Introduction to Information Retrieval (Chapter 5 Index compression)

There are three benefits for index compression:

- Disk space can be reduced considerably. Compression ratios of 1:4 are easy to achieve, potentially cutting the cost of storing the index by 75%.
- The response time of the IR system substantially. Because compared to expend a disk seek, compression can fit a lot more information into the main memory. The posting list can be decompressed, and the query can be entirely done in memory. Since the use of caching is increased, the response time of the IR system can be decreased substantially.
- Faster transfer of data from disk to memory. Efficient decompression algorithms run so fast on modern hardware that the
 total time of transferring a compressed chunk of data from disk and then decompressing it is usually less than transferring
 the same chunk of data in uncompressed form.

1. Statistical properties of terms in information retrieval

In general, the statistics in Table 5.1 show that preprocessing affects the size of the dictionary and the number of nonpositional postings significantly.

Table 5.1 The effect of preprocessing on the number of terms, nonpositional postings, and tokens for Reuters-RCV1. " Δ %" indicates the reduction in size from the previous line, except that "30 stop words" and "150 stop words" both use "case folding" as their reference line. "T%" is the cumulative ("total") reduction from unfiltered. We performed stemming with the Porter stemmer (Chapter 2, page 31).

	(distinct) terms			nonpositional postings			tokens (= number of position entries in postings)			
	number	$\Delta\%$	Ť%	number	$\Delta\%$	T%	number	$\Delta\%$	T%	
unfiltered	484,494			109,971,179			197,879,290			
no numbers	473,723	-2	-2	100,680,242	-8	-8	179,158,204	-9	-9	
case folding	391,523	-17	-19	96,969,056	-3	-12	179,158,204	-0	-9	
30 stop words	391,493	-0	-19	83,390,443	-14	-24	121,857,825	-31	-38	
150 stop words	391,373	-0	-19	67,001,847	-30	-39	94,516,599	-47	-52	
stemming	322,383	-17	-33	63,812,300	-4	-42	94,516,599	-0	-52	

Assuming one machine word per posting, what is the size of the uncompressed (nonpositional) index for different tokenizations based on Table 5.1?

According to the assumption - one machine word per posting - and table 4.2, the avg size of per posting is 4.5bytes. Thus, the size of unfiltered is $109,971,179\times4.5\approx495MB$, the size of no numbers is $495-495\times0.08\approx455MB$, the size of case folding is $495-495\times0.12\approx436MB$, the size of 30 stop words is $495-495\times0.24\approx376MB$, the size of 150 stop words is $495-495\times0.39\approx302MB$, the size of stemming is $495-495\times0.42\approx287MB$.

1.1 Heaps' law: Estimating the number of terms

Heaps' law, which is an effective method for getting a handle on vocabulary size, estimates vocabulary size as a function of collection size.

$$M = kT^b (1)$$

where T is the number of tokens in the collection, and M is the vocabulary size. Typical values for the parameters k and b are: $30 \le k \le 100$ and $b \approx 0.5$. For instance, for the 1000020 tokens, Heaps' law predicts $44 \times 1000020^{0.49} \approx 38323$ terms.

Overall, the parameter k is quite variable because vocabulary growth depends a lot on the nature of the collection and how it is processed. Case-folding and stemming reduce the growth rate of the vocabulary, whereas including numbers and spelling errors increases it. From the Heaps' law, we could draw two conclusions:

- The dictionary size continues to increase with more documents in the collection, rather than a maximum vocabulary size being reached.
- The size of the dictionary is quite large for large collections.

1.2 Zipf's law: Modeling the distribution of terms

Zipf's law: A commonly used model of the distribution of terms in a collection. Zipf's told us the collection frequency cf_i of the i th most common term is proportional to 1/i:

$$cf_i \propto \frac{1}{i}$$
 (2)

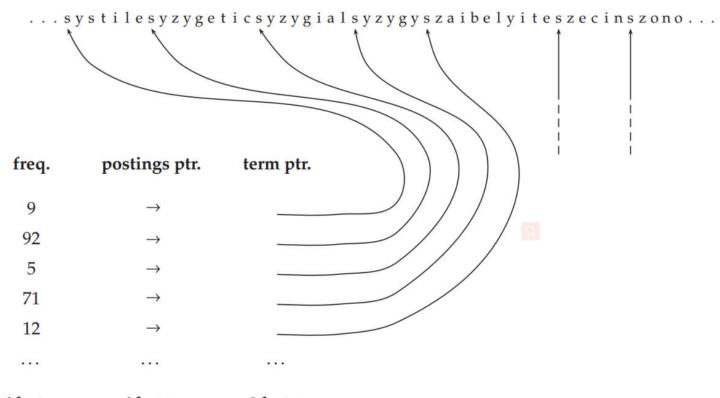
So if the most frequent term occurs cf_1 times, then the second most frequent term has half as many occurrences, the third most frequent term a third as many occurrences, and so on.

