

Project presentation

GROUP 10

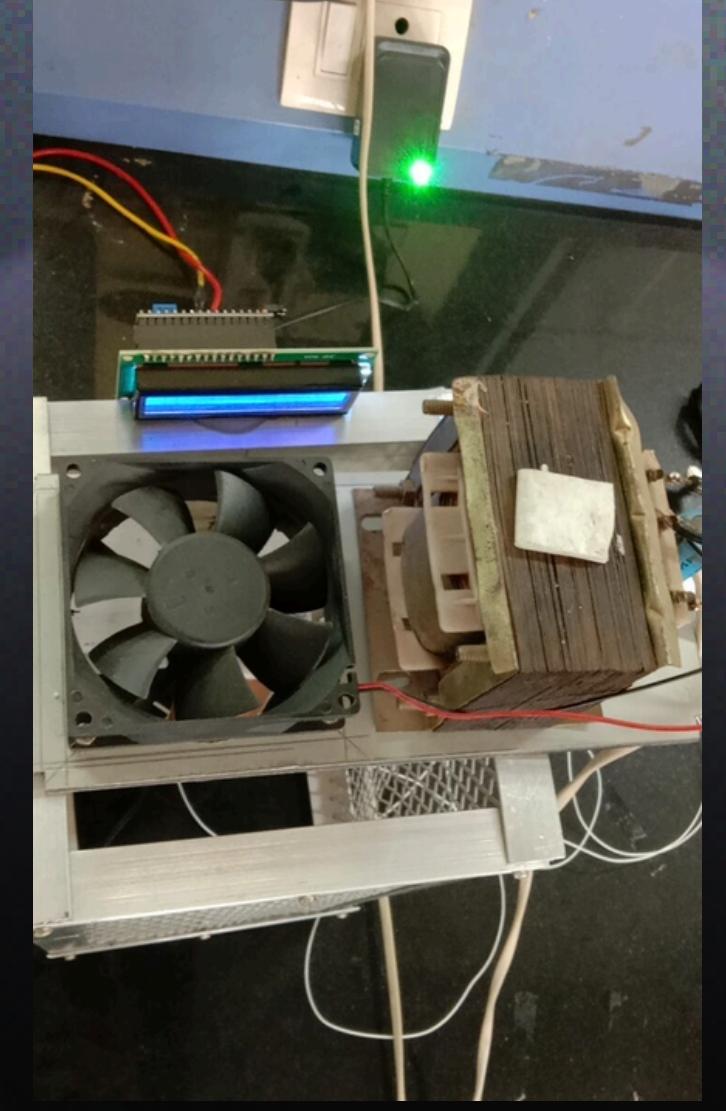
GROUP MEMBERS

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- INTRODUCTION OF THE PROBLEM

Title - Understanding Convection: Natural vs Mixed Cooling

Objective - Compare experimental and theoretical heat transfer coefficients h for natural convection and mixed convection (where forced convection opposes natural convection).



Experimental setup

- **Components:**
 - **Vertical hollow copper rod (OD: 39.86 mm, ID: 34.26 mm, length: 200 mm).**
 - **Internal heater + 3 temperature sensors (T₂, T₃, T₄) along the rod.**
 - **Ambient sensor (T₁) + Data acquisition system.**
 - **Fan for forced convection.**

• INNOVATIVE ASPECTS

- Combines experimental data processing with theoretical correlations (e.g., Churchill–Bernstein) to cross-validate convective heat transfer coefficients.
- Enables a deep comparison between lumped capacitance model results and external flow correlation predictions, showing the limitations of theoretical models under real conditions.
- Cooling phase studied for comprehensive understanding of transient and steady-state convection.
- Simulates real-world applications (e.g., vertical hollow pipes in heat exchangers or chimneys).

