#### In [2]:

```
import numpy as np
import random
import mpmath as mp
import pandas as pd
mp.dps=40
```

#### In [3]:

```
def ABCindeks(drevo): #izracun ABC indeksa za neko drevo, len(drevo[u]) ti da dolzino s
eznama sosedov za vozlisce u torej je to stopnja vozlisca u
    produkt = 1
    for u in drevo:
        for v in drevo[u]:
            produkt = produkt * (len(drevo[u]) + len(drevo[v]) - 2) / (len(drevo[u]) *
len(drevo[v]))
    return sqrt(produkt)
#ABCindeks(G)
```

#### In [3]:

```
def minABCindeks(n): #izracun najmanjsega ABC indeksa za vsa drevesa z n vozlisci, vrne
tudi seznam dreves, ki imajo ta najmanjsi indeks
    min_indeks = None
    for dr in graphs.trees(n):
        if min indeks == None:
            min_indeks = ABCindeks(dr)
            drevesa_z_min_ind = [dr]
        else:
            if ABCindeks(dr) < min_indeks:</pre>
                min_indeks = ABCindeks(dr)
                drevesa_z_min_ind = [dr]
            elif ABCindeks(dr) == min_indeks:
                drevesa_z_min_ind.append(dr)
            else:
                continue
    return min indeks , drevesa z min ind
#minABCindeks(9)
```

#### In [40]:

#### Out[40]:

```
[(1, [Graph on 1 vertex]),
 (0, [Graph on 2 vertices]),
 (1/4, [Graph on 3 vertices]),
 (1/8, [Graph on 4 vertices]),
 (1/16, [Graph on 5 vertices]),
 (1/32, [Graph on 6 vertices]),
 (1/64, [Graph on 7 vertices, Graph on 7 vertices]),
 (1/128, [Graph on 8 vertices, Graph on 8 vertices]),
 (1/256,
  [Graph on 9 vertices,
  Graph on 9 vertices,
  Graph on 9 vertices,
  Graph on 9 vertices]),
 (1/576, [Graph on 10 vertices]),
 (1/1152, [Graph on 11 vertices]),
 (5/12288, [Graph on 12 vertices]),
 (1/5184, [Graph on 13 vertices]),
 (3/32768, [Graph on 14 vertices]),
 (25/589824, [Graph on 15 vertices]),
 (25/1179648, [Graph on 16 vertices, Graph on 16 vertices]),
 (5/524288, [Graph on 17 vertices])]
```

#### In [4]:

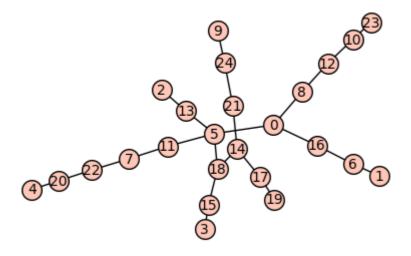
```
def SA algoritem boljsi(n, T=100, fun=ABCindeks): #algoritem za iskanje drevesa z najma
njšim ABC indeksom za drevesa z več vozlišči. Algoritm vrne min_indekse in pripajadoca
drevesa po 100, 1000 in 10000 korakih
    drevo =graphs.RandomTree(n)
    najboljse drevo, najboljsa vrednost = drevo, fun(drevo) ### zacetno drevo proglasim
o za najboljso in tudi za trenutno izbrano
    trenutno_drevo, trenutna_vrednost = drevo, fun(drevo)
    for i in range(10000):
        listi_drevesa = []
        stopnje vozlisc = trenutno drevo.degree()
        for i in range(n):
            if stopnje vozlisc[i] == 1:
                listi_drevesa.append(i)
                                                     ### sedaj imamo vse liste drevesa
        stevilo listov = len(listi drevesa)
        nakljucni_list = listi_drevesa[random.randint(0,stevilo_listov - 1)] ### izbere
mo nakljucni list
        popravek = copy(trenutno_drevo) ### ustvarimo kopijo drevesa na katerem bomo
 izvedli zamenjavo
        ostala_vozlisca = [x for x in popravek.vertices() if x!=nakljucni_list]
        povezava = (nakljucni_list, trenutno_drevo[nakljucni_list][0]) ### list bo imel
Le enega soseda
        popravek.delete edge(povezava)
        izbrano vozlisce = ostala vozlisca[random.randint(0, len(ostala vozlisca) -1)]
        popravek.add_edge(nakljucni_list, izbrano_vozlisce) #### dodamo povezavo na kop
iji
        vrednost_popravka = fun(popravek)
        if (najboljsa_vrednost > vrednost_popravka):
             najboljse drevo, najboljsa vrednost = popravek, fun(popravek)
             trenutno drevo, trenutna vrednost = popravek, fun(popravek)
        elif (trenutna_vrednost > vrednost_popravka) or (mp.exp((-(vrednost_popravka -
trenutna_vrednost)/T)) > random.random()): ### popravek je sprejet ce je bila vrednost
popravka manjsa od trenutne vrednosti ali pa
            trenutno_drevo, trenutna_vrednost = popravek, fun(popravek)
        T = T/(i+1)
    return najboljse_drevo
```

```
In [5]:
```

