

**xspech**

main program

[called by: .] [calls: [global:readin](#), [global:wrtend](#), [preset](#), [packxi](#), [volume](#), [pc00aa](#), [newton](#), [dforce](#), [hesian](#), [ra00aa](#), [bnorml](#), [sc00aa](#), [jo00aa](#) and [pp00aa](#).]**contents**

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**1.1 reading input, allocating global variables**

1. The input namelists and geometry are read in via a call to [global:readin](#). A full description of the required input is given in [global](#).
2. Most internal variables, global memory etc., are allocated in [preset](#).

**1.2 preparing output file `.ext.sp.its`**

1. The file `.ext.sp.its` is created. This file contains the interface geometry at each iteration, which is useful for constructing movies illustrating the convergence. The format of this file is:

```

open(zunit,file="."//trim(ext)//".sp.its",status="unknown",form="unformatted")
write(zunit) mn, Mvol, Nfp ! integer;
write(zunit) im(1:mn) ! integer;
write(zunit) in(1:mn) ! integer;
! begin do loop over iterations;
write(zunit) wflag, iflag, Energy, rflag ! written in global.h:wrtend; perhaps redundant;
write(zunit) iRbc(1:mn,0:Mvol) ! real;
write(zunit) iZbs(1:mn,0:Mvol) ! real;
write(zunit) iRbs(1:mn,0:Mvol) ! real;
write(zunit) iZbc(1:mn,0:Mvol) ! real;
! end do loop over iterations;

```

**1.3 “packing” geometrical degrees-of-freedom into vector**

1. If `NGdof.gt.0`, where `NGdof` counts the geometrical degrees-of-freedom, i.e. the  $R_{bc}$ ,  $Z_{bs}$ , etc., then [packxi](#) is called to “pack” the geometrical degrees-of-freedom into `position(0:NGdof)`.

**1.4 initialize adiabatic constants**

1. If [Ladiabatic.eq.0](#), then the “adiabatic constants” in each region,  $P_v$ , are calculated as

$$P_v \equiv p_v V_v^\gamma, \quad (1)$$

where  $p_v \equiv$  [pressure\(vvol\)](#), the volume  $V_v$  of each region is computed by [volume](#), and the adiabatic index  $\gamma \equiv$  [gamma](#).

**1.5 solving force-balance**

1. If there are geometrical degress of freedom, i.e. if `NGdof.gt.0`, then

If [Lfindzero.gt.0](#), call [newton](#) to find extremum of constrained energy functional using a Newton method, [NAG: C05PDF](#);

## 1.6 post diagnostics

1. The pressure is computed from the adiabatic constants from Eqn.(1), i.e.  $p = P/V^\gamma$ .
2. The Beltrami/vacuum fields in each region are re-calculated using `dforce`.
3. If `Lcheck.eq.5 .or. LHevalues .or. LHevectors .or. Lperturbed.eq.1`, then the “Hessian” matrix is examined using `hesian`.

## 1.7 free-boundary: re-computing normal field

1. If `Lfreebound.eq.1` and `Lfindzero.gt.0` and `mfreeits.ne.0`, then the magnetic field at the computational boundary produced by the plasma currents is computed using `bnorml`.
2. The “new” magnetic field at the computational boundary produced by the plasma currents is updated using a Picard scheme:

$$\mathbf{Bns}_i^j = \lambda \mathbf{Bns}_i^{j-1} + (1 - \lambda) \mathbf{Bns}_i, \quad (2)$$

where  $j$  labels free-boundary iterations, the “blending parameter” is  $\lambda \equiv \text{gBnbld}$ , and  $\mathbf{Bns}_i$  is computed by virtual casing. The subscript “ $i$ ” labels Fourier harmonics.

3. If the new (unblended) normal field is not sufficiently close to the old normal field, as quantified by `gBntol`, then the free-boundary iterations continue. This is quantified by

$$\sum_i |\mathbf{Bns}_i^{j-1} - \mathbf{Bns}_i|/N, \quad (3)$$

where  $N$  is the total number of Fourier harmonics.

4. There are several choices that are available:
  - (a) if `mfreeits = -2` : the vacuum magnetic field (really, the normal component of the field produced by the external currents at the computational boundary) required to hold the given equilibrium is written to file. This information is required as input by FOCUS (2017)<sup>1</sup> for example. (This option probably needs to be revised.)
  - (b) if `mfreeits = -1` : after the plasma field is computed by virtual casing, the vacuum magnetic field is set to exactly balance the plasma field (again, we are really talking about the normal component at the computational boundary.) This will ensure that the computational boundary itself is a flux surface of the total magnetic field.
  - (c) if `mfreeits = 0` : the plasma field at the computational boundary is not updated; no “free-boundary” iterations take place.
  - (d) if `mfreeits > 0` : the plasma field at the computational boundary is updated according to the above blending Eqn.(2), and the free-boundary iterations will continue until either the tolerance condition is met (see `gBntol` and Eqn.(3)) or the maximum number of free-boundary iterations, namely `mfreeits`, is reached. For this case, `Lzerovac` is relevant: if `Lzerovac = 1`, then the vacuum field is set equal to the normal field at every iteration, which results in the computational boundary being a flux surface. (I am not sure if this is identical to setting `mfreeits = -1`; the logic etc. needs to be revised.)

## 1.8 output files: vector potential

1. The vector potential is written to file using `ra00aa`.

## 1.9 final diagnostics

1. `sc00aa` is called to compute the covariant components of the magnetic field at the interfaces; these are related to the singular currents;
2. if `Lcheck = 1`, `jo00aa` is called to compute the error in the Beltrami equation;
3. `pp00aa` is called to construct the Poincaré plot;

## 1.10 restart files

1. `global:wrtend` is called to write the restart files.

## 1.11 subroutine : ending

1. Closes output files, writes screen summary.

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<sup>1</sup>Caoxiang Zhu, Stuart Hudson et al., *Nucl. Fusion* **58**, 016008 (2017)