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%% Problem 1 & 2
clc; close all; clearvars; set(groot,"defaultTextInterpreter","latex");
rng(0,"v4");

% Simulation variables
dt = 1; % Process time step, s
dtMeas = 2;
tNextMeas = dtMeas;
meas_available = 0;
tMax = 202; % Max time, s

% Kalman Filter variables
var_init_uncertainty = [100^2; 100];
var_meas_noise = 100^2;
var_process_noise = [0; 0];

n = length(var_init_uncertainty);
m = length(var_meas_noise);

R = diag(var_meas_noise); % mxm Measurement noise matrix
P = diag(var_init_uncertainty); % nxn Covariance matrix
q = 0.002;
Q = [(dt^3)/3, (dt^2)/2; (dt^2)/2, dt].*q; % nxn

PHI = [1 dt; 0 1]; % State transition matrix
H = [1 0]; % Measurement matrix

x0_true = [0; 24.6];
x0_est = [0; 0];

% For storing process
saveVars = {"T", "X_true", "X_est", "Z_true", "Z_est", "P_est", "P_plot", "q"};

T = 0:dt:tMax;
t_length = length(T);
X_true = nan(n,t_length); % True state vectors (n x steps)
X_est = nan(n,t_length); % Estimate state vectors (n x steps)
Z_true = nan(m,t_length); % True measurement vectors (m x steps)
Z_est = nan(m,t_length); % Estimate measurement vectors (m x steps)
P_est = nan(n,n,t_length); % Estimate variance vectors (n x n steps)
P_plot= nan(n,n,t_length);
xtrue = x0_true;
xest = x0_est;

for i = 1:length(T)
    t = T(i);

    if t>=tNextMeas
        tNextMeas = t+dtMeas;
        meas_available=1;
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else
    meas_available=0;
end

if meas_available == 1
    X_true(:,i) = xtrue;
    X_est(:,i) = xest;
    Z_true(:,i) = H*X_true(:,i) + sqrt(R)*randn(m,1);
    Z_est(:,i) = H*X_est(:,i);
    P_est(:,:,i) = P;
    P_plot(:,i) = diag(P_est(:,:,i));

    % Gain Matrix
    K = P_est(:,:,i)*H'/(H*P_est(:,:,i)*H' + R);

    % States updated with measurement information
    X_est(:,i) = X_est(:,i) + K*(Z_true(:,i) - Z_est(:,i));

    % Covariance matrix updated with measurement information
    I = eye(n);
    P_est(:,:,i) = (I - K*H)*P_est(:,:,i);
    P_plot(:,i) = diag(P_est(:,:,i));
else
    X_true(:,i) = xtrue;
    X_est(:,i) = xest;
    Z_true(:,i) = nan(m,1);
    Z_est(:,i) = nan(m,1);
    P_est(:,:,i) = P;
    P_plot(:,i) = diag(P_est(:,:,i));
end

t = t+dt;

% SIM propagation
if (80 <= t) && (t < 120)
    accel = -0.3925;
else
    accel = 0;
end

xtrue = PHI*X_true(:,i) + dt*[0; accel];

% STATE propagation
xest= PHI*X_est(:,i);
P = PHI*P_est(:,:,i)*PHI' + Q;

end

clearvars("-except",saveVars{:})
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```
%% Estimate plots
figure()
est_plot = tiledlayout(2,1);
title(est_plot, sprintf("Vehicle State Estimation q = %.3f",q));
xlabel(est_plot, "Time(s)");

nexttile
plot(T(1:2:end),X_true(1,1:2:end), "k",T(1:2:end),X_est(1,1:2:end), "r",T(1:2:end),Z_true(1:2:end), "b*");
ylabel("Position, m")
legend("$X_1$", "$\hat{X}_1$", "$Z$", "Location", "northeast", "interpreter", "latex")

nexttile
plot(T(1:2:end),X_true(2,1:2:end), "k",T(1:2:end),X_est(2,1:2:end), "r");
ylabel("Velocity, m/s");
legend("$X_2$", "$\hat{X}_2$", "Location", "northeast", "interpreter", "latex")

%% Error plots
figure()
err_plot = tiledlayout(2,1);
title(err_plot, sprintf("Estimation Error q = %.3f",q));
xlabel(est_plot, "Time(s)");

nexttile
plot(T(1:2:end),X_est(1,1:2:end)-X_true(1,1:2:end), "r", ...
     T(1:2:end),sqrt(P_plot(1,1:2:end)), "b", T(1:2:end), -sqrt(P_plot(1,1:2:end)), "b");
ylabel("Position Error")

nexttile
plot(T(1:2:end),X_est(2,1:2:end)-X_true(2,1:2:end), "r", ...
     T(1:2:end),sqrt(P_plot(2,1:2:end)), "b", T(1:2:end), -sqrt(P_plot(2,1:2:end)), "b");
ylabel("Velocity Error")
```