plot of required latency bound in X-axis, versus, average number of MULEs required to satisfy the latency bound in that case across its 6 random distributions, in Y-axis. The graph "Average latency achieved vs Number of MULEs employed" for a case is the plot of number of MULEs employed in the case in X-axis,

Table 5.1: Table of flat points in sample sensor node fields

Number of sensors	max point	flat point	δf	δm
50	15	8	790 s	120 s
60	14	9	872 s	68 s
70	15	8	897 s	102 s
80	15	9	1042 s	106 s
90	17	9	1076 s	144 s
100	18	11	1155 s	113 s

versus, the average latency achieved by these many MULEs in this case, across the 6 random distributions.

Each of the following subsections contain results for the respective cases.

As we can see from the "Number of MULEs required vs Required latency bound" graphs of each case, the decrease in number of MULEs required to fulfill the required latency bound, is not uniform with respect to the increase in the latency bound. For instance, in 70 sensors case, for an increase of latency bound from 100 seconds to 290 seconds decreases the number of MULEs required from 13 to 6. However, for further drop in number of MULEs from 6 to 1, the increase in latency bound is from 290 seconds to 1140 seconds. Similarly, from the "Average latency achieved vs Number of MULEs employed" graphs of each case, we can observe that the decrease in the affordable latency bound is not uniform with respect to the increase in the number of MULEs employed. E.g in 70 sensors case, increasing the number of MULEs from 1 to 8 causes the affordable latency to drop from 1100 seconds to 202 seconds. But, a further increase of 7 MULEs decreases the latency only to 100 seconds.

Therefore, we can conclude that the relation between latency bound and the number of MULEs required is not linear, and after a certain number of MULEs employed, additional MULEs do not achieve significant latency decrease. Let us call this number of MULEs a "flat point" for convenience of reference. Also, let the number of MULEs to achieve latency of 100 seconds in a case be called its "max point". The existence of flat points should be apparent from the table 5.1. Let δf be decrease in latency from 1 MULE to flat point and δm be decrease in latency from flat point to max point in the following table.

