

## Math 343 - Lab 3

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a)

The hypothesis for the test is:

$H_0$ :  $\mu_1 = \mu_2 = \mu_3$ .

$H_a$ : At least one  $\mu_i$  is different.

The test statistic  $F = 7.91$ .

The P-value = 0.006.

Since the P-value  $< \alpha = 0.5$  we can conclude the following: There is not enough statistic evidence to support the hypothesis that  $\mu_1 = \mu_2 = \mu_3$ .

b)

An estimate of the overall mean  $\mu$ , is given by the following:

$$\begin{aligned}\hat{\mu} &= \frac{1}{a} \sum_{i=1}^a \hat{\mu}_i \\ &= (13.4 + 38.2 + 73)/4 \\ &= 41.5\bar{3}\end{aligned}$$

An estimate of the variance  $\sigma^2$  of the random error term  $\epsilon_{ij}$  can be pulled from the pooled standard deviation in Minitab:

$$S_p^2 = 23.7978^2 = 566.335$$

c)

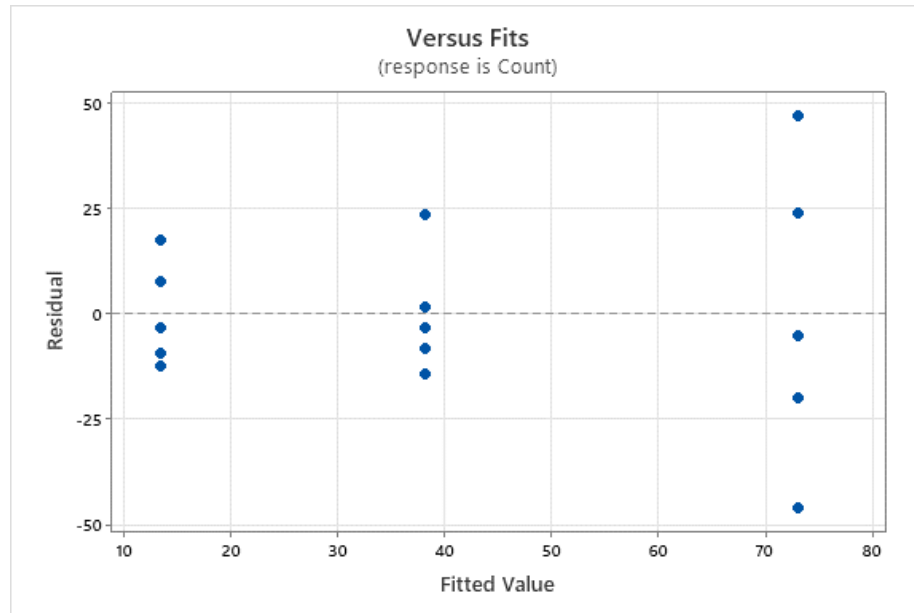


Figure 1: The residual plot from Minitab.

The residual plot seems to indicate heteroskedasticity. The data appears to have a bell like shape where data with a lower fitted value has a smaller residual spread.

d)

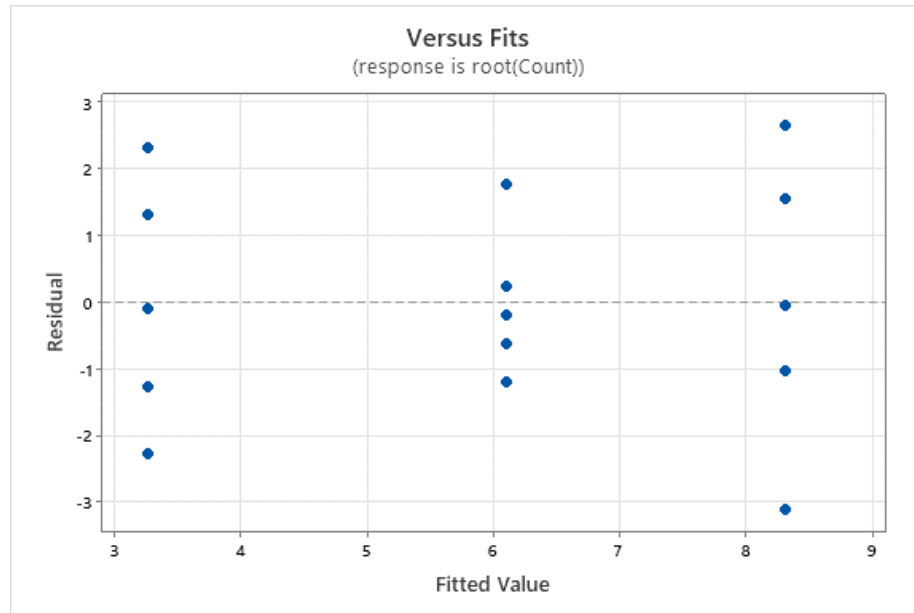


Figure 2: The residual plot from Minitab after a transformation on the response.

It would seem that a transformation of a square root on the response has remedied the heteroskedasticity. However more test should be performed to verify there are no more violations to the model assumptions.

e)

The hypothesis for the normality of the residuals is:

$H_0$ : The data are drawn from a normal distribution.

$H_a$ : The data are not drawn from a normal distribution.

The P-value = 0.801 for the Anderson-Darling normality test. Since this P-value is larger than  $\alpha$ , we can conclude the following.

The evidence from the data is consistent with the data being drawn from a normal distribution.

f)

The hypothesis for the Levene test for equality of population variances at  $\alpha = 0.05$  is:

$$H_0: \sigma_1^2 = \sigma_2^2 = \sigma_3^2$$

$H_a$ : At least one  $\sigma_i^2$  is different.

Since the P-value = 0.372 is greater than  $\alpha = 0.05$ , we can conclude the following. The evidence from the data is consistent with  $\sigma_1^2 = \sigma_2^2 = \sigma_3^2$ , ie, all of the variances are equal.

g)

The hypothesis for the Bartlett's test for equality of three population variances is the same as above. Note that this test makes the strong assumption that the data is distributed normally, and is only accurate if that assumption is met.

i.

Since the P-value = 0.449 is greater than  $\alpha$ , this test results in the same conclusion as above. That is, the evidence from the data is consistent with all of the variances being equal.

ii.

If there were a considerable difference in the results from the 2 tests I would check the following:

1. Check if the data is normal through a hypothesis test.
2. If the data was normal, I would trust the Bartlett's test for the following reasons:
  - This test assumes normality and the data is normally distributed.
  - This test is more powerful than Levene's.
3. If the data was **not** normal, I would trust the Modified Levene's test for the following reasons:
  - This test is robust for normality.

**h)**

The predicted value of the after-treatment particle count for the 1<sup>st</sup> method is  $3.26252^2 = 10.64$ .