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## 1 Setup

### 1.1 Remap Escape

```
setxkbmap -option caps:swapescape # X11
gsettings set org.gnome.desktop.input-sources xkb-options
["'caps:swapescape'"] # Wayland
```

### 1.2 vimrc

```
se nu rnu cin ts=4 sw=4 | sy on
inoremap {<CR> {<CR>}<Esc>0
nnoremap j gj
nnoremap k gk
colo evening
:bad input.txt
:let @# = 'input.txt'
ca Hash w !cpp -dD -P -fpreprocessed \ | tr -d "[:space:]"
\ | md5sum \ | cut -c-6
```

### 1.3 default code [b7320]

```
#include <bits/stdc++.h>
using namespace std;

#ifdef MIKU
```

```
string dbmc = "\033[1;38;2;57;197;187m", dbrs = "\033[0m";
#define debug(x...) cerr << dbmc << "[" << #x << "]" : ",
dout(x)
void dout() { cerr << dbrs << endl; }
template <typename T, typename ...U>
void dout(T t, U ...u) { cerr << t << (sizeof...(u) ? ", " :
""); dout(u...); }
#else
#define debug(...) 39
#endif

#define fs first
#define sc second
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
using ll = long long;
typedef pair<int, int> pii;

void miku() {
    int a, b;
    cin >> a >> b;
    debug(a, b);
    cout << "DEC0*" << a * b << '\n';
}

int32_t main() {
    cin.tie(0) -> sync_with_stdio(false);
    cin.exceptions(cin.failbit);
    miku();
    return 0;
}
```

## 2 Graph

### 2.1 Block Cut Tree [a7ea1]

```
// [0, n): round points, [n, tr.size()): square points
// take care of cases when n=1
struct BlockCutTree { // 0 based
    vector<vector<int>> paths, tr;
    vector<int> idx, low, stk;
    int gid, dfn;
    int n;
    BlockCutTree(int _n) {
        n = _n;
        paths = tr = vector<vector<int>>(n);
        gid = 0;
        idx = low = vector<int>(n, -1);
        stk.clear();
    }
    void add_edge(int a, int b) {
        paths[a].push_back(b);
        paths[b].push_back(a);
    }
    void dfs(int now) {
        idx[now] = low[now] = ++dfn;
        stk.push_back(now);
        for(auto nxt:paths[now]) {
            if (idx[nxt] == -1) {
                dfs(nxt);
                low[now] = min(low[now], low[nxt]);
                if (low[nxt] == idx[now]) {
                    tr.push_back({});
                    int t = -1;
                    do {
                        t = stk.back();
                        stk.pop_back();
                        tr[gid+n].push_back(t);
                        tr[t].push_back(gid+n);
                    } while(t != nxt);
                    tr[now].push_back(gid+n);
                }
            }
        }
    }
};
```

```

        tr[gid+n].push_back(now);
        gid ++;
    }
}
else low[now] = min(low[now], idx[nxt]);
}
return;
}
vector<vector<int>> solve() {
    dfn = 0;
    for(int i = 0; i < n; i++) {
        if (idx[i] == -1) dfs(i);
    }
    return tr;
}
};

```

## 2.2 Dinic [9befe]

```

struct Dinic { // 0-indexed
    // watch out for e.f overflow
    struct E { int v, c, f; };
    vector<vector<int>> g;
    vector<int> p, d;
    vector<E> e;
    queue<int> q;
    void init(int n) {
        g.resize(n);
        p.resize(n);
        d.resize(n);
    }
    void ae(int u, int v, int cu, int cv = 0) {
        g[u].push_back(e.size());
        e.push_back(E{v, cu, 0});
        g[v].push_back(e.size());
        e.push_back(E{u, cv, 0});
    }
    bool bfs(int s, int t, int l) {
        fill(d.begin(), d.end(), -1);
        d[s] = 0;
        q.push(s);
        while (q.size()) {
            int u = q.front();
            q.pop();
            for (auto &ei : g[u]) {
                if ((!(e[ei].c - e[ei].f) >> (30 - l))) continue;
                int v = e[ei].v;
                if (d[v] == -1) {
                    d[v] = d[u] + 1;
                    q.push(v);
                }
            }
        }
        return d[t] != -1;
    }
    int dfs(int u, int t, int fl) {
        if (u == t) return fl;
        for (int &i = p[u]; i < g[u].size(); i++) {
            int ei = g[u][i];
            if (e[ei].f == e[ei].c || d[e[ei].v] != d[u] + 1)
                continue;
            if (int re = dfs(e[ei].v, t, min(fl, e[ei].c - e[ei].f))) {
                e[ei].f += re;
                e[ei ^ 1].f -= re;
                return re;
            }
        }
        return 0;
    }
    int flow(int s, int t) {