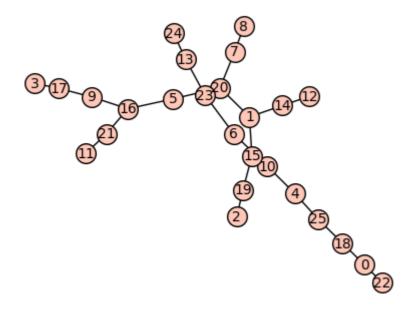
```
for i in range(25,41):
    print("Graf s {} vozlisci".format(i))
    show(SA_algoritem_boljsi(i))
```

#### Graf s 25 vozlisci

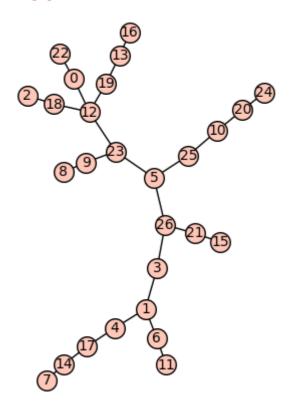
### Out[5]:



Graf s 26 vozlisci

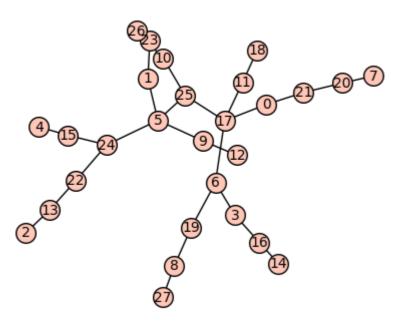


Graf s 27 vozlisci

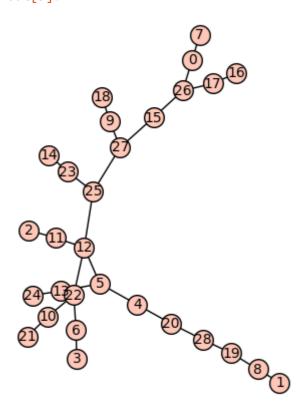


Graf s 28 vozlisci

### Out[5]:

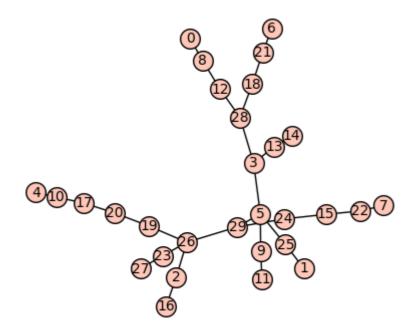


Graf s 29 vozlisci

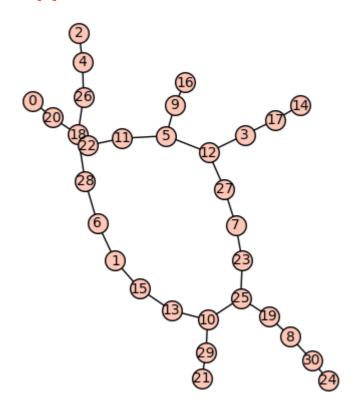


#### Graf s 30 vozlisci

### Out[5]:

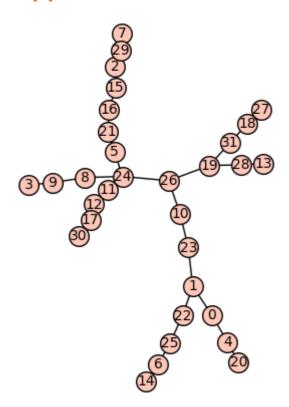


