ENM 3600: Introduction to Data-driven Modeling

Lecture #7: Bayesian Linear regression



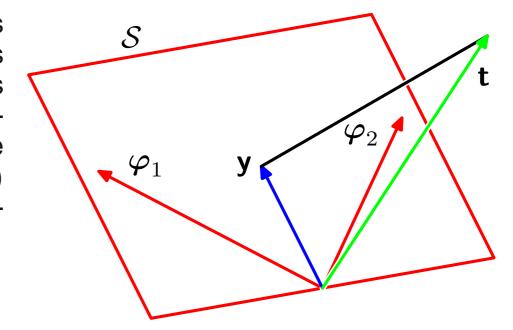
Linear regression

$$f: \mathcal{X} o \mathcal{Y}$$
 $\mathcal{D} = \{oldsymbol{x}, oldsymbol{y} \in \mathcal{X}, oldsymbol{y} \in \mathcal{Y}$ $oldsymbol{y} = f(oldsymbol{x}) + \epsilon$ $f(oldsymbol{x}) = w^T oldsymbol{x}$

"It's not just about lines and planes!"

Geometric interpretation

Figure 3.2 Geometrical interpretation of the least-squares solution, in an N-dimensional space whose axes are the values of t_1, \ldots, t_N . The least-squares regression function is obtained by finding the orthogonal projection of the data vector \mathbf{t} onto the subspace spanned by the basis functions $\phi_j(\mathbf{x})$ in which each basis function is viewed as a vector $\boldsymbol{\varphi}_j$ of length N with elements $\phi_j(\mathbf{x}_n)$.



Linear regression with basis functions

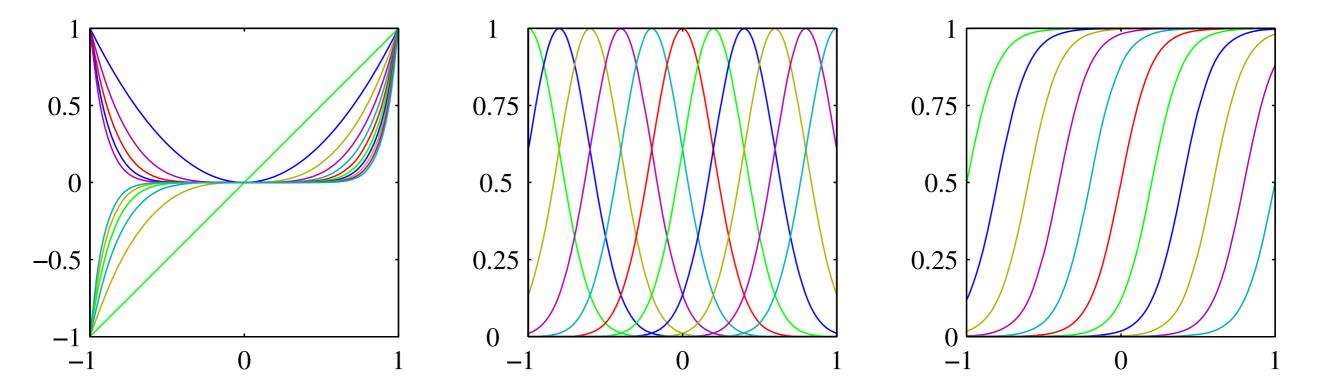
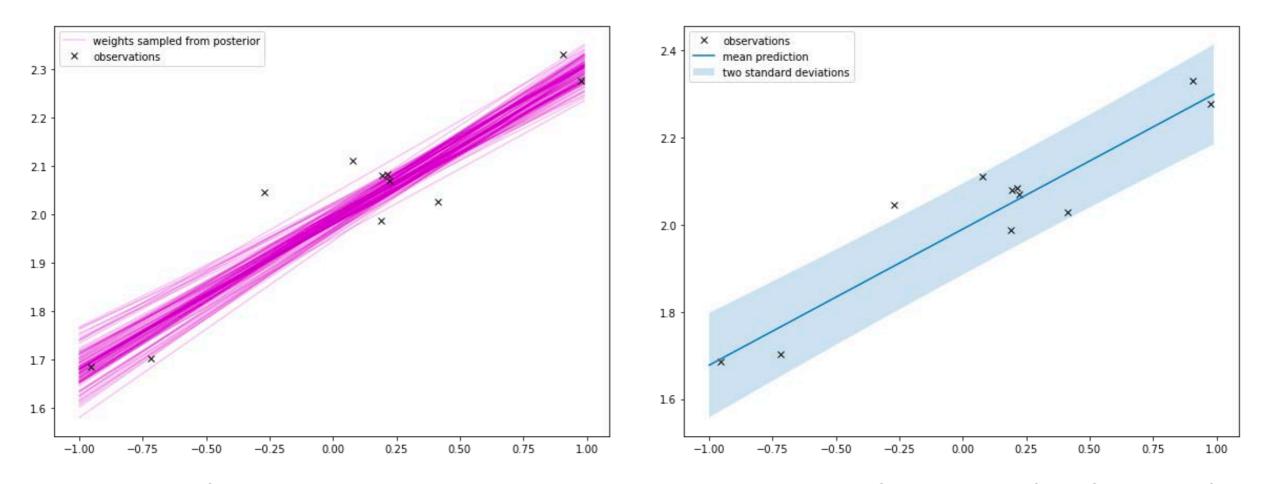
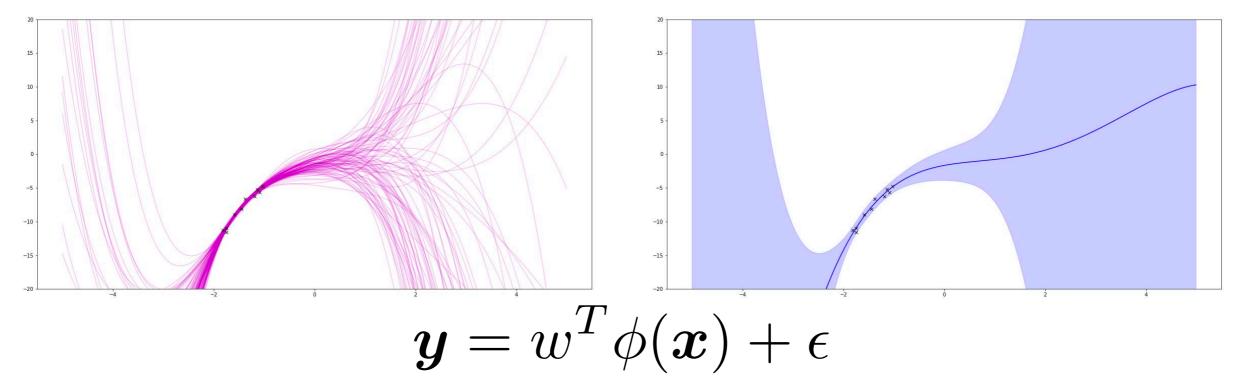


Figure 3.1 Examples of basis functions, showing polynomials on the left, Gaussians of the form (3.4) in the centre, and sigmoidal of the form (3.5) on the right.

Bayesian linear regression with basis functions



Nonlinear functions can be approximating using basis functions (or features)



Bayesian linear regression

