

Write short note on time complexity & space complexity.

i] Time Complexity:-

- Time complexity is the computational complexity describing the amount of time required for the execution of an algorithm.
- Time complexity measures the time taken by every statement of the algorithm.
- Hence it highly depends on the size of processed data.
- It helps to define the effectiveness of an algorithm and to evaluate its performance.
- It takes as notation the mathematical symbols O , Ω , Θ .
- There are different types of time complexity depends on time spent by each algorithm till it reaches the end of its execution. therefore it depends on statements in a program.

ii] Space complexity:-

- When an algorithm is executed on a computer it necessarily requires a specific amount of memory space.
- Space complexity represents the amount of memory one program uses in order to achieve its execution.
- Because a program needs memory to store input data and temporal values while being executed.
- It also helps to evaluate a solution.
- It's represented using same notations as time complexity.

- Similar to time complexity, there are different types of space complexity, depends on the memory consumed by each algorithm.

2] Explain recursive functions with an example.

- = 1] A function which calls itself directly or indirectly again and again until some specified condition is satisfied is known as Recursive function.
- 2] It repeatedly invokes the mechanism, the consequently increases the overhead of function calls.
- 3] This repetition can be expensive in terms of both processor time and memory space.

example.

program to find factorial of a given number recursively

```
#include <iostream.h>
#include <conio.h>
int fact(int n);
void main()
{
    int num, result;
    clrscr();
    cout << "Enter number";
    cin >> num;
    result = fact(num);
    cout << "factorial is " << result;
    getch();
}
```

```

int fact(int n)
{
    int f=1;
    if (n <= 0)
    {
        return 1;
    }
    else
    {
        f = n * fact(n-1);
        return f;
    }
}

```

3] Distinguish between Merge sort and Quick sort.

Merge sort	Quick sort
1] The array is split into two sub-arrays ($n/2$) where 'n' is the number of elements in the array	1] The array is split into a specific number of parts in a specific ratio.
2] It is based on divide and conquer strategy	2] It is based on divide and conquer strategy.
3] Merge sort is considered as an external sorting algorithm	3] It is also known as partition exchange sort. consider as an internal sorting algorithm.
	4] It is

Merge Sort

- 4] It's worst case complexity is $O(n \log n)$, where 'n' is number of element
- 5] It works with any size of the array, be it small or large.
- 6] It is considered to be a stable sorting algorithm.
- 7] It requires ~~less~~ additional space / memory
- 8] It uses three arrays, where two of them store two halves of the array and the third array store the final sorted list

Quick sort.

- 4] It's worst case complexity is $O(n^2)$.
- 5] It works well with large number of elements in an array.
- 6] It is not considered a stable sorting method
- 7] It uses ^{less} additional space / memory.
- 8] It uses a key element to sort elements.

4] Explain Recursive Binary Search algorithm with suitable examples.

- 1] Compare x with the middle element.
- 2] If x matches with the middle element, return the mid index
- 3] Else if x is greater than the mid element, then x can only lie in the right half subarray after the mid element.

So we recur for the right half.
4] Else (x is smaller) recur for the left half.

Algo

binarySearch(arr, x, low, high)

if low > high
return false;

else

mid := (low + high) / 2;

if x == arr[mid]
return mid;

else if x > arr[mid]

return binarySearch(arr, x, mid + 1, high);

else

return binarySearch(arr, x, low, mid - 1);

5] Explain Merge sort and trace this algorithm
for n = 8 elements: 29, 12, 35, 23, 45, 34, 20, 48.

6] What is heap and write a algorithm of Heap sort.

= Heap:- In computer science, a heap is a specialized tree based data structure which is essentially an almost complete tree that satisfies the heap property.

Algorithm

Insert (a, n)

{

$i := n;$

$item := a[n];$

 while $((i > 1) \text{ and } (a[\lfloor i/2 \rfloor] < item))$ do

 {

$a[i] := a[\lfloor i/2 \rfloor];$

 }

$a[i] := item;$

 return true;

}

7] What is heap and write a algorithm of Heap sort using adjust and heapify

= A heap is a complete binary tree, and the binary tree is a tree in which the node can have utmost two children.

9) Define union, find and write an algorithm of collapsing find algorithm

i) Union:- Join two subsets into a single subset. Here first check if the two subsets belong to same set. If no, then we cannot perform union.

ii) Find:- Determine which subset a particular element is in. This can be used for determining if two elements are in the same subset.

Algorithm:-

collapsingFind(element, set)

```
{
    temp := element;
    while set[element] >= 0 do
    {
        element := set[element];
    }
    while element != temp do
    {
        j = set[element];
        set[element] := temp;
        element = j;
    }
    return temp;
}
```


10] Write an algorithm of recursive MaxMin

Algorithm

```
maxmin(max1, min2)
```

```
{
```

```
    if (i == j)
```

```
        max1 = min1 = num[i];
```

```
    elseif (i == j - 1)
```

```
    {
```

```
        if (num[i] < num[j])
```

```
        {
```

```
            max1 = num[j];
```

```
            min1 = num[i];
```

```
        }
```

```
    else
```

```
    {
```

```
        max1 = num[i];
```

```
        min1 = num[j];
```

```
    }
```

```
}
```