

# Species persistence under climate and fishing

Emma Fuller, Eleanor Brush, Malin Pinsky

## 1 Abstract

When the climate changes, the habitat in which organisms can survive and reproduce moves through space. This change does not occur in isolation but rather appears on a background of other disturbances. In order to understand how two disturbances, range shift and harvesting, interact and affect population persistence, we studied an integrodifference model that explicitly included the mechanisms of dispersal and reproduction. If the viable habitat moves too quickly or harvesting pressure is too great, the population is driven extinct. We found the rates of harvesting and environmental shift required to allow the population to persist and studied how these critical parameters depend on the growth rate and dispersal behavior of the population. We then measured the interaction between the stressors. The stressors interact nearly additively: we found very low positive synergy at those levels of the stressors that almost drive the population extinct. Positive synergy suggests that harvesting may aggravate the population's sensitivity to a shifting range. Finally, we introduced two conservation techniques into simulations of the population model – threshold harvest rules and marine protected areas (MPAs) – and found that these approaches could mitigate, under some circumstances, the negative interaction of the two stressors.

**Keywords:** Climate change, fishing, integrodifference model, synergy, multiple

21 disturbances

## 22 **2 Introduction**

23 There are many stressors that can disturb an ecosystem. Ecologists have quantified the  
24 effects of a number of stressors individually [Wilcove et al., 1998, Crain et al., 2008,  
25 Darling and Côté, 2008], but less work has been done to measure the effects of multiple  
26 stressors and the interactions between them. If disturbances interact synergistically, a  
27 perturbation that has little effect when it occurs individually may amplify the disturbance  
28 caused by a coincident perturbation [Crain et al., 2008, Darling and Côté, 2008, Nye et al.,  
29 2013, Gurevitch et al., 2000]. In the most extreme (and worrying) cases, synergistic  
30 interactions between multiple stressors will drive a population extinct even though it could  
31 persist in the face of any single stressor (i.e. Pelletier et al. [2006]). If disturbances interact  
32 antagonistically, on the other hand, the effects of multiple stressors may be less than that  
33 predicted by any stressor individually. Since disturbances rarely occur in isolation, it is  
34 important to measure the synergy between disturbances in order to understand how a  
35 system will be affected by their presence and to understand when multiple disturbances will  
36 drive a population extinct [Doak and Morris, 2010, Fordham et al., 2013, Folt et al., 1999].  
37 Climate change and fishing have been identified as the two largest human impacts on the  
38 ocean [Halpern et al., 2008]. They therefore present an important case study of how  
39 disturbances interact in their effects on biological populations. Further, understanding  
40 these interactions will be crucial to managing populations subjected to both of these  
41 disturbances. Marine fish are already moving in response to climate change [Perry et al.,  
42 2005, Hiddink and ter Hofstede, 2008, Rijnsdorp et al., 2009, Dulvy et al., 2008, Simpson

et al., 2011] and they are projected to continue moving in the future [Kell et al., 2005, Mackenzie et al., 2007]. Species that are likely to undergo or already undergoing shifts in range are also subject to harvesting, in addition to many other disturbances including pollution, ocean acidification, habitat fragmentation, and invasive species [Wilcove et al., 1998, Sala, 2000, Assessment, 2005, Pinsky et al., 2013, Barry et al., 1995, Nye et al., 2009]. Empirical case studies have identified interactions between overfishing and temperature-driven range shifts that suggest synergy in the magnitude of the disturbance [Ling et al., 2009] and have demonstrated synergistic effects in microcosm experiments between warming temperatures, harvesting and connectivity [Mora et al., 2007]. This empirical work underscores the importance of understanding how range shifts and harvesting interact.

A common approach to predicting future population distributions under climate change has been to use bioclimatic-envelope models (also known as species distribution models – SDMs). These statistical models typically correlate presence-absence data with biophysical characteristics such as mean or maximum temperatures, rainfall, or salinity, to explain and predict how species ranges’ will differ under climate change [Elith et al., 2006, Guisan and Thuiller, 2005, Guisan and Zimmermann, 2000]. Despite these models’ widespread adoption, SDMs have frequently been criticized as oversimplified as they lack species interactions, dispersal and reproductive processes [Kearney and Porter, 2009, Zarnetske et al., 2012, Robinson et al., 2011]. Recent work on range shifts has addressed some of these gaps by explicitly including dispersal and reproduction [Berestycki et al., 2009, Zhou and Kot, 2011]. However these models only address one disturbance: that of climate-driven range shifts.

Work considering the joint impacts of climate and fishing often consider climate

fluctuations (large anomalies around the mean) rather than directional changes in climate  
 [Walters and Parma, 1996, King and McFarlane, 2006]. When the effects of climate-driven  
 range shifts on fishing are considered, the models are typically case-specific and detailed,  
 integrating multiple drivers and disturbances [Cheung et al., 2010, Lindegren et al., 2010,  
 Brown et al., 2010, Merino et al., 2010a,b, Plaganyi et al., 2011, Ainsworth et al., 2011,  
 Zhang et al., 2011, Barange et al., 2011, Howard et al., 2013]. These predicted impacts are  
 important for management and conservation planning [Allison et al., 2009], however these  
 models are so complex that understanding the relative importance of particular drivers,  
 disturbances, and interactions is difficult (but see Nye et al. [2013] for an approach using  
 ecosystem-level models to discern relative importance of disturbances). The degree of  
 detail and case-specificity in these studies makes it difficult to draw general conclusions.  
 Here we constructed an analytical model of a fish population subject to both harvesting  
 and climate change-induced range-shift. We explicitly included two mechanistic processes  
 central to species' responses to climate and fishing: reproduction and dispersal. Previous  
 work has highlighted the importance of these two processes and their vulnerability to  
 climate change [Fordham et al., 2013, Hastings et al., 2005]. We found that climate-driven  
 range shifts and fishing interact synergistically, when their effects are measured by absolute  
 drop in biomass. We also found how the threshold level of harvesting that suffices to drive  
 the population extinct depends on how quickly the range is shifting.  
 We also examined the effect of threshold harvesting rules and marine protected areas  
 (MPAs) on species persistence. Protected areas have been suggested as a key form of  
 climate insurance and stepping stones to help species keep up with a changing environment  
 [Thomas et al., 2012, Hannah et al., 2007]. MPAs are frequently recommended for  
 conservation of biodiversity and improved fisheries yield [Gaines et al., 2010a], and we

evaluate whether MPAs established for those purposes could improve species persistence when habitat is shifting rapidly. We found that MPAs can help a species persist with higher harvesting pressure, but does not change the maximum climate velocity with which a species can keep up.

## 3 Methods

We studied the dynamics of a fish population constrained to a single, one-dimensional habitat patch by their inability to reproduce outside of the patch. This viable habitat patch (here after ‘patch’) is shifting at a fixed velocity and fish at each point in space can be harvested. We first measured the drop in biomass caused by range shifts, harvesting, and both stressors together in order to determine whether they interact synergistically. We then determined the climate velocity and harvesting rate that would drive the population extinct. We finally implemented marine protected areas (MPAs) and threshold harvesting rules in numerical simulations of the model to determine how these management strategies affect population persistence.

**3.1 The Model** In the model of Zhou and Kot [2011], the adults from the current year produce offspring according to a recruitment function, and these offspring disperse across the one-dimensional world according to a dispersal kernel to become the next generation’s adults. We extend this model by additionally subjecting the adults to harvesting before they produce offspring so that only a proportion of the fish survive to reproduce. These processes— recruitment, harvesting, and dispersal— are incorporated into an integrodifference model to describe how the population changes over time. If  $n_t(x)$  is the density of fish at position  $x$  at time  $t$ , then the density of fish at the next generation is

113 given by

$$n_{t+1}(x) = \int_{-\frac{L}{2}+ct}^{\frac{L}{2}+ct} k(x-y)f((1-h)n_t(y))dy, \quad (1)$$

114 where  $h$  is the proportion of adults harvested,  $f(n)$  is the recruitment function giving the  
115 number of offspring produced by a population of size  $n$  (accounting for density  
116 dependence),  $k(x-y)$  is the dispersal kernel giving the probability of a larva traveling from  
117 position  $y$  to position  $x$ ,  $L$  is the length of the patch, and  $c$  is the rate at which it shifts  
118 across space. We chose to use a Beverton-Holt recruitment function,

$$f(n_t) = \frac{R_0 n_t}{1 + \left(\frac{R_0-1}{K}\right) n_t}.$$

119 Regardless of the exact functional form of the recruitment function, a critical parameter of  
120 the recruitment function in determining population persistence is how quickly recruitment  
121 increases when the population size is near (but above) 0, which is equivalent to the  
122 intrinsic growth rate,  $R_0 = f'(0)$ . Analyzing this kind of model becomes easier if the  
123 dispersal kernel is separable into its dependence on the source of larvae and its dependence  
124 on the destination of the larvae, i.e. if there are functions  $a_i, b_i$  such that  
125  $k(x-y) = \sum_{i=1}^{\infty} a_i(x)b_i(y)$  and we use such a kernel in our analytical expressions. We  
126 provide a list of variables and functions in Table 1.