Graf s 31 vozlisci

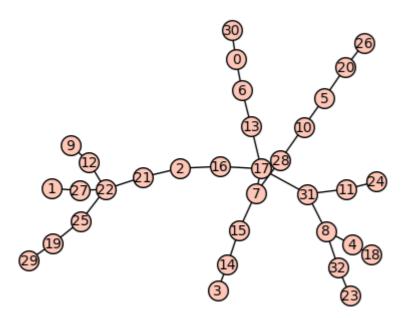


Graf s 32 vozlisci

### Out[5]:

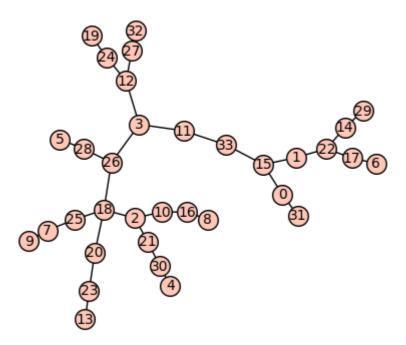


Graf s 33 vozlisci

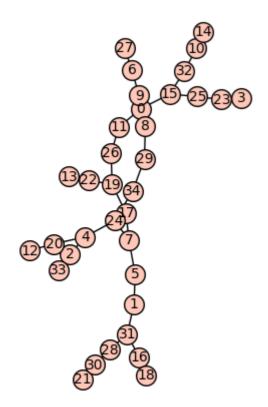


Graf s 34 vozlisci

### Out[5]:

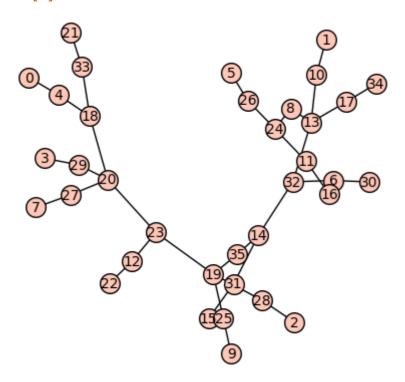


Graf s 35 vozlisci

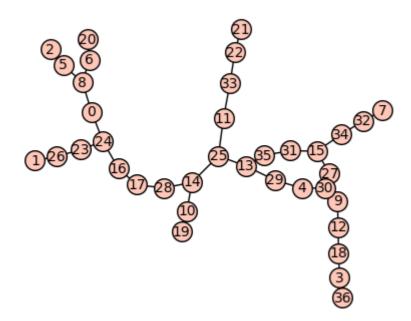


Graf s 36 vozlisci

# Out[5]:

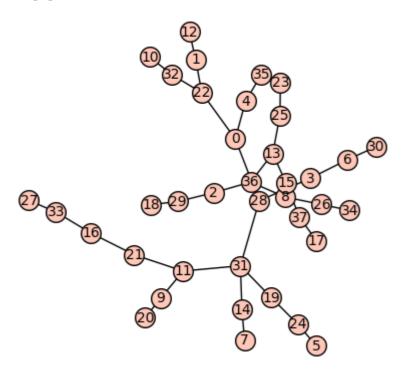


Graf s 37 vozlisci

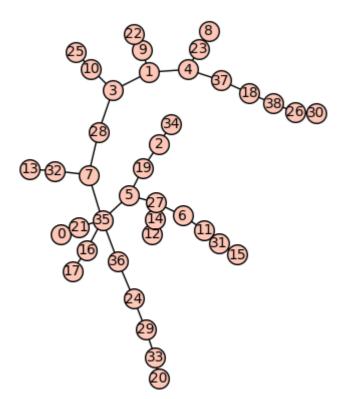


Graf s 38 vozlisci

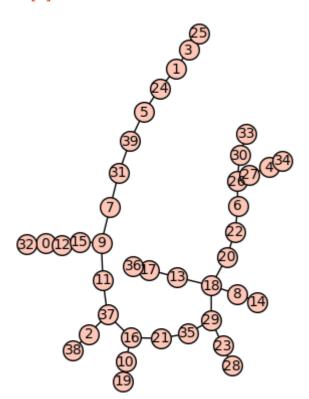
### Out[5]:



