

**# Expand  $\sin(x)$  as Taylor series about  $x = \pi/2$  upto 3rd degree term.**

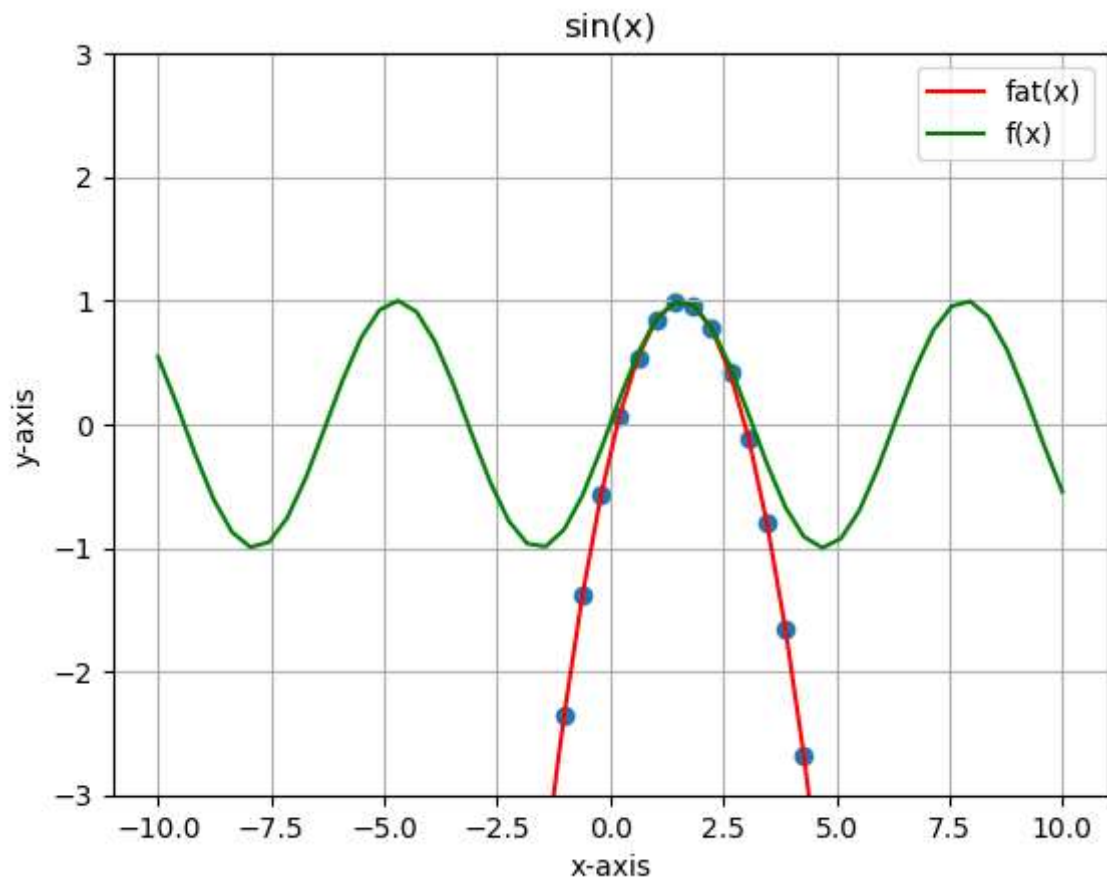
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In [1]: import numpy as np
import matplotlib.pyplot as plt
from sympy import *
x=symbols('x')
f=sin(x)
a= float(pi/2)
df= diff(f , x)
d2f = diff(f ,x , 2)
d3f = diff(f ,x , 3)
fat = lambdify(x , f)
dfat = lambdify(x , df)
d2fat = lambdify(x , d2f)
d3fat = lambdify(x , d3f)
f=fat(a)+((x-a)/factorial(1))*dfat(a)+((x-a)**2/factorial(2))*d2fat(a)+((x-a)**3/factorial(3))*d3fat(a)
display(simplify(f))
fat = lambdify(x,f)

def f(x):
    return np.sin(x)
x=np.linspace(-10,10)
plt.plot(x, fat(x), color='red',label='fat(x)')
plt.plot(x, f(x), color='green',label='f(x)')
plt.ylim([-3 , 3])
plt.title('sin(x)')
plt.xlabel('x-axis')
plt.ylabel('y-axis')
plt.scatter(x, fat(x))
plt.legend()
plt.grid()
plt.show()

```

$$-1.02053899928946 \cdot 10^{-17} x^3 - 0.5 x^2 + 1.5707963267949 x - 0.23370055013617$$



**# Find the Maclaurin series expansion of  $\sin(x) + \cos(x)$  upto 3rd degree term.**

```

In [2]: import numpy as np
import matplotlib.pyplot as plt
from sympy import *
x=symbols('x')
f=sin(x)+cos(x)
a=0
df= diff(f , x)
d2f = diff(f ,x , 2)
d3f = diff(f ,x , 3)
fat = lambdify(x , f)
dfat = lambdify(x , df)
d2fat = lambdify(x , d2f)
d3fat = lambdify(x , d3f )
f=fat(a)+((x-a)/factorial(1))*dfat(a)+((x-a)**2/factorial(2))*d2fat(a)+((x-a)**3/factorial(3))*d3fat(a)
display(simplify(f))
fat = lambdify(x,f)

def f(x):
    return np.sin (x)+np.cos(x)
x=np.linspace(-10,10)
plt.plot(x, fat(x), color='red',label='fat(x)')
plt.plot(x, f(x), color='green',label='f(x)')
plt.ylim([-3 , 3])
plt.title('sin(x)+cos(x)')
plt.xlabel('x-axis')
plt.ylabel('y-axis')
plt.scatter(x, fat(x))
plt.legend()
plt.grid()
plt.show()

```

$$-0.1666666666666667x^3 - 0.5x^2 + 1.0x + 1.0$$

