

## L22 Rat in a Maze Problem - I

Monday, June 19, 2023 1:52 PM

Consider a rat placed at (0, 0) in a square matrix of order  $N \times N$ . It has to reach the destination at  $(N-1, N-1)$ . Find all possible paths that the rat can take to reach from source to destination. The directions in which the rat can move are 'U'(up), 'D'(down), 'L'(left), 'R'(right). Value 0 at a cell in the matrix represents that it is blocked and rat cannot move to it while value 1 at a cell in the matrix represents that rat can travel through it.

Note: In a path, no cell can be visited more than one time. If the source cell is 0, the rat cannot move to any other cell.

Example 1:

Input:

$N = 4$

$m[][] = \{\{1, 0, 0, 0\}, \{1, 1, 0, 1\}, \{1, 1, 0, 0\}, \{0, 1, 1, 1\}\}$

Output:

DDRRR DRDRR

Explanation:

The rat can reach the destination at (3, 3) from (0, 0) by two paths - DDRRR and DRDRR, when printed in sorted order we get DDRRR DRDRR.

Example 2:

Input:

$N = 2$

$m[][] = \{\{1, 0\}, \{1, 0\}\}$

Output:

-1

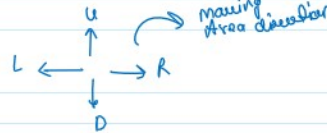
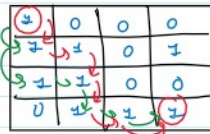
Explanation:

No path exists and destination cell is blocked.

→ Basically we finding all the path that take Rat Reach Source to destination

UP

Thought Process



DDRRR, DRDRR → Answer is Lexicographical Order

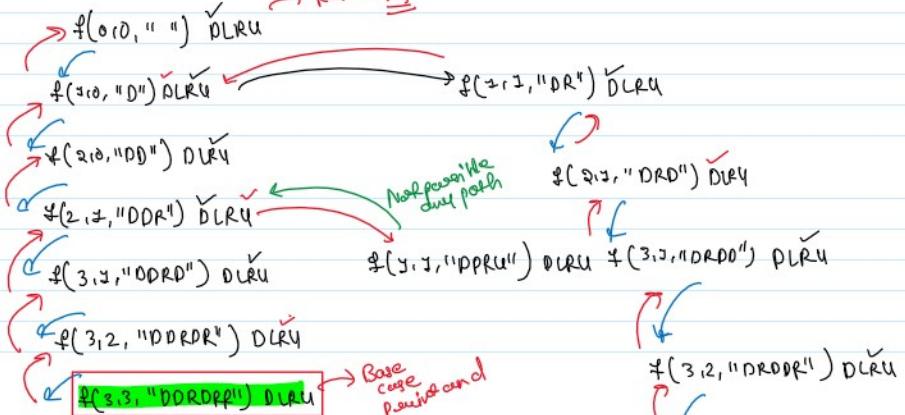
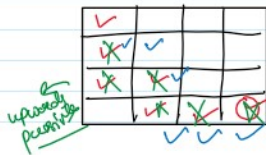
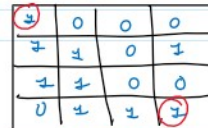
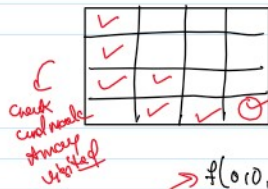
→ This type of problem we solved using Recursion

→ we follow the Lexicographical Order

(DLRU)

Maze

→ Maintaining the visited array



→ Because every cell 4 different call for every direction.

→ Backtracking and unmark from the visited array

→ Base case return and unmark from the visited array

UP

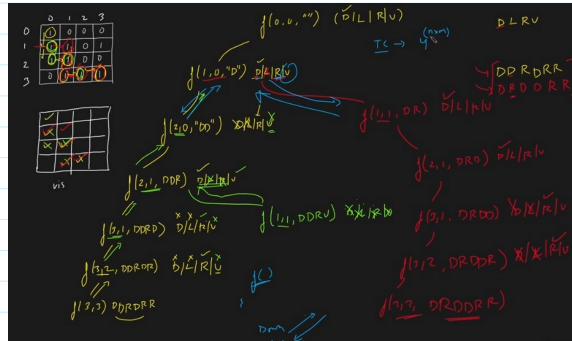
**Time Complexity:**  $O(4^{(m*n)})$ , because on every cell we need to try 4 different directions.

**Space Complexity:**  $O(m*n)$ , Maximum Depth of the recursion tree(auxiliary space).

directions.