Graf s 39 vozlisci



Graf s 40 vozlisci



#### In [5]:

```
def SA algoritem koraki(n, T=100, fun=ABCindeks): #algoritem za iskanje drevesa z najma
njšim ABC indeksom za drevesa z več vozlišči. Algoritm vrne min_indekse in pripajadoca
 drevesa po 100, 1000 in 10000 korakih
    drevo =graphs.RandomTree(n)
    scale = np.sqrt(T)
    trenutna_vrednost = fun(drevo)
    history = [drevo]
    for i in range(10000):
        listi_drevesa = []
        stopnje vozlisc = drevo.degree()
        for i in range(n):
            if stopnje vozlisc[i] == 1:
                listi_drevesa.append(i)
                                                      ### sedaj imamo vse liste drevesa
        stevilo_listov = len(listi_drevesa)
        nakljucni_list = listi_drevesa[random.randint(0,stevilo_listov - 1)] ### izbere
mo nakljucni list
        popravek = copy(drevo) ### ustvarimo kopijo drevesa na katerem bomo izvedli z
amenjavo
        ostala_vozlisca = [x for x in popravek.vertices() if x!=nakljucni_list]
        povezava = (nakljucni_list, drevo[nakljucni_list][0]) ### list bo imel le enega
soseda
        popravek.delete edge(povezava)
        izbrano vozlisce = ostala vozlisca[random.randint(0, len(ostala vozlisca) -1)]
        popravek.add_edge(nakljucni_list, izbrano_vozlisce) #### dodamo povezavo na kop
iji
        vrednost_popravka = fun(popravek)
        if (trenutna_vrednost > vrednost_popravka) or (mp.exp((-(vrednost_popravka - tr
enutna vrednost)/T)) > random.random()): ### popravek je sprejet ce je bila vrednost po
pravka manjsa od trenutne vrednosti ali pa
            drevo = popravek
        trenutna_vrednost = fun(drevo)
        T = 0.9*T
        history.append(drevo)
    return fun(history[0]), fun(history[99]), fun(history[999]), fun(history[999]), hi
story[0], history[99], history[999], history[9999]
```

#### In [10]:

```
df = pd.DataFrame(vrednosti_koraki, columns =['Stevilo vozlisc', 'K0', 'K100', 'K1000',
'K10000'])
df #### opazimo, da je 1000 korakov ze dovolj
```

#### Out[10]:

	Stevilo vozlisc	K0	K100	K1000	K10000
0	10	8.230453e-03	2.314815e-03	1.953125e-03	1.953125e-03
1	11	1.736111e-03	9.765625e-04	9.765625e-04	9.765625e-04
2	12	1.066667e-02	6.510417e-04	4.882812e-04	4.882812e-04
3	13	4.340278e-04	4.882812e-04	2.441406e-04	2.441406e-04
4	14	3.429355e-04	1.627604e-04	1.085069e-04	1.085069e-04
5	15	2.286237e-04	4.938272e-04	5.425347e-05	5.425347e-05
6	16	5.715592e-05	3.616898e-05	2.543132e-05	2.543132e-05
7	17	1.607510e-05	4.233772e-05	1.271566e-05	1.271566e-05
8	18	7.144490e-06	1.905197e-05	6.028164e-06	6.028164e-06
9	19	5.208333e-06	2.172589e-05	3.814697e-06	3.814697e-06
10	20	3.456790e-05	2.381497e-06	1.507041e-06	1.507041e-06
11	21	1.589457e-06	5.298191e-06	9.536743e-07	9.536743e-07
12	22	5.023470e-06	2.116886e-06	3.973643e-07	3.973643e-07
13	23	6.697960e-07	8.477105e-07	1.766064e-07	1.766064e-07
14	24	6.279337e-07	2.109857e-07	7.358598e-08	7.358598e-08
15	25	2.531250e-06	3.675149e-07	3.679299e-08	3.679299e-08
16	26	5.518949e-08	1.102545e-07	1.362703e-08	1.362703e-08
17	27	4.410179e-08	4.709503e-07	7.726528e-09	7.726528e-09
18	28	8.573388e-08	4.961452e-08	6.208817e-09	6.208817e-09
19	29	1.277534e-08	3.270488e-08	2.299562e-09	2.299562e-09
20	30	1.148484e-08	1.324548e-08	1.022028e-09	1.022028e-09
21	31	2.907100e-09	3.024814e-09	4.850638e-10	4.850638e-10
22	32	2.205090e-09	1.178705e-08	2.555069e-10	2.555069e-10
23	33	1.064612e-09	1.451911e-09	1.453550e-10	1.453550e-10
24	34	2.197768e-09	8.066171e-10	4.790754e-11	4.790754e-11
25	35	5.450813e-10	5.677931e-10	2.694799e-11	2.694799e-11

#### In [14]:

Out[14]:

35

#### In [5]:

```
def SA_algoritem(n, T=100, fun=ABCindeks): #algoritem za iskanje drevesa z najmanjšim A
BC indeksom za drevesa z več vozlišči
    drevo =graphs.RandomTree(n)
    scale = np.sqrt(T)
    trenutna_vrednost = fun(drevo)
    history = [drevo]
    for i in range(10000):
        listi_drevesa = []
        stopnje_vozlisc = drevo.degree()
        for i in range(n):
            if stopnje_vozlisc[i] == 1:
                listi_drevesa.append(i)
                                                      ### sedaj imamo vse liste drevesa
        stevilo_listov = len(listi_drevesa)
        nakljucni_list = listi_drevesa[random.randint(0,stevilo_listov - 1)] ### izbere
mo nakljucni list
        popravek = copy(drevo) ### ustvarimo kopijo drevesa na katerem bomo izvedli z
amenjavo
        ostala_vozlisca = [x for x in popravek.vertices() if x!=nakljucni_list]
        povezava = (nakljucni_list, drevo[nakljucni_list][0]) ### list bo imel le enega
soseda
        popravek.delete_edge(povezava)
        izbrano_vozlisce = ostala_vozlisca[random.randint(0, len(ostala_vozlisca) -1)]
        popravek.add_edge(nakljucni_list, izbrano_vozlisce) #### dodamo povezavo na kop
iji
        vrednost_popravka = fun(popravek)
        if (trenutna_vrednost > vrednost_popravka) or (mp.exp((-(vrednost_popravka - tr
enutna_vrednost)/T)) > random.random()): ### popravek je sprejet ce je bila vrednost po
pravka manjsa od trenutne vrednosti ali pa
            drevo = popravek
        trenutna vrednost = fun(drevo)
        T = 0.9*T
        history.append(drevo)
    return trenutna_vrednost, fun(history[0]), drevo
```

#### In [30]:

#### Out[30]:

```
[(1/512, Graph on 10 vertices),
 (1/1152, Graph on 11 vertices),
 (1/2048, Graph on 12 vertices),
 (5/24576, Graph on 13 vertices),
 (1/8192, Graph on 14 vertices),
 (1/18432, Graph on 15 vertices),
 (1/36864, Graph on 16 vertices),
 (5/442368, Graph on 17 vertices),
 (1/147456, Graph on 18 vertices),
 (5/1769472, Graph on 19 vertices),
 (1/589824, Graph on 20 vertices),
 (1/1179648, Graph on 21 vertices),
 (1/2654208, Graph on 22 vertices),
 (5/28311552, Graph on 23 vertices),
 (1/9437184, Graph on 24 vertices),
 (1/21233664, Graph on 25 vertices),
 (1/37748736, Graph on 26 vertices),
 (1/83886080, Graph on 27 vertices),
 (125/41278242816, Graph on 28 vertices),
 (1/268435456, Graph on 29 vertices),
 (5/3221225472, Graph on 30 vertices),
 (5/6442450944, Graph on 31 vertices),
 (25/77309411328, Graph on 32 vertices),
 (25/173946175488, Graph on 33 vertices),
 (1/13759414272, Graph on 34 vertices),
 (5/115964116992, Graph on 35 vertices)]
```

#### In [101]:

```
# recimo da naju zanimajo premeri teh grafov, uporabiva Lahko metodo diameter za objekt
e graphs
premeri = []
for (vrednost, seznam_grafov) in rezultati:
    pr = []
    for graf in seznam_grafov:
        pr.append(graf.diameter())
    premeri.append(pr)
print(premeri)
```

```
[[0], [1], [2], [3], [4], [5], [6, 4], [7, 5], [8, 6, 6, 4], [5], [6], [5], [6], [7, 6], [6]]
```

#### In [104]:

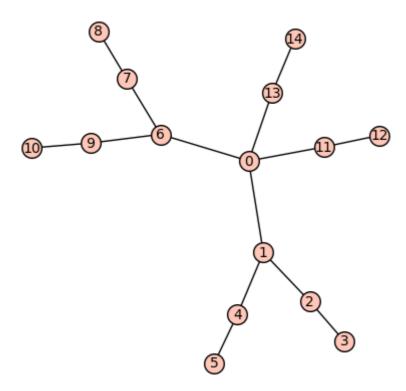
```
premeri2 = []
for (vrednost, graf) in rezultati2:
    premeri2.append([graf.diameter()])
print(premeri2)
```

```
[[5], [6], [7], [7], [7], [11], [11], [7], [11], [13], [15], [16], [13], [15], [9], [13], [11], [12], [12], [10], [14], [12], [17], [12], [12]]
```

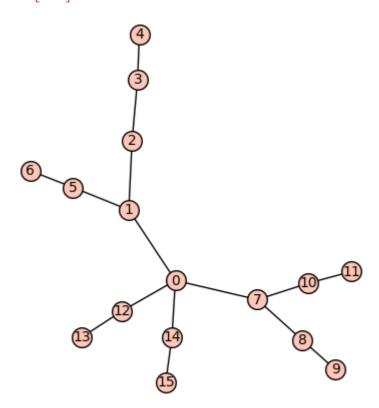
### In [126]:

```
for i in range(14,17):
    show(rezultati[i][1][0])
```

