

**numrec**

miscellaneous “numerical” routines

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**1.1 Outline**

This file contains various miscellaneous “numerical” routines as described below.

**1.2 gi00ab**

1. This routine assigns the Fourier mode labels that converts a double-sum into a single sum; i.e., the  $m_j$  and  $n_j$  are assigned where

$$f(\theta, \zeta) = \sum_{n=0}^N f_{0,n} \cos(-n N_P \zeta) + \sum_{m=1}^M \sum_{n=-N}^N f_{m,n} \cos(m\theta - n N_P \zeta) \quad (1)$$

$$= \sum_j f_j \cos(m_j \theta - n_j \zeta), \quad (2)$$

where  $N \equiv \text{Ntor}$  and  $M \equiv \text{Mpol}$  are given on input, and  $N_P \equiv \text{Nfp}$  is the field periodicity.

**1.3 tffft**

1. This constructs the “forward” Fourier transform.
2. Given a set of data,  $(f_i, g_i)$  for  $i = 1, \dots, N_\theta N_\zeta$ , on a regular two-dimensional angle grid, where  $\theta_j = 2\pi j/N_\theta$  for  $j = 0, N_\theta - 1$ , and  $\zeta_k = 2\pi k/N_\zeta$  for  $k = 0, N_\zeta - 1$ . The “packing” is governed by  $i = 1 + j + k N_\theta$ . The “discrete” resolution is  $N_\theta \equiv \text{Nt}$ ,  $N_\zeta \equiv \text{Nz}$  and  $\text{Ntz} = \text{Nt} \times \text{Nz}$ , which are set in [preset](#).
3. The Fourier harmonics consistent with Eqn.(2) are constructed. The mode identification labels appearing in Eqn.(2) are  $m_j \equiv \text{im}(j)$  and  $n_j \equiv \text{in}(j)$ , which are set in [global](#) via a call to [gi00ab](#).

**1.4 invfft**

1. Given the Fourier harmonics, the data on a regular angular grid are constructed.
2. This is the inverse routine to **tffft**.

**1.5 gauleg**

1. Compute Gaussian integration weights and abscissae.
2. From Numerical Recipes.