5.1.1 50 sensors

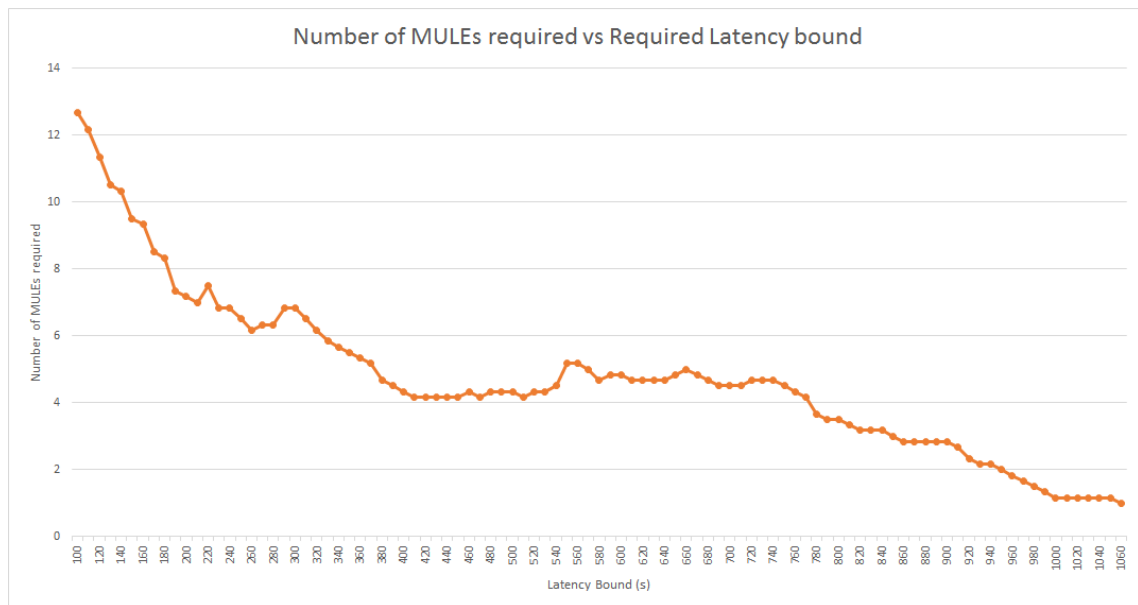


Figure 5.1: Number of MULEs required vs Required latency bound for 50 sensors

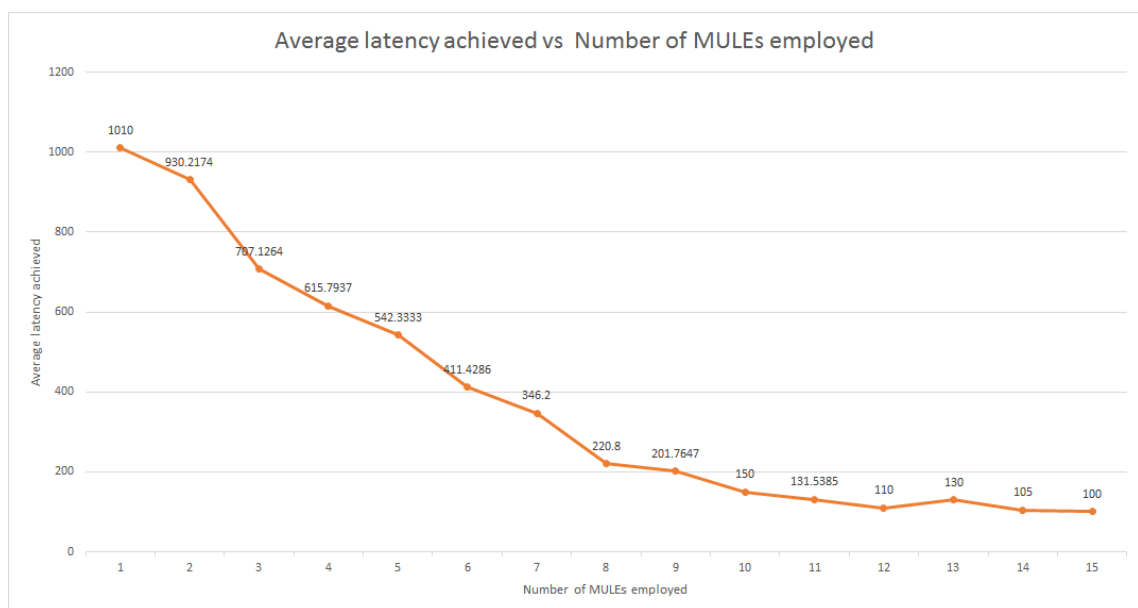


Figure 5.2: Average latency achieved vs Number of MULEs employed for 50 sensors

5.1.2 60 sensors

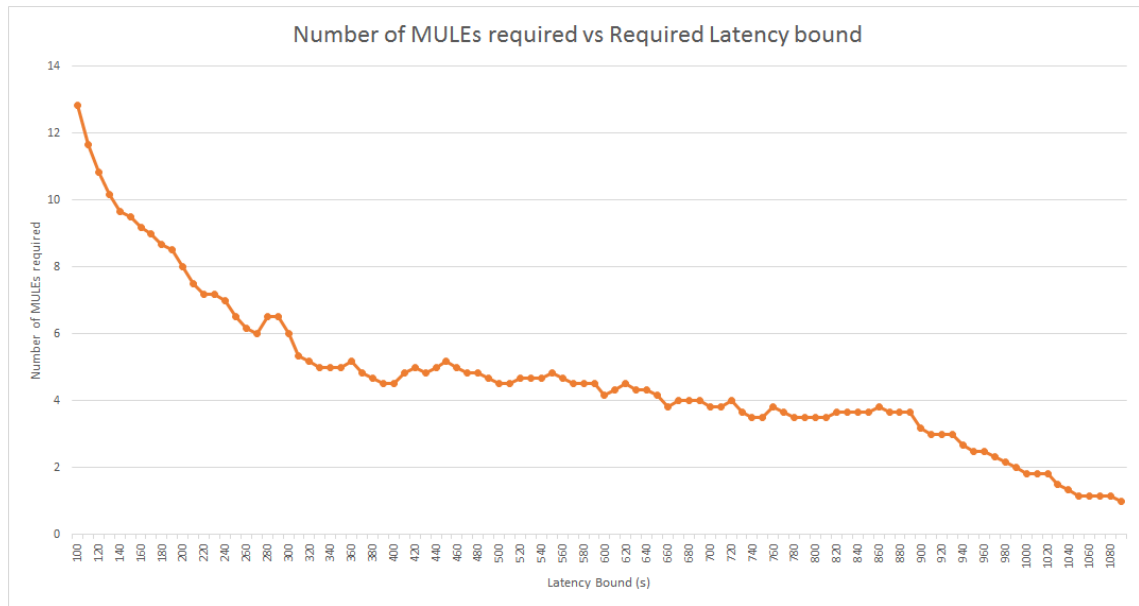


Figure 5.3: Number of MULEs required vs Required latency bound for 60 sensors

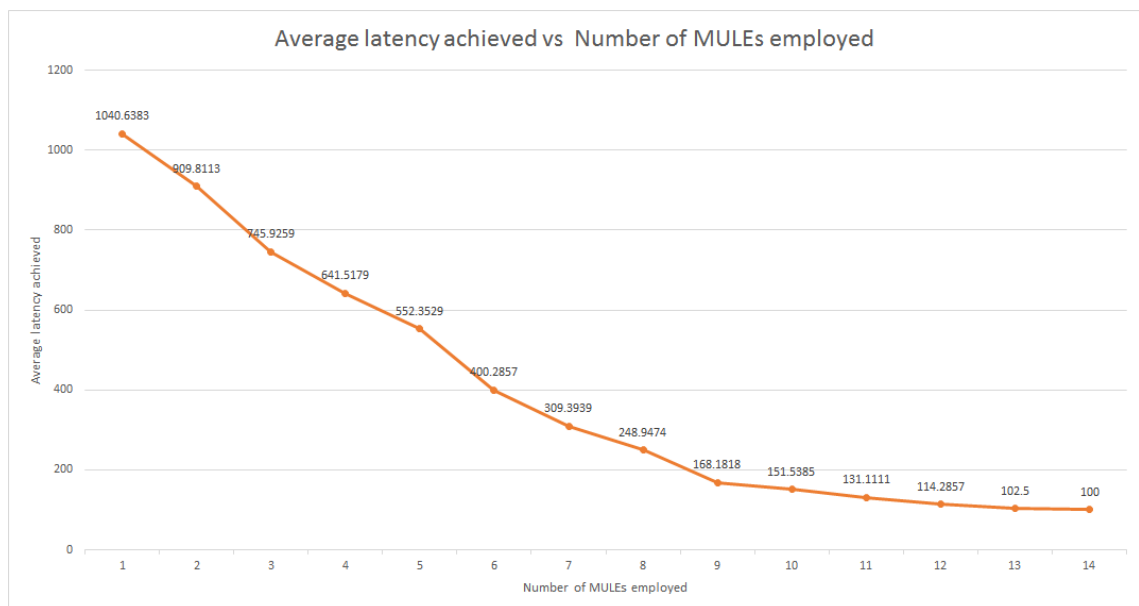