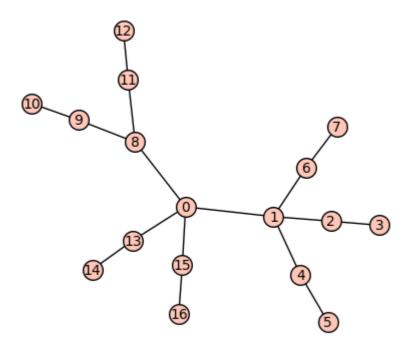
### Out[126]:



### Out[126]:



### Out[126]:



#### In [113]:

```
#ce naju zanimajo dolzine najdaljsih poti v grafih
def najdaljsa_pot(graf):
    najdaljsa = 0
    for u in graf:
                              #gremo cez vsa vozlisca v grafu
        if len(graf[u]) == 2: #ce imajo stopnjo = 2 nadaljujemo
            soseda = graf[u]
            s = u #dolocimo sedanje vozlisce
            dolzina = 3
                               #sedaj imamo pot dolzine vsaj 3 - sedanje vozlišče in nj
egova soseda
            if len(graf[soseda[0]]) != 2: #preverimo ali ima vsaj eno od sosednjih vozl
isc stopnjo neenako 2 (da ne zacnemo steti sredi poti)
                p = soseda[0] #dolocimo prejsnje vozlisce (tisto s stopnjo neenako 2)
                n = soseda[1] # in naslednje vozlisce
            elif len(graf[soseda[1]]) != 2:
                p = soseda[1]
                n = soseda[0]
            else: #ce imata obe sosednji vozlisci stopnjo 2 smo na sredi poti in tega p
rimera ne preverjamo
                continue
            while len(graf[n]) == 2: #z while zanko se bomo sedaj premikali po poti dok
ler ne naletimo na vozlisce ki nima stopnje = 2
                dolzina += 1 #za vsako naslednje vozlisce povecamo dolzino
                p = s #premanemo vozlisca: novo prejsnje je staro sedanje,
                s = n #novo sedanje je staro naslednje
                if graf[s][0] != p: #novo naslednje je tisto od sosedov novega sedanjeg
a ki ni enako novemu prejsnjemu
                    n = graf[s][0]
                else:
                    n = graf[s][1]
        else:
            continue
        if dolzina > najdaljsa: #ce smo nasli novo najdaljso pot jo shranimo
            najdaljsa = dolzina
    return najdaljsa
najdaljse poti = []
for (vrednost, seznam_grafov) in rezultati:
    dol = []
    for graf in seznam_grafov:
        dol.append(najdaljsa pot(graf))
    najdaljse poti.append(dol)
print(najdaljse poti)
```

```
[[0], [0], [3], [4], [5], [6], [7, 3], [8, 4], [9, 5, 4, 3], [3], [3], [3], [3], [3], [4], [3]]
```

#### In [114]:

```
### Longest thread SA
najdaljse_poti2 = []
for (vrednost, graf) in rezultati2:
    najdaljse_poti2.append([najdaljsa_pot(graf)])
print(najdaljse_poti2)
```

#### In [19]:

#### Out[19]:

```
[(1, [0], 'sum=0', 'abc_indeks=1'),
 (2, [0, 0], 'sum=0', 'abc_indeks=0'),
 (3, [0, 0, 0], 'sum=0', 'abc_indeks=1/4'),
 (4, [0, 0, 0, 0], 'sum=0', 'abc_indeks=1/8'),
 (5, [0, 0, 0, 0, 0], 'sum=0', 'abc_indeks=1/16'),
 (6, [0, 0, 0, 0, 0], 'sum=0', 'abc_indeks=1/32'),
 (7, [0, 0, 0, 0, 0, 0], 'sum=0', 'abc_indeks=1/64'),
 (7, [1, 0, 0, 0, 0, 0], 'sum=1', 'abc_indeks=1/64'),
 (8, [0, 0, 0, 0, 0, 0, 0], 'sum=0', 'abc_indeks=1/128'),
 (8, [1, 0, 0, 0, 0, 0, 0], 'sum=1', 'abc_indeks=1/128'),
(9, [0, 0, 0, 0, 0, 0, 0, 0], 'sum=0', 'abc_indeks=1/256'), (9, [0, 1, 0, 0, 0, 0, 0, 0], 'sum=1', 'abc_indeks=1/256'), (9, [1, 0, 0, 0, 0, 0, 0, 0], 'sum=1', 'abc_indeks=1/256'), (9, [1, 0, 0, 0, 0, 0, 0, 0], 'sum=1', 'abc_indeks=1/256'), (9, [1, 0, 0, 0, 0, 0, 0, 0], 'sum=1', 'abc_indeks=1/256'),
 (10, [1, 1, 0, 0, 0, 0, 0, 0, 0], 'sum=2', 'abc_indeks=1/576'),
 (11, [1, 1, 0, 0, 0, 0, 0, 0, 0, 0], 'sum=2', 'abc_indeks=1/1152'),
 (12, [1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0], 'sum=2', 'abc_indeks=5/1228
8'),
 (13, [1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0], 'sum=3', 'abc_indeks=1/518
4'),
 (14,
  [1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
  'sum=2',
  'abc_indeks=3/32768'),
 (15,
  [1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0],
  'sum=3',
  'abc_indeks=25/589824'),
  [1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0],
  'sum=3',
  'abc indeks=25/1179648'),
 (16,
  [1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0],
  'sum=3',
  'abc_indeks=25/1179648'),
 (17,
  [1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0],
  'sum=3',
  'abc_indeks=5/524288'),
  [1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0]
  'abc indeks=125/28311552'),
 (19,
  [1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
  'sum=3',
  'abc_indeks=7/3276800')]
```