**Space Complexity:**  $O(m \cdot n)$ , Maximum Depth of the recursion tree(auxiliary space).

↳ maximum depth of the recursion



```
from typing import List

class Solution:
    # Usage
    def findPathHelper(self, i: int, j: int, a: List[List[int]], n: int, ans: List[str], move: str,
                      vis: List[List[int]]):

        # Base Case
        if i == n - 1 and j == n - 1:
            ans.append(move)
            return

        # downward
        if i + 1 < n and not vis[i + 1][j] and a[i + 1][j] == 1:
            vis[i][j] = 1
            self.findPathHelper(i + 1, j, a, n, ans, move + 'D', vis)
            vis[i][j] = 0

        # left
        if j - 1 >= 0 and not vis[i][j - 1] and a[i][j - 1] == 1:
            vis[i][j] = 1
            self.findPathHelper(i, j - 1, a, n, ans, move + 'L', vis)
            vis[i][j] = 0

        # right
        if j + 1 < n and not vis[i][j + 1] and a[i][j + 1] == 1:
            vis[i][j] = 1
            self.findPathHelper(i, j + 1, a, n, ans, move + 'R', vis)
            vis[i][j] = 0

        # upward
        if i - 1 >= 0 and not vis[i - 1][j] and a[i - 1][j] == 1:
            vis[i][j] = 1
            self.findPathHelper(i - 1, j, a, n, ans, move + 'U', vis)
            vis[i][j] = 0

    def findPath(self, m: List[List[int]], n: int) -> List[str]:
        ans = []
        vis = [[0 for _ in range(n)] for _ in range(n)]

        if m[0][0] == 1:
            self.findPathHelper(0, 0, m, n, ans, "", vis)
        return ans
```

```
import java.util.ArrayList;

public class L21 Maze_1 {
    public static void main(String[] args) {
        System.out.println("L21_Maze_1");
    }
}

// Usage
class Solution {
    # Usage
    private static void solve(int i, int j, int a[][], int n, ArrayList<String> ans, String move,
                             vis[][]):
        if (i == n - 1 && j == n - 1) {
            ans.add(move);
            return;
        }

        // downward
        if (i + 1 < n && vis[i + 1][j] == 0 && a[i + 1][j] == 1) {
            vis[i][j] = 1;
            solve(i + 1, j, a, n, ans, move + 'D', vis);
            vis[i][j] = 0;
        }

        // left
        if (j - 1 >= 0 && vis[i][j - 1] == 0 && a[i][j - 1] == 1) {
            vis[i][j] = 1;
            solve(i, j - 1, a, n, ans, move + 'L', vis);
            vis[i][j] = 0;
        }

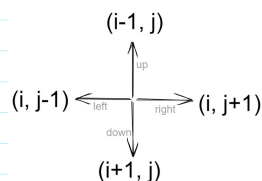
        // right
        if (j + 1 < n && vis[i][j + 1] == 0 && a[i][j + 1] == 1) {
            vis[i][j] = 1;
            solve(i, j + 1, a, n, ans, move + 'R', vis);
            vis[i][j] = 0;
        }

        // upward
        if (i - 1 >= 0 && vis[i - 1][j] == 0 && a[i - 1][j] == 1) {
            vis[i][j] = 1;
            solve(i - 1, j, a, n, ans, move + 'U', vis);
            vis[i][j] = 0;
        }
    }

    # Usage
    public static ArrayList<String> findPath(int[][] a, int n) {
        int vis[][] = new int[n][n];
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                vis[i][j] = 0;
            }
        }

        ArrayList<String> ans = new ArrayList<>();
        if (a[0][0] == 1) solve(0, 0, a, n, ans, move "", vis);
        return ans;
    }
}
```

But, writing an individual code for every direction is a lengthy process therefore we truncate the 4 "if statements" into a single for loop using the following approach.



	D	L	R	U
di[]	+1	+0	+0	-1
dj[]	+0	-1	+1	+0

```

// Optimized Code
// row typing (agor list)

class Solution {
public:
    def solve(self, i: int, j: int, a: List[List[int]], n: int, ans: List[str], move: str, vis: List[List[int]], di: List[int], dj: List[int]):
        if i == n - 1 and j == n - 1:
            ans.append(move)
            return
            dir = "BLRU"
        for ind in range(4):
            nexti = i + di[ind]
            nextj = j + dj[ind]
            if nexti >= 0 and nextj >= 0 and nexti < n and nextj < n and not vis[nexti][nextj] and a[nexti][nextj] == 1:
                vis[i][j] = 1
                self.solve(nexti, nextj, a, n, ans, move + dir[ind], vis, di, dj)
                vis[i][j] = 0

    def findPath(self, a: List[List[int]], n: int) -> List[str]:
        ans = []
        vis = [[0 for _ in range(n)] for _ in range(n)]
        di = [+1, 0, 0, -1]
        dj = [0, -1, 1, 0]
        if a[0][0] == 1:
            self.solve(0, 0, n, n, ans, "", vis, di, dj)
        return ans

```

→ 4 direction

→ wordy calculation

→ More Ballary approach



```

// More Optimized Code
// n is the given matrix and n is the order of matrix
// Usage:
class Solution {
public:
    private static void solve(int i, int j, int a[][], int n, ArrayList<String> ans, String move,
        int vis[][], int di[], int dj[]) {
        if (i == n - 1 && j == n - 1) {
            ans.add(move);
            return;
        }
        String dir = "BLRU";
        for (int ind = 0; ind < 4; ind++) {
            int nexti = i + di[ind];
            int nextj = j + dj[ind];
            if (nexti >= 0 && nextj >= 0 && nexti < n && nextj < n &&
                vis[nexti][nextj] == 0 && a[nexti][nextj] == 1) {
                vis[i][j] = 1;
                solve(nexti, nextj, a, n, ans, move + dir.charAt(ind), vis, di, dj);
                vis[i][j] = 0;
            }
        }
    }
    no usages
    public static ArrayList<String> findPath(int[][] a, int n) {
        int vis[][] = new int[n][n];
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                vis[i][j] = 0;
            }
        }
        int di[] = {
            +1,
            0,
            0,
            -1
        };
        int dj[] = {
            0,
            -1,
            1,
            0
        };
        ArrayList<String> ans = new ArrayList<>();
        if (a[0][0] == 1) solve(0, 0, a, n, ans, "", vis, di, dj);
        return ans;
    }
}

```