Figure 5.4: Average latency achieved vs Number of MULEs employed for 60 sensors

5.1.3 70 sensors

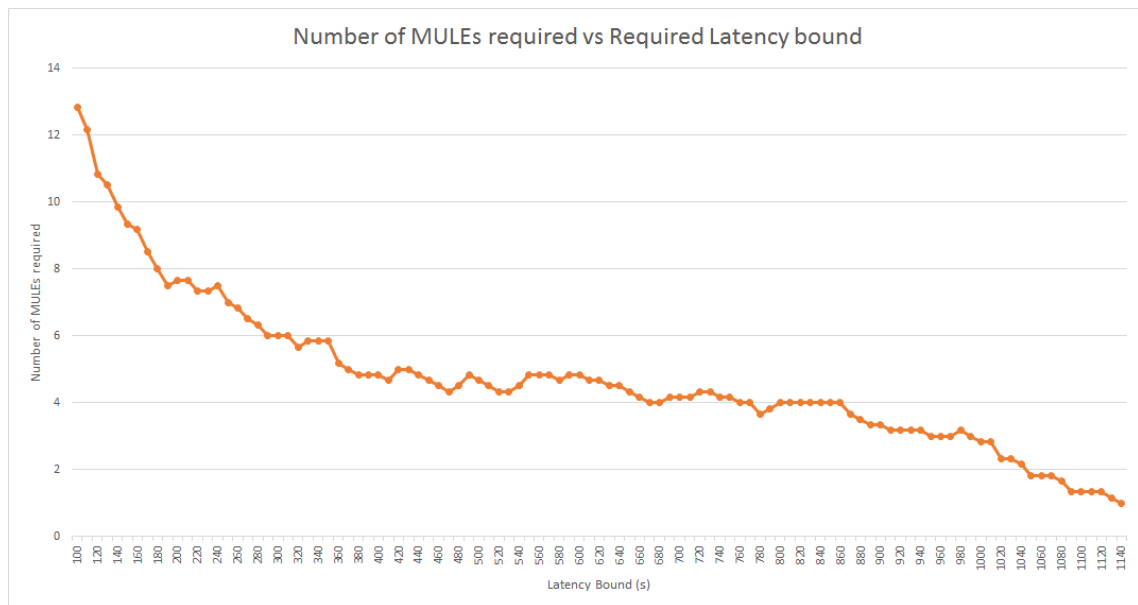


Figure 5.5: Number of MULEs required vs Required latency bound for 70 sensors

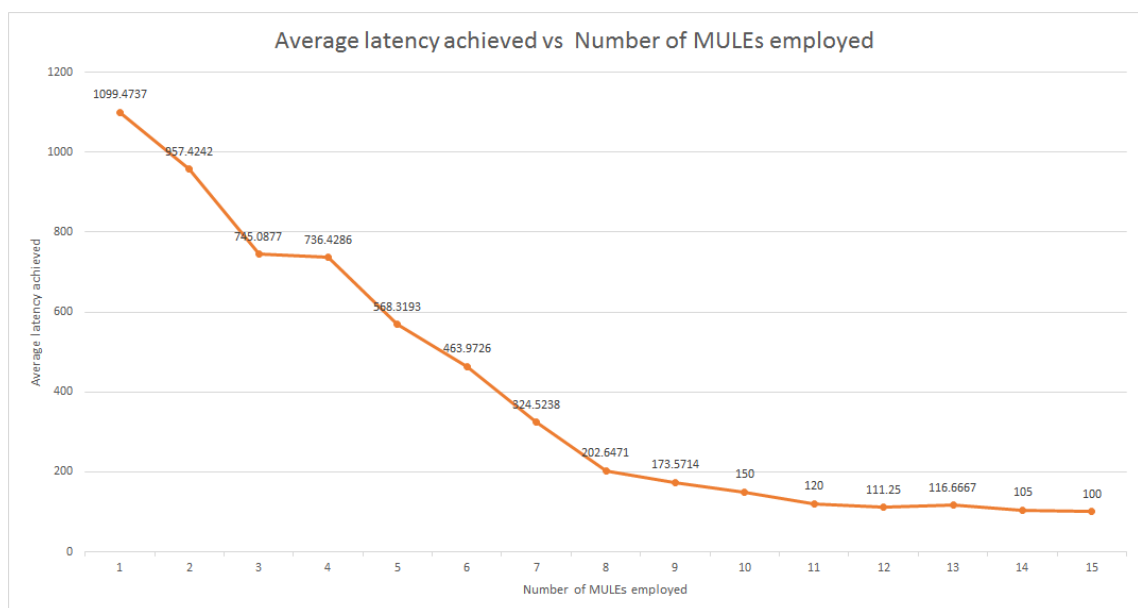


Figure 5.6: Average latency achieved vs Number of MULEs employed for 70 sensors

5.1.4 80 sensors

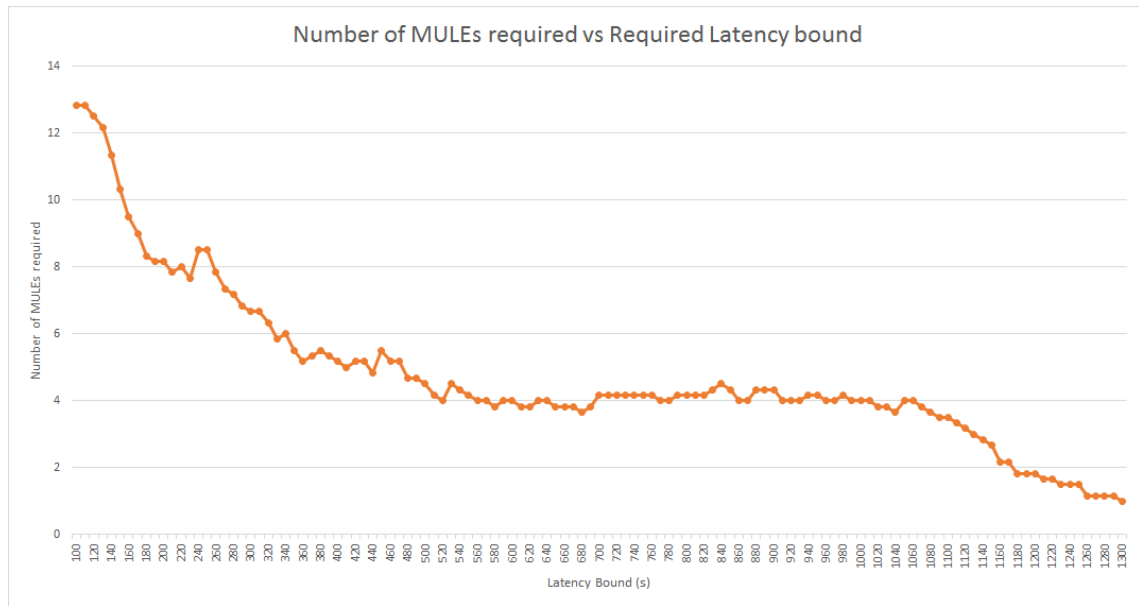


Figure 5.7: Number of MULEs required vs Required latency bound for 80 sensors

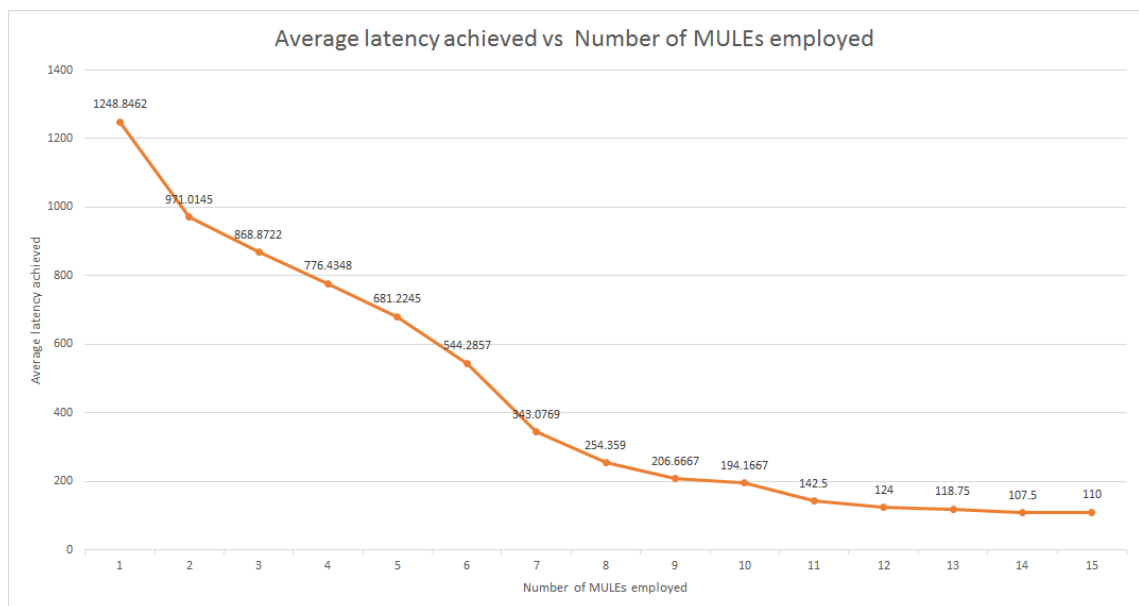


