

Expectimax Search

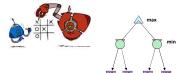
CSE 415: Introduction to Artificial Intelligence University of Washington Spring, 2019

Credit goes to Dan Klein and Pieter Abbeel, Univ. of California, for the slides of this lecture.

Uncertain Outcomes



Worst-Case vs. Average Case



Idea: Uncertain outcomes controlled by chance, not an adversary!

Expectimax Search

- Why wouldn't we know what the result of an action will be?
 Explicit randomness: rolling dice
 Unpredictable opponents: the ghosts respond randomly
 Actions can fall: when moving a robot, wheels might slip

- Values should now reflect average-case (expectimax) outcomes, not worst-case (minimax) outcomes
- Expectimax search: compute the average score under optimal
- Max nodes as in minimax search
- Max houses as in minimax search
 Chance nodes are like min nodes but the outcome is uncertain
 Calculate their expected utilities
 I.e. take weighted average (expectation) of children

- Later, we'll learn how to formalize the underlying uncertain-result problems as Markov Decision Processes

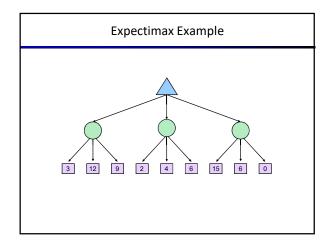
Expectimax Pseudocode def value(state): if the state is a terminal state: return the state's util ty if the next agent is MAX: return max-value(state) if the next agent is EXP: return exp-value(state) def exp-value(state): def max-value(state): initialize v = 0 initialize $v = -\infty$ for each successor of state: for each successor of state: p = probability(successor) v += p * value(successor) v = max(v, value(successor)) return v return v

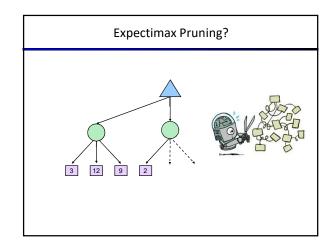
Expectimax Pseudocode

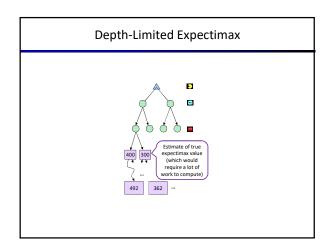
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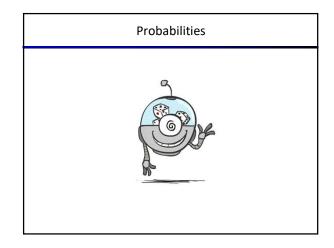


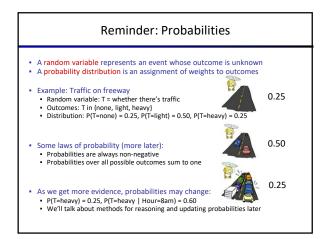
v = (1/2)(8) + (1/3)(24) + (1/6)(-12) = 10

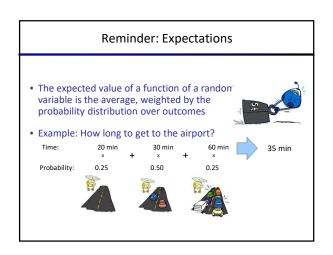


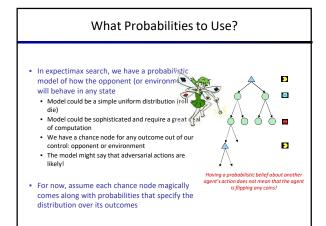


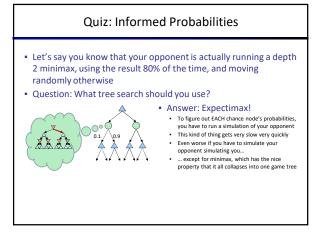


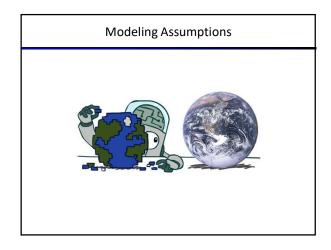


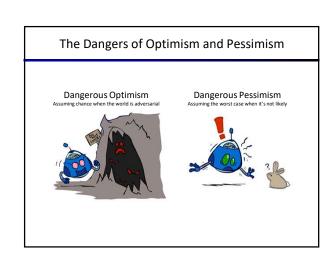


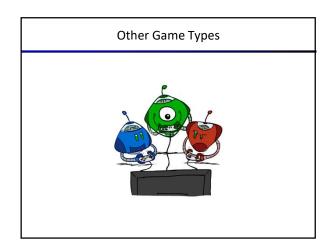


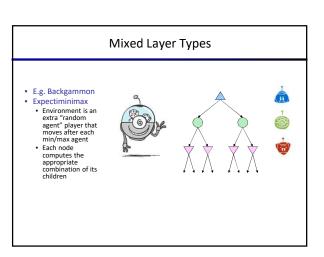












Example: Backgammon

- Dice rolls increase b: 21 possible rolls with 2 dice
 Backgammon ≈ 20 legal moves
 Depth 2 = 20 x (21 x 20)³ = 1.2 x 10³
- As depth increases, probability of reaching a given search node shrinks
 So usefulness of search is diminished
 So limiting depth is less damaging
 But pruning is trickier...
- Historic AI: TDGammon uses depth-2 search + very good evaluation function + reinforcement learning: world-champion level play

• 1st Al world champion in any game!



