#### 1 Galant Programmer Documentation

Animation programmers can write algorithms in notation that resembles textbook pseudocode. The animation examples have used procedural syntax for function calls, as in, for example, setWeight(v,0). Java (object oriented) syntax can also be used: v.setWeight(0).

The source code for an algorithm begins with any number (including none) of global variable declarations and function definitions. This is followed by the code for the algorithm itself, starting with the keyword algorithm. A *code block* is a sequence of statements, each terminated by a semicolon, just as in Java. The main algorithm has the form

```
\begin{array}{c} {\rm algorithm} \ \{ \\ code \ block \\ \} \end{array}
```

Declarations of global variables are also like those of Java:

```
type\ variable\_name; or
```

type [] variable\_name;

to declare an array of the given type. All variables must be initialized either within a function definition or in the algorithm. The Java incantation

```
type variable_name = new type[ size ]
```

is used to initialize an array with size elements intialized to null or 0. Arrays use 0-based indexing: the largest index is size - 1. Function declarations are described in more detail in Section 1.2.1 below.

Central to the Galant API is the graph object: currently all other parts of the API refer to it. The components of a graph are declared to be of type Node or Edge and can be accessed/modified via a variety of functions/methods. When an observer or explorer interacts with the animation they move either forward or backward one step at a time. All aspects of the graph API therefore refer to the current state of the graph, the set of states behaving as a stack. API calls that change the state of a node or an edge automatically generate a next step, but the programmer can override this using a beginStep() and endStep() pair. For example, the beginning of our implementation of Dijkstra's algorithm looks like

```
beginStep();
for_nodes(node) {
    setWeight(node, INFINITY);
    nodePQ.add(node);
}
endStep();
```

Without the beginStep/endStep override, this initialization would require the observer to click through multiple steps (one for each node) before getting to the interesting part of the animation.

Functions and macros for the graph as a whole are shown in Table 1, while Table 2 lists some algorithm functions not related to any aspect of a graph.

The nodes and edges, of type Node and Edge, respectively, are subtypes of GraphElement. Arbitrary attributes can be assigned to each graph element. In the GraphML file these show up as, for example,

```
<node attribute_1="value_1" ... attribute_k="value_k" />
```

Each node and edge has a unique integer id. The id's are assigned consecutively as nodes/edges are created and may not be altered. The id of a node or edge can be accessed via the id() function. Often, as is the case with the depth-first search algorithm, it makes sense to use arrays indexed by node or edge id's. Since graphs may be generated externally and/or have undergone deletions of nodes or edges, the id's are not always contiguous. The functions nodeIds() and edgeIds() return the size of an array large enough to accommodate the appropriate id's as indexes. So code such as

```
Integer myArray[] = new Integer[nodeIds()];
```