127 At equilibrium, the population will be described by a traveling wave, where the density of  
128 fish at a given point in space will change but the density of fish at a location relative to the  
129 shifting patch will not. We sought to describe how the population is distributed over the  
130 viable patch as it shifts through the world in order to study the size of the population at  
131 equilibrium and whether or not the population could persist. The traveling wave  $n^*$  must

132 satisfy

$$n^*(\bar{x}) = \int_{-\frac{L}{2}}^{\frac{L}{2}} k(\bar{x} + c - \bar{y}) f((1 - h)) n^*(\bar{y}) d\bar{y}, \quad (2)$$

133 where  $\bar{x} \in \left[-\frac{L}{2}, \frac{L}{2}\right]$  describes the position within the patch [Zhou and Kot, 2011]. Zhou and  
 134 Kot [2011] only considered whether a shifting environment will drive a population extinct,  
 135 however to quantify the effects of both a shifting environment and harvesting pressure we  
 136 must also find the total biomass in the equilibrium traveling wave. For a separable kernel,  
 137 the equilibrium traveling pulse  $n^*(x)$  must satisfy

$$n^*(x) = \sum_{i=1}^{\infty} a_i(x) \int_{-\frac{L}{2}}^{\frac{L}{2}} b_i(y - c) f((1 - H(n^*(y))) n^*(y)) dy = \sum_{i=1}^{\infty} m_i a_i(x), \quad (3)$$

138 where the  $m_i$  satisfy the recursive equations

$$m_i = \int_{-\frac{L}{2}}^{\frac{L}{2}} b_i(y - c) f\left((1 - h) \sum_{j=1}^{\infty} m_j a_j(x)\right) dy. \quad (4)$$

139 [Latore et al., 1998]. Equation 4 allowed us to find the values of  $m_i$  numerically. We then  
 140 found the total biomass in the equilibrium traveling pulse by using these  $m_i$  and  
 141 integrating Equation 3.

142 **3.2 Calculating Synergy** In order to quantify whether the two stressors are interacting  
 143 additively, synergistically, or antagonistically, we found the total biomass of the population  
 144 when it reached an equilibrium traveling pulse and compared this equilibrium biomass in  
 145 the presence and absence of each stressor individually or the two stressors together.  
 146 We used  $B_0$  to denote the equilibrium biomass without either stressor,  $B_h$  the equilibrium  
 147 biomass with harvesting but a constant environment,  $B_c$  the equilibrium biomass with a

148 shifting environment but no harvesting, and  $B_{\text{hc}}$  the equilibrium biomass with both  
 149 stressors. For each stressor or combination of stressors, we found the drop in biomass  
 150 caused by stressor  $s$ ,

$$E_s = B_0 - B_s.$$

151 If the stressors do not interact, the drop caused by both stressors would be the sum of the  
 152 drops caused by either individually. The synergy is therefore defined as

$$S = E_{\text{hc}} - (E_{\text{h}} + E_{\text{c}}).$$

153 If the stressors aggravate each other, the effect of both stressors is worse than would be  
 154 expected from considering either stressor individually, and synergy is positive. If the  
 155 stressors alleviate each other, the effect of both stressors is better than would be expected  
 156 from considering either stressor individually, and synergy is negative. If the effect of both  
 157 stressors is exactly as expected from considering either stressor individually, there is no  
 158 interaction and no synergy.

159 **3.3 Persistence** One possible equilibrium traveling wave that solves Equation 2 is the  
 160 ‘trivial’ traveling pulse,  $n^*(\bar{x}) = 0$  for all  $x \in \left[-\frac{L}{2}, \frac{L}{2}\right]$ , i.e. a patch with no fish in it. If a  
 161 population becomes very small (or if we introduce a small population), one of two things  
 162 can happen. First, the population may crash and the trivial traveling pulse without any  
 163 fish may appear again. Second, those small numbers may increase and form a stable  
 164 population. In this sense, a small population can be thought of as a perturbation to the  
 165 trivial traveling pulse. If the trivial pulse is stable, the system will return to the trivial



166 pulse even after a perturbation in the form of the introduction of a small population. If a  
 167 population is to persist, even when it is small it must be able to avoid extinction and grow.  
 168 For this to be the case, the trivial pulse must be unstable to small perturbations.  
 169 We would like to know the rate of environmental shift and the harvesting rate such that as  
 170 long as the environment moves more slowly or we harvest less severely than those  
 171 parameters, then the population will be able to persist. We call these, respectively, the  
 172 critical rate of environmental shift,  $c^*$ , and the critical harvesting rate,  $h^*$ . We found these  
 173 rates by finding the parameters that make the trivial pulse unstable. In our analyses, as in  
 174 [Latore et al., 1998], we used the separable Gaussian kernel given by

$$k(x - y) = \frac{1}{2\sqrt{D\pi}} e^{\frac{-(x-y)^2}{4D}}.$$

175 To find analytical results about the Gaussian kernel, we approximated the kernel, as  
 176 described in the Appendix. Analytical results for a separable sinusoidal kernel are also  
 177 described in the Appendix. We used simulations to analyze a Laplace dispersal kernel that  
 178 is not amenable to this method, as described below.  
 179 For each kernel, the population's ability to persist depends on properties of the population  
 180 itself– the expected distance a larva disperses ( $\langle d \rangle$ ) and the intrinsic growth rate ( $R_0$ );  
 181 properties of the environment– the length of the viable patch ( $L$ ) and how quickly the  
 182 environment is shifting ( $c$ ); and the harvesting rate ( $h$ ). Whereas equilibrium biomass  
 183 depends on the function form of recruitment, population persistence only depends on the  
 184 intrinsic growth rate  $R_0$ . If the environment shifts more quickly than the critical rate  $c^*$  or  
 185 the population is harvested at more than the critical rate  $h^*$  then the population will not  
 186 be able to persist, as described in the Appendix. For a Gaussian kernel, the critical rates  $c^*$

187 and  $h^*$  are those values of  $c$  and  $h$  such that

$$R_0(1-h)2\sqrt{2}\exp\left(\frac{-c^2}{8D}\right)\left[\operatorname{erf}\left(\frac{L-c}{2\sqrt{2D}}\right)-\operatorname{erf}\left(\frac{-L-c}{2\sqrt{2D}}\right)\right]=1.$$

188 A similar expression for a sinusoidal kernel is derived in the appendix. For both kernels,  
189 the critical harvesting proportion can be approximated by a function that looks like

$$h^* \sim 1 - \frac{1}{R_0} \cdot C(L, R_0) f(\langle d \rangle, c^2, L^2 + 3c^2), \quad (5)$$

190 where  $C(L, R_0)$  is a decreasing function of the length of the viable patch and the intrinsic  
191 growth rate.

192 **3.4 Simulations** We used simulations to extend the basic integrodifference model in two  
193 ways that make it analytically intractable. First, we examined the sensitivity of the model  
194 to choice of dispersal kernel by using the Laplace dispersal kernel,

$$k(x-y) = \frac{1}{2} b e^{-b|x-y|},$$

195 a commonly used model of larval dispersal [?]. Second, we examined harvesting rules more  
196 complex than harvesting a constant proportion of the population. Whereas population  
197 persistence in the analytical model does not depend on the functional form of recruitment  
198  $f$ , to perform simulations we must specify a recruitment function. Again, we chose to use a  
199 Beverton-Holt function. In the first generation, we seeded the world with 50 individuals at  
200 a single point, as in [Zhou and Kot, 2011]. We first ran through 150 generations in order  
201 for the population to reach equilibrium without harvesting or climate shift. We then added  
202 harvesting pressure, allowed the population to again reach equilibrium, and finally added

climate change by moving the viable patch. Equilibrium biomass is calculated as the mean biomass of 300 time steps once the difference in biomass between time step  $t$  and  $t + 1$  was no greater than 0.1.

We added harvesting pressure by harvesting a constant proportion of the population, in order to confirm our analytical results. We then evaluated the effect of a threshold harvest rule and marine protected areas (MPAs). With a threshold rule, we evaluated the population at each point in space to determine how much harvesting should occur. If the population abundance was below the designated threshold, no harvesting occurred. If the population exceeded the threshold, then a proportion of the ‘surplus’ individuals were harvested.