- # Methodology:

Steps

1. Heat the rod to a steady-state temperature.
2. Set Voltage=42V and current=0.26 A
3. Cool under natural convection (no fan) and record $T(t)$.
4. Repeat cooling under mixed convection (with fan). In this scenario forced convection is acting opposite to natural convection
5. Average sensor temperatures ($T_{avg}=T_2+T_3+T_4/3$).
6. Use laptop to keep data of temperature with time

- Theory:-
Theoretical Background

- Lumped Capacitance Validity :
 - $Bi = hLc / K < 0.1$ (validated for copper rod)

- Key Formulas :
 - $Ra = Gr \cdot Pr$, $Re = \rho VD / \mu$

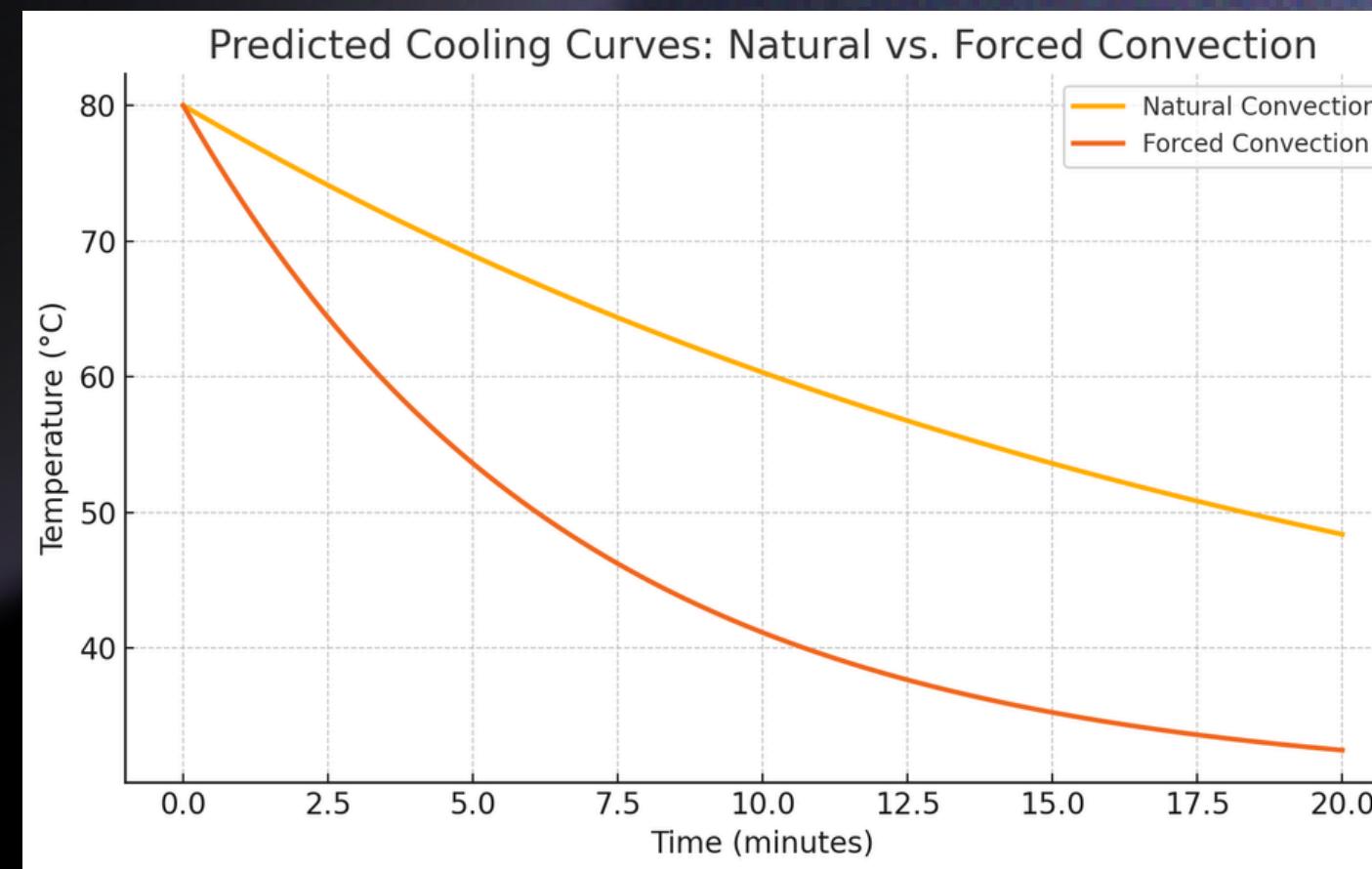
Churchill–Bernstein Correlation

$$Nu_D = 0.3 + \frac{0.62 Re_D^{1/2} Pr^{1/3}}{[1 + (0.4/Pr)^{2/3}]^{1/4}} \cdot \left[1 + \left(\frac{Re_D}{282000} \right)^{5/8} \right]^{4/5}$$

- Results:-

- Expected Results

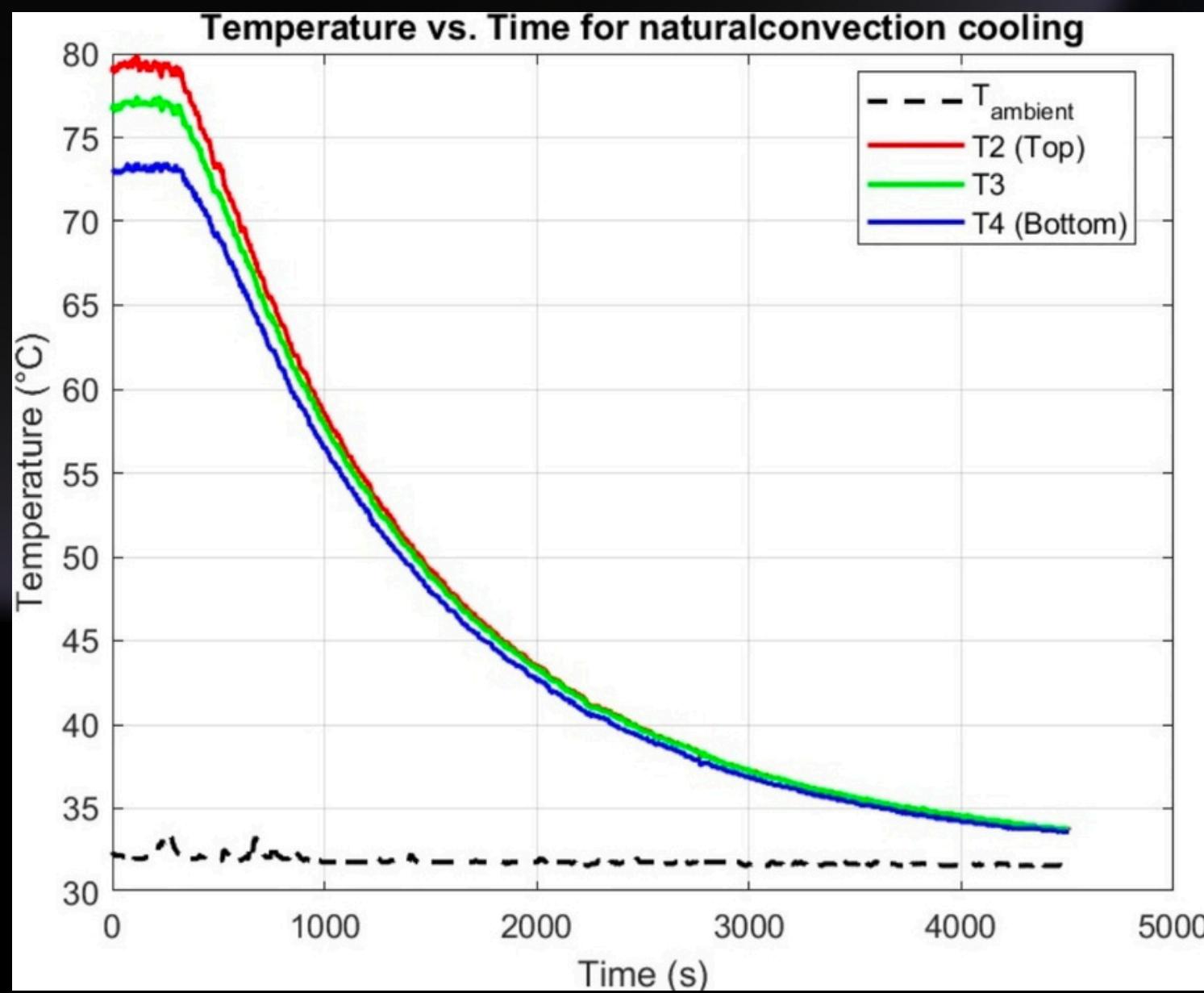
- **Simulation Graph:** Predicted $T(t)$ curves for natural vs. Forced convection.



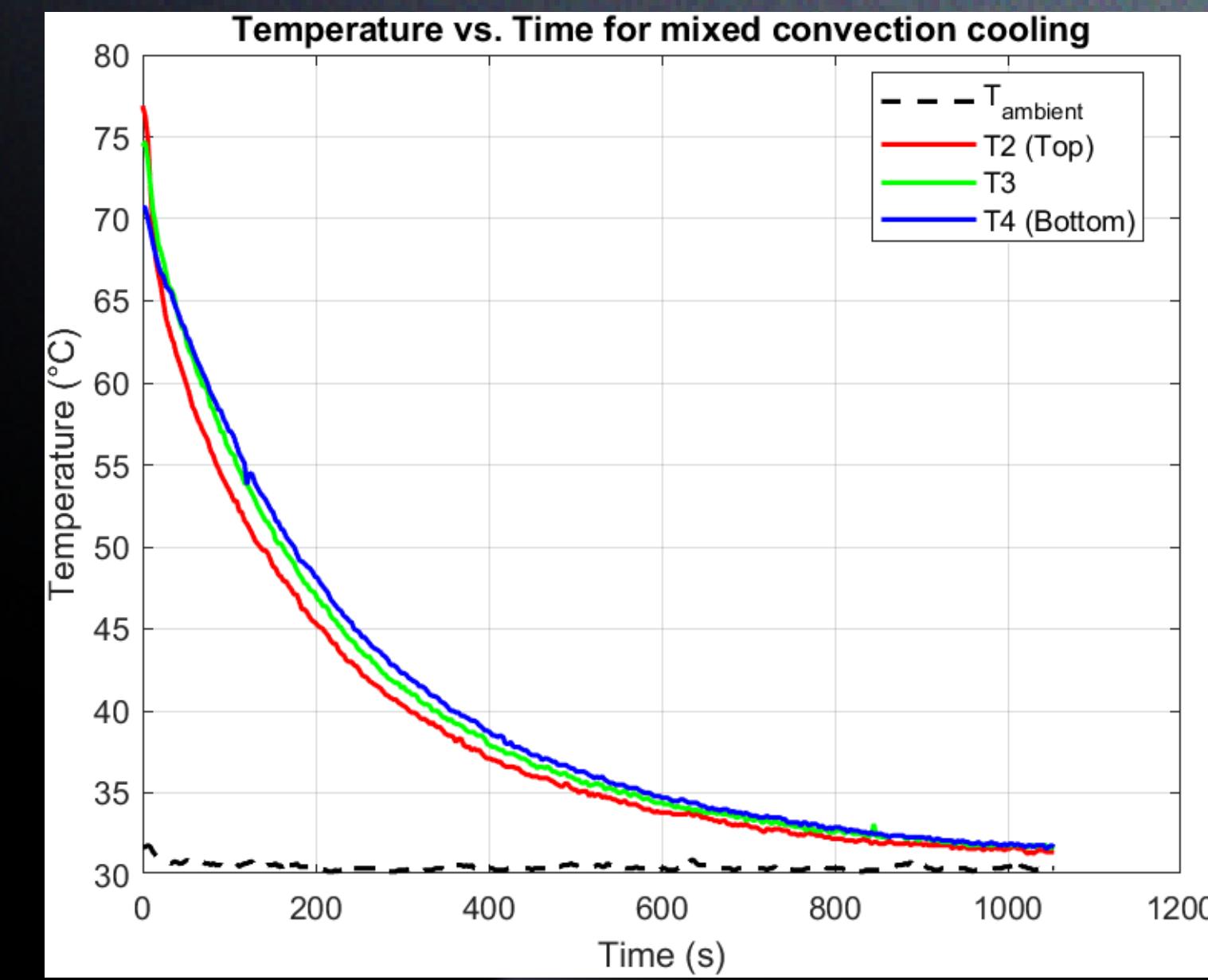
- **Assumptions:** Negligible radiation, Uniform airflow (Forced), steady.

• Temperature vs. Time graph

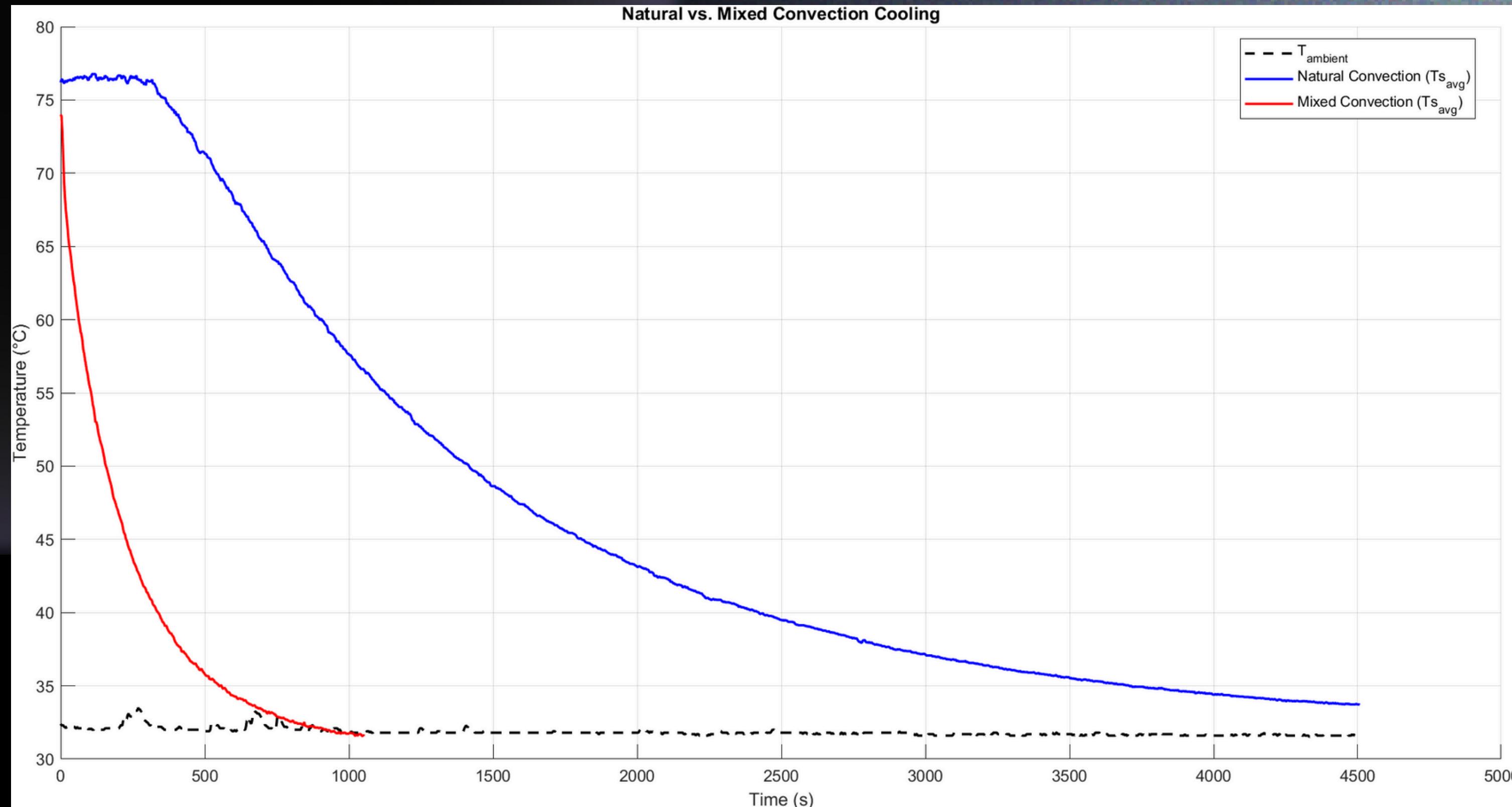
• Natural convection



• Mixed convection (forced - natural): Rapid cooling.



- Natural vs Mixed Convection Cooling



• Logarithmic Plots & Linear Fit:

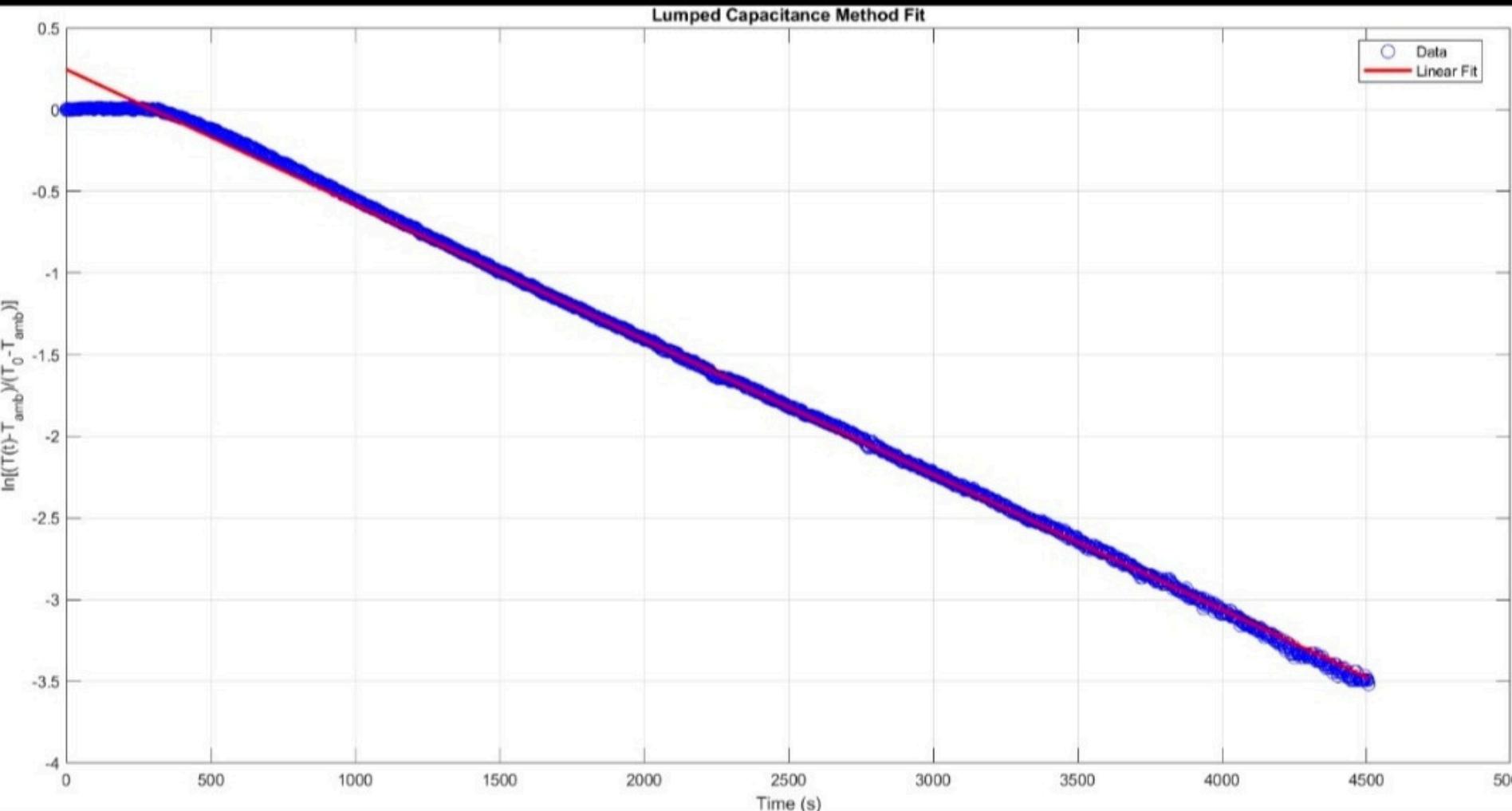
$\ln(\Delta T)$ vs. t for both cases.

Natural:

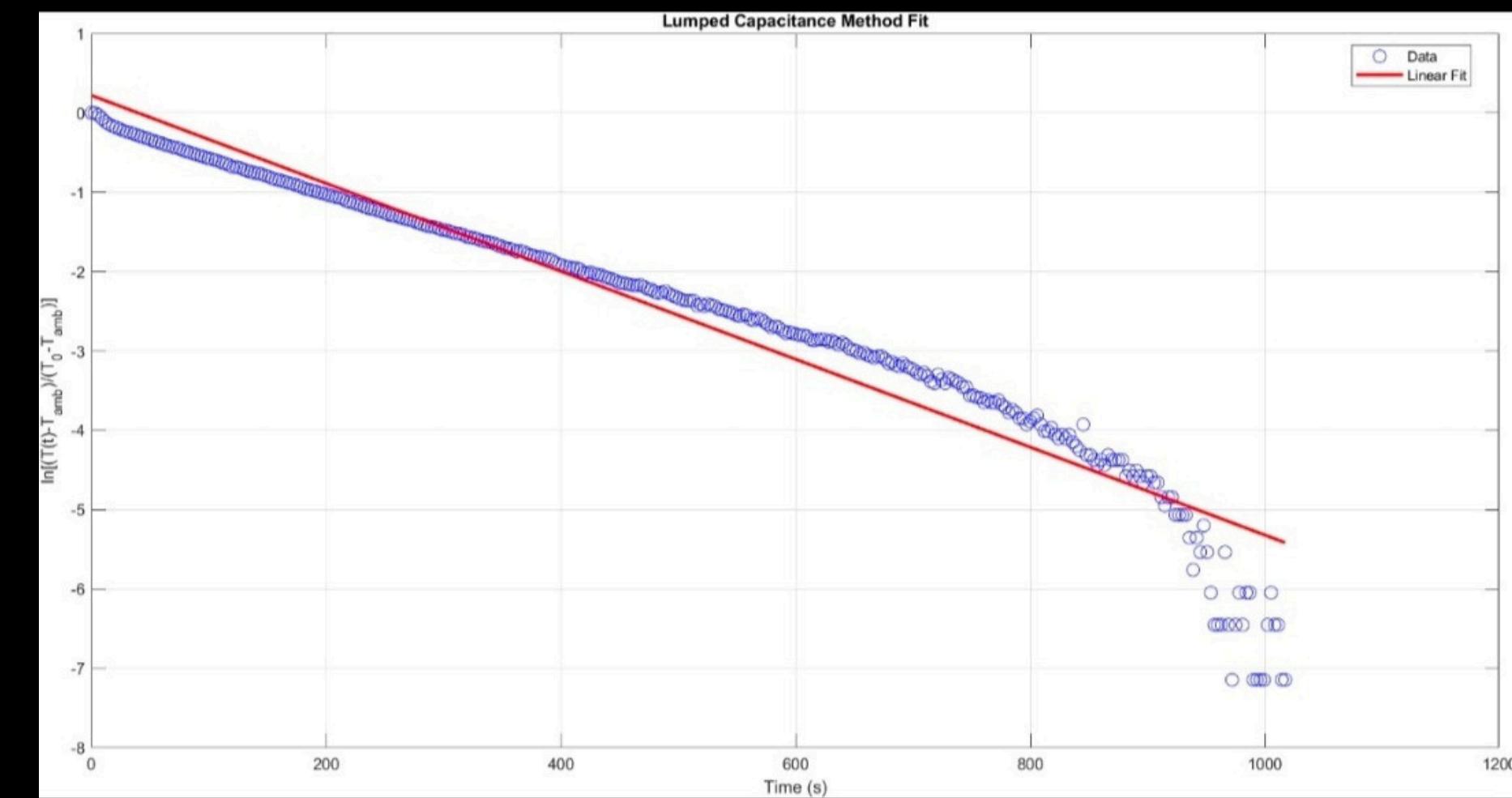
$$\text{Slope} = -0.0008 \rightarrow h_{\text{exp}} = 8.2 \text{ W/m}^2 \cdot \text{K}$$

Mixed (forced - natural): Slope = -0.0055 $\rightarrow h_{\text{exp}} = 49.76 \text{ W/m}^2 \cdot \text{K}$

Natural convection



Mixed Convection



Sample Calculation

Natural convection

$G_L = \text{Grashof number}$

$$G_L = \frac{g\beta(T_s - T_\infty)L^3}{V^2}$$

$$= \frac{(9.81)(0.0034)(76.33 - 32.1)(0.2)^3}{2.25 \times 10^{10}}$$

$$= \frac{(9.81)(0.0034)(44.93)(0.0008)}{2.25 \times 10^{10}}$$

$$\boxed{G_L = 52.453 \times 10^5}$$

$$P_8 = \frac{V}{d} = \frac{1.5 \times 10^{-5}}{1.11 \times 10^{-4}} = 1.35 \times 10^{-1} = 0.135$$

$$Ra_L = G_L \cdot P_8 = (52.453 \times 10^5)(0.135)$$

$$\boxed{Ra_L = 7.081155 \times 10^5}$$

$$\text{For } [10^4 < Ra_L < 10^9], Nu_L = 0.59(Ra_L)^{1/4}$$

$$= (0.59)(7081155)^{1/4} = 0.59 \times 29.01$$

$$\boxed{Nu_L = 17.11}$$

$$h_{\text{theoretical}} = \frac{Nu_L \cdot K}{L} = \frac{(17.11)(0.026)}{0.2}$$

$$\boxed{h = 2.243 \frac{W}{m^2 \cdot K}}$$

Mixed convection

Sample calculation

Fan velocity calculation
electrical parameter

- Voltage = 18.6V
- Current = 0.2A
- Power = $\sqrt{I} = 18.6 \times 0.2 = 5.21 \text{ watt}$

Fan flow rate estimation

- Standard 80-90 mm computer fan operating at 5.21W
- Typical flow rate: approx. 30CFM (cubic feet per minute)

Air velocity calculation

- Fan Area (A) = $\pi \times (0.045)^2 = 0.00636 \text{ m}^2$ (90 mm fan)
- Flow rate: $30 \text{ CFM} = 0.0142 \text{ m}^3/\text{s}$
- Raw velocity: $\frac{\text{Flow rate}}{\text{Area}} = \frac{0.0142}{0.00636} = 2.23 \text{ m/s}$
- Effective velocity at cylinder surface (80% efficiency)
 $= 2.23 \times 0.8 = 1.78 \text{ m/s}$

Mixed convection calculation

Parameters:

Copper rod outer diameter (OD) = 0.03986 m

Copper rod inner diameter (ID) = 0.03426 m

Length (L) = 0.2 m

$L_c = 0.2$

Surface Area = $\pi \times OD \times L = 0.02504 \text{ m}^2$

$K_{copper} = 401 \text{ W/m} \cdot \text{K}$

$\rho_{copper} = 8960 \text{ kg/m}^3$

Air properties

$K_{air} = 0.02662 \text{ W/m} \cdot \text{K}$

$\Pr = 0.7255$

$$C_{copper} = 385 \text{ J/kg} \cdot \text{K}$$

$$m = \frac{8 \times \pi}{4} \times (OD^2 - ID^2) \times L = 0.311 \text{ kg}$$

$$V = 1702 \times 10^{-5} \text{ m}^3/\text{s}$$

$$\rho_{air} = 1.127 \text{ kg/m}^3$$

Forced convection

$$Re = \frac{V_m \times OD}{\nu} = 4171$$

correlation (Churchill - Bernstein):

for $Re \times Pr > 10^2$

$$Nu = 0.3 + \left[\frac{0.62 \times \sqrt{Re} \Pr^{1/3}}{1 + (0.41 \Pr)^{2/3}} \right]^{1/4} \left[1 + \left(\frac{Re}{282000} \right)^{5/8} \right]^{1/5}$$

Putting all values we get

$$Nu_f = 31.92$$

$$h_{\text{forced}} = \frac{Nu_f \cdot K_{air}}{OD} = 21.31 \frac{W}{m^2 \cdot K}$$

Mixed convection (forced opposing natural)

We use following correlation for this case

$$h_{\text{mixed}} = (h_{\text{forced}}^3 - h_{\text{natural}}^3)^{1/3}$$

$$h_{\text{mixed}} = (121.31^3 - 2.24^3)^{1/3}$$

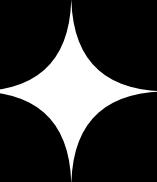
$$h_{\text{mixed}} = 21.34 \frac{W}{m^2 \cdot K}$$

- Theoretical vs. Experimental h

- Comparison

- Natural convection $h_{\text{theory}} = 2.243 \text{ W/m}^2 \cdot \text{K}$ vs. $h_{\text{exp}} = 7.43 \text{ W/m}^2 \cdot \text{K}$
 - Mixed convection: $h_{\text{theory}} = 21.34 \text{ W/m}^2 \cdot \text{K}$ vs. $h_{\text{exp}} = 49.76 \text{ W/m}^2 \cdot \text{K}$
 - Forced convection: $h_{\text{theory}} = 21.31 \text{ W/m}^2 \cdot \text{K}$

Conclusions & Future Work



- **Conclusions :**
 - **Forced convection significantly increased heat dissipation compared to natural convection.**
 - **The setup provided clear insights into transient vs. steady-state heat transfer behavior.**
- **Future Work :**
 - **Changes the direction of forced convection like in direction of natural convection or in opposite direction of natural convection**
 - **Extend the experiment to vary air flow velocities and study transition from laminar to turbulent external flow.**
 - **Compare results for different materials (e.g., aluminum, stainless steel) to explore thermal conductivity effects.**