|   | notions a list of the modes of the growth, type Madalist is built   |
|---|---|
| $List\langleNode angle \; getNodes()$   | returns a list of the nodes of the graph; type NodeList is built  |
| NodeList getNodes()                     | into Galant and essentially equivalent to the Java List(Node); see Table 6  |
| List〈Edge〉edges()                       | returns a list of edges of the graph; return type EdgeList is anal-   |
| EdgeList edges()                        | ogous to NodeList   |
| · ·                                     | equivalent to for ( Node v : nodes() ) { statement; };  |
| for_nodes(v) { statement; }             | the statements are executed for each node v   |
| for_edges(e) { statement; }             | analogous to for_nodes  |
| Integer numberOfNodes()                 | returns the number of nodes   |
| Integer numberOfEdges()                 | returns the number of edges   |
| int id(Node v), int id(Edge e)          | returns the unique identifier of v or e   |
| , | returns the largest node/edge identifier plus one; useful when an   |
| int nodelds(), int edgelds()            | array is to be indexed using node/edge identifiers, since these are   |
| ()                                      | not necessarily contiguous  |
| (51 ) (51 )                             | returns the source/target of edge e, sometimes called the (arrow)   |
| source(Edge e), target(Edge e)          | tail/head or source/destination   |
| Integer degree(Node v)                  |   |
| Integer indegree(Node v)                | the number of edges incident on v, total, incoming and outgoing;  |
| Integer outdegree(Node v)               | if the graph is undirected, the outdegree is the same as the degree   |
| EdgeList edges(Node v)                  | returns a list of v's indicent, incoming or outgoing edges, respec-   |
| EdgeList inEdges(Node v)                | tively; outgoing edges are the same as incident edges if the graph  |
| EdgeList outEdges(Node v)               | is undirected   |
| Node otherEnd(Edge e, Node v)           | returns the node opposite v on edge e; if v is the source otherEnd  |
| Node otherEnd(Node v, Edge e)           | returns the target and vice-versa   |
| NodeList neighbors(Node v)              | returns a list of nodes adjacent to v   |
| for_adjacent(v, e, w) { code block }    | for_adjacent executes the code block for each edge e incident on  |
| for_incoming(v, e, w) { code block }    | v, where $w$ is otherEnd(e, $v$ ); $v$ must already be declared but $e$   |
| for_outgoing(v, e, w) { code block }    | and w are declared by the macro; the other two are analogous for  |
| for_outgoing(v, e, w) { code block }    | incoming and outgoing edges   |
| getStartNode()                          | returns the first node in the list of nodes, typically the one with   |
| •                                       | smallest id; used by algorithms that require a start node   |
| isDirected()                            | returns true if the graph is directed   |
| setDirected(boolean directed)           | makes the graph directed or undirected depending on whether   |
| Set Directed (Boolean arrected)         | directed is true or false, respectively   |
|   | returns a new node and adds it to the list of nodes; the id is the  |
| Node addNode()                          | smallest integer not currently in use as an id; attributes such as  |
| Node addNode(Integer x, Integer y)      | weight, label and position are absent and must be set explicitly  |
|   | by appropriate method calls; the second version sets the position   |
|   | of the node at (x,y)  |
|   | adds an edge from the source to the target (source and target are   |
| addEdge(Node source, Node target)       | interchangeable when graph is undirected); the second variation specifies id's of the nodes to be connected; as in the case of adding |
| addEdge(int sourceld, int targetId)     | a node, the edge is added to the list of edges and its weight and   |
|   | label are absent  |
| deleteNode(Node v)                      | removes node v and its incident edges from the graph  |
| deleteEdge(Edge e)                      | removes edge e from the graph   |
| dolocolugo(Lugo c)                      | 1 como cos cago e ironi uno grapii  |

Table 1: Functions and macros that apply to the structure of a graph.

| print(String s)               | prints s on the console; useful for debugging                        |
|-------------------------------|--|
| display(String s)             | writes the string <b>s</b> at the top of the window                  |
| String getMessage()           | returns the message currently displayed on the message banner        |
| error(String s)               | prints s on the console with a stack trace; also displays s in popup |
|                               | window with an option to view the stack trace; the algorithm         |
|                               | terminates and the user can choose whether to terminate Galant       |
|                               | entirely or continue interacting                                     |
| haginStan() andStan()         | any actions between a beginStep() and an endStep() take place        |
| beginStep(), endStep()        | atomically, i.e., all in a single "step forward" action by the user  |
| N. I N. I. (C                 | pops up a window with the given message and prompts the user         |
|                               | to enter the identifier of a node, which is returned; if no node     |
| Node getNode(String message)  | with that id exists, an error popup is displayed and the user is     |
|                               | prompted again   |
|                               | pops up a window with the given message and prompts the user         |
|                               | to enter the identifiers of two nodes, the endpoints of an edge,     |
| Node setEdse(String masses)   | which is returned; if either id has no corresponding node or the     |
| Node getEdge(String message)  | the two nodes are not connect by an edge (in the right direction     |
|                               | if the graph is directed), an error popup is displayed and the user  |
|                               | is prompted again  |
| Integer integer(String s)     | performs conversion from a string to an integer/double; useful       |
| Double real(String s)         | when parsing labels that represent numbers                           |
| windowWidth(), windowHeight() | current width and height of the window, in case the algorithm        |
|                               | wants to rescale the graph   |

Table 2: Utility functions.

```
for_nodes(v) {
    myArray[id(v)] = ...
}
is increase to exercise the series
```

is immune to array out of bounds errors.

### 1.1 Node and edge methods

Nodes and edges have 'getters' and 'setters' for a variety of attributes, i.e.,  $seta(\langle a's \ type \rangle \ x)$  and

 $\langle a's \text{ type} \rangle$  geta(), where a is the name of an attribute such as Color, Label or Weight. A more convenient way to access these standard attributes omits the prefix get and uses procedural syntax: color(x) is a synomym for x.getColor(), for example. Procedural syntax for the setters is also available: setColor(x,c) is a synonym for x.setColor(c). In the special cases of color and label it is possible to omit the set (since it reads naturally): color(x,c) instead of setColor(x,c).

# 1.1.1 Logical attributes: functions and macros

**Nodes.** From a node's point of view we would like information about the adjacent nodes and incident edges. The relevant *methods* require the use of Java generics, but macros are provided to simplify graph API access. The macros, which have equivalents in GDR, are:

- for\_adjacent(x, e, y) { statements } executes the list of statements for each edge incident on x. The statements can refer to x, or e, the current incident edge, or y, the other endpoint of e. The macro assumes that x has already been declared as Node but e and y are declared automatically.
- for\_outgoing(Node x, Edge e, Node y){ statements } behaves like for\_adjacent except that, when the graph is directed, it iterates only over the

edges whose source is x (it still iterates over all the edges when the graph is undirected).

• for\_incoming(Node x, Edge e, Node y) { statements } behaves like for\_adjacent except that, when the graph is directed, it iterates only over the edges whose sink is x (it still iterates over all the edges when the graph is undirected).

The actual API methods hiding behind these macros are (these are Node methods):

- List<Edge> getIncidentEdges() returns a list of all edges incident to this node, both incoming and outgoing.
- List<Edge> getOutgoingEdges() returns a list of edges directed away from this node (all incident edges if the graph is undirected).
- List<Edge> getIncomingEdges() returns a list of edges directed toward this node (all incident edges if the graph is undirected).
- Node travel(Edge e) returns the other endpoint of e.

The above all use Java syntax, as in v.travel(e). The following are node-related functions with procedural syntax.

- degree(v), indegree(v) and outdegree(v) return the appropriate integers.
- otherEnd(v, e), where v is a node and e is an edge returns node w such that e connects v and w; the programmer can also say otherEnd(e, v) in case she forgets the order of the arguments.
- neighbors(v) returns a list of the nodes adjacent to node v.

Edges. The logical attributes of an edge are its source and target (destination).

- setSourceNode(Node) and Node getSourceNode()
- setDestNode(Node) and Node getDestNode()
- getOtherEndPoint(Node u) returns v where this edge is either uv or vu.

**Graph Elements.** Nodes and edges both have a mechanism for setting (and getting) arbitrary attributes of type Integer, String, and Double. the relevant methods are

setIntegerAttribute(String key,Integer value)

to associate an integer value with a node and

Integer getIntegerAttribute(String key)

to retrieve it. String and Double attributes work the same way as integer attributes. These are useful when an algorithm requires arbitrary information to be associated with nodes and/or edges. The user-defined attributes may differ from one node or edge to the next. For example, some nodes may have a depth attribute while others do not.

#### 1.1.2 Geometric attributes

Currently, the only geometric attributes are the positions of the nodes. Unlike GDR, the edges in Galant are all straight lines and the positions of their labels are fixed. The relevant methods for nodes – using procedural syntax – are int getX(Node), int getY(Node) and Point getPosition(Node) for the 'getters'. To set a position, one should use either setPosition(Node,Point) or setPosition(Node,int,int). Once a node has an established position, it is possible to change

or setPosition(Node,int,int). Once a node has an established position, it is possible to change only one coordinate using setX(Node,int) or setY(Node,int). Object-oriented variants of all of these, e.g., v.setX(100), are also available.

Ordinarily nodes can be moved by the user during algorithm execution and the resulting positions persist after execution terminates. For some algorithms, such as sorting, the algorithm itself needs to move nodes. It is desirable then to keep the user from moving nodes. The declaration movesNodes() at the beginning of an algorithm accomplishes this.

| RED     | = | "#ff0000" |
|---------|---|-----------|
| BLUE    | = | "#00ff00" |
| GREEN   | = | "#0000ff" |
| YELLOW  | = | "#ffff00" |
| MAGENTA | = | "#ff00ff" |
| CYAN    | = | "#00ffff" |
| TEAL    | = | "#009999" |
| VIOLET  | = | "#9900cc" |
| ORANGE  | = | "#ff8000" |
| GRAY    | = | "#808080" |
| BLACK   | = | "#000000" |
| WHITE   | = | "#ffffff" |

Table 3: Predefined color constants.