```

```

        int ans = 0;
        for (int l = 0; l < 31; l++) {
            while (bfs(s, t, l)) {
                fill(p.begin(), p.end(), 0);
                while (auto re = dfs(s, t, INT_MAX)) ans += re;
            }
        }
        return ans;
    }
    bool inscut(int k) {
        return d[k] != -1;
    }
};

```

## 2.3 Dominator Tree [3b89c]

```

struct DominatorTree{
    //l-indexed
    //not reachable from s -> not on tree
    int n;
    vector<vector<int>> G,rG;
    vector<int> pa,dfn,id;
    int dfnCnt;
    vector<int> semi,idom,best;
    vector<vector<int>> ret;
    void init(int _n){
        n=_n;
        G = rG = ret = vector<vector<int>>(n+1);
        pa = dfn = id = vector<int>(n+1,-1);
        dfnCnt = 0;
        semi = idom = best = vector<int>(n+1,-1);
    }
    void add_edge(int u,int v){
        G[u].push_back(v);
        rG[v].push_back(u);
    }
    void dfs(int u){
        id[dfn[u]++]=dfnCnt++;
        for(auto v:G[u]) if(!dfn[v]){
            dfs(v,pa[dfn[v]]=dfn[u]);
        }
    }
    int find(int y,int x){
        if(y<=x)return y;
        int tmp=find(pa[y],x);
        if(semi[best[y]]>semi[best[pa[y]]])
            best[y]=best[pa[y]];
        return pa[y]=tmp;
    }
    void tarjan(int root){
        dfnCnt=0;
        for(int i=1;i<=n;++i){
            dfn[i]=idom[i]=0;
            ret[i].clear();
            best[i]=semi[i]=i;
        }
        dfs(root);
        for(int i=dfnCnt;i>1;--i){
            int u=id[i];
            for(auto v:rG[u]) if(v=dfn[v]){
                find(v,pa[i]);
                semi[i]=min(semi[i],semi[best[v]]);
            }
            ret[semi[i]].push_back(i);
            for(auto v:ret[pa[i]]){
                find(v,pa[i]);
                idom[v] = semi[best[v]]==pa[i] ? pa[i] : best[v];
            }
            ret[pa[i]].clear();
        }
        for(int i=2; i<=dfnCnt; ++i){

```

```

    if(idom[i]!=semi[i]) idom[i]=idom[idom[i]];
    ret[id[idom[i]]].push_back(id[i]);
}
}
vector<vector<int>> solve(int s){
    tarjan(s);
    return ret;
}
};

```

## 2.4 Euler Tour [d857a]

```

struct EulerTour{
    // undirected graph, 0-indexed, fails if doesn't exist
    // for directed graph, remove the g[b].push_back(pii(a,
    id)) line in add_edge
    // returns the order of edges
    vector<vector<pii>> g;
    vector<int> ptr;
    vector<bool> vis;
    vector<int> re;
    int n, ecnt;
    void init(int _n){
        n = _n;
        ecnt = 0;
        g = vector<vector<pii>>(n);
        ptr = vector<int>(n);
    }
    void add_edge(int a, int b, int id = -1){
        if(id == -1) id = ecnt;
        g[a].push_back(pii(b, id));
        g[b].push_back(pii(a, id));
        ecnt++;
    }
    void dfs(int now){
        for(int &i = ptr[now]; i < g[now].size(); i++){
            auto [to, eid] = g[now][i];
            if(vis[eid]) continue;
            vis[eid] = true;
            dfs(to);
            re.push_back(eid);
        }
        return;
    }
    vector<int> solve(int s){
        re.clear();
        vis = vector<bool>(ecnt, 0);
        dfs(s);
        reverse(re.begin(), re.end());
        return re;
    }
};

```

## 2.5 Gomory Hu [3ab29]

```

// needs dinic
struct GomoryHuTree{//0-indexed
#define pii pair<int,int>
#define tiii tuple<int,int,int>
    vector<tiii> edges;
    vector<vector<pii>> tr;
    vector<int> p;
    int n;
    GomoryHuTree(int _n = 0){
        n = _n;
        p = vector<int>(_n, 0);
        tr = vector<vector<pii>>(_n);
    }
    void add_edge(int a, int b, int c){