2 Dictionary compression

2.1 Dictionary as a string

There is some data structure for the dictionary store:

- An array of fixed-width entries. Allocate 20 bytes for the term itself, 4 bytes for its document frequency, and 4 bytes for the pointer to its postings list. Thus, for Reuters-RCV1, we need $M \times (20+4+4) = 400,000 \times 28 = 11.2$ megabytes (MB) for storing the dictionary in this scheme.
- Dictionary-as-a-string storage. As for fixed-width entries, the average length of a term in English is about eight characters, so on average, we are wasting twelve characters in the fixed-width scheme. In addition, the character length is more than twelve in few words. To overcome those shortcomings of fixed-width, we could sort the dictionary terms as one long string of characters and apply term pointers to locate terms, as shown in Figure 5.4.



4 bytes 4 bytes 3 bytes

Figure 5.4 Dictionary-as-a-string storage. Pointers mark the end of the preceding term and the beginning of the next. For example, the first three terms in this example are systile, syzygetic, and syzygial.

Because the average length of a term in English is about eight characters and the number of terms for Reuters-RCV1 is 400000, the term pointers resolve $400000 \times 8 = 3.2 \times 10^6$ positions. So the term pointers need to be $log_2 3.2 \times 106 \approx 22$ bits or 3 bytes long.

For dictionary-as-a-string storage, we need $400000 \times (4+4+3+8) = 7.6$ MB for the Reuters-RCV1 dictionary: 4 bytes each for frequency and postings pointer, 3 bytes for the term pointer, and 8 bytes on average for the term. Compared to fixed-width (11.2MB), one-third space is saved.

• Blocked storage. Based on Dictionary-as-a-string, We can further compress the dictionary by grouping terms in the string into blocks of size k and keeping a term pointer only for the first term of each block (Figure 5.5). In this scheme, the length of each term is needed for encoding, and some term pointers can be eliminated (Figure 5.5).

...7 systile 9 syzygetic 8 syzygial 6 syzygy11 szaibelyite 6 szecin...

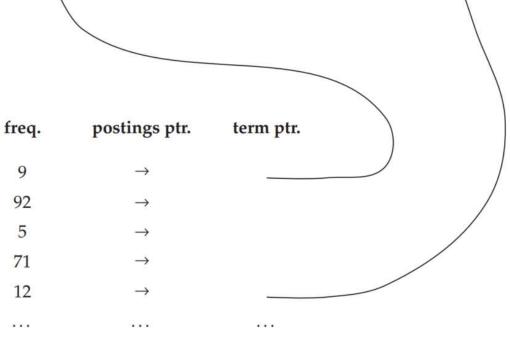


Figure 5.5 Blocked storage with four terms per block. The first block consists of systile, syzygetic, syzygial, and syzygy with lengths of seven, nine, eight, and six characters, respectively. Each term is preceded by a byte encoding its length that indicates how many bytes to skip to reach subsequent terms.

In Figure 5.5, the number 7, 9, 8, 11, 6 is the length of the character in this block.

By increasing the block size k, we get better compression. However, there is a tradeoff between compression and the speed of term lookup. Because, in the block inner, the binary search can not be supported.

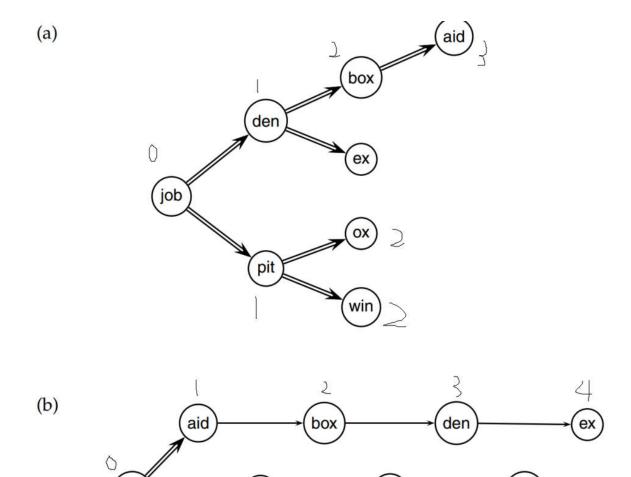


Figure 5.6 Search of the uncompressed dictionary (a) and a dictionary compressed by blocking with k = 4 (b).