## 1.1.3 Display attributes

Each node and edge has both a (double) weight and a label. The weight is also a logical attribute in that it is used implicitly as a key for sorting and priority queues. The label is simply text and may be interpreted however the programmer chooses. Aside from the setters and getters: setWeight(double), Double getWeight(), setLabel(String) and String getLabel(), the programmer can also manipulate and test for the absence of weights/labels using clearWeight() and boolean hasWeight(), and the corresponding methods for labels. The procedural variants in this case are setWeight(Node,double), Double weight(Node), label(Node,String), and String label(Node)

Nodes can either be plain, highlighted (selected), marked (visited) or both highlighted and marked. Being highlighted alters the the boundary (color and thickness) of a node (as controlled by the implementation), while being marked affects the fill color. Edges can be plain or selected, with thickness and color modified in the latter case.

The relevant methods are (here Element refers to either a Node or an Edge):

- highlight(Element), unHighlight(Element) and Boolean isHighlighted(Element)
- correspondingly, setSelected(true), setSelected(false), and boolean isSelected()
- mark(Node), unMark(Node) and Boolean isMarked(Node), equivalently Boolean marked(Node).

Although the specific colors for displaying selected nodes or edges are predetermined, the animation implementation can modify the color of a node boundary or an edge, thus allowing for many different kinds of highlighting. The setColor and getColor methods use String arguments using the RGB format #RRGGBB; for example, the string #0000ff is blue. The predefined color constants are listed in Table 3.

Of the attributes listed above, weight, label, color and position can be accessed and modified by the user as well as the program. In all cases, modifications by execution of the animation are ephemeral – the graph returns to its original state after execution.

A summary of functions relevant to node and edge attributes (their procedural versions) is given in Table 4.

# 1.1.4 Global access for individual node/edge attributes and graph attributes

It is sometimes useful to access or manipulate attributes of nodes and edges globally. For example, an algorithm might want to hide node weights entirely because they are not relevant or hide them

<sup>&</sup>lt;sup>1</sup> The *get* is omitted here for more natural syntax.

<sup>&</sup>lt;sup>2</sup> A natural syntax that resembles English. However, setLabel(Node, String) is also allowed.

| id(element)  | returns the unique identifier of the node or edge  |
|--|--|
| source(Edge e), target(Edge e)   | returns the source/target of edge e, sometimes called the  |
|  | (arrow) tail/head or source/destination  |
| mark(Node v), unmark(Node v)   | shades the interior of a node or undoes that   |
| Boolean marked(Node v)   | returns true if the node is marked makes the node or edge highlighted, i.e., thickens the border   |
| <pre>highlight(element), unhighlight(element)</pre>  | or line and makes it red / undoes the highlighting   |
| Boolean highlighted(element)   | returns true if the node or edge is highlighted  |
| <pre>select(element), deselect(element) selected(element)</pre>  | synonyms for highlight, unhighlight and highlighted  |
| Double weight(element) setWeight(element, double weight)   | get/set the weight of the element  |
| showWeight(element), hideWeight(element)   | make the weight of the element visible/invisible, query their  |
| Boolean weightIsVisible(element)   | visibility; weights of the element type have to be globally  |
| Boolean weightIsHidden(element)  | visible – see Table 5 – for showWeight to have an effect   |
| String label(element) label(element, Object obj)   | get/set the label of the element, the Object argument allows<br>an object of any other type to be converted to a (String)<br>label, as long as there is a toString method, which is true<br>of all major classes (you have to be careful, for example, to<br>use Integer instead of int)   |
| <pre>showLabel(element), hideLabel(element) Boolean labelIsVisible(element) Boolean labelIsHidden(element)</pre> | analogous to the corresponding weight functions  |
| hide(element), show(element) Boolean hidden(element) Boolean visible(element)                                    | makes nodes/edges disappear/reappear and tests whether<br>they are visible or hidden; useful when an algorithm (log-<br>ically) deletes objects, but they need to be revealed again<br>upon completion   |
| String color(element) color(element, String c) uncolor(element)  | get/set/remove the color of the border of a node or line representing an edge; colors are encoded as strings of the form "#RRBBGG", the RR, BB and GG being hexadecimal numbers representing the red, blue and green components of the color, respectively; see Table 3 for a list of predefined colors; when an element has no color, the line is thinner and black                 |
| boolean set( <i>element</i> , String key, 〈 <i>type</i> 〉 value)   | sets an arbitrary attribute, key, of the element to have a value of a given type, where the type is one of Integer, Double, Boolean or String; in the special case of Boolean the third argument may be omitted and defaults to true; so set(v,"attr") is equivalent to set(v,"attr",true); returns true if the element already has a value for the given attribute, false otherwise |
| boolean clear(element, String key)   | removes the attribute key from the element; if the key refers<br>to a Boolean attribute, this is logically equivalent to making<br>it false  |
| ⟨type⟩ get⟨type⟩(element, String key) Boolean is(element, String key)  | returns the value associated with key or null if the graph has no value of the given type for key, i.e., if no set(String key, \langle type \rangle value) has occurred; in the special case of a Boolean attribute, the second formulation may be used; the object-oriented syntax, such as e.is("inTree"), sometimes reads more naturally  |

Table 4: Functions that query and manipulate attributes of individual nodes and edges. Here, element refers to either a Node or an Edge, both the type and the formal parameter.

| Boolean nodeLabelsAreVisible() Boolean edgeLabelsAreVisible()                                     | returns true if node/edge labels/weights are globally visible, the  |
|---|---|
| Boolean nodeWeightsAreVisible() Boolean edgeWeightsAreVisible()                                   | default state, which can be altered by hideNodeLabels(), etc., defined below  |
| hideNodeLabels(), hideEdgeLabels() hideNodeWeights(), hideEdgeWeights()                           | hides all node/edge labels/weights; typically used at the beginning of an algorithm to hide unnecessary information; labels and weights are shown by default  |
| showNodeLabels(), showEdgeLabels() showNodeWeights(), showEdgeWeights()                           | undoes the hiding of labels/weights   |
| hideAllNodeLabels() hideAllEdgeLabels() hideAllNodeWeights() hideAllEdgeWeights()                 | hides all node/edge labels/weights even if they are visible globally by default or by showNodeLabels(), etc., or for individual nodes and edges; in order for the label or weight of a node/edge to be displayed, labels/weights must be visible globally and its label/weight must be visible; initially, all labels/weights are visible, both globally and for individual nodes/edges; these functions are used to hide information so that it can be revealed subsequently, one node or edge at a time |
| showAllNodeLabels() showAllEdgeLabels() showAllNodeWeights() showAllEdgeWeights()                 | makes all individual node/edge weights/labels visible if they are globally visible by default or via showNodeLabels(), etc.; this undoes the effect of hideAllNodeLabels(), etc., and of any individual hiding of labels/weights  |
| clearNodeLabels(), clearEdgeLabels() clearNodeWeights(), clearEdgeWeights()                       | gets rid of all node/edge labels/weights; this not only makes<br>them invisible, but also erases whatever values they have  |
| showNodes(), showEdges()  | undo any hiding of nodes/edges that has taken place during the algorithm  |
| clearNodeMarks() clearNodeHighlighting() clearEdgeHighlighting()                                  | unmarks all nodes, unhighlights all nodes/edges, respectively   |
| clearNodeLabels() clearNodeWeights() clearEdgeLabels() clearEdgeWeights()                         | erases labels/weights of all nodes/edges; useful if an algorithm needs to start with a clean slate with respect to any of these attributes  |
| clearAllNode(String attribute) clearAllEdge(String attribute)                                     | erases values of the given attribute from all nodes/edges, a generalization of clearNodeLabels, etc.  |
| boolean set(String attribute, $\langle type \rangle$ value)                                       | sets an arbitrary attribute of the graph to have a value of a given type, where the type is one of Integer, Double, Boolean or String; in the special case of Boolean the second argument may be omitted and defaults to true; so set("attr") is equivalent to set("attr",true); returns true if the graph already has a value for the given attribute, false otherwise   |
| $\langle type \rangle$ get $\langle type \rangle$ (String attribute) Boolean is(String attribute) | returns the value associated with attribute or null if the graph has no value of the given type for attribute, i.e., if no set(String attribute, \langle type \rangle value) has occurred; in the special case of a Boolean attribute, the second formulation may be used   |
| clearAllNode(String attribute) clearAllEdge(String attribute)                                     | erases the value of the given attribute for all nodes/edges   |

Table 5: Functions that query and manipulate graph node and edge attributes globally, i.e., for all nodes or edges at once. Also included are functions that deal with graph attributes.

initially and reveal them for individual nodes as the algorithm progresses. These functionalities can be accomplished by hideNodeWeights or hideAllNodeWeights, respectively. A summary of these capabilities is given in Table 5.

## 1.2 Additional programmer information

A Galant algorithm/program is executed as a method within a Java class. In order to shield the Galant programmer from Java ideosyncrasies, some features have been added.

### 1.2.1 Definition of Functions/Methods

```
A programmer can define arbitrary functions (methods) using the construct

function [return_type] name ( parameters ) {
      code block
}

The behavior is like that of a Java method. So, for example,

function int plus( int a, int b ) {
    return a + b;
}

is equivalent to

static int plus( int a, int b ) {
    return a + b;
}
```

The return\_type is optional. If it is missing, the function behaves like a void method in Java. An example is the recursive

```
function visit( Node v ) \{ code \}
```

The conversion of functions into Java methods when Galant code is compiled is complex and may result in indecipherable error messages.

### 1.2.2 Data Structures

Galant provides some standard data strutures for nodes and edges automatically. These are described in detail in Table 6.

## NodeList and EdgeList: lists of nodes or edges, respectively.

| Node first(NodeList L) Edge first(EdgeList L) | returns the first element of this list   |
|---|--|
| add(Node v, NodeList L)                       | adds the node/edge to the end of the list L; along with first we   |
| add(Edge e, EdgeList L)                       | get the effect of a queue  |
| remove(Node v, NodeList L)                    | removes the first occurrence of node v or edge e from L  |
| remove(Edge e, EdgeList L)                    | removes the first occurrence of node v or edge e from L  |
| sort(NodeList L), sort(EdgeList L)            | use the weights of the nodes/edges to sort the list $L$ ; sort is actually a macro that invokes Java Collections.sort( $L$ ); this means that $L$ can be any collection (list, stack, queue, set) of comparable elements |

### NodeQueue and EdgeQueue: queues of nodes or edges, respectively.

| void enqueue(Node v), void enqueue(Edge e) | adds v or e to the rear of the queue                            |
|--|---|
| Node dequeue(), Edge dequeue()             | returns and removes the Node or Edge at the front of the queue; |
|  | returns null if the queue is empty                              |
| Node remove(), Edge remove()               | returns and removes the Node or Edge at the front of the queue; |
|  | throws an exception if the queue is empty                       |
| Node element(), Edge element()             | returns the Node or Edge at the front of the queue without re-  |
|  | moving it; throws an exception if the queue is empty            |
| Node peek(), Edge peek()                   | returns the Node or Edge at the front of the queue without re-  |
|  | moving it; returns null if the queue is empty                   |
| size()                                     | returns the number of elements in the queue                     |
| isEmpty()                                  | returns true if the queue is empty                              |

# NodeStack and EdgeStack: stacks of nodes or edges, respectively.

| void push(Node v), void push(Edge e) | adds $v$ or $e$ to the top of the stack  |
|--------------------------------------|--|
| Node pop(), Edge pop()               | returns and removes the Node or Edge at the top of the stack; throws an exception if the stack is empty  |
| Node peek(), Edge peek()             | returns the Node or Edge at the top of the stack without removing it; returns null if the stack is empty |
| size(), isEmpty()                    | analogous to the corresponding queue methods   |

## NodePriorityQueue and EdgePriorityQueue: priority queues of nodes or edges, respectively.

| · 1 1/N1 1 \                          |  |
|---------------------------------------|--|
| void add(Node v),                     | adds v or e to the priority queue; the priority is defined to be its   |
| void add(Edge e)                      | weight – see Section 1.1.3   |
| Node removeMin(), Edge removeMin()    | returns and removes the Node or Edge with minimum weight;              |
|                                       | returns null if the queue is empty                                     |
| boolean remove(Node v),               |  |
| boolean remove(Edge e)                | removes v or e; returns true if the v or e is present, false otherwise |
|                                       | changes the weight of v or e to the new key and reorganizes            |
| void decreaseKey(Node v, double key), | the priority queue appropriately; since this is accomplished by        |
| void decreaseKay(Edge e, double key)  | removing and reinserting the object, i.e., inefficiently, this method  |
|                                       | can also be used to increase the key                                   |
| size(), isEmpty()                     | analogous to the corresponding queue methods                           |

Table 6: Built-in data structures and their methods. These methods use object-oriented syntax:  $\langle structure \rangle.\langle method \rangle (\langle arguments \rangle)$  and are created using, e.g., NodeQueue Q = new NodeQueue(); the new operator in Java.