MPAs are a form of management designed to check the impact of fishing on targeted populations and are typically designed to meet either conservation or fishery management goals [Agardy, 1994, Holland and Brazee, 1996, Gaines et al., 2010b]. To implement an MPA management strategy in our model, we examine the effect of both of these commonly advocated approaches. While both conservation and fisheries oriented MPA schemes align in their goal of maintaining a sustainable fished population, they differ in desired level of adult spillover. Fisheries-oriented MPAs are often designed such that they maximize adult spillover into fishable areas by creating many small reserves closely spaced [Hastings and Botsford, 2003]. The converse of this is the goal of conservation-oriented MPAs which seek to reduce adult spillover by minimizing the ratio between the reserve edge length relative to area protected [Gaines et al., 2010b].

Networks of MPAs were introduced into our simulations by designating segments of space in which harvesting was forbidden (i.e. harvesting rates were equal to 0).

Conservation-oriented MPAs, are frequently large and rarely part of a larger network of

reserves [Hastings and Botsford, 2003]. For solitary reserves to be successful at protecting target species, they must encompass self-sustaining fish populations [Hastings and Botsford, 2006, Gaines et al., 2010b]. As such modeling studies estimate that isolated reserves must be at least as large as the average dispersal distance for the targeted fish species [Lockwood et al., 2002, Hastings and Botsford, 2003, Botsford et al., 2001, Gaines et al., 2010a]. To implement conservation MPAs we created reserves with a length of 4 times the average dispersal distance and had a distance of 8 times the average dispersal distance between them to ensure that populations would be self sustaining and not dependent on other dispersal for other reserves [Lockwood et al., 2002].

Previous work has shown that if MPAs are to benefit fisheries, the reserves should be broken into a network, closely spaced to maximize adult spillover into fishable areas and export of larvae from reserve to reserve [Hastings and Botsford, 2003, Gaylord et al., 2005, Gaines et al., 2010b]. To mimic this management scheme, MPAs had a length of  $\frac{1}{3}$  of the average dispersal distance and had a distance of  $\frac{2}{3}$  of the average dispersal distance between them.

## 4 Results

**4.1 Interactions Between Stressors** We found very low levels of positive synergy between the two stressors in our analysis of the Gaussian kernel (Figure 2). Where there is positive synergy, a doubly stressed population loses more biomass than would be predicted from either stressor individually. The stressors interact most strongly when they are both high, shortly before they drive the population extinct. However, the excess loss in biomass is extremely low, making it difficult to distinguish positive synergy from additive

interactions. We found similar analytical results for a sinusoidal dispersal kernel and our simulations with a Laplace kernel produce similar results which indicates that this result is robust to changes in the dispersal kernel.

As the harvesting rate  $h$  increases, the critical rate of environmental shift  $c^*$  decreases: the environment must move more slowly to accommodate the population growing more slowly (Figure 1). Conversely, as the rate of environmental shift  $c$  increases, the critical harvesting rate  $h^*$  decreases (Figure 1). This means that a harvesting rate that is sustainable in the absence of environmental shift may no longer be sustainable if the environment starts shifting. When the harvesting pressure has exceeded the critical harvesting rate  $h^*$  or the environment is shifting more quickly than the critical rate of environmental shift  $c^*$ , the biomass of the population at equilibrium will be equal to 0. Before those thresholds are reached, the equilibrium biomass of the population decreases as either the harvesting pressure increases or the environmental shifts more quickly (Figure 1). The simulations replicate the analytical results with the critical speed  $c^*$  declining as the critical harvest rate  $h^*$  increases and vice versa (Figure 3a).

It is always the case that increasing the intrinsic growth rate,  $R_0$ , of the population increases the critical speed  $c^*$  and the critical harvesting rate  $h^*$ , since a population that grows more quickly can recover more quickly from losses caused by these disturbances. However, whether or not dispersing farther is better depends on how quickly the environment is shifting (Figure 1). When the environment is shifting slowly, dispersing farther is detrimental since many larvae will disperse too far away from the viable patch. When the environment is shifting quickly, on the other hand, dispersing farther can help the population persist because some larvae will disperse into the space that will become viable shortly in the future. This affects the critical harvesting rate: at a low rate of

environmental shift, populations that disperse less can be harvested more severely than those that disperse further, whereas at a high rate of environmental shift, populations that disperse further can be harvested more severely.

**4.2 Management Strategies** We found that when thresholds are in place, the harvesting rate no longer determines the critical rate of environmental shift  $c^*$  (Figure 3). We also examined the effect of marine protected areas (MPAs) on the population's persistence to see whether it might extend the range of harvesting and climate change parameters where the fish population could survive. With MPAs in place, the population had a slightly higher abundance along the edges of the patch where the population is limited by harvesting, which translated into a slightly increased critical harvest rate (Figure 3).

## 5 Discussion

Knowing whether two disturbances interact in their impacts for a given population is important for management. The co-occurrence of climate change-driven range shifts and fishing mean that there is the potential for synergistic interactions, which have been largely unexamined. Here we have built a general model to examine how climate and harvesting interact to affect species persistence by incorporating dispersal and reproduction. To quantify the interaction between the stressors, we measured the synergy between their effects on population biomass. We found positive synergy between the stressors and that the synergy is greatest in the region of parameter space where the equilibrium biomass is smallest. We found similar results from the analytically derived biomass and the simulation derived biomass. This indicates that this result is robust to changes in the dispersal kernel.

295 We chose to measure the effect of each stressor by the absolute drop in biomass caused by  
 296 the stressor, and we used the sum of the individual effects for our null prediction of the  
 297 effect of both stressors, as in [Crain et al., 2008, Darling and Côté, 2008, Nye et al., 2013].  
 298 We could also have measured the effect by the percentage drop caused by the stressor(s)  
 299 and used a multiplicative null prediction for the effect of both stressors. In general,  
 300 measuring synergy against an additive null prediction is more conservative than measuring  
 301 synergy multiplicatively: the presence of additive synergy implies multiplicative synergy,  
 302 but not vice versa [Crain et al., 2008, Folt et al., 1999]. Since we found small levels of  
 303 positive additive synergy between the two stressors, other measures of synergy might show  
 304 even higher levels of interaction.

305 While we did find synergy between the stressors, the drop in biomass caused by both  
 306 stressors was never very much higher than the null prediction, i.e. synergistic effects were  
 307 quite small. However, the fact that synergy is highest in those populations whose  
 308 persistence is most tenuous is worrisome from a conservation perspective. Additionally, the  
 309 fact that we found additive synergy means that harvesting levels or rate of environment  
 310 shift that are sustainable individually together can drive a population to extinction.

311 Synergy between harvesting and climate changes has been identified in experimental  
 312 populations [Mora et al., 2007], in specific populations [Planque et al., 2010], and at the  
 313 ecosystem level [Kirby et al., 2009, Planque et al., 2010]. However, these results are not  
 314 directly comparable to ours because they focus on different aspects of climate change, e.g.  
 315 warming temperature [Mora et al., 2007, Kirby et al., 2009] or a more variable climate  
 316 [Planque et al., 2010]. Additionally, in the experimental populations, synergy was identified  
 317 between warming and harvesting but not between habitat fragmentation [Mora et al.,  
 318 2007]. Nevertheless, our results generally agree with these empirical findings and it is

therefore important to take the effects of both stressors into consideration when designing conservation and management strategies.

We also derived expressions for critical harvesting rates and critical rates of environmental shift for a separable Gaussian kernel and found these critical rates using numerical simulations of a Laplace kernel. For each kernel we studied, we found that the higher the growth rate and the better the mean dispersal distance matches the rate of environmental shift, the better a population can adjust to harvest and climate change. More interestingly, we found a negative relationship between the critical harvesting rate and the rate of environmental shift. That is, the more quickly the environment shifts the less harvesting it takes to drive the population extinct. The curved line separating parameters that will allow the population to persist from those that won't is another indication of an interaction between the stressors.

Our results suggest that particular combinations of harvesting and rate of environmental shift will affect some species more than others. As shown in Figure 1, species with a shorter generation time and a longer average dispersal distance will better track a high rate of environmental shift relative to a species that has a long generation time and short dispersal distance. This is in agreement with empirical work which has found that fish which shifted in response to warming in North Sea had faster life histories than non shifting species (smaller body sizes, faster maturation, smaller sizes at maturity) [Perry et al., 2005].