Figure 5.8: Average latency achieved vs Number of MULEs employed for 80 sensors

5.1.5 90 sensors

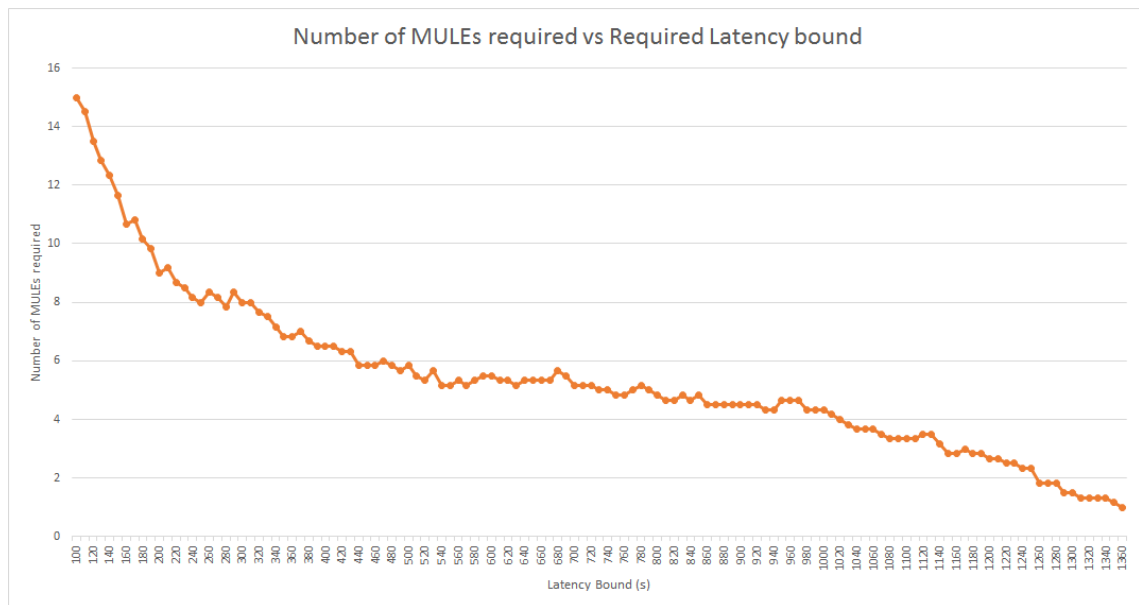


Figure 5.9: Number of MULEs required vs Required latency bound for 90 sensors

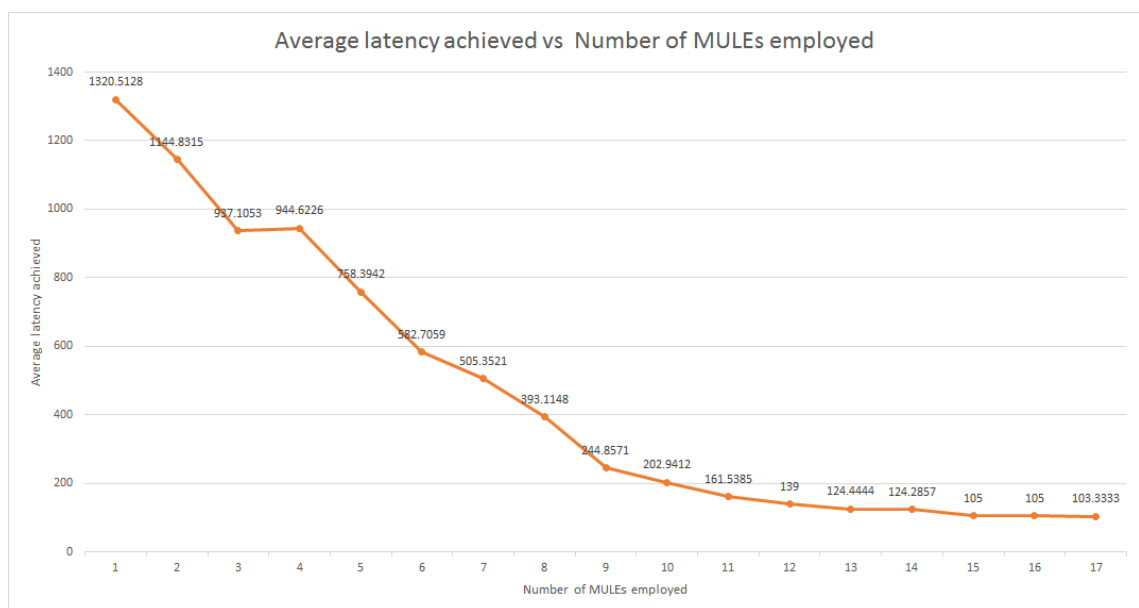


Figure 5.10: Average latency achieved vs Number of MULEs employed for 90 sensors

5.1.6 100 sensors

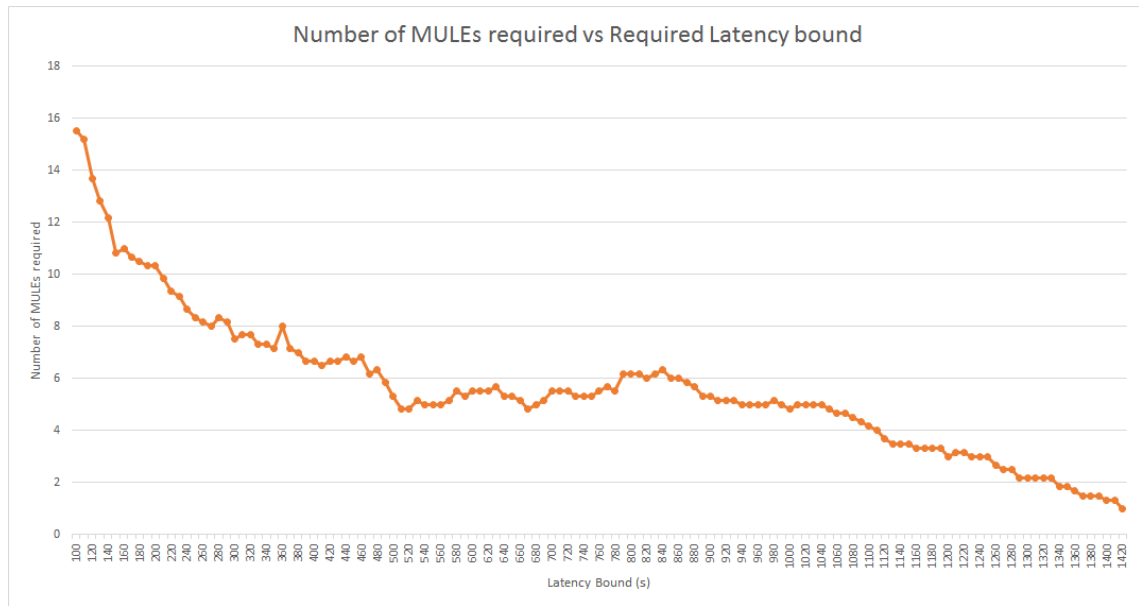


Figure 5.11: Number of MULEs required vs Required latency bound for 100 sensors

