Module 5.5: Nesterov Accelerated Gradient Descent

Question

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- Yes, let's look at Nesterov accelerated gradient

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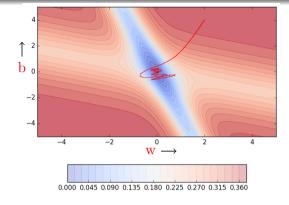
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Update rule for NAG

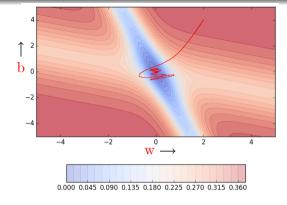
$$\begin{split} w_{look_ahead} &= w_t - \gamma \cdot update_{t-1} \\ update_t &= \gamma \cdot update_{t-1} + \eta \nabla w_{look_ahead} \\ w_{t+1} &= w_t - update_t \end{split}$$

We will have similar update rule for b_t

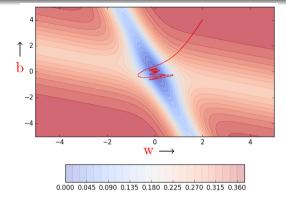
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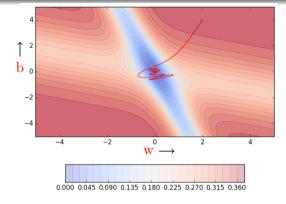
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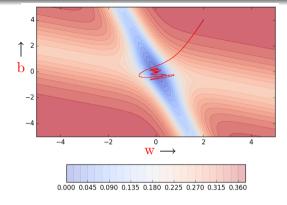
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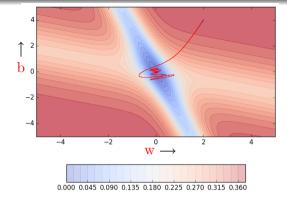
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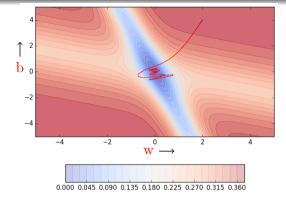
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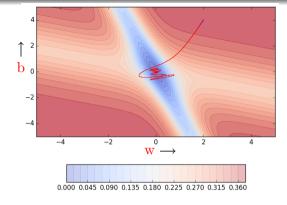
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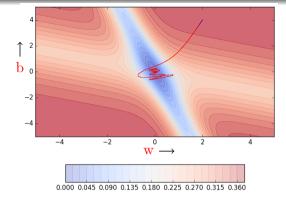
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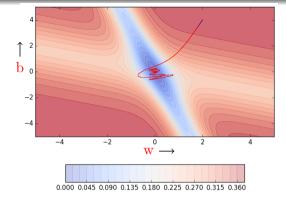
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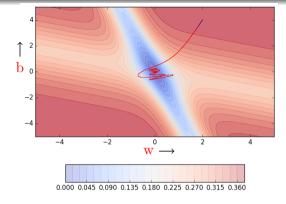
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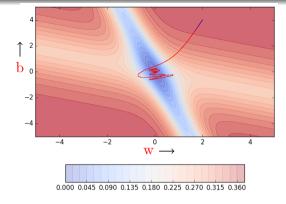
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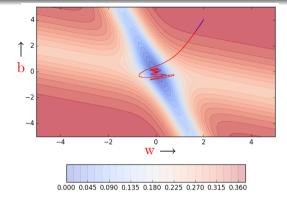
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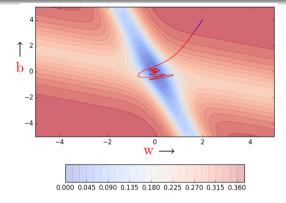
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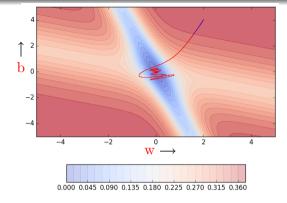
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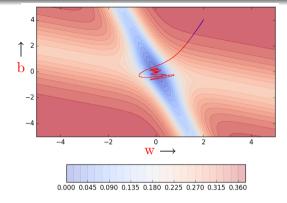
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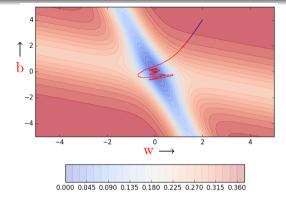
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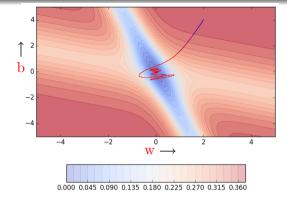
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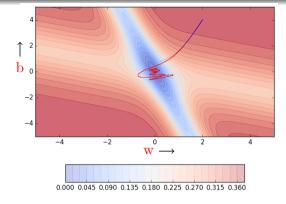
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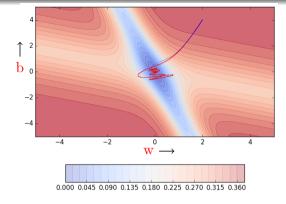
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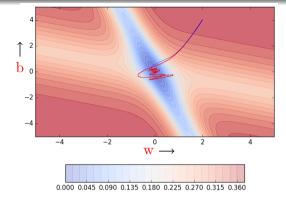
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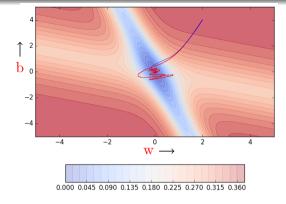
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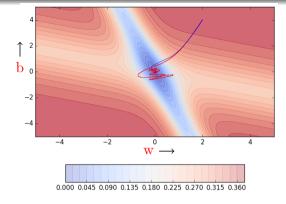
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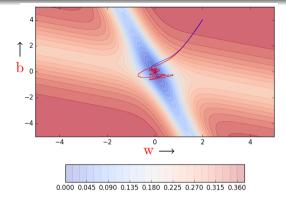
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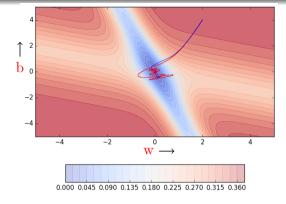
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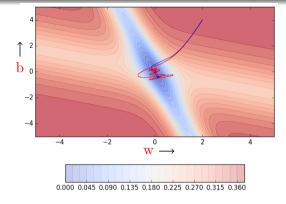
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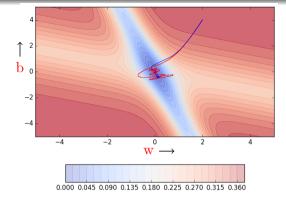
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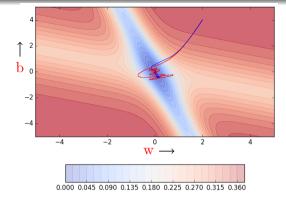
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def do nesterov accelerated gradient descent() :
w, b, eta = init w, init b , 1.0
 prev v w, prev v b, qamma = 0, 0, 0.9
 for i in range(max epochs) :
     dw, db = 0, 0
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     v b = gamma * prev v b
     for x,y in zip(X, \overline{Y}):
         dw += grad w(w - v w, b - v b, x, y)
         db += grad b(w - v w, b - v b, x, y)
     v w = gamma * prev v w + eta *
     v b = gamma * prev v b + eta * db
     w = w - v w
     b = b - v b
     prev v w = v w
     prev v b = v b
```



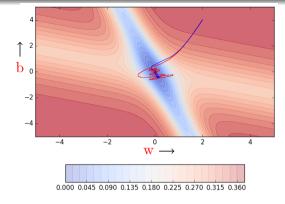
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     v b = gamma * prev v b + eta * db
     w = w - v w
     b = b - v b
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```



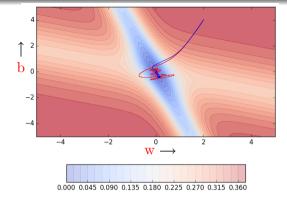
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         db += grad b(w - v w, b - v b, x, y)
     v w = gamma * prev v w + eta *
     v b = gamma * prev v b + eta * db
     w = w - v w
     b = b - v b
     prev v w = v w
     prev v b = v b
```