We also examined whether frequently recommended management approaches ensure species persistence. We found increases in the population's biomass at equilibrium and an improved ability to persist. Protected areas have been advanced as a way to help organisms keep pace with range shifts, as well as to ameliorate anthropogenic disturbances like harvesting and habitat fragmentation [Lawler et al., 2010, Hannah et al., 2007,



Botsford et al., 2001, Gaylord et al., 2005, Hastings and Botsford, 2003, Thomas et al., 2012]. Our results, that spatial management increased the maximum harvesting rate at which the population could survive, support the idea that MPAs could be used to reduce the impact of harvesting. However we did not find any evidence that MPAs increased the climate velocity under which the population could persist. The second management approach we investigated, harvesting thresholds, are already widely implemented in fisheries management, and we found that this management tactic alleviates interactions between the two stressors. While the management strategies only change harvesting practices and do not directly address the effects of climate change, understanding how they ameliorate synergistic affects between harvesting and range shifts will help to better implement harvesting rules and place protected areas.

The advantage of a simple model like ours is that it is general enough to be applied to a number of systems. However, it ignores many of the complexities present in marine fisheries. We do not include Allee effects, so that even if the population shrank to very low levels it was possible for it to persist over time. However, we found that qualitatively similar results about the interaction between climate and harvesting would hold for a model with a recruitment function with Allee effect. We also did not include age structure in our model. The effects of both harvesting and climate change may be different across different age classes; including this level of complexity is left for future work. Similarly, we did not include any mechanisms aside from larval dispersal by which the population could keep up with a shifting climate. Besides these species-specific extensions, this modeling framework could be extended to consider species interactions, especially predator-prey pairs. By introducing a predatory species, we would be imposing yet another stressor on the focus species [Ling et al., 2009, Gurevitch et al., 2000]and we are interested in

measuring the interaction between the effects of this stressor and the two we consider here. Using a simple mechanistic model like the one we present here provides a useful framework for incorporating additional ecological complexities which can mediate species persistence under multiple disturbances. Exploring how species interactions, age structure, and additional disturbances (i.e. pollution, disease, physiological response to temperature) affect population viability will improve our predictions and help us to understand whether species will persist under predicted climate and harvesting regimes. Finally, this work can help make general predictions as to whether specific life histories are likely to be selected over others as harvesting and/or range shifts increase.

## Acknowledgements

We thank Catherine Offord and Will Scott for their contributions to an earlier version of this manuscript.

## References

- M. Tundi Agardy. Advances in marine conservation: the role of marine protected areas. *Trends in Ecology & Evolution*, 9(7):267–270, 1994. ISSN 0169-5347.
- C. H. . H. Ainsworth, J. F. . F. Samhour, D. S. . S. Busch, W. W. L. Cheung, J. Dunne, and T. A. . A. Okey. Potential impacts of climate change on northeast pacific marine foodwebs and fisheries. *ICES Journal of Marine Science*, 68(6):1217–1229, 7 2011. ISSN 1054-3139. doi: 10.1093/icesjms/fsr043.
- Edward H. Allison, Allison L. Perry, Marie-Caroline . C. Badjeck, W. Neil Adger, Katrina Brown, Declan Conway, Ashley S. Halls, Graham M. Pilling, John D. Reynolds, Neil L. Andrew, and Nicholas K. Dulvy. Vulnerability of national economies to the impacts of climate change on fisheries. *Fish and Fisheries*, 10(2):173–196, 6 2009. ISSN 14672960. doi: 10.1111/j.1467-2979.2008.00310.x.

- Millennium Ecosystem Assessment. *Ecosystems and human well-being*, volume 5. Island Press Washington, DC, 2005.
- Manuel Barange, Icarus Allen, Eddie Allison, Marie-Caroline Badjeck, Juila Blanchard, Benjamin Drakeford, Nicholas K. Dulvy, James Harle, Robert Holmes, Jason Holt, Simon Jennings, Jason Lowe, Gorka Merino, Christian Mullan, Graham Pilling, Lynda Rodwell, Emma Tompkins, Francisco Werner, and KL Cochrane. *Response of ocean ecosystems to climate warming*, volume 18, page 440. Wiley-Blackwell, New Jersey, 2011. doi: 10.1029/2003GB002134.
- J. P. Barry, C. H. Baxter, and S. E. Gilman. Climate-related, long-term faunal changes in a california rocky intertidal community. *Science*, 267(5198):672–675, 1995.
- H. Berestycki, O. Diekmann, C. J. Nagelkerke, and P. A. Zegeling. Can a species keep pace with a shifting climate? *Bull Math Biol*, 71(2):399–429, 2 2009. ISSN 1522-9602. doi: 10.1007/s11538-008-9367-5.
- Louis W. Botsford, Alan Hastings, and Steven D. Gaines. Dependence of sustainability on the configuration of marine reserves and larval dispersal distance. *Ecology Letters*, 4: 144–150, 2001. ISSN 1461-0248.
- Louis W. Botsford, Matthew D. Holland, Jameal F. Samhouri, J. Wilson White, and Alan Hastings. Importance of age structure in models of the response of upper trophic levels to fishing and climate change. *ICES Journal of Marine Science: Journal du Conseil*, 68(6): 1270–1283, 2011.
- C. J. Brown, E. A. Fulton, A. J. Hobday, R. J. Matear, H. P. Possingham, C. Bulman, V. Christensen, R. E. Forrest, P. C. Gehrke, N. A. Gribble, S. P. Griffiths, H. Lozano-Montes, J. M. Martin, S. Metcalf, T. A. Okey, R. Watson, and A. J. Richardson. Effects of climate-driven primary production change on marine food webs: implications for fisheries and conservation. *Global Change Biology*, 16(4):1194–1212, 4 2010. ISSN 13541013. doi: 10.1111/j.1365-2486.2009.02046.x.
- William WL Cheung, Vicky WY Lam, Jorge L. Sarmiento, Kelly Kearney, R. E. G. Watson, Dirk Zeller, and Daniel Pauly. Large-scale redistribution of maximum fisheries catch potential in the global ocean under climate change. *Global Change Biology*, 16(1):24–35, 2010. ISSN 1354-1013.
- Caitlin Mullan Crain, Kristy Kroeker, and Benjamin S. Halpern. Interactive and cumulative effects of multiple human stressors in marine systems. *Ecol Lett*, 11(12):1304–15, 12 2008. ISSN 1461-0248. doi: 10.1111/j.1461-0248.2008.01253.x.
- Emily S. Darling and Isabelle M. Côté. Quantifying the evidence for ecological synergies. *Ecol Lett*, 11(12):1278–86, 12 2008. ISSN 1461-0248. doi: 10.1111/j.1461-0248.2008.01243.x.
- Daniel F. Doak and William F. Morris. Demographic compensation and tipping points in climate-induced range shifts. *Nature*, 467(7318):959–62, 10 2010. ISSN 1476-4687. doi: 10.1038/nature09439.

- Nicholas K. Dulvy, Stuart I. Rogers, Simon Jennings, Vanessa Stelzenmiller, Stephen R. Dye, and Hein R. Skjoldal. Climate change and deepening of the north sea fish assemblage: a biotic indicator of warming seas. *Journal of Applied Ecology*, 45(4):1029–1039, 8 2008. ISSN 00218901. doi: 10.1111/j.1365-2664.2008.01488.x.
- Jane Elith, Catherine H. Graham, Robert P Anderson, Miroslav Dudík, Simon Ferrier, Antoine Guisan, Robert J Hijmans, Falk Huettmann, John R Leathwick, Anthony Lehmann, Jin Li, and Lucia G Lohmann. Novel methods improve prediction of species’ distributions from occurrence data. *Ecography*, 29(2):129–151, 2006.
- C. L. Folt, C. Y. Chen, M. V. Moore, and J. Burnaford. Synergism and antagonism among multiple stressors. *Limnology and Oceanography*, 44(3):864–877, 1999.
- D. A. . A. Fordham, C. Mellin, B. D. . D. Russell, H. R. . R. Akçakaya, C. J. A. Bradshaw, M. E. . E. Aiello-Lammens, MJ J. Caley, S. D. . D. Connell, S. Mayfield, S. A. . A. Shepherd, and B. W. . W. Brook. Population dynamics can be more important than physiological limits for determining range shifts under climate change. *Global Change Biology*, page n/a, 6 2013. doi: 10.1111/gcb.12289.
- Steven D. Gaines, Sarah E. Lester, Kirsten Grorud-Colvert, Christopher Costello, and Richard Pollnac. Evolving science of marine reserves: new developments and emerging research frontiers. *Proc Natl Acad Sci U S A*, 107(43):18251–5, 10 2010a. ISSN 1091-6490. doi: 10.1073/pnas.1002098107.
- Steven D. Gaines, Crow White, Mark H. Carr, and Stephen R. Palumbi. Designing marine reserve networks for both conservation and fisheries management. *Proc Natl Acad Sci U S A*, 107(43):18286–93, 10 2010b. ISSN 1091-6490. doi: 10.1073/pnas.0906473107.
- Brian Gaylord, Steven D. Gaines, David A. Siegel, and Mark H. Carr. Marine reserves exploit population structure and life history in potentially improving fisheries yields. *Ecological Applications*, 15(6):2180–2191, 2005.
- Antoine Guisan and Wilfried Thuiller. Predicting species distribution: offering more than simple habitat models. *Ecology Letters*, 8(9):993–1009, 9 2005. ISSN 1461-023X. doi: 10.1111/j.1461-0248.2005.00792.x.
- Antoine Guisan and Niklaus E. Zimmermann. Predictive habitat distribution models in ecology. *Ecological modelling*, 135(2):147–186, 2000.
- Jessica Gurevitch, Janet A. Morrison, and Larry V. Hedges. The interaction between competition and predation: A metaanalysis of field experiments. *The American Naturalist*, 155(4):435–453, 4 2000. ISSN 0003-0147. doi: 10.1086/303337.
- Benjamin S. Halpern, Shaun Walbridge, Kimberly A. Selkoe, Carrie V. Kappel, Fiorenza Micheli, Caterina D’Agrosa, John F. Bruno, Kenneth S. Casey, Colin Ebert, Helen E. Fox, Rod Fujita, Dennis Heinemann, Hunter S. Lenihan, Elizabeth M. P. Madin, Matthew T. Perry, Elizabeth R. Selig, Mark Spalding, Robert Steneck, and Reg Watson. A global map of human impact on marine ecosystems. *Science*, 319(5865):948–52, 2 2008. ISSN 1095-9203. doi: 10.1126/science.1149345.