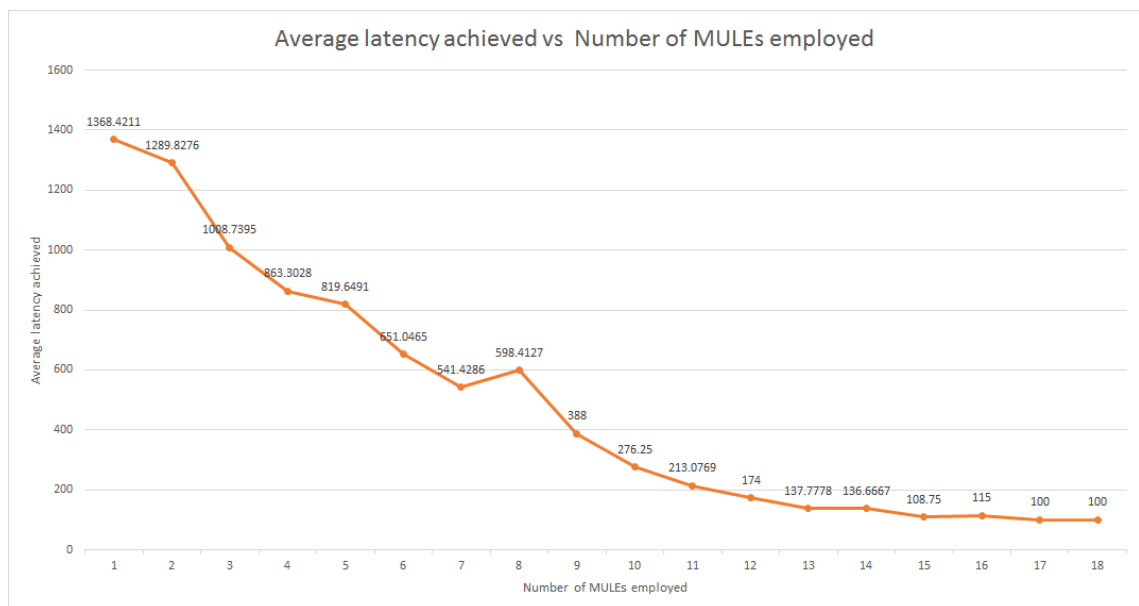


Figure 5.12: Average latency achieved vs Number of MULEs employed for 100 sensors

Chapter 6

Future work

In this thesis, we have provided a heuristic to collect data from a given sparse sensor network field and a bounded latency. The heuristic outputs the number of MULEs required for achieving the latency goal. We have also deduced the minimum latency supportable for any sensor network field which uses this heuristic for data collection.

However, we believe that the potential of application of Steiner trees for data collection may go further.

6.1 Data collection with convex obstacle avoidance

Consider the current problem of data collection from a sparse sensor network, inside a simple convex polygon as the containing field. If we place 2D obstacles in the field in the shape of convex polygons, the problem becomes data collection with convex obstacle avoidance.

The Obstacle Avoiding Euclidean Steiner tree (OAEST) problem [40] is already known. Given a set P of points in a 2D plane contained within a polygon, with polygon holes inside it as obstacles, compute an EMST, such that no edge of the required graph may intersect with either the polygon boundary or the obstacle polygons inside it.

If there is only single polygon obstacle, then [2] can be used. Solving the problem for multiple convex polygonal obstacles is suggested as future work here.

6.2 Further optimization on TSP tour of a MULE

We can apply the work of [38] here. First, we have to cover the sensor field with discs of radius *half* the range of the sensors. This way, the MULE need not travel to the center of a

location node disc for data collection, and the location node can be treated as a communication area [38]. Then after applying their algorithm on our set of location nodes, we can reduce our TSP time by 15-20%.

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