

## L8 Implementation of LFU

The Pre-requisite of this problem is you must solved the previous problem and is (LR4) Last Recently used for this problem (LF4) Last Frequently used

Now The Other problem state that we design the(LFU) data structure which have two Different Functionality

→ get()  
→ peek()

As we know that what is the work of get and put function

get(key)

Get function Return the value of the key if that key exist otherwise  
Return  $\{-\}$

`put(key, value)`

→ update the value of key if such key already exist and if such key are not present so simply insert such key

When the curv. closer structure were filled then removed the LF4 group and if more than one LF4 exist then

→ Removed the LRU entry from all the LRU queues



The Main task of this problem is we designed an algorithm with Space complexity  $O(1)$   
Both function work in the Constant time



## # Let's Deep Run and Understand

Size = 2 → even Ceteral Structure size not more than 2

`put(7,10)`

So what can we do is we deal with frequency and Assign one sheet pair

frequency      pair  
4 → (4,10)

put(3,20)

Again meet pair frequency is one so again exchange that pair into our ds

frequency pair  
 $\downarrow \rightarrow$  ( $1,10$ ) ( $2,120$ )

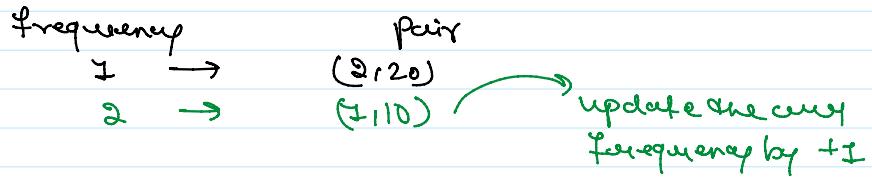


get(1)

get(2)

Once you call get function so return that value of that pair and increase the frequency of that pair by +1

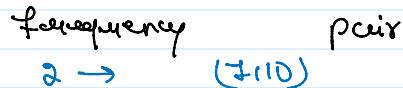
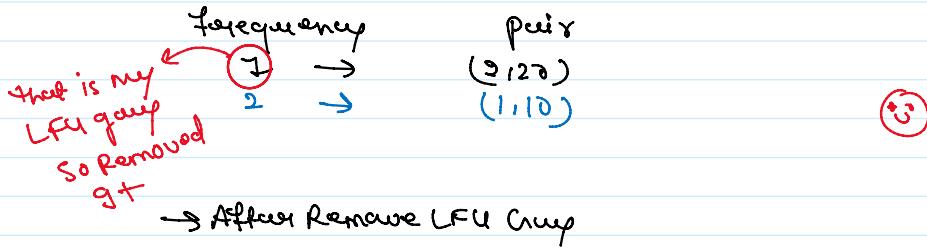
$$\text{ans} = 10$$



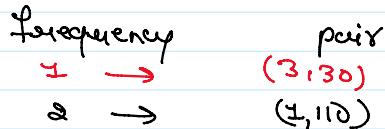
put(3, 30)

Now we will insert put that pair into the data structure because my cache size is full that is ② so what g do

→ Removed the least frequent guy



→ Now after removed the LRU guy put that new pair in placed of that



get(2)

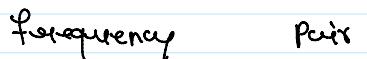
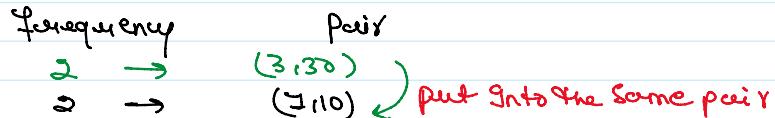
New that keep 2nd present into the list means cache is ①

$$\text{ans} = -1$$

get(3)

Now 3 is present into the my cache data structure so return its value and change its frequency by +1

$$\text{ans} = 30$$



$$2 \rightarrow (1, 10) (3, 30)$$

put(4,40)

Now in this case my cache is full so removed LRU guy from the data structure  
→ but there is problem we have more than one pair in the  
LRU guy so what we do in this case

→ As we know previously if we have more than 1 LRU so removed  
LRU guy from all these LRU guys

frequency	pair
2 →	(4,40) (3,30) Removed it

→ that is my LRU pair so removed it

frequency	pair
2 →	(3,30)

→ Now after removed LRU pair put the new pair

frequency	pair
1 →	(4,40)
2 →	(3,30)

get(2)

New that key 2 is present into the Cache data structure so return 1  
ans = -1

get(3)

Yes key = 3 are present into the Cache data structure so return its value and increment  
its frequency by +1

ans = 30

frequency	pair
1 →	(4,40)
2 →	(3,30)



get(4)

Yes key = 4 are present into the Cache data structure so return its value and increment  
its frequency by +1

ans = 40

frequency	pair
2 →	(4,40)
3 →	(3,30)

Now that is the Approach how to put and get function are work let's discuss the  
Algorithm of this concept with time O(1)

## Requirement

We Required One Doubly linked List

→ Same Concept and logic Used here and we used into the LRU Implementation  
only Little Changes were applied on it

### Algorithm:

- • get(key):
  - If key is not present in cache, return -1
  - Get the node from the cache
  - Update the node frequency
  - Remove the node from the DLL of node's previous frequency
  - Add the node to the DLL with the node's updated frequency
  - Update min frequency value
  
- • put(key, value):
  - If key is present in cache
    - Similar logic to that of get function
    - Only difference being that we need to update the value here
  - If key not present in cache
    - If the cache has already reached its capacity, delete the tail node from the DLL with least frequency
    - Create the new node with the (key, value) pair passed as arguments
    - Add the node to the frequency table with frequency key = 1
    - Add the node to the cache
    - Update min frequency to be 1

→ Our Algorithm logic that we implement into our code

Source = Leetcode Dition



## # Implementation Python

```
# lc: https://leetcode.com/problems/lru-cache/
# codeStudio:
https://www.codingninjas.com/codestudio/problems/lrucache\_3114758?leftPanelTab=0
# ib: https://www.interviewbit.com/problems/lru-cache/

import collections
class ListNode:
    def __init__(self, key, val):
        self.key = key
        self.val = val
        self.freq = 1
        self.prev = None
        self.next = None

class DLL:
    def __init__(self):
        self.head = ListNode(0, 0)
        self.tail = ListNode(0, 0)
        self.head.next = self.tail
        self.tail.prev = self.head
        self.size = 0

    def insertHead(self, node):
        headNext = self.head.next
        self.head.next = node
        node.prev = self.head
        node.next = headNext
        headNext.prev = node
        self.size += 1

class LFUCache:
    def __init__(self, capacity):
        self.capacity = capacity
        self.curSize = 0
        self.minFrequency = float('inf')
        self.cache = {}
        self.frequencyMap = {}

    def get(self, key):
        if key not in self.cache:
            return -1
        node = self.cache[key]
        self._updateFrequency(node)
        return node.val

    def _updateFrequency(self, node):
        freq = node.freq
        if freq == self.minFrequency and self.frequencyMap[freq].size == 1:
            self.frequencyMap.pop(freq)
            self.minFrequency += 1
        else:
            self.frequencyMap[freq].remove(node)
        node.freq += 1
        if node.freq not in self.frequencyMap:
            self.frequencyMap[node.freq] = DLL()
        self.frequencyMap[node.freq].insertHead(node)

    def put(self, key, value):
        if self.capacity == 0:
            return
        if key in self.cache:
            node = self.cache[key]
            self._updateFrequency(node)
            node.val = value
        else:
            if self.curSize == self.capacity:
                del self.cache[self.frequencyMap[self.minFrequency].tail.prev]
                self.frequencyMap[self.minFrequency].size -= 1
                if self.frequencyMap[self.minFrequency].size == 1:
                    self.frequencyMap.pop(self.minFrequency)
                    self.minFrequency += 1
            node = ListNode(key, value)
            self.cache[key] = node
            self.frequencyMap[1].insertHead(node)
            self.curSize += 1
            self.minFrequency = 1
```

## Implementation Java

```
import java.util.*;
public class L8_LFU_Cache {
    public static void main(String[] args) {
        System.out.println("L8_LFU_Cache");
    }
}

class LFUCache {
    final int capacity;
    int curSize;
    int minFrequency;
    Map<Integer, DLLNode> cache;
    Map<Integer, DoubleLinkedList> frequencyMap;

    /**
     * @param capacity: total capacity of LFU Cache
     * @param curSize: current size of LFU cache
     * @param minFrequency: frequency of the last linked list (the minimum frequency of entire LFU cache)
     * @param cache: a hash map that has key to Node mapping, which used for storing all nodes by their keys
     * @param frequencyMap: a hash map that has key to linked list mapping, which used for storing all
```

```

def insertHead(self, node):
    headNext = self.head.next
    headNext.prev = node
    self.head.next = node
    node.prev = self.head
    node.next = headNext
    self.size += 1

def removeNode(self, node):
    node.next.prev = node.prev
    node.prev.next = node.next
    self.size -= 1

def removeTail(self):
    tail = self.tail.prev
    self.removeNode(tail)
    return tail

class LFUCache:

    def __init__(self, capacity: int):
        self.cache = {}
        self.freqTable = collections.defaultdict(DLL)
        self.capacity = capacity
        self.minFreq = 0

    def get(self, key: int) -> int:
        if key not in self.cache:
            return -1
        return self.updateCache(self.cache[key], key, self.cache[key].val)

    def put(self, key: int, value: int) -> None:
        if not self.capacity:
            return
        if key in self.cache:
            self.updateCache(self.cache[key], key, value)
        else:
            if len(self.cache) == self.capacity:
                prevTail = self.freqTable[self.minFreq].removeTail()
                del self.cache[prevTail.key]
                node = ListNode(key, value)
                self.freqTable[1].insertHead(node)
                self.cache[key] = node
                self.minFreq = 1

        def updateCache(self, node, key, value):
            node = self.cache[key]
            node.val = value
            prevFreq = node.freq
            node.freq += 1
            self.freqTable[prevFreq].removeNode(node)
            self.freqTable[node.freq].insertHead(node)
            if prevFreq == self.minFreq and self.freqTable[prevFreq].size == 0:
                self.minFreq += 1
            return node.val

    # Your LFUCache object will be instantiated and called as such:
    # obj = LFUCache(capacity)
    # param_1 = obj.get(key)
    # obj.put(key,value)

```

mapping, which used for storing all nodes by their keys  
 \* @param frequencyMap: a hash map that has key to linked list mapping, which used for storing all double linked list by their frequencies  
 \* \*/

```

public LFUCache(int capacity) {
    this.capacity = capacity;
    this.curSize = 0;
    this.minFrequency = 0;

    this.cache = new HashMap<>();
    this.frequencyMap = new HashMap<>();
}

/** get node value by key, and then update node frequency as well as relocate that node */
public int get(int key) {
    DLLNode curNode = cache.get(key);
    if (curNode == null) {
        return -1;
    }
    updateNode(curNode);
    return curNode.val;
}

/**
 * add new node into LFU cache, as well as double linked list
 * condition 1: if LFU cache has input key, update node value and node position in list
 * condition 2: if LFU cache does NOT have input key
 * - sub condition 1: if LFU cache does NOT have enough space, remove the Least Recent Used node
 *   in minimum frequency list, then add new node
 * - sub condition 2: if LFU cache has enough space, add new node directly
 * */
public void put(int key, int value) {
    // corner case: check cache capacity initialization
    if (capacity == 0) {
        return;
    }

    if (cache.containsKey(key)) {
        DLLNode curNode = cache.get(key);
        curNode.val = value;
        updateNode(curNode);
    } else {
        curSize++;
        if (curSize > capacity) {
            // get minimum frequency list
            DoubleLinkedList minFreqList =
            frequencyMap.get(minFrequency);
            cache.remove(minFreqList.tail.prev.key);

            minFreqList.removeNode(minFreqList.tail.prev);
            curSize--;
        }
        // reset min frequency to 1 because of adding new node
    }
}

```

## Important Point

One of the  
Hardest problems  
ON the based is N  
(Stack, queue)  
and  
(linkedlist)  


```
minFrequency = 1;
DLLNode newNode = new DLLNode(key, value);

// get the list with frequency 1, and then add
new node into the list, as well as into LFU cache
DoubleLinkedList curList =
frequencyMap.getOrDefault(1, new
DoubleLinkedList());
curList.addNode(newNode);
frequencyMap.put(1, curList);
cache.put(key, newNode);
}

public void updateNode(DLLNode curNode) {
int curFreq = curNode.frequency;
DoubleLinkedList curList =
frequencyMap.get(curFreq);
curList.removeNode(curNode);

// if current list is the last list which has lowest
frequency and current node is the only node in that list
// we need to remove the entire list and then
increase min frequency value by 1
if (curFreq == minFrequency && curList.listSize ==
0) {
minFrequency++;
}

curNode.frequency++;
// add current node to another list has current
frequency + 1,
// if we do not have the list with this frequency,
initialize it
DoubleLinkedList newList =
frequencyMap.getOrDefault(curNode.frequency, new
DoubleLinkedList());
newList.addNode(curNode);
frequencyMap.put(curNode.frequency, newList);
}

/*
 * @param key: node key
 * @param val: node value
 * @param frequency: frequency count of current
node
 * (all nodes connected in same double linked list has
same frequency)
 * @param prev: previous pointer of current node
 * @param next: next pointer of current node
 */
class DLLNode {
int key;
int val;
int frequency;
DLLNode prev;
DLLNode next;

public DLLNode(int key, int val) {
this.key = key;
this.val = val;
this.frequency = 1;
}
}
```

```
/*
 * @param listSize: current size of double linked list
 * @param head: head node of double linked list
 * @param tail: tail node of double linked list
 */
class DoubleLinkedList {
    int listSize;
    DLLNode head;
    DLLNode tail;
    public DoubleLinkedList() {
        this.listSize = 0;
        this.head = new DLLNode(0, 0);
        this.tail = new DLLNode(0, 0);
        head.next = tail;
        tail.prev = head;
    }
}

/** add new node into head of list and increase list
size by 1 */
public void addNode(DLLNode curNode) {
    DLLNode nextNode = head.next;
    curNode.next = nextNode;
    curNode.prev = head;
    head.next = curNode;
    nextNode.prev = curNode;
    listSize++;
}

/** remove input node and decrease list size by 1
*/
public void removeNode(DLLNode curNode) {
    DLLNode prevNode = curNode.prev;
    DLLNode nextNode = curNode.next;
    prevNode.next = nextNode;
    nextNode.prev = prevNode;
    listSize--;
}

/**
 * Your LFUCache object will be instantiated and called
as such:
* LFUCache obj = new LFUCache(capacity);
* int param_1 = obj.get(key);
* obj.put(key,value);
*/

```