As shown in Figure 5.6, for the uncompressed dictionary, the binary search can be applied. Thus, for the eight-term dictionary, the average steps are $(0+1+2+3+2+1+2+2)/8 \approx 1.6$. For a dictionary compressed by blocking with k=4, the average step is (0+1+2+3+4+1+2+3)/8=2.

RCV1 dictionary compression summary:

Technique	Size (MB)
Fixed width	11.2
Dictionary-as-String with pointers to every term	7.6
+ blocking, k = 4	7.2
+ blocking + front coding	5.9

3. Postings file compression

Reuters-RCV1 has 800000 documents, 200 tokens per document, six characters per token, and 100000000 postings. Thus, the size of the collection is about $800,000\times200\times6bytes=960MB$. Document identifiers are $log_2800000\approx20bits=20/8bytes$. The size of the uncompressed postings file is $1000000000\times20/8=250MB$.

In order to decrease the required bits per document representation, the gap can be applied (shown in Table 5.3).

Table 5.3 Encoding gaps instead of document IDs. For example, we store gaps 107, 5, 43, ..., instead of docIDs 283154, 283159, 283202, ... for computer. The first docID is left unchanged (only shown for arachnocentric).

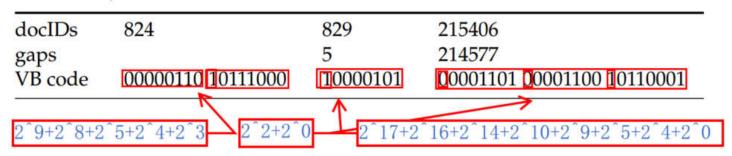
	encoding	postings	s list								
the	docIDs gaps			283042	1	283043	1	283044	1	283045	•••
computer	docIDs gaps	•••		283047	107	283154	5	283159	43	283202	
arachnocentric	docIDs gaps	252000 252000	248100	500100							

As we can see, the gaps between postings are short, requiring a lot less space than 20 bits to store.

3.1 Variable byte codes

To encode small numbers in less space than large numbers, Variable byte (VB) encoding was proposed. VB encoding uses an integral number of bytes to encode a gap. In VB encoding, the first bit of the byte is a continuation bit. It is set to 1 for the last byte of the encoded gap and to 0 otherwise (Table 5.4).

Table 5.4 VB encoding. Gaps are encoded using an integral number of bytes. The first bit, the continuation bit, of each byte indicates whether the code ends with this byte (1) or not (0).



For VB encoding, 1 byte can represent the integer from 0 to 2^7 , 2 bytes can represent the integer from 2^7 to 2^{14} , and so on.

To decode a variable byte code, we read a sequence of bytes with continuation bit 0 terminated by a byte with continuation bit 1 (include this byte). By setting the continuation bit (the boundary of encodings), we could parse the number from a sequence.

The VB encoding and decoding algorithm are illustrated below.

```
VBEncodeNumber(n)
1 bytes \leftarrow ()
2 while true
3 do Prepend(bytes, n mod 128)
4
        if n < 128
5
          then BREAK
6
        n \leftarrow n \text{ div } 128
   bytes[Length(bytes)] += 128
    return bytes
VBENCODE(numbers)
   bytestream \leftarrow \langle \rangle
2 for each n \in numbers
3 do bytes \leftarrow VBENCODENUMBER(n)
        bytestream \leftarrow Extend(bytestream, bytes)
4
5
   return bytestream
VBDecode(bytestream)
1 numbers \leftarrow \langle \rangle
2 \quad n \leftarrow 0
3 for i \leftarrow 1 to Length(bytestream)
4
   do if bytestream[i] < 128
          then n \leftarrow 128 \times n + bytestream[i]
5
          else n \leftarrow 128 \times n + (bytestream[i] - 128)
6
7
                 Append(numbers, n)
8
                n \leftarrow 0
    return numbers
```

Figure 5.8 VB encoding and decoding. The functions div and mod compute integer division and remainder after integer division, respectively. Prepend adds an element to the beginning of a list, for example, Prepend $(\langle 1, 2 \rangle, \langle 3, 4 \rangle) = \langle 1, 2, 3, 4 \rangle$. Extend extends a list, for example, Extend $(\langle 1, 2 \rangle, \langle 3, 4 \rangle) = \langle 1, 2, 3, 4 \rangle$.