```

```

        edges.push_back(tiii(a,b,c));
    }
    vector<vector<pii>> make_tree(){
        fill(p.begin(), p.end(), 0);
        tr = vector<vector<pii>>(n);
        for(int i = 1; i < p.size(); i++){
            Dinic din(n);
            for(auto &[a,b,w]:edges){
                din.add_edge(a,b,w,w);
            }
            int w = din.flow(i, p[i]);
            tr[i].push_back(pii(p[i], w));
            tr[p[i]].push_back(pii(i, w));
            for(int j = i+1; j < n; j++){
                if(p[j] == p[i] && din.inScut(j)) p[j] = i;
            }
        }
        return tr;
    }
}
#undef pii
#undef tiii
};

```

## 2.6 Incremental SCC [d8b55]

```

struct IncrementalSCC{
#define pii pair<int,int>
#define fs first
#define sc second
#define tiii tuple<int,int,int>
    //if u == v : ans[i] = -1
    //if not connected : ans[i] = m
    //all 0-indexed
    int n;
    vector<int> ans;
    int m;
    vector<tiii> all;
    vector<int> SCC(int n, vector<vector<int>>& paths){
        vector<int> scc_id(n, -1), idx(n, -1), low(n, -1), st;
        int cnt = 0, gcnt = 0;
        function<void(int)> dfs = [&](int now) -> void{
            low[now] = idx[now] = cnt++;
            st.push_back(now);
            for(auto nxt:paths[now]){
                if(scc_id[nxt] != -1) continue;
                if(idx[nxt] == -1){
                    dfs(nxt);
                    low[now] = min(low[now], low[nxt]);
                }
                else{
                    low[now] = min(low[now], idx[nxt]);
                }
            }
            if(low[now] == idx[now]){
                int id = -1;
                while(id != now){
                    id = st.back();
                    st.pop_back();
                    scc_id[id] = gcnt;
                }
                gcnt++;
            }
        };
        for(int i = 0; i < n; i++){
            if(scc_id[i] == -1) dfs(i);
        }
        return scc_id;
    }
    vector<int> mapping;
    void dc(int l, int r, vector<tiii> &edges){
        if(l == r){

```

```

    for(auto &[id,_,_]:edges)ans[id] = min(ans[id],l);
    return;
}
int mid = (l+r)>>1;
int cnt = 0;
for(auto &[t,u,v]:edges){
    if(mapping[u] == -1)mapping[u] = cnt++;
    if(mapping[v] == -1)mapping[v] = cnt++;
}
n = cnt;
vector<vector<int>> paths(n);
vector<int> vv;
for(auto &[t,u,v]:edges){
    vv.push_back(u);
    vv.push_back(v);
    u = mapping[u],v = mapping[v];
    if(t<=mid)paths[u].push_back(v);
}
for(auto &i:vv)mapping[i] = -1;

auto scc_id = SCC(n,paths);
vector<tiii> vl,vr;
for(auto &[t,u,v]:edges){
    if(scc_id[u] == scc_id[v]){
        ans[t] = min(ans[t],mid);
        vl.push_back(tiii(t,u,v));
    }
    else{
        u = scc_id[u],v = scc_id[v];
        vr.push_back(tiii(t,u,v));
    }
}
vector<tiii>().swap(edges);
dc(l,mid,vl);
dc(mid+1,r,vr);
return;
}
void add_edge(int u,int v){
    all.push_back(tiii(all.size(),u,v));
}
vector<tiii> solve(){//[time,u,v]
    m = all.size();
    vector<tiii> ret(m);
    for(auto [t,u,v]:all)ret[t] = tiii(m,u,v);
    for(auto [t,u,v]:all)n = max({n,u,v});
    n++;
    ans = vector<int>(m,m);
    for(auto [t,u,v]:all){
        if(u == v)ans[t] = -1;
    }
    mapping = vector<int>(n,-1);
    dc(0,m,all);
    for(int i = 0;i<m;i++)get<0>(ret[i]) = ans[i];
    return ret;
}
IncrementalSCC(){
    ans.clear();
    n = m = 0;
}
#undef tiii
#undef pii
#undef fs
#undef sc
};

```

## 2.7 KM [2bf04]

```

// Kuhn-Munkres : Bipartite matching with "maximum" weight
in  $O(n^3)$ 
// NOTICE THAT match[y] = x
struct KM{

```

```

    const static int M = 500; // modify maximum number of
    vertices
    int n;
    ll ans = 0;
    // 0-base
    vector<vector<ll>> w; // input weighted edges w[x][y]
    vector<int> match; // match[y] = x
    vector<ll> lx, ly, slack;
    bitset<M> visx, visy; // initialize with all zero

    // abbr
    # define forx for(int x=0; x<n; x++)
    # define fory for(int y=0; y<n; y++)
    # define z match[y]

    bool dfs(int x){
        visx[x] = 1;
        fory{
            if(visy[y]) continue;
            ll d = lx[x]+ly[y]-w[x][y];
            if(!d){
                visy[y] = 1;
                if(z== -1 || (!visx[z] && dfs(z))){
                    z = x;
                    return 1;
                }
            }
            else if(d<slack[y]) slack[y] = d;
        }
        return 0;
    }

    bool augment(){
        fory if(!visy[y] && !slack[y]){
            visy[y] = 1;
            if(z== -1) return 1;
            else if(!visx[z] && dfs(z)){
                z = -1;
                return 1;
            }
        }
        return 0;
    }

    void relabel(){
        ll d = INT64_MAX;
        fory if(!visy[y]) d = min(d, slack[y]);
        forx if(visx[x]) lx[x] -= d;
        fory{
            if(visy[y]) ly[y] += d;
            else slack[y] -= d;
        }
    }

    KM(vector<vector<ll>> &W): n(W.size()), w(W) { // input
    edges' weight
        //initialize
        slack.resize(n);
        match.assign(n, -1);
        lx.assign(n, INT64_MIN);
        ly.assign(n, 0);
        forx fory lx[x] = max(lx[x], w[x][y]);
        //matching
        forx{
            visx.reset();
            visy.reset();
            visx[x] = 1;
            fory slack[y] = lx[x]+ly[y]-w[x][y];
            while(!augment()) relabel();
            visx.reset();
            visy.reset();
            dfs(x);
        }
    }
}

```

```

//summing
forx ans += lx[x];
fory ans += ly[y];
}

# undef forx
# undef fory
# undef z
};

```

## 2.8 Max Clique [0de04]

```

constexpr size_t kN = 150; using bits = bitset<kN>;
#define _all(T) T.begin(),T.end()
struct MaxClique {
    bits G[kN], cs[kN];
    int ans, sol[kN], q, cur[kN], d[kN], n;
    void init(int _n) {
        n = _n;
        for (int i = 0; i < n; ++i) G[i].reset();
    }
    void add_edge(int u, int v) { G[u][v] = G[v][u] = 1; }
    void pre_dfs(vector<int> &v, int i, bits mask) {
        if (i < 4) {
            for (int x : v) d[x] = (int)(G[x] & mask).count();
            sort(_all(v), [&](int x, int y) {
                return d[x] > d[y]; });
        }
        vector<int> c(v.size());
        cs[1].reset(), cs[2].reset();
        int l = max(ans - q + 1, 1), r = 2, tp = 0, k;
        for (int p : v) {
            for (k = 1; (cs[k] & G[p]).any(); ++k);
            if (k >= r) cs[++r].reset();
            cs[k][p] = 1;
            if (k < l) v[tp++] = p;
        }
        for (k = l; k < r; ++k)
            for (auto p = cs[k]._Find_first();
                 p < kN; p = cs[k]._Find_next(p))
                v[tp] = (int)p, c[tp] = k, ++tp;
        dfs(v, c, i + 1, mask);
    }
    void dfs(vector<int> &v, vector<int> &c,
             int i, bits mask) {
        while (!v.empty()) {
            int p = v.back(); v.pop_back(); mask[p] = 0;
            if (q + c.back() <= ans) return;
            cur[q++] = p;
            vector<int> nr;
            for (int x : v) if (G[p][x]) nr.push_back(x);
            if (!nr.empty()) pre_dfs(nr, i, mask & G[p]);
            else if (q > ans) ans = q, copy_n(cur, q, sol);
            c.pop_back(); --q;
        }
    }
    int solve() {
        vector<int> v(n); iota(_all(v), 0);
        ans = q = 0; pre_dfs(v, 0, bits(string(n, '1')));
        return ans; // sol[0 ~ ans-1]
    }
};

```

## 2.9 Minimum Cost Maximum Flow [80eed]

```

#define T ll
const T inf = 1e12;
struct MCMF{//TC:0(VEF)
    struct E{

```

```

        int t,f;
        T c,w;
        E(int tt,T cap,T wei):t(tt),c(cap),w(wei),f(0){}
    };
    vector<E> e;
    vector<vector<int>>> paths;
    vector<T> dis;
    vector<int> pre;
    vector<bool> inq;
    queue<int> q;
    int n;
    MCMF(int _n = 0){
        n = _n;
        paths = vector<vector<int>>>(n);
        e.clear();
        pre = vector<int>(n);
        dis = vector<T>(n);
        inq = vector<bool>(n);
    }
    void add_edge(int a,int b,int c,int d){//from,to,cap,wei
        paths[a].push_back(e.size());
        e.push_back(E(b,c,d));
        paths[b].push_back(e.size());
        e.push_back(E(a,0,-d));
    }
    bool SPFA(int s,int t){
        fill(dis.begin(),dis.end(),inf);
        fill(pre.begin(),pre.end(),-1);
        dis[s] = 0;
        q.push(s);inq[s] = true;
        while(!q.empty()){
            auto now = q.front();q.pop();
            inq[now] = false;
            //assert(dis[now]>=0);
            for(auto &eid:paths[now]){
                if(e[eid].f == e[eid].c)continue;
                int nxt = e[eid].t;
                if(dis[nxt]>dis[now]+e[eid].w){
                    pre[nxt] = eid;
                    dis[nxt] = dis[now]+e[eid].w;
                    if(!inq[nxt]){
                        inq[nxt] = true;
                        q.push(nxt);
                    }
                }
            }
        }
        return dis[t] != inf;
    }
    T flow(int s,int t,int cnt = INT_MAX){//cnt is the number
of flows
        T ans = 0;
        while(cnt--&&SPFA(s,t)){
            ans += dis[t];
            int now = t;
            while(pre[now] != -1){
                int eid = pre[now];
                e[eid].f++;
                e[eid^1].f--;
                now = e[eid^1].t;
            }
        }
        return ans;
    }
};
#undef T

```



## 2.10 Minimum Cost Maximum Flow

[b5b00]

```
struct Matching {
    queue<int> q; int ans, n;
    vector<int> fa, s, v, pre, match;
    int Find(int u) {
        return u == fa[u] ? u : fa[u] = Find(fa[u]);
    }
    int LCA(int x, int y) {
        static int tk = 0; tk++; x = Find(x); y = Find(y);
        for (;;) swap(x, y) if (x != n) {
            if (v[x] == tk) return x;
            v[x] = tk;
            x = Find(pre[match[x]]);
        }
    }
    void Blossom(int x, int y, int l) {
        for (; Find(x) != l; x = pre[y]) {
            pre[x] = y, y = match[x];
            if (s[y] == 1) q.push(y), s[y] = 0;
            for (int z: {x, y}) if (fa[z] == z) fa[z] = l;
        }
    }
    bool Bfs(auto &&g, int r) {
        iota(fa.begin(), fa.end(), 0); ranges::fill(s, -1);
        q = queue<int>(); q.push(r); s[r] = 0;
        for (; !q.empty(); q.pop()) {
            for (int x = q.front(); int u : g[x])
                if (s[u] == -1) {
                    if (pre[u] = x, s[u] = 1, match[u] == n) {
                        for (int a = u, b = x, last;
                             b != n; a = last, b = pre[a])
                            last = match[b], match[b] = a, match[a] = b;
                        return true;
                    }
                    q.push(match[u]); s[match[u]] = 0;
                } else if (!s[u] && Find(u) != Find(x)) {
                    int l = LCA(u, x);
                    Blossom(x, u, l); Blossom(u, x, l);
                }
        }
        return false;
    }
    Matching(auto &&g) : ans(0), n(int(g.size())),
        fa(n+1), s(n+1), v(n+1), pre(n+1, n), match(n+1, n) {
        for (int x = 0; x < n; ++x)
            if (match[x] == n) ans += Bfs(g, x);
        // match[x] == n means not matched
    }; // test @ yosupo judge
```

## 3 Data Structure

### 3.1 Dynamic Convex Hull [98f67]

```
#define ll long long
// only works for integer coordinates!! maintain max

struct Line {
    mutable ll a, b, p;
    bool operator<(const Line &rhs) const { return a <
        rhs.a; }
    bool operator<(ll x) const { return p < x; }
};

struct CHT : multiset<Line, less<>> {
    static const ll kInf = 1e18;
    ll Div(ll a, ll b) { return a / b - ((a ^ b) < 0 && a %
        b); }
    bool isect(iterator x, iterator y) {
        if (y == end()) { x->p = kInf; return 0; }
        if (x->a == y->a) x->p = x->b > y->b ? kInf : -kInf;
```

```
        else x->p = Div(y->b - x->b, x->a - y->a);
        return x->p >= y->p;
    }
    void addline(ll a, ll b) {
        auto z = insert({a, b, 0}), y = z++, x = y;
        while (isect(y, z)) z = erase(z);
        if (x != begin() && isect(--x, y)) isect(x, y =
            erase(y));
        while ((y = x) != begin() && (--x)->p >= y->p) isect(x,
            erase(y));
    }
    ll query(ll x) {
        auto l = *lower_bound(x);
        return l.a * x + l.b;
    }
};
```

### 3.2 Link Cut Tree [08546]

```
#define ll long long
// 1-based, needs splay
// vertex add paths sum link-cut

struct LCT{
    Splay sp;
    void access(int x){
        sp.splay(x);
        sp.ch[x][1] = 0;
        sp.pull(x);
        while(sp.fa[x]){
            int u = sp.fa[x];
            sp.splay(u);
            sp.push(u);
            sp.ch[u][1] = x;
            sp.pull(u);
            sp.splay(x);
        }
    }
    void makeroot(int x){
        access(x); sp.splay(x);
        sp.rev[x] ^= 1;
    }
    void link(int u, int v){
        makeroot(u);
        sp.splay(u);
        sp.fa[u] = v;
    }
    void cut(int u, int v){
        makeroot(u);
        access(v);
        sp.splay(v);
        int lc = sp.ch[v][0];
        sp.fa[lc] = 0;
        sp.ch[v][0] = 0;
        sp.pull(v);
    }
    ll path_sum(int u, int v){
        makeroot(u);
        access(v);
        sp.splay(v);
        return sp.sum[v];
    }
    void addval(int u, int val){
        sp.splay(u);
        sp.val[u] += val;
        sp.pull(u);
        return;
    }
    int find(int p){
        access(p);
        return sp.get_sz(p, 1);
    }
};
```

```
};
```

### 3.3 Li Chao [7c3a7]

```
// range add line get min
// can even be used if modifies aren't range modify
#define ll long long
const ll SZ = 8e6+10;
const ll inf = 3e18;
vector<ll> all; // coordinates are stored here
struct Line{
    ll m,b;
    Line(ll mm = 0,ll bb = 0):m(mm),b(bb){}
    ll operator()(ll k){
        return m*k+b;
    }
};
struct LiChao{
#define ls now*2+1
#define rs now*2+2
#define mid ((l+r)>>1)
    Line seg[SZ];
    LiChao(){
        fill(seg,seg+SZ,Line(0,inf));
    }
    void modify(int now,int l,int r,int s,int e,Line v){
        if(l == r){
            if(seg[now](all[l])>v(all[l]))swap(seg[now],v);
            return;
        }
        if(l>=s&&e>=r){
            if(seg[now](all[mid])>v(all[mid]))swap(seg[now],v);
            if(seg[now].m<v.m)modify(ls,l,mid,s,e,v);
            else modify(rs,mid+1,r,s,e,v);
        }
        else{
            if(mid>=s)modify(ls,l,mid,s,e,v);
            if(mid<e)modify(rs,mid+1,r,s,e,v);
        }
        return;
    }
    ll getval(int now,int l,int r,int p){
        if(l == r)return seg[now](all[p]);
        if(mid>=p)return min(seg[now](all[p]),getval(ls,l,mid,p));
        else return min(seg[now](all[p]),getval(rs,mid+1,r,p));
    }
    void add_line(int s,int e,Line v){
        modify(0,0,all.size()-1,s,e,v);
        return;
    }
    ll getmin(int p){
        return getval(0,0,all.size()-1,p);
    }
}
#undef ls
#undef rs
#undef mid
};
#undef ll long long
```

### 3.4 Splay [214ae]

```
#define ll long long
const int SZ = 2e5+10;
//1-indexed,0 used for nullptr
//range reverse range sum
struct Splay{
#define ls ch[x][0]
#define rs ch[x][1]
```

```
#define p fa[x]
#define g fa[fa[x]]
ll val[SZ];
ll sum[SZ];
int ch[SZ][2],fa[SZ],cnt,rev[SZ],sz[SZ];
void pull(int x){
    if(!x)return;
    sum[x] = sum[ls]+sum[rs]+val[x];
    sz[x] = sz[ls]+sz[rs]+1;
    return;
}
void push(int x){
    if(!x)return;
    if(rev[x]){
        swap(ls,rs);
        rev[ls] ^= 1;
        rev[rs] ^= 1;
        rev[x] = 0;
    }
    pull(x);
    return;
}
Splay(){
    fill(sz+1,sz+SZ,1);
    return;
}
int newnode(){
    return ++cnt;
}
int dir(int x){//is ls or rs
    return ch[p][1] == x;
}
bool isroot(int x){//the || is for LCT
    return !p||ch[p][dir(x)] != x;
}
void rot(int x){ //g, p, x, here are _g, _p, _x
    int _p = p, _g = g, _x = x;
    push(_g); push(_p); push(_x);
    int d = dir(_x);
    if(!isroot(_p))ch[_g][dir(_p)] = _x;
    fa[ch[_x][d^1]] = _p;
    ch[_p][d] = ch[_x][d^1];
    fa[_x] = _g;
    fa[_p] = _x;
    ch[_x][d^1] = _p;
    pull(_p);
    pull(_x);
    return;
}
void splay(int x){
    if(!x)return;
    while(!isroot(x)){
        push(g); push(p); push(x);
        if(!isroot(p)){
            rot(dir(p) == dir(x)? p: x);
        }
        rot(x);
    }
    push(x);
    return;
}
int get_sz(int x,int y){
    push(x);
    while(x&&sz[ls]+1 != y){
        if(sz[ls]>=y)x = ls;
        else{
            y -= sz[ls]+1;
            x = rs;
        }
        push(x);
    }
    return x;
}
```

```

void merge(int a,int b){
    if(!a||!b)return;
    splay(a);splay(b);
    a = get_sz(a,sz[a]);
    b = get_sz(b,1);
    splay(a);splay(b);
    ch[a][1] = b;
    fa[b] = a;
    pull(a);
    return;
}
pair<int,int> split(int a,int s){
    splay(a);
    if(!s)return make_pair(0,a);
    int b = get_sz(a,s);
    splay(b);
    pair<int,int> re;
    re.first = b;
    re.second = ch[b][1];
    fa[ch[b][1]] = 0;
    ch[b][1] = 0;
    pull(b);
    return re;
}
#undef ls
#undef rs
#undef p
#undef g
};

```

### 3.5 Treap [ff400]

```

#define ll long long
// range reverse range add range sum
// need to push before using the info on node
struct node{
    int pri;
    int pl,pr;
    ll sum,tag,val;
    int sz;
    int rev;
    node(){
        pl = pr = sum = tag = 0;
        sz = 0;
        rev = 0;
        pri = rand();
    }
};

const int SZ = 2e5+10;
struct Treap{
    node nd[SZ];
    int cnt = 0;
    Treap(){
        cnt = 0;
    }
    int newNode(){
        cnt++;
        nd[cnt].sz = 1;
        return cnt;
    }
    void pull(int now){
        if(!now)return;
        nd[now].sz = nd[nd[now].pr].sz+nd[nd[now].pl].sz+1;
        ll ls =
nd[nd[now].pl].sum+nd[nd[now].pl].tag*nd[nd[now].pl].sz;
        ll rs =
nd[nd[now].pr].sum+nd[nd[now].pr].tag*nd[nd[now].pr].sz;
        nd[now].sum = nd[now].val+ls+rs;
        return;
    }
}

```

```

void push(int now){
    if(!now)return;
    if(nd[now].rev){
        swap(nd[now].pl,nd[now].pr);
        if(nd[now].pl)nd[nd[now].pl].rev ^= 1;
        if(nd[now].pr)nd[nd[now].pr].rev ^= 1;
        nd[now].rev = 0;
    }
    int tl = nd[now].pl,tr = nd[now].pr;
    nd[now].val += nd[now].tag;
    if(tl)nd[tl].tag += nd[now].tag;
    if(tr)nd[tr].tag += nd[now].tag;
    nd[now].tag = 0;
    pull(now);
}
int merge(int a,int b){
    if(!a)return b;
    if(!b)return a;
    if(nd[a].pri>nd[b].pri){
        push(a);
        nd[a].pr = merge(nd[a].pr,b);
        pull(a);
        return a;
    }
    else{
        push(b);
        nd[b].pl = merge(a,nd[b].pl);
        pull(b);
        return b;
    }
}
void split(int now,int &a,int &b,int tar){
    if(!now){
        a = b = 0;
        return;
    }
    push(now);
    if(nd[nd[now].pl].sz+1<=tar){
        a = now;
        split(nd[now].pr,nd[a].pr,b,tar-
(nd[nd[now].pl].sz+1));
    }
    else{
        b = now;
        split(nd[now].pl,a,nd[b].pl,tar);
    }
    pull(a);
    pull(b);
    return;
}
};
Treap T;

```

### 3.6 Quadrangle [1d61e]

```

struct QUADRANGLE {
    struct TUPLE {
        int l, r, id;
        TUPLE() {}
        TUPLE(int _l, int _r, int _id) : l(_l), r(_r), id(_id)
    }
};
int n, now;
deque<TUPLE> dq;

int calc_dp(int id, int i) {
    // ...
}
bool cmp(int cid, int pid, int i) {
    // ...
}

```



```

void init(int _n) {
    n = _n;
    now = 1;
    dq.clear();
}
void kill_head() {
    now++;
    if (dq.front().l == dq.front().r) dq.pop_front();
    else dq.front().l++;
}
void push(int id) {
    while (dq.size()) {
        TUPLE tl = dq.back();
        dq.pop_back();
        if (cmp(id, tl.id, tl.l)) {
            continue;
        }
        int l = tl.l, r = tl.r + 1;
        while (l + 1 < r) {
            int mid = (l + r) >> 1;
            (cmp(id, tl.id, mid) ? r : l) = mid;
        }
        dq.push_back(TUPLE(tl.l, l, tl.id));
        if (r <= n) dq.push_back(TUPLE(r, n, id));
        return;
    }
    dq.push_back(TUPLE(now, n, id));
}
int determine(int id) {
    return calc_dp(dq.front().id, id);
}
};

```

### 3.7 SMAWK [f3776]

```

// For all 2x2 submatrix:
// If M[1][0] < M[1][1], M[0][0] < M[0][1]
// If M[1][0] == M[1][1], M[0][0] <= M[0][1]
// M[i][ans_i] is the best value in the i-th row
VI smawk(int N, int M, auto &&select) {
    auto dc = [&](auto self, const VI &r, const VI &c) {
        if (r.empty()) return VI{};
        const int n = (int)r.size(); VI ans(n), nr, nc;
        for (int i : c) {
            while (!nc.empty() &&
                select(r[nc.size() - 1], nc.back(), i))
                nc.pop_back();
            if ((int)(nc.size()) < n) nc.push_back(i);
        }
        for (int i = 1; i < n; i += 2) nr.push_back(r[i]);
        const auto na = self(self, nr, nc);
        for (int i = 1; i < n; i += 2) ans[i] = na[i >> 1];
        for (int i = 0, j = 0; i < n; i += 2) {
            ans[i] = nc[j];
            const int end = i + 1 == n ? nc.back() : ans[i + 1];
            while (nc[j] != end)
                if (select(r[i], ans[i], nc[++j])) ans[i] = nc[j];
        }
        return ans;
    };
    VI R(N), C(M); iota(all(R), 0), iota(all(C), 0);
    return dc(dc, R, C);
}
bool min_plus_conv_select(int r, int u, int v) {
    auto f = [](int i, int j) {
        if (0 <= i - j && i - j < n) return b[j] + a[i - j];
        return 2100000000 + (i - j);
    };
    return f(r, u) > f(r, v);
} // if f(r, v) is better than f(r, u), return true

```

## 4 Geometry

### 4.1 Point [eb195]

```

template<typename T = int>
struct Pt {
    T x, y;
    Pt (T xx = (T)(0), T yy = (T)(0)) : x(xx), y(yy) {}
    Pt operator+(Pt b) const { return Pt(x+b.x, y+b.y); }
    Pt operator-(Pt b) const { return Pt(x-b.x, y-b.y); }
    T operator*(Pt b) const { return x*b.x + y*b.y; }
    T operator^(Pt b) const { return x*b.y - y*b.x; }
    T operator/(Pt b) const { return x*b.y - y*b.x; }
    auto operator<=>(const Pt& b) const = default; // since C++20
    friend int dir(Pt a, Pt b) { // returns sign(a ^ b)
        auto re = a ^ b;
        return re < 0 ? -1 : re > 0 ? 1 : 0;
    }
    friend bool onseg(Pt x, Pt s, Pt e) {
        if (((e-x)^(s-x)) != 0) return false;
        else if ((s-x)*(e-x) > 0) return false;
        return true;
    }
    friend int intersect(Pt s1, Pt e1, Pt s2, Pt e2) { // returns 0
        // if doesn't intersect, 1 if intersect, 2 if on line
        if (onseg(s1, s2, e2) || onseg(e1, s2, e2) || onseg(s2, s1, e1) ||
            onseg(e2, s1, e1)) return 2;
        if (dir(s1-s2, e2-s2)*dir(e1-s2, e2-s2) < 0 && dir(s2-s1, e1-s1)*
            dir(e2-s1, e1-s1) < 0) return 1;
        return 0;
    }
};

```

### 4.2 Convex Hull [17050]

```

// needs Point.cpp
template<typename T = int>
struct ConvexHull {
    // returns in clockwise direction
    // returns strictly on convex hull
    vector<Pt<T>> solve(vector<Pt<T>> v) {
        sort(v.begin(), v.end());
        vector<Pt<T