

Solve for X^T

$$X^T \Sigma^{-1} (\mu_K - \mu_d) - \frac{1}{2} (\mu_K + \mu_d)^T \Sigma^{-1} (\mu_K - \mu_d) + \log\left(\frac{\pi_K}{\pi_d}\right) = 0$$

$$\pi_K = .5$$

$$\pi_K = \pi_d$$

$$\log(1) = 0$$

$$X^T \Sigma^{-1} (\mu_K - \mu_d) - \frac{1}{2} (\mu_K + \mu_d)^T \Sigma^{-1} (\mu_K - \mu_d) = 0$$

~~Q1~~

$$\Sigma^{-1} = ? \quad \Sigma = \begin{pmatrix} 1.0 & 0 \\ 0 & .5625 \end{pmatrix}^{-1} \cdot \begin{pmatrix} 1 & 0 \\ 0 & .5625 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1.778 \end{pmatrix}$$

$$\mu_K - \mu_d = \begin{pmatrix} 0 \\ 0 \end{pmatrix}_{\mu_d} \begin{pmatrix} 2 \\ -2 \end{pmatrix}_{\mu_K} = \begin{pmatrix} 2 \\ -2 \end{pmatrix}$$

$$\begin{matrix} (2 \times 2) & 2 \times (1) & (2 \times 1)^T & (2 \times 2) \\ X^T \begin{pmatrix} 1 & 0 \\ 0 & 1.778 \end{pmatrix} \begin{pmatrix} 2 \\ -2 \end{pmatrix} - \frac{1}{2} \begin{pmatrix} 2 \\ -2 \end{pmatrix}^T \begin{pmatrix} 1 & 0 \\ 0 & 1.778 \end{pmatrix} \begin{pmatrix} 2 \\ -2 \end{pmatrix} = 0 \end{matrix}$$

$$X^T \begin{pmatrix} 2 \\ -3.556 \end{pmatrix} - \frac{1}{2} \begin{pmatrix} 2 & -3.556 \end{pmatrix} \begin{pmatrix} 2 \\ -2 \end{pmatrix} = 0$$

$1 \times 2 \quad 2 \times 1$

$$X^T \begin{pmatrix} 2 \\ -3.556 \end{pmatrix} - \frac{1}{2} (11.112) = 0$$

$$X^T \begin{pmatrix} 2 \\ -3.556 \end{pmatrix} - 5.556 = 0$$

~~$$X^T \begin{pmatrix} 2 \\ -3.556 \end{pmatrix} - 5.556 = 0$$~~

$$2x_1 - 3.556x_2 - 5.556 = 0$$

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