#### In [20]:

#### Out[20]:

[(1, 0),(2, 2),(3, 2),(4, 2),(5, 2),(6, 2),(7, 2),(7, 3),(8, 2),(8, 3),(9, 2),(9, 3),(9, 3),(9, 4),(10, 4),(11, 4),(12, 5),(13, 5),(14, 6),(15, 6),(16, 6),(16, 6),(17, 7), (18, 7),

(19, 8)

#### In [115]:

```
#### koliko listov SA Algo
stevilo_listov2 = []
for (vrednost, graf) in rezultati2:
    listi = 0
    for u in graf:
        if len(graf[u]) == 1:
            listi += 1
        stevilo_listov2.append((graf.order(), listi))
    listi = 0
stevilo_listov2
```

#### Out[115]:

```
[(10, 4),
 (11, 4),
 (12, 4),
 (13, 4),
 (14, 5),
 (15, 5),
 (16, 4),
 (17, 4),
 (18, 7),
 (19, 5),
 (20, 4),
 (21, 3),
 (22, 4),
 (23, 6),
 (24, 5),
 (25, 8),
 (26, 7),
 (27, 9),
 (28, 7),
 (29, 10),
 (30, 10),
 (31, 8),
 (32, 8),
 (33, 9),
 (34, 11),
```

(35, 10)

#### In [22]:

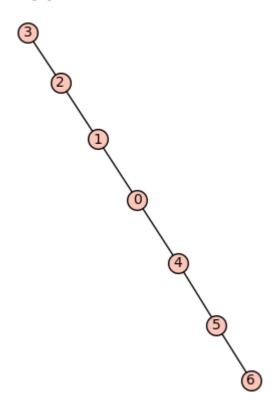
```
### stopnja vsakega vozlišča
povezave_indeksi = []
for (vrednost, seznam_grafov) in rezultati:
    for graf in seznam_grafov:
        indeksi = []
        for u in graf:
            indeksi.append(len(graf[u]))
        povezave_indeksi.append((graf.order(),indeksi))
        indeksi = []
povezave_indeksi
```

#### Out[22]:

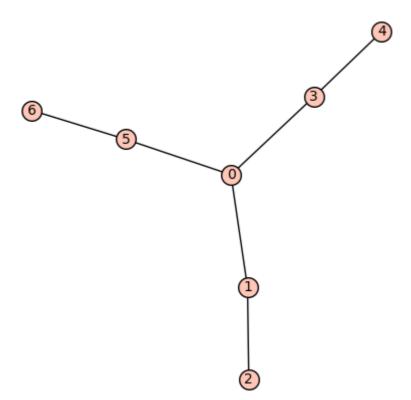
```
[(1, [0]),
 (2, [1, 1]),
 (3, [2, 1, 1]),
 (4, [2, 2, 1, 1]),
 (5, [2, 2, 1, 2, 1]),
 (6, [2, 2, 2, 1, 2, 1]),
 (7, [2, 2, 2, 1, 2, 2, 1]),
 (7, [3, 2, 1, 2, 1, 2, 1]),
 (8, [2, 2, 2, 2, 1, 2, 2, 1]),
 (8, [3, 2, 2, 1, 2, 1, 2, 1]),
 (9, [2, 2, 2, 2, 1, 2, 2, 2, 1]),
 (9, [2, 3, 2, 1, 2, 1, 2, 2, 1]),
 (9, [3, 2, 2, 1, 2, 2, 1, 2, 1]),
 (9, [4, 2, 1, 2, 1, 2, 1, 2, 1]),
 (10, [3, 3, 2, 1, 2, 1, 2, 1, 2, 1]),
 (11, [3, 3, 2, 1, 2, 1, 2, 2, 1, 2, 1]),
 (12, [4, 3, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1]),
 (13, [3, 3, 2, 1, 2, 1, 3, 2, 1, 2, 1, 2, 1]),
 (14, [4, 4, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1]),
 (15, [4, 3, 2, 1, 2, 1, 3, 2, 1, 2, 1, 2, 1, 2, 1]),
 (16, [4, 3, 2, 2, 1, 2, 1, 3, 2, 1, 2, 1, 2, 1, 2, 1]),
 (16, [4, 3, 2, 1, 2, 1, 3, 2, 1, 2, 1, 2, 2, 1, 2, 1]),
 (17, [4, 4, 2, 1, 2, 1, 2, 1, 3, 2, 1, 2, 1, 2, 1, 2, 1]),
 (18, [4, 3, 2, 1, 2, 1, 3, 2, 1, 2, 1, 3, 2, 1, 2, 1, 2, 1]),
 (19, [5, 4, 2, 1, 2, 1, 2, 1, 3, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1])
```