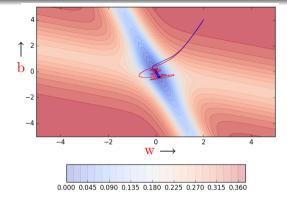
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     v w = gamma * prev v w
     v b = gamma * prev v b
     for x,y in zip(X, \overline{Y}):
         dw += grad w(w - v w, b - v b, x, y)
         db += grad b(w - v w, b - v b, x, y)
     v w = gamma * prev v w + eta *
     vb = gamma * prev vb + eta * db
     w = w - v w
     b = b - v b
     prev v w = v w
     prev v b = v b
```



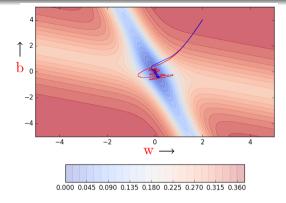
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     w = w - v w
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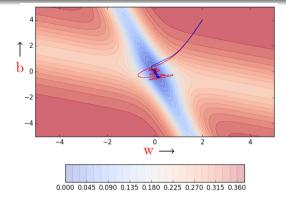
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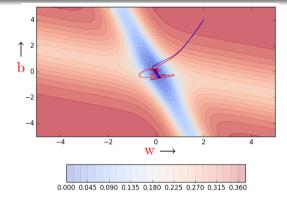
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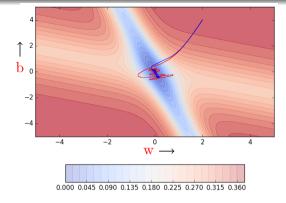
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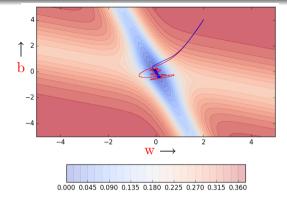
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     b = b - v b
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```



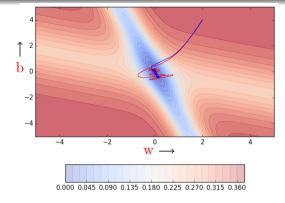
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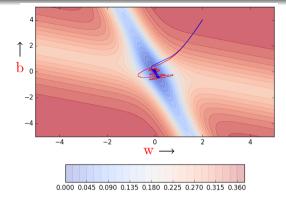
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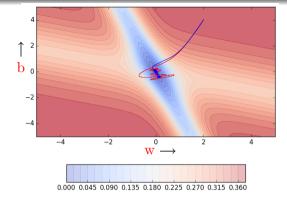
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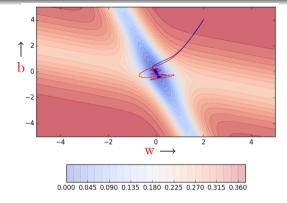
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Observations about NAG

• Looking ahead helps NAG in correcting its course quicker than momentum based gradient descent

Observations about NAG

- Looking ahead helps NAG in correcting its course quicker than momentum based gradient descent
- Hence the oscillations are smaller and the chances of escaping the minima valley also smaller