

Математический анализ

1 Неопределённые интегралы

1.

$$\int \frac{2}{x+3} dx = 2 \ln |x+3| + C.$$

2.

$$\begin{aligned} \int \frac{x^3 - 5x + 8}{x^2 - 2x + 4} dx &= \int \left(x + \frac{2x^2 - 9x + 8}{x^2 - 2x + 4} \right) dx = \int \left(x + 2 - \frac{5x}{x^2 - 2x + 4} \right) dx = \\ &= \frac{x^2}{2} + 2x - \int \frac{5x}{x^2 - 2x + 4} dx = (u = x-1) = \frac{x^2}{2} + 2x - \int \frac{5u+5}{u^2+3} du = \\ &= \frac{x^2}{2} + 2x - \int \frac{5d(u^2+3)}{2(u^2+3)} - 5 \int \frac{1}{u^2+3} du + C = \\ &= \frac{x^2}{2} + 2x + \frac{5}{2} \ln(u^2+3) - \frac{5}{\sqrt{3}} \arctan \frac{u}{\sqrt{3}} + C = \\ &= \frac{x^2}{2} + 2x + \frac{5}{2} \ln(x^2 - 2x + 4) - \frac{5}{\sqrt{3}} \arctan \frac{x-1}{\sqrt{3}} + C. \end{aligned}$$

3. Имеем

$$\begin{aligned} \int \frac{\sin 3x}{(1-2\cos 3x)^2} dx &= \int \frac{d \cos 3x}{-3(1-2\cos 3x)^2} dx = (u = \cos 3x) = \int \frac{du}{-3(1-2u)^2} = \\ &= \int \frac{d(1-2u)}{6(1-2u)^2} = (v = 1-2u) = \int \frac{dv}{6v^2} = -\frac{1}{6v} + C = -\frac{1}{6(1-2u)} + C = \\ &= -\frac{1}{6(1-2\cos 3x)} + C. \end{aligned}$$