γ Codes

 γ code = <length code, offset code>

Table 5.5 Some examples of unary and γ codes. Unary codes are only shown for the smaller numbers. Commas in γ codes are for readability only and are not part of the actual codes.

number	unary code	length	offset	γ code
0	0			
1	10	0		0
2	110	10	0	10,0
3	1110	10	1	10,1
4	11110	110	00	110,00
9	1111111110	1110	001	1110,001
13		1110	101	1110,101
24		11110	1000	11110,1000
511		111111110	11111111	111111110,11111111
1025		11111111110	0000000001	11111111110,00000000001

- unary code: Represent n as n 1s with a final 0. For example, 3 = 1110, 4 = 11110, 5 = 111110;
- offset: is a natural number in binary, but with the leading 1 removed. For example, 2=0, (10 is the real binary but leading 1 is removed), 3=1, (11 is the real binary but leading 1 is removed), 4=00, (100 is the real binary but leading 1 is removed);
- length: encodes the length of offset in unary code. For example, if the offset is 0 or 1, the length of offset is 1, the unary code of 1 is 10. If offset is 00, the length of offset is 2, the unary code of 1 is 110;
- γ code: the combination of length and offset.

Via the offset code, we could determine the docID, and via the length, we could determine the boundary of each γ code. The length of offset is $\lfloor log_2G \rfloor$ bits and the length of length is $\lfloor log_2G \rfloor + 1$ bits, so the length of the entire code is $2 \times \lfloor log_2G \rfloor + 1$ bits.

The compression ratio for the index in Table 5.6 is about 25%: 400 MB (uncompressed, each posting stored as a 32-bit word) versus 101 MB (γ) and 116 MB (VB).

Table 5.6 Index and dictionary compression for Reuters-RCV1. The compression ratio depends on the proportion of actual text in the collection. Reuters-RCV1 contains a large amount of XML markup. Using the two best compression schemes, γ encoding and blocking with front coding, the ratio compressed index to collection size is therefore especially small for Reuters-RCV1: $(101 + 5.9)/3600 \approx 0.03$.

data structure	size in MB		
dictionary, fixed-width	11.2		
dictionary, term pointers into string	7.6		
\sim , with blocking, $k=4$	7.1		
\sim , with blocking & front coding	5.9		
collection (text, xml markup etc)	3600.0		
collection (text)	960.0		
term incidence matrix	40,000.0		
postings, uncompressed (32-bit words)	400.0		
postings, uncompressed (20 bits)	250.0		
postings, variable byte encoded	116.0		
postings, γ encoded	101.0		

 $[\]gamma$ Codes achieve great compression ratios – about 15% better than variable byte codes for Reuters-RCV1. But they are expensive to decode.

Summary

- Compression ratios of 1:4 are easy to achieve, potentially cutting the cost of storing the index by 75%.
- If the main goal of compression is to conserve disk space, then the speed of compression algorithms is of no concern. But for improved cache utilization and faster disk-to-memory transfer, decompression speeds must be high.
- Heaps' law estimates vocabulary size as a function of collection size. $M=kT^b$, where T is the number of tokens in the collection, and M is the vocabulary size.
- Zipf's law: A commonly used model of the distribution of terms in a collection. $cf_i \propto \frac{1}{i}$.
- For most IR systems, variable byte codes offer an excellent tradeoff between time and space.
- Variable byte codes process queries two times faster than either bit-level compressed indexes or uncompressed indexes with a 30% penalty in compression ratio compared with the best bit-level compression method (Scholer et al. 2002).
- Compressed indexes can be superior to uncompressed indexes not only in disk usage but also in query processing speed (Scholer et al. 2002).
- Compared with VB codes, "variable nibble" codes showed 5% to 10% better compression and up to one-third worse effectiveness in one experiment (Anh and Moffat 2005).
- Trotman (2003) also recommends using VB codes unless disk space is at a premium.
- Zhang et al. (2007) investigate the increased effectiveness of caching when a number of different compression techniques
 for postings lists are used on modern hardware.
- δ codes and γ codes were introduced by Elias (1975), who proved that both codes are universal.

- δ codes perform better than γ codes if large numbers (greater than 15) dominate.
- Using parameterized codes for index compression, codes that explicitly model the probability distribution of gaps for each term. For example, they show that Golomb codes achieve better compression ratios than γ codes for large collections (Witten et al., 1999).
- The distribution of gaps in a postings list depends on the assignment of docIDs to documents.
- Assigning docIDs in a small range to documents in a cluster where a cluster can consist of all documents in a given time
 period, on a particular website, or sharing another property. As a result, when a sequence of documents from a cluster
 occurs in a postings list, their gaps are small and can be more effectively compressed.
- Document compression can also be important in an efficient information retrieval system.