- Lee Hannah, Guy Midgley, Sandy Andelman, Miguel Araújo, Greg Hughes, Enrique Martinez-Meyer, Richard Pearson, and Paul Williams. Protected area needs in a changing climate. *Frontiers in Ecology and the Environment*, 5(3):131–138, 2007.
- Alan Hastings and Louis W. Botsford. Comparing designs of marine reserves for fisheries and for biodiversity. *Ecological Applications*, 13(sp1):65–70, 2003.
- Alan Hastings and Louis W. Botsford. Persistence of spatial populations depends on returning home. *Proceedings of the National Academy of Sciences*, 103(15):6067–6072, 2006.
- Alan Hastings, Kim Cuddington, Kendi F. Davies, Christopher J. Dugaw, Sarah Elmendorf, Amy Freestone, Susan Harrison, Matthew Holland, John Lambrinos, Urmila Malvadkar, Brett A. Melbourne, Kara Moore, Caz Taylor, and Diane Thomson. The spatial spread of invasions: new developments in theory and evidence. *Ecology Letters*, 8(1):91–101, 2005. ISSN 14610248. doi: 10.1111/j.1461-0248.2004.00687.x.
- J. G. Hiddink and R. ter Hofstede. Climate induced increases in species richness of marine fishes. *Global Change Biology*, 14(3):453–460, 3 2008. ISSN 1354-1013. doi: 10.1111/j.1365-2486.2007.01518.x.
- Daniel S. Holland and Richard J. Brazee. Marine reserves for fisheries management. *Marine Resource Economics*, 11:157–172, 1996.
- Jennifer Howard, Eleanora Babij, Roger Griffis, Brian Helmuth, Stewart Allen, Guillermo Auad, Russell Beard, Mary Boatman, Nicholas Bond, Timothy Boyer, David Brown, Patricia Clay, Katherine Crane, Scott Cross, Michael Dalton, Jordan Diamond, Robert Diaz, Quay Dortch, Emmett Duffy, Deborah Fauquier, William Fisher, Michael Graham, Benjamin Halpern, Lara Hansen, Bryan Hayum, Samuel Herrick, Anne Hollowed, David Hutchins, Elizabeth Jewett, Di Jin, Nancy Knowlton, Dawn Kotowicz, Trond Kristiansen, Peter Little, Cary Lopez, Philip Loring, Rick Lumpkin, Amber Mace, Katheryn Mengerink, J. Ru Moorison, Jason Murray, Karma Norman, James O’Donnell, James Overland, Rost Parsons, Neal Pettigrew, Lisa Pfeiffer, Emily Pidgeon, Mark Plummer, Jeffrey Polovina, Josie Quintrell, Teresa Rowles, Jeffrey Runge, Michael Rust, Eric Sanford, Ewe Send, Merrill Singer, Cameron Speir, Diane Stanitski, Carol Thornber, Cara Wilson, and Yan Xue. Oceans and marine resources in a changing climate. Technical report, Oceanography and Marine Biology: An Annual Review, 2013.
- Michael Kearney and Warren Porter. Mechanistic niche modelling: combining physiological and spatial data to predict species’ ranges. *Ecol Lett*, 12(4):334–50, 4 2009. ISSN 1461-0248. doi: 10.1111/j.1461-0248.2008.01277.x.
- L. Kell, G. Pilling, and C. O’Brien. Implications of climate change for the management of north sea cod (gadus morhua). *ICES Journal of Marine Science*, 62(7):1483–1491, 10 2005. ISSN 10543139. doi: 10.1016/j.icesjms.2005.05.006.
- J. R. King and G. A. McFarlane. A framework for incorporating climate regime shifts into the management of marine resources. *Fisheries Management and Ecology*, 13(2):93–102, 2006.

- Richard R. Kirby, Gregory Beaugrand, and John A. Lindley. Synergistic effects of climate and fishing in a marine ecosystem. *Ecosystems*, 12:548–556, 2009.
- J. Latore, P. Gould, and A. M. Mortimer. Spatial dynamics and critical patch size of annual plant populations. *Journal of Theoretical Biology*, 190(3):277–285, 1998.
- Joshua J. Lawler, Timothy H. Tear, Chris Pyke, M. Rebecca Shaw, Patrick Gonzalez, Peter Kareiva, Lara Hansen, Lee Hannah, Kirk Klausmeyer, Allison Aldous, Craig Bienz, and Sam Pearsall. Resource management in a changing and uncertain climate. *Frontiers in Ecology and the Environment*, 8(1):35–43, 2 2010. ISSN 1540-9295. doi: 10.1890/070146.
- Martin Lindegren, Christian Möllmann, Anders Nielsen, Keith Brander, Brian R. MacKenzie, and Nils Chr Stenseth. Ecological forecasting under climate change: the case of baltic cod. *Proc Biol Sci*, 277(1691):2121–30, 7 2010. ISSN 1471-2954. doi: 10.1098/rspb.2010.0353.
- S. D. Ling, C. R. Johnson, S. D. Frusher, and K. R. Ridgway. Overfishing reduces resilience of kelp beds to climate-driven catastrophic phase shift. *Proceedings of the National Academy of Sciences*, 106(52):22341–22345, 2009.
- Dale R. Lockwood, Alan Hastings, and Louis W. Botsford. The effects of dispersal patterns on marine reserves: does the tail wag the dog? *Theor Popul Biol*, 61(3):297–309, 5 2002. ISSN 0040-5809. doi: 10.1006/tpbi.2002.1572.
- Brian R. Mackenzie, Henrik Gislason, Christian Möllmann, and Friedrich W. Köster. Impact of 21st century climate change on the baltic sea fish community and fisheries. *Global Change Biology*, 13(7):1348–1367, 7 2007. ISSN 1354-1013. doi: 10.1111/j.1365-2486.2007.01369.x.
- Gorka Merino, Manuel Barange, and Christian Mullan. Climate variability and change scenarios for a marine commodity: Modelling small pelagic fish, fisheries and fishmeal in a globalized market. *Journal of Marine Systems*, 81(1–2):196 – 205, 2010a. ISSN 0924-7963. doi: 10.1016/j.jmarsys.2009.12.010. URL <http://www.sciencedirect.com/science/article/pii/S0924796309003480>.
- Gorka Merino, Manuel Barange, Christian Mullan, and Lynda Rodwell. Impacts of global environmental change and aquaculture expansion on marine ecosystems. *Global Environmental Change*, 20(4):586–596, 10 2010b. ISSN 09593780. doi: 10.1016/j.gloenvcha.2010.07.008.
- Camilo Mora, Rebekka Metzger, Audrey Rollo, and Ransom A. Myers. Experimental simulations about the effects of overexploitation and habitat fragmentation on populations facing environmental warming. *Proc Biol Sci*, 274(1613):1023–8, 4 2007. ISSN 0962-8452. doi: 10.1098/rspb.2006.0338.
- Janet A. Nye, Jason S. Link, Jonathan A. Hare, and William J. Overholtz. Changing spatial distribution of fish stocks in relation to climate and population size on the northeast united states continental shelf. *Marine Ecology Progress Series*, 393:111–129, 10 2009. ISSN 0171-8630. doi: 10.3354/meps08220.

- Janet A. Nye, Robert J. Gamble, and Jason S. Link. The relative impact of warming and removing top predators on the northeast us large marine biotic community. *Ecological Modelling*, 264:157–168, 8 2013. ISSN 03043800. doi: 10.1016/j.ecolmodel.2012.08.019.
- E. Pelletier, P. Sargian, J. Payet, and S. Demers. Ecotoxicological effects of combined uvb and organic contaminants in coastal waters: a review. *Photochemistry and photobiology*, 82(4):981–993, 2006. ISSN 0031-8655.
- Allison L. Perry, Paula J. Low, Jim R. Ellis, and John D. Reynolds. Climate change and distribution shifts in marine fishes. *Science*, 308:1912–1915, 2005.
- Malin L. Pinsky, Boris Worm, Michael J. Fogarty, Jorge L. Sarmiento, and Simon A. Levin. Marine taxa track local climate velocities. *Science*, 341(6151):1239–42, 9 2013. ISSN 1095-9203. doi: 10.1126/science.1239352.
- E. E. . E. Plaganyi, S. J. . J. Weeks, T. D. . D. Skewes, M. T. . T. Gibbs, E. S. . S. Poloczanska, A. Norman-Lopez, L. K. . K. Blamey, M. Soares, and W. M. L. Robinson. Assessing the adequacy of current fisheries management under changing climate: a southern synopsis. *ICES Journal of Marine Science*, 68(6):1305–1317, 7 2011. ISSN 1054-3139. doi: 10.1093/icesjms/fsr049.
- Benjamin Planque, Jean-Marc Fromentin, Philippe Cury, Kenneth F. Drinkwater, Simon Jennings, R. Ian Perry, and Souad Kifani. How does fishing alter marine populations and ecosystems sensitivity to climate? *Journal of Marine Systems*, 79:403–417, 2010.
- A. D. . D. Rijnsdorp, M. A. . A. Peck, G. H. . H. Engelhard, C. Mollmann, and J. K. . K. Pinnegar. Resolving the effect of climate change on fish populations. *ICES Journal of Marine Science*, 66(7):1570–1583, 8 2009. ISSN 1054-3139. doi: 10.1093/icesjms/fsp056.
- L. M. . M. Robinson, J. Elith, A. J. . J. Hobday, R. G. . G. Pearson, B. E. . E. Kendall, H. P. . P. Possingham, and A. J. . J. Richardson. Pushing the limits in marine species distribution modelling: lessons from the land present challenges and opportunities. *Global Ecology and Biogeography*, 20(6):789–802, 11 2011. doi: 10.1111/j.1466-8238.2010.00636.x.
- Tristan Rouyer, Alexander Sadykov, Jan Ohlberger, and Nils Chr Stenseth. Does increasing mortality change the response of fish populations to environmental fluctuations? *Ecol Lett*, 15(7):658–65, 7 2012. ISSN 1461-0248. doi: 10.1111/j.1461-0248.2012.01781.x.
- O. E. . E. Sala. Global biodiversity scenarios for the year 2100. *Science*, 287(5459):1770–1774, 3 2000. ISSN 00368075. doi: 10.1126/science.287.5459.1770.
- Stephen D. Simpson, Simon Jennings, Mark P. Johnson, Julia L. Blanchard, Pieter-Jan J. Schön, David W. Sims, and Martin J. Genner. Continental shelf-wide response of a fish assemblage to rapid warming of the sea. *Curr Biol*, 21(18):1565–70, 9 2011. ISSN 1879-0445. doi: 10.1016/j.cub.2011.08.016.
- Chris D. Thomas, Phillipa K. Gillingham, Richard B. Bradbury, David B. Roy, Barbara J. Anderson, John M. Baxter, Nigel A. D. Bourn, Humphrey Q. P. Crick, Richard A. Findon,

Richard Fox, Jenny A. Hodgson, Alison R. Holt, Mike D. Morecroft, Nina J. O’Hanlon,  
Tom H. Oliver, James W. Pearce-Higgins, Deborah A. Procter, Jeremy A. Thomas,  
Kevin J. Walker, Clive A. Walmsley, Robert J. Wilson, and Jane K. Hill. Protected  
areas facilitate species’ range expansions. *Proc Natl Acad Sci U S A*, 109(35):14063–8, 8  
2012. ISSN 1091-6490. doi: 10.1073/pnas.1210251109.

Carl Walters and Ana M. Parma. Fixed exploitation rate strategies for coping with effects  
of climate change. *Canadian Journal of Fisheries and Aquatic Sciences*, 53(1):148–158,  
1996. URL 2.

David S. Wilcove, David Rothstein, Jason Dubow, Ali Phillips, and Elizabeth Losos. Quan-  
tifying threats to imperiled species in the united states. *BioScience*, 48(8):607–615, 1998.

Phoebe L. Zarnetske, David K. Skelly, and Mark C. Urban. Ecology. biotic multipliers of  
climate change. *Science*, 336(6088):1516–8, 6 2012. ISSN 1095-9203. doi: 10.1126/science.  
1222732.

C. I. . I. Zhang, A. B. . B. Hollowed, J-B . B. Lee, and D-H . H. Kim. An iframe approach  
for assessing impacts of climate change on fisheries. *ICES Journal of Marine Science*, 68  
(6):1318–1328, 7 2011. ISSN 1054-3139. doi: 10.1093/icesjms/fsr073.

Ying Zhou and Mark Kot. Discrete-time growth-dispersal models with shifting species ranges.  
*Theoretical Ecology*, 4(1):13–25, 2 2011. ISSN 1874-1738. doi: 10.1007/s12080-010-0071-3.



## 601 6 Figures

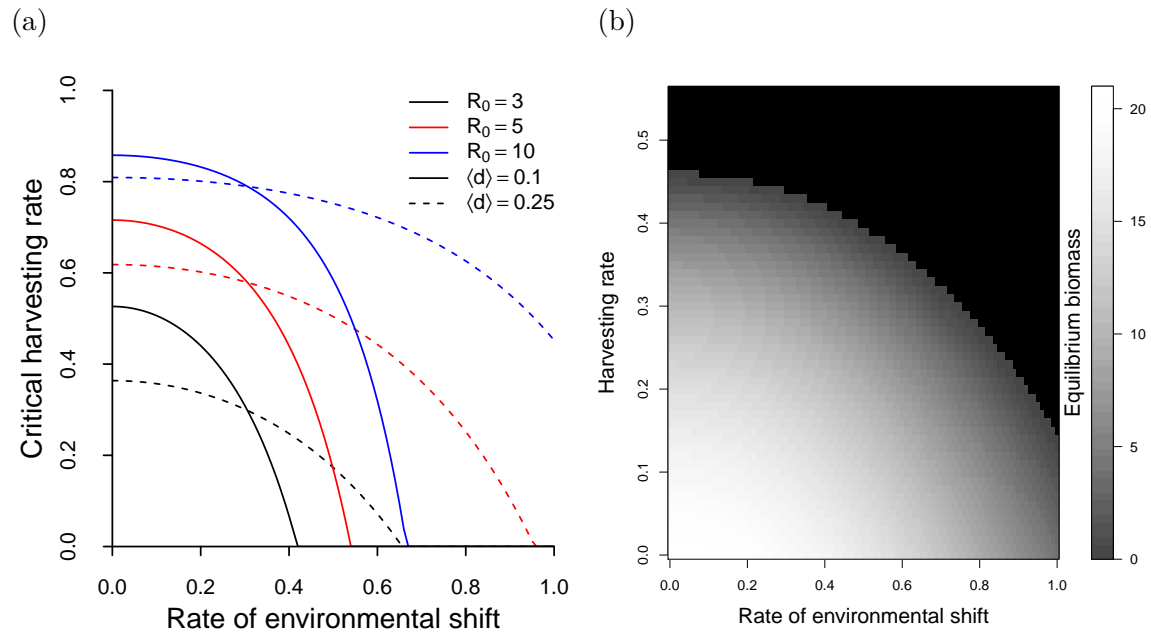


Figure 1

602 **Figure 1:** (a) The equilibrium biomass of the population as a function of the rate of envi-  
 603 ronmental shift on the x-axis and the harvesting rate on the y-axis. These results are from  
 604 a Gaussian dispersal kernel with parameters  $L = 1$ ,  $R_0 = 5$ ,  $\langle d \rangle = 0.399$ . (b) The critical  
 605 harvesting rate on the y-axis as a function of the rate of environmental shift on the x-axis.  
 606 Black lines correspond to a growth rate of  $R_0 = 3$ , red to  $R_0 = 7$ , and blue to  $R_0 = 10$ . Solid  
 607 lines correspond to an average dispersal distance  $\langle d \rangle = 0.1$  and dashed lines correspond to  
 608 an average dispersal distance  $\langle d \rangle = 0.25$ . These results are from an approximated Gaussian  
 609 dispersal kernel with  $L = 1$ .

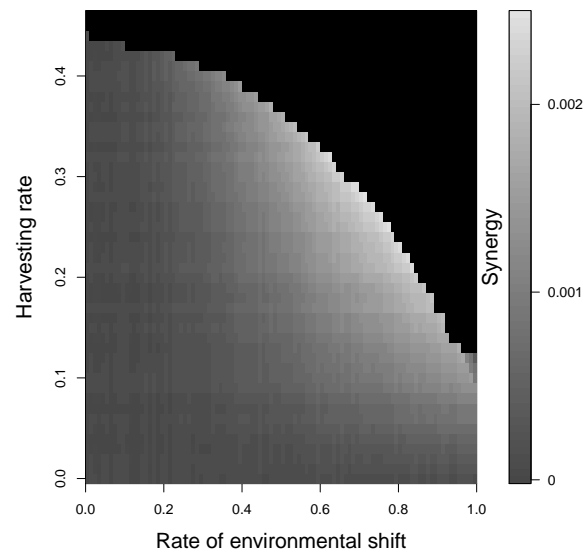
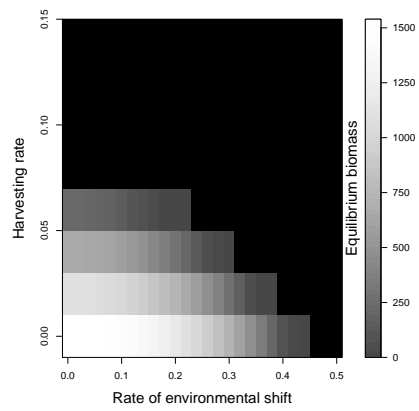


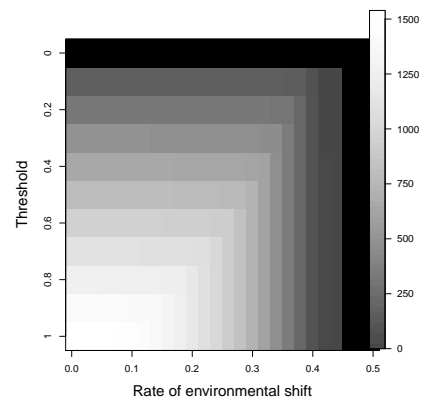
Figure 2

610 **Figure 2:** Positive synergy between the two stressors. The x-axis shows the rate of environ-  
611 mental shift, the y-axis shows the harvesting rate, and the color indicates the loss in biomass  
612 in the doubly stressed population in excess of the sum of the losses caused by each stressor  
613 individually,  $E_{hc} - E_h - E_c$ . These results are from an approximated Gaussian dispersal  
614 kernel with parameters  $L = 1$ ,  $R_0 = 5$ ,  $\langle d \rangle = 0.399$ .

(a)



(b)



(c)

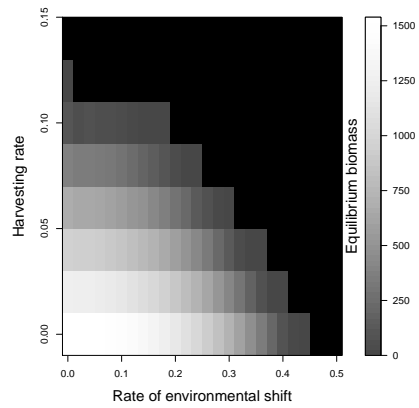


Figure 3

615 **Figure 3:** The equilibrium biomass of the population as a function of the rate of environmen-  
 616 tal shift on the x-axis and the harvesting rate on the y-axis with and without management  
 617 strategies. (a) No management. (b) Threshold harvesting levels. (c) MPAs. These results  
 618 are from a simulation with a Laplacian dispersal kernel with parameters  $L = 1$ ,  $R_0 = 5$ ,  
 619  $K = 100$ , and  $\langle d \rangle = 2$ .

## 7 Tables

Table 1: Table of variables used in the text

Variable	Definition
$n_t(x)$	density of fish at position $x$ at time $t$
$n^*(\bar{x})$	density of fish at equilibrium at position $\bar{x}$ relative to the patch
$k(x - y)$	dispersal kernel, probability of larva traveling from position $y$ to position $x$
$\langle d \rangle$	expected distance traveled by larva
$f(n)$	recruitment function, number of offspring produced by a population of size $n$
$R_0$	intrinsic growth rate, $R_0 = f'(0)$
$h$	proportion of adults harvested
$L$	patch length
$c$	rate of environmental shift

## 8 Appendix

As in Zhou et al. [Zhou and Kot, 2011], let  $k(x - y)$  be a dispersal kernel and let  $f(y)$  be a recruitment function. The integrodifference model describing the population over time is given by

$$n_{t+1}(x) = \int_{-L/2+ct}^{L/2+ct} k(x - y)f(n_t(y))dy. \quad (6)$$

To find a traveling pulse, we are only interested in the population density as a function of the location within the patch rather than absolute position,  $\bar{x} \equiv x - ct$ .

$$n^*(\bar{x}) \equiv n^*(x - ct) = n_t(x). \quad (7)$$

Then (6) gives us an expression for  $n^*$ :

$$\begin{aligned} n^*(\bar{x} - c) &= \int_{-L/2}^{L/2} k(\bar{x} - \bar{y})f(n^*(\bar{y}))d\bar{y} \\ \Rightarrow n^*(\bar{x}) &= \int_{-L/2}^{L/2} k(\bar{x} + c - \bar{y})f(n^*(\bar{y}))d\bar{y} \end{aligned} \quad (*)$$

If  $f(0) = 0$ ,  $n^*(\bar{x}) \equiv 0$  for all  $\bar{x} \in [-L/2, L/2]$  is a trivial solution to this problem, i.e. if there are no fish anywhere there won't be at any time in the future. The population can be said to be persistent if the trivial traveling pulse is unstable since even when there are very small population levels, the population won't crash to 0. To evaluate stability (i.e. persistence), we will introduce a small perturbation to the traveling pulse  $n^*(\bar{x})$ ,

$$\begin{aligned} n_t(x) &= n^*(\bar{x}) + \xi_t(x) \\ \Rightarrow \xi_{t+1}(x) &= \int_{-L/2+ct}^{L/2+ct} k(x - y)f'(n^*(\bar{y}))\xi_t(y)dy \text{ by linearizing around the traveling pulse and using } (*) \\ \Rightarrow \xi_{t+1}(x) &= \int_{-L/2+ct}^{L/2+ct} k(x - y)f'(0)\xi_t(y)dy \text{ if we're interested in the stability of the trivial traveling pulse} \end{aligned}$$

If we assume  $\xi_t(x) = \lambda^t u(x - ct)$  for some  $\lambda \in \mathbb{R}$  and  $u : [-L/2, L/2] \rightarrow \mathbb{R}$ , then

$$\begin{aligned} \lambda u(x - ct - c) &= f'(0) \int_{-L/2+ct}^{L/2+ct} k(x - y)u(y - ct)dy \\ \lambda u(\bar{x}) &= f'(0) \int_{-L/2}^{L/2} k(\bar{x} + c - \bar{y})u(\bar{y})d\bar{y} \end{aligned}$$

Define the integral operator

$$\psi_f(g)(x) = \int_{-L/2}^{L/2} f'(0)k(x + c - y)g(y)dy.$$

so that the perturbation to the traveling pulse will satisfy

$$\psi_f(u)(x) = \lambda u(x) \quad (8)$$



Then the trivial traveling pulse is unstable when the dominant eigenvalue of  $\psi_f$  is greater than 1.

Let  $f$  denote the recruitment function, let  $h$  denote a harvesting function and let  $m(y) = f(y - h(y))$ , i.e.  $m$  denotes the number of offspring after the adults have been harvested. Note that  $m'(0) = f'(0)(1 - h'(0))$ , assuming  $h(0) = 0$  (which must be the case).

Suppose  $u$  is an eigenfunction of  $\psi_f$  with eigenvalue  $\lambda$ . Then

$$\begin{aligned}\psi_m(u)(x) &= \int_{-L/2}^{L/2} m'(0)k(x + c - y)u(y)dy \\ &= (1 - h'(0)) \int_{-L/2}^{L/2} f'(0)k(x + c - y)u(y)dy \\ &= (1 - h'(0))\psi_f(u)(x) \\ &= (1 - h'(0))\lambda u(x)\end{aligned}$$

so that  $u$  is also an eigenfunction of  $\psi_m$ , now with eigenvalue  $(1 - h'(0))\lambda$ .

**8.1 Separable dispersal kernels** Jentzsch's theorem shows that there is an eigenfunction  $u$ , provided that the kernel  $k$  satisfy some properties. Finding the eigenfunction is in general a hard problem to solve. It becomes easier if the kernel  $k$  is separable, i.e. there are functions  $a_n, b_n$  such that  $k(x - y) = \sum_{n=1}^{\infty} a_n(x)b_n(y)$ . In that case, (8) becomes

$$\begin{aligned}\lambda u(x) &= f'(0) \sum_{n=1}^{\infty} \left( a_n(x) \int_{-L/2}^{L/2} b_n(y - c)u(y)dy \right) \\ \Rightarrow \lambda \int_{-L/2}^{L/2} b_k(x - c)u(x)dx &= f'(0) \sum_{n=1}^{\infty} \left( \int_{-L/2}^{L/2} b_n(x - c)u(x)dx \right) \left( \int_{-L/2}^{L/2} a_n(y)b_k(y - c)dy \right) \\ \Rightarrow \lambda d_k &= f'(0) \sum_{n=1}^{\infty} A_{nk}d_n\end{aligned}\tag{**}$$

where

$$A_{nk} = \int_{-L/2}^{L/2} a_n(x)b_k(x - c)dx \text{ and } d_k = \int_{-L/2}^{L/2} b_k(x - c)u(x)dx$$

**8.2 Gaussian dispersal kernel** The Gaussian dispersal kernel is given by

$$k(|x - y|) = \frac{1}{2\sqrt{D\pi}} e^{-\frac{(x-y)^2}{4D}}.$$

As in [Latore et al., 1998], this separable kernel can be written as

$$k(|x - y|) = \sum_{n=0}^{\infty} a_n(x)b_n(y)$$

where

$$a_n(x) = b_n(x) = \frac{1}{\sqrt{2n!}\sqrt{D\pi}} e^{-x^2/4D} \left( \frac{x}{\sqrt{2D}} \right)^n.$$

As a first approximation to  $k$  we ignore all but the  $0^{th}$  terms for  $a_n$  and  $b_n$  so that Equation \*\* becomes

$$\begin{aligned}\lambda d_0(c) &= f'(0)A_{00}(c)d_0(c) \\ \Rightarrow \lambda &= R_0(1-h)A_{00}(c) \\ \text{where } A_{00}(c) &= 2\sqrt{2} \exp\left(\frac{-c^2}{8D}\right) \left[ \operatorname{erf}\left(\frac{L-c}{2\sqrt{2D}}\right) - \operatorname{erf}\left(\frac{-L-c}{2\sqrt{2D}}\right) \right]\end{aligned}$$

640 where  $\operatorname{erf}$  is the error function. The critical rate of environmental shift  $c^*$  and the critical  
641 harvesting rate  $h^*$  are those values of  $c$  and  $h$ , respectively, that make  $\lambda = 1$ .

**8.3 Sinusoidal dispersal kernel** A sinusoidal dispersal kernel is given by

$$k(x-y) = \begin{cases} \frac{w}{2} \cos(w(x-y)) & , \quad |x-y| \leq \frac{\pi}{2w} \\ 0 & , \quad |x-y| > \frac{\pi}{2w} \end{cases}$$

642 where  $L$  is the length of the patch and we assume  $\frac{\pi}{2w} > L, c < \frac{\pi}{2w} - L$ .

In this case,  $k(x-y) = \frac{w}{2} \cos(wx) \cos(w(y-c)) + \frac{w}{2} \sin(wx) \sin(w(y-c))$  so that  $A_{ij}$  and  $d_i$  can be found for  $i, j = 1, 2$  and (\*\*) reduces to

$$\lambda^2 - \left( \frac{R_0(1-h)wL}{2} \cos(wc) \right) \lambda + \frac{R_0^2(1-h)^2}{16} (w^2L^2 - \sin^2(wL)) = 0.$$

643 If we solve for  $\lambda$ , we find

$$\lambda = R_0(1-h) \left[ \frac{wL \cos(wc)}{4} + \frac{1}{4} \sqrt{\sin^2(wL) - w^2L^2 \sin^2(wc)} \right]. \quad (9)$$

Zhou et al. [Zhou and Kot, 2011] solve for the critical speed,  $c^*$ , at the population will be driven extinct:

$$c^* = c^*(R_0) = \frac{1}{w} \cos^{-1} \left[ \frac{16 + R_0^2(1-h)^2(w^2L^2 - \sin^2(wL))}{8R_0(1-h)wL} \right].$$

Similarly, we can solve for the critical harvesting rate,  $h^*$ , at which the population will be driven extinct:

$$h^* = 1 - \frac{1}{R_0} \cdot \frac{4wL}{w^2L^2 - \sin^2(wL)} \left[ \cos(wc) - \sqrt{\cos^2(wc) - 1 + \frac{\sin^2(wL)}{w^2L^2}} \right]$$

#### 8.4 Approximate Critical Harvesting Proportions

We will use the following Taylor series to make approximations of the critical harvesting

proportions under the two dispersal kernels:

$$\begin{aligned}\cos(x) &= 1 - \frac{x^2}{2} \\ \cos^2(x) &= 1 - x^2 \\ \sin^2(x) &= x^2 - \frac{x^4}{3} \\ erf(x) &= \frac{2}{\sqrt{\pi}}(x - \frac{x^3}{3}) \\ \exp(x) &= 1 + x + \frac{x^2}{2}\end{aligned}$$

644 For the sinusoidal kernel we found

$$h^* = 1 - \frac{1}{R_0} \cdot \frac{4wL}{w^2L^2 - \sin^2(wL)} \left[ \cos(wc) - \sqrt{\cos^2(wc) - 1 + \frac{\sin^2(wL)}{w^2L^2}} \right] \quad (10)$$

Using the Taylor series and the fact that  $w = \frac{\sqrt{\frac{\pi^2}{4} - 2}}{\sigma}$  where  $\sigma^2$  is the variance of the sinusoidal kernel,

$$\begin{aligned}h^* &\sim 1 - \frac{1}{R_0} \cdot \frac{12wL}{w^4L^4} \left[ 1 - \frac{w^2c^2}{2} - \sqrt{1 - w^2c^2 - \frac{w^2L^2}{3}} \right] \\ &= 1 - \frac{1}{R_0} \cdot \frac{4\sqrt{3}}{L^3(\pi^2 - 8)^{3/2}} \cdot \sigma \left[ 8\sqrt{3}\sigma^2 - (\pi^2 - 8)\sqrt{3}c^2 - 4\sigma\sqrt{12\sigma^2 - (\pi^2 - 8)(3c^2 + L^2)} \right]\end{aligned}$$

645 For the Gaussian kernel we found

$$h^* = 1 - \frac{2\sqrt{2}\exp\left(\frac{c^2}{8D}\right)}{R_0 \left[ erf\left(\frac{L-c}{2\sqrt{2D}}\right) - erf\left(\frac{-L-c}{2\sqrt{2D}}\right) \right]} \quad (11)$$

Using the Taylor series and the fact that  $D = \frac{\sigma^2}{2}$  where  $\sigma^2$  is the variance of the exponential kernel,

$$\begin{aligned}h^* &\sim 1 - \frac{\sqrt{2\pi}(1 + \frac{c^2}{8D} + \frac{c^4}{128D^2})}{R_0\sqrt{\pi} \left[ \frac{L-c}{2\sqrt{2D}} - \frac{(L-c)^3}{3(2\sqrt{2D})^3} - \frac{-L-c}{2\sqrt{2D}} + \frac{(-L-c)^3}{3(2\sqrt{2D})^3} \right]} \\ &= 1 - \frac{1}{R_0} \cdot \frac{3\sqrt{2\pi}}{8L} \cdot \frac{(32\sigma^4 + 8c^2\sigma^2 + c^4)}{\sigma(12\sigma^2 - (L^2 + 3c^2))}\end{aligned}$$

646 In the case of both kernels, the critical harvesting proportion can be approximated by a  
647 function that looks like

$$h^* \sim 1 - \frac{1}{R_0} \cdot C(L)f(\sigma^2, c^2, L^2 + 3c^2) \quad (12)$$

648 where  $C(L, R_0)$  is a decreasing function of the length of the viable patch and the intrinsic  
649 growth rate.