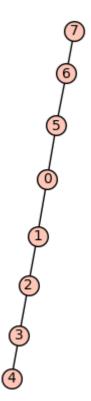
### In [7]:

```
for (vrednost, seznam) in rezultati:
   if len(seznam) > 1:
      for graf in seznam:
        show(graf)
```

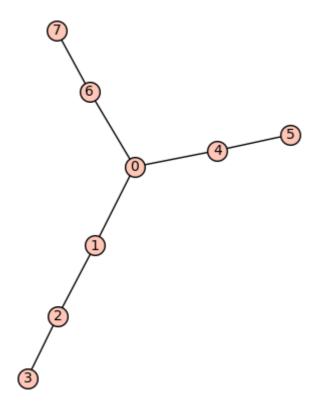


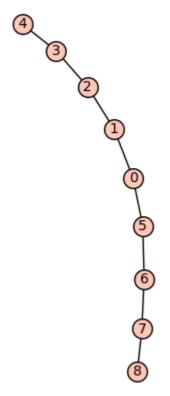
### Out[7]:



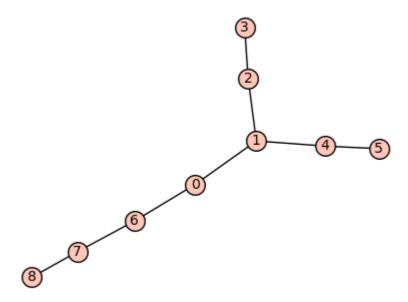


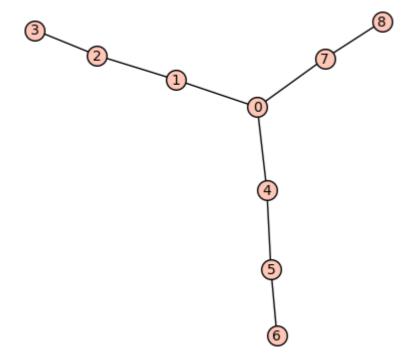
# Out[7]:



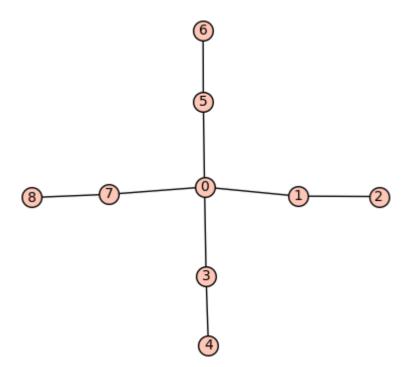


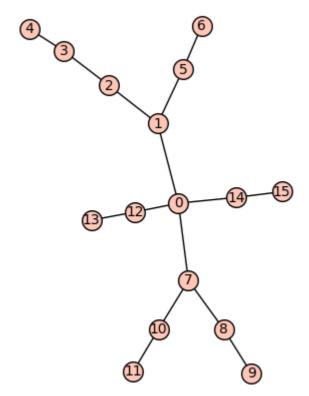
### Out[7]:



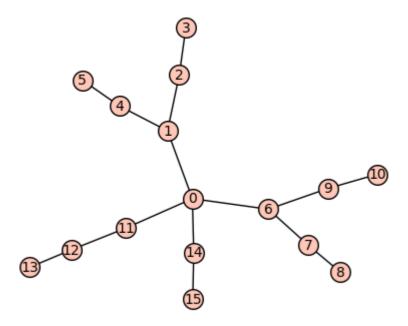


### Out[7]:





### Out[7]:



### In [0]: