

# SQP11 Sliding Window Maximum

Sunday, December 4, 2022 5:28 PM

## L10 Sliding Window Maximum

Problem Statement: Given an array of integers with  $k$  integers and every task is finding the maximum element of every window of size  $k$ . That is the question says

Example

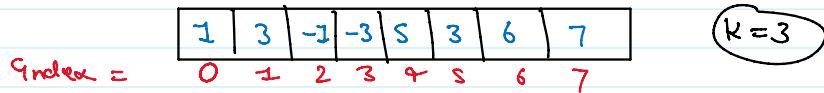
Input: nums = [1,3,-1,-3,5,3,6,7], k = 3	
Output: [3,3,5,6,7]	
Explanation:	
Window position	
Max	
[1 3 -1] -3 5 3 6 7	3
1 [3 -1 -3] 5 3 6 7	3
1 3 [-1 -3 5] 3 6 7	5
1 3 -1 [-3 5] 3 6 7	5
1 3 -1 -3 [5 3] 6 7	6
1 3 -1 -3 [5 3 6] 7	6
1 3 -1 -3 [5 3 6] 7	7

That is my answer

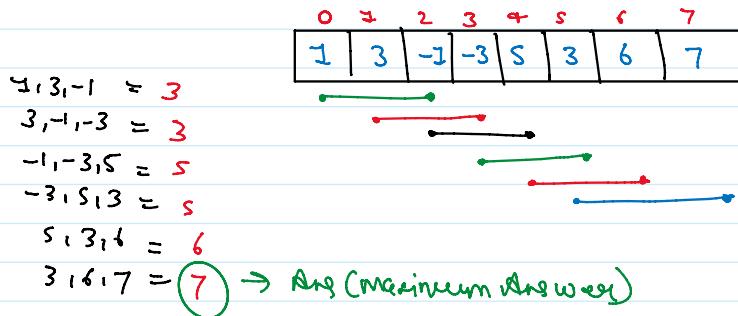


# Thought Process

→ Always start with Brute Force Approach in interviews then go with the Optimized



→ Now let's say we start with iteration from 0 and finding all the possible Subarray with the length of  $k$



# How it looks like in my code

for ( $i=0$  to  $\text{len}(\text{arr}) - k$ ) {

$\text{max} = \text{arr}[i]$

    for ( $j=i$  to  $i+k-1$ ) {

$\text{max} = \max(\text{max}, \text{arr}[j])$

    return  $\text{max}$

}

That is one my possible answer code



Time Complexity =  $O(N \times k) \approx O(N^2)$

→ That is Quadratic time so interviewer asked to optimized that approach

→ That is Quadratic time so interviewer asked to Optimized Approach

## # Optimized Approach

Index =  $\begin{array}{ccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \boxed{1} & 3 & -1 & -3 & 5 & 3 & 6 & 7 \end{array}$

K=3

→ Now here again we used the concept of Next Greater element that we learned previously

→ In this concept we store one element into the Increasing fashion ↑

→ In this problem we store one element into the decreasing order ↓

→ We required the degree data structure

→ We start iteration from index = 0

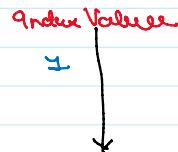
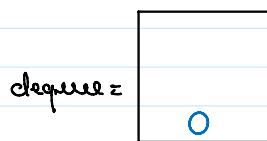
→ And maintain the degree property that is decreasing order ↓ and push that index into the degree



Index =  $\begin{array}{ccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \boxed{1} & 3 & -1 & -3 & 5 & 3 & 6 & 7 \end{array}$

K=3

→ i



i = 0

→ Now check if degree is empty then simply put one i into the degree

i = 1

→ Again same approach follow and maintain the property of degree and check

→ And check if degree is Not Empty So  
existing element is > then over(i) ✓

✓ → if that condition case True then simply put next index into the degree

X → otherwise Removed next element  
from the degree that is < than over(i)



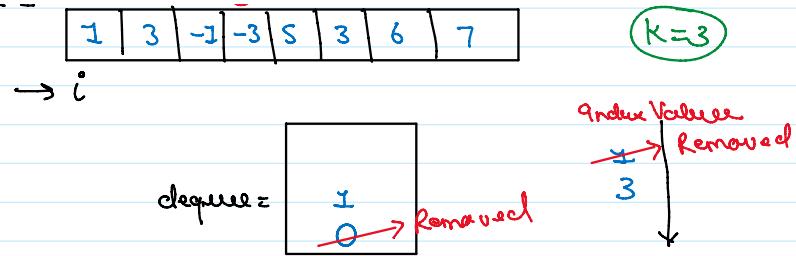
over(i) = 3

→ Index = 1 < 3 ✓ (Removed from degree) → arr[i] < degree[over(i)] ✓

Index =  $\begin{array}{ccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \boxed{1} & 3 & -1 & -3 & 5 & 3 & 6 & 7 \end{array}$

K=3

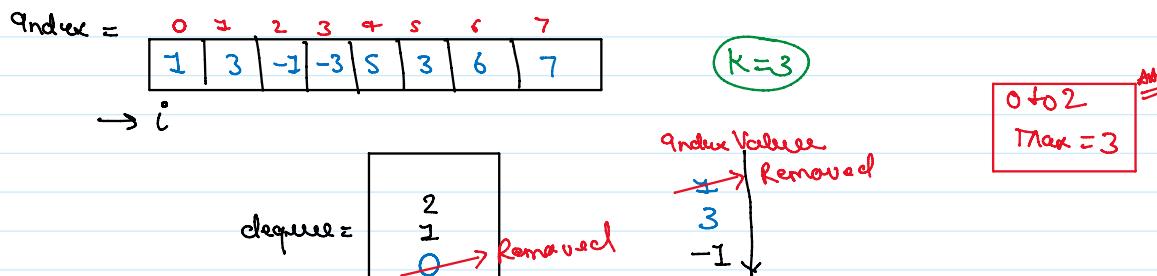
→ i



$i=2$

$\rightarrow$  Again same Approach follow and check if the dequeue follows the property or Not

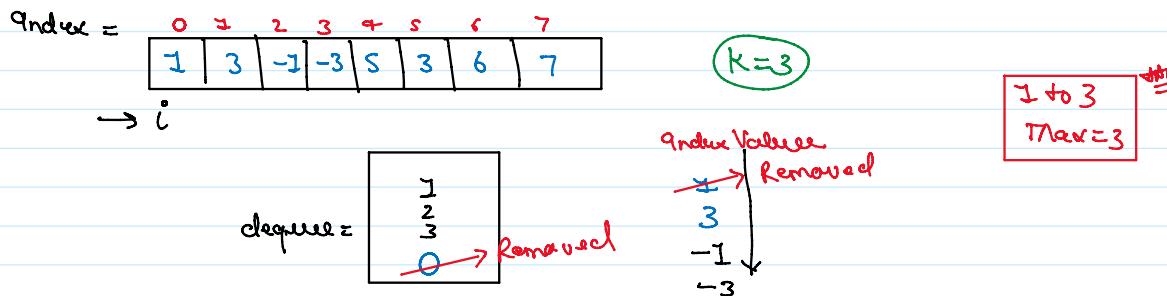
$\text{arr}[i] = -1 < \text{dequeue.front}$  ✓  
 $\rightarrow$  So simply append that  $i$  into the dequeue



$i=3$

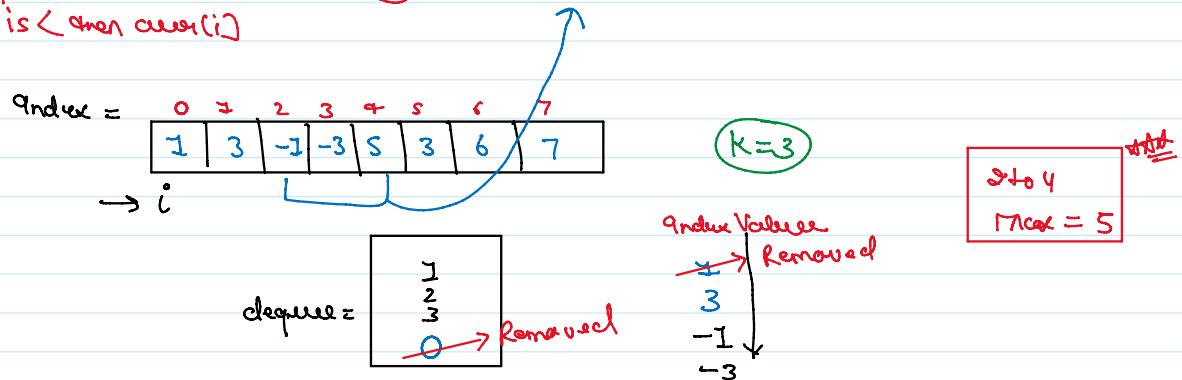
$\rightarrow$  Again same Approach follow and check if the dequeue follows the property follow or Not

$\text{arr}[i] = -3 < \text{dequeue.front}$  ✓  
 $\rightarrow$  So simply append that  $i$  into the dequeue

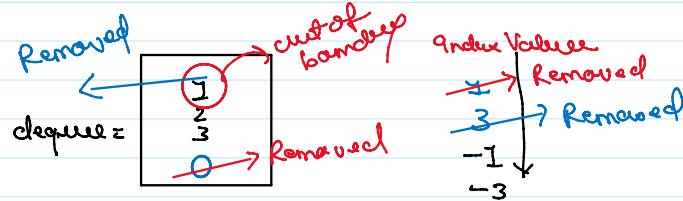


$i=4$

Once we complete the one half of the  $K$  that means removed all the element from the dequeue that is  $<$  than  $\text{arr}[i]$



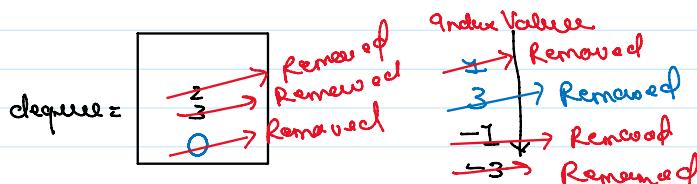
→ And check if any queue element is smaller than my boundary so simply pop from the front



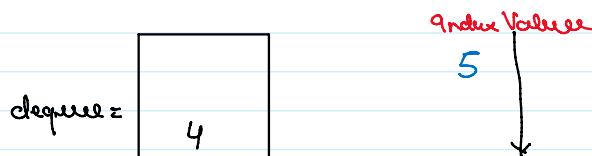
My boundary is  $[2, 4]$



→ After removing my out of boundary element check from the back ← if any thing that is < even  $\text{arr}(i)$  in queue so simply remove cell element from the deque



→ After removed All the element that is < than  $\text{arr}(i)$  simply put the  $i$  into the deque

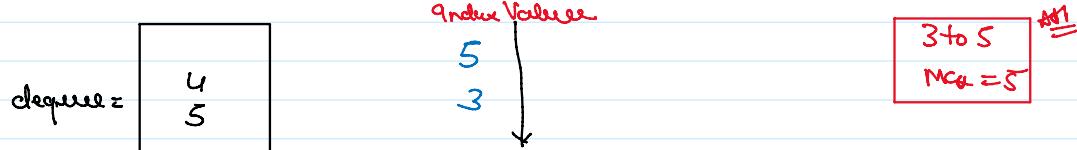


$i = 5$

→ Again same approach follow and check if the deque follows the property follow or not

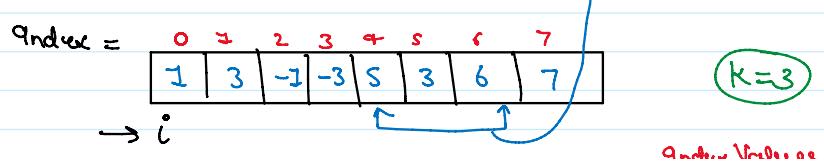
$\text{arr}(i) = 3 < \text{dequeue.front}$  ✓

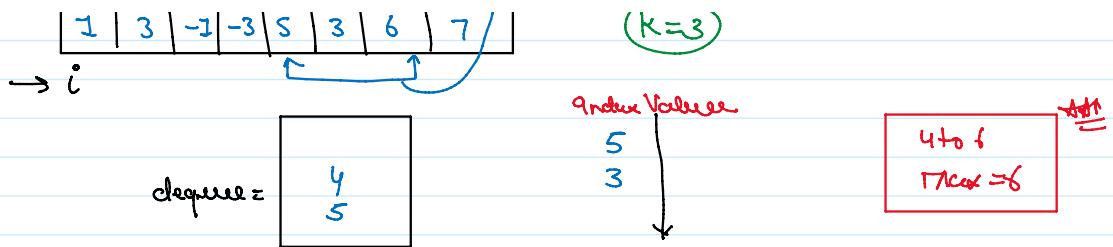
→ So simply append index  $i$  into the deque



$i = 6$

Once we complete one half of the  $(k)$  that means removed cell one element from the deque that is < than  $\text{arr}(i)$



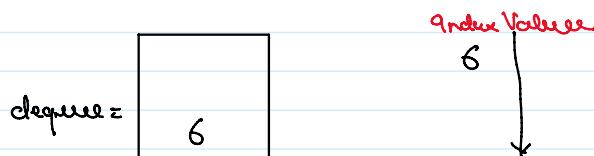


$$\text{My boundary} = [4, 6]$$

- Now No any element meet out of bound on the dequeue
- check from the back ← if any element meet is < even  $\text{cur}(i)$  into the dequeue so Removed cell

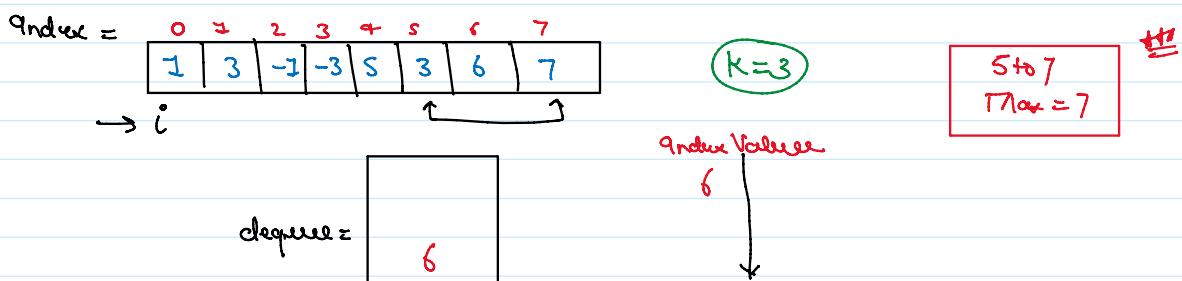


→ all the removed from back part  $i$  into the dequeue



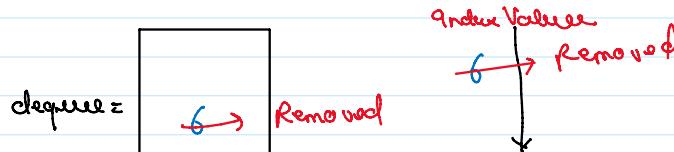
$$i=7$$

Once we complete the one half of the  $(k)$  that means removed all the element from the dequeue and it is < even  $\text{cur}(i)$

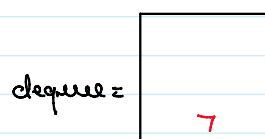


$$\text{My boundary} = [5, 7]$$

- Now No any element meet out of bound on the dequeue ✓
- check from the back ← if any element meet is < even  $\text{cur}(i)$  into the dequeue so Removed cell



→ *current removed from back put i into the deque*



Index Value

7

That is one my last Maximum  
under the window of k

Maximum All Window = 



Time Complexity =  $O(N) + O(N) \approx O(N)$

→ Few linear iteration

→ Few remaining are out of bound index and their all element next is < than arr[i] from deque

→ That is Amortized Time Complexity

Space Complexity =  $O(K)$



→ at one time only we stored the last max k element into the deque

## # Implementation Python

```
# lc: https://leetcode.com/problems/sliding-window-maximum/submissions/
# gfg: https://practice.geeksforgeeks.org/problems/maximum-of-all-subarrays-of-size-k3101/1

import collections
class Solution:
    def maxSlidingWindow(self, nums: List[int], k: int) -> List[int]:
        res = []
        window = collections.deque()
        for i, num in enumerate(nums):

            while window and num >= nums[window[-1]]:
                window.pop()

            window.append(i)

            if i >= k - 1:
                res.append(nums[window[0]])

            if i - window[0] + 1 == k:
                window.popleft()

        return res
```

## # Implementation Java

```
import java.util.*;
public class L10_Sliding_Window_Maximum {
    public static void main(String[] args) {
        System.out.println("L10_Sliding_Window_Maximum");
    }
}

class OptimizedSolution {
    public int[] maxSlidingWindow(int[] nums, int k) {

        int n = nums.length;
        int[] r = new int[n - k + 1];
        int ri = 0;
        // store index

        Deque<Integer> q = new ArrayDeque<>();
        for (int i = 0; i < nums.length; i++) {

            // remove numbers out of range k
            if (!q.isEmpty() && q.peek() == i - k) {
                q.poll();
            }

            // remove smaller numbers in k range as they are
            while (q.size() > 0 && q.peek() <= nums[i]) {
                q.poll();
            }
            q.add(i);
            if (i >= k - 1) {
                r[ri] = q.peek();
                ri++;
            }
        }
        return r;
    }
}
```

```
window.pop();  
return res
```



```
q.poll();  
} // remove smaller numbers in k range as they are  
useless  
while (!q.isEmpty() && nums[q.peekLast()]  
< nums[i]) {  
    q.pollLast();  
}  
q.offer(i);  
  
if (i >= k - 1) {  
    r[ri++] = nums[q.peek()];  
}  
return r;  
}  
}
```