

# Implementing Neural Network with Backpropagation on CIFAR-10 Dataset using C++

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## **Abstract**

We have seen a rising interest in multi-layer neural networking in recent years on all kinds of industries, from data science to robotics, from big data to the industrial complex. These applications are used for numerous image processing computer vision activities. In this paper, I will discuss how to implement the backpropagation algorithm in a multi-layer neural network. I will be using a popular CIFAR-10 dataset to train the network. CIFAR-10 dataset contains thousands of pictures that we can use to train the network and find anticipated results.

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# 1 Introduction

The neural network at its highest level is simple, all it does you give it some inputs as binary mode and it will give you a prediction as an output. based on the output you can decide whether to keep continue to get the output till you get the desired result or to stop with the current out. Backpropagation is an algorithm to train the neural network. The backpropagation used in a feed-forward artificial neural network. We can use this algorithm to train large deep learning networks. In this paper, we will discuss how to implement the algorithm in a neural network. It is very important to learn the basic functions and it will help us to implement the mathematics on a real-life data set using a c++ program.

## 2 Neural Network

Neural networks are computing systems inspired by the biological neural network. The artificial neural network learns to perform by observing examples without specific rules. Before learning how back-propagation works we need to learn more about neural networks. We need to learn a basic neural network specifically multi-layer perception. A multi-layer neural network is a common kind of neural network. Every layer can have a various amount of neurons. Each neuron would be connected to each neuron of the previous or next layer.

Figure 1 shows a small example of a multilayer neural network, here every circle is a neuron. This network will take three inputs on its input level, each will be connected to three neurons of the hidden layer. The hidden layer has three neurons, each will also be connected to two output neurons of the output layer.

### 2.1 Inputs

Inputs are the layer where data are being consumed. We can create a number of different channels from which data can be fed. The target of data being fed is to get a prediction from the data. We have to break into binary signals. We can create a different channel for different binary signals. Each channel will represent a neuron.

### 2.2 Training Set

The training set would be the inputs are being fed into the network. In our case it CIFAR-10 dataset. The training set would be used for training the network for a certain scope from which the network can make a prediction.

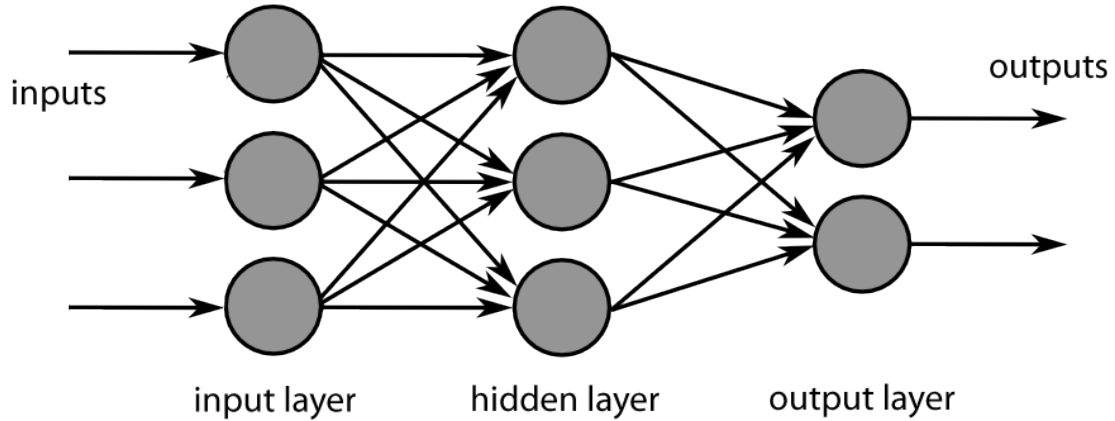


Figure 1: Multi-layer Neural Network.

## 2.3 Outputs

The neural network has an output level. The outputs can be valued between 0 to 1. Also could be Boolean or discrete value.

## 2.4 Activation Function

Every neuron has a numeric weight. The weights and the sigmoid function are used to determine the output for each neuron. In a neural network, our objective is to take weight space to count and determine the output.

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

## 2.5 Weight Space

Every neuron has a numeric weight. The weights and the sigmoid function are used to determine the output for each neuron. In a neural network, our objective is to take weight space to count and determine the output.

## 2.6 Initialization

Initialization refers to the setting of the weights at the beginning of the calculation. We can determine the weights randomly, we can also assign them and start optimizing

from the input layer with the bias node. We have to make sure each signal is passing forward with the right calculation.

## 2.7 Forward Pass

The forward pass refers to taking the input into count, using activation function, weights and the bias node we are passing forward the output to the next level. After input level comes to the hidden layer. We have to do the same calculation for the hidden layer. The output for the hidden layer will go to the output layer.

## 2.8 Gradient Descent

The network will be trained using a mathematical technique called gradient descent. By calculating the gradient of a function we can determine the error of the network. We will have the partial derivatives of all weights and biases. We will multiply the gradient by a small learning rate value. Then subtract the derivatives from the weights and biases to decrease the error amount. This is called gradient descent.

# 3 Neural Network Learning

Neural Network learning happens in six stages, at the end of these stages the model would be ready to make a prediction. Base on that we can redefine and restart the process again.

In order to write the algorithm on a c++ code we need to come out with a plan. A step by step way to implement the algorithm and train the model.

1. Initialization
2. Forward Propagation
3. Error Function
4. Back-Propagate Error Function
5. Predict
6. Iterate Convergence

## 4 Initialization

We would need a class initiation, where we could define the functions responsible for creating and defining the network architecture, various weight matrices, bias vector,

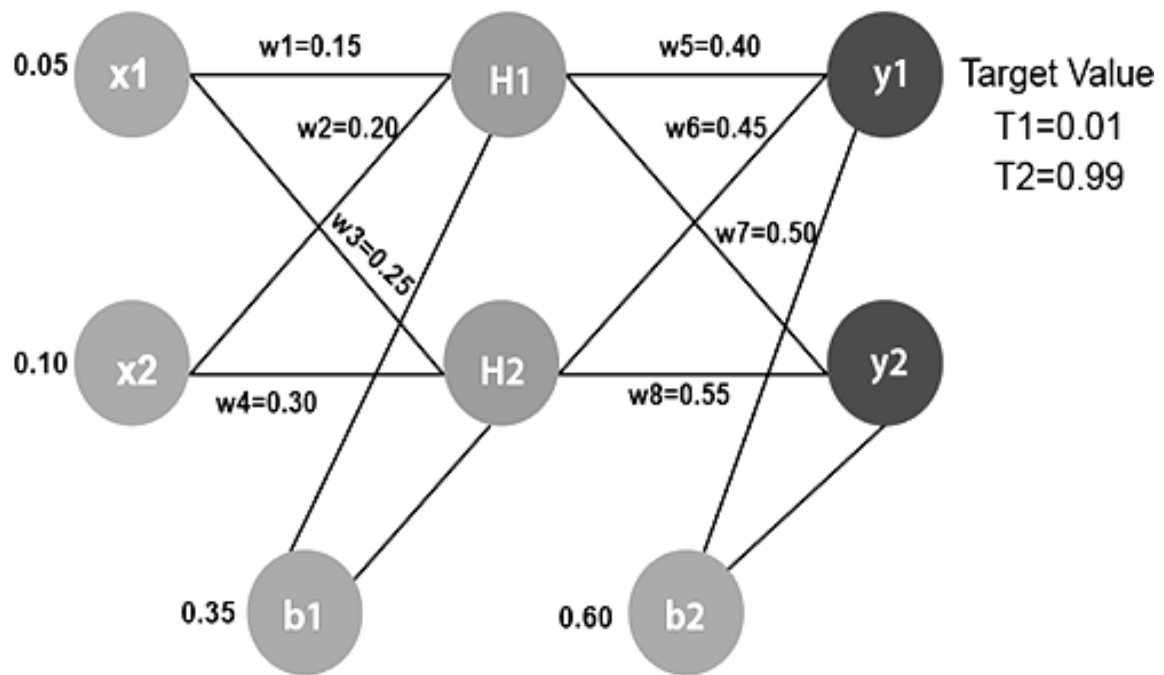


Figure 2: Multi-layer Neural Network with weight.

activation vector.

Every neuron has weight which we should maintain. Every input neuron will have weight and bias node also have weight. We would need to store the weights to use them throughout the program. It is better to assign a small number between 0 to 1 for the weights.

A network architecture have different layers. The input layer is the starting layer for our training data set. After that comes the hidden layer, then the output layer. We can architect layers as arrays and the whole network will be a network of arrays.

In figure 2 the initial values for input  $x1$ ,  $x2$  and bias nodes  $b1$ ,  $b2$  are,

$$x1 = 0.05, x2 = 0.10$$

$$b1 = 0.35, b2 = 0.60$$

Initial weights are,

$$w1 = 0.15, w2 = 0.20, w3 = 0.25, w4 = 0.30$$

$$w5 = 0.40, w6 = 0.45, w7 = 0.50, w8 = 0.55$$

Target values are,

$$T1 = 0.01, T2 = 0.99$$

Now our task is to calculate the error function from these initial values.

## 5 Forward Propagation

We can calculate an output from a neural network by propagating an input signal through each layer until the output layer outputs its values. We call this forward-propagation.

To find the value of  $H1$  we first multiply the input value from the weights as

$$H1 = x1 * w1 + x2 * w2 + b1$$

$$H1 = 0.05 * 0.15 + 0.10 * 0.20 + 0.35$$

$$H1 = 0.3775$$

To calculate the final result of  $H1$ , we performed the sigmoid function as



$$H1_{Final} = \frac{1}{1 + \frac{1}{e^{H1}}}$$

$$H1_{Final} = \frac{1}{1 + \frac{1}{e^{0.3775}}}$$

$$H1_{Final} = 0.59326992$$

We will calculate the value of H2 in the same way as H1

$$H2 = x1 * w3 + x2 * w4 + b1$$

$$H2 = 0.05 * 0.25 + 0.10 * 0.30 + 0.35$$

$$H2 = 0.3925$$

To calculate the final result of H2, we performed the sigmoid function as

$$H2_{Final} = \frac{1}{1 + \frac{1}{e^{H2}}}$$

$$H2_{Final} = \frac{1}{1 + \frac{1}{e^{0.3925}}}$$

$$H2_{Final} = 0.596884$$

Now, we calculate the values of y1 and y2 in the same way as we calculate the H1 and H2.

To find the value of y1, we first multiply the input value i.e., the outcome of H1 and H2 from the weights as

$$y1 = H1 * w5 + H2 * w6 + b2$$

$$y1 = 0.5932699 * 0.40 + 0.5968843 * 0.45 + 0.60$$

$$y1 = 1.1059059$$

To calculate the final result of y1 we performed the sigmoid function as

$$y1_{Final} = \frac{1}{1 + \frac{1}{e^{y1}}}$$

$$y1_{Final} = \frac{1}{1 + \frac{1}{e^{1.105905}}}$$

$$y1_{Final} = 0.751365$$

We will calculate the value of y2 in the same way as y1

$$y2 = H1 * w7 + H2 * w8 + b2$$

$$y2 = 0.5932699 * 0.50 + 0.5968843 * 0.55 + 0.60$$

$$y2 = 1.2249214$$

To calculate the final result of H1, we performed the sigmoid function as

$$y2_{Final} = \frac{1}{1 + \frac{1}{e^{y2}}}$$

$$y2_{Final} = \frac{1}{1 + \frac{1}{e^{1.2249214}}}$$

$$y2_{Final} = 0.772928465$$

Our target values are 0.01 and 0.99. Our y1 and y2 value is not matched with our target values T1 and T2.

Now, we will find the total error, which is simply the difference between the outputs from the target outputs. The total error is calculated as

$$E_{Total} = \sum \frac{1}{2}(target - output)^2$$

$$E_{Total} = \frac{1}{2}(T1 - y1_{Final})^2 + \frac{1}{2}(T2 - y2_{Final})^2$$

$$E_{Total} = \frac{1}{2}(0.01 - 0.751365)^2 + \frac{1}{2}(0.99 - 0.772928465)^2$$

$$E_{Total} = 0.274811084 + 0.0235600257$$

$$E_{Total} = 0.29837111$$

Now, we will backpropagate this error to update the weights using a backward pass.

## 6 Back-Propagate Error Function

To update the weight, we calculate the error correspond to each weight with the help of a total error. The error on weight  $w$  is calculated by differentiating total error with respect to  $w$ .

$$Error_w = \frac{\sigma E_{Total}}{\sigma W}$$

We perform backward process so first consider the last weight  $w_5$  as

$$Error_{w_5} = \frac{\sigma E_{Total}}{\sigma w_5}$$

## 7 Train Network

## 8 Predict

## 9 Iterate Convergence

## 10 CIFAR-10 Dataset

## 11 Result

## 12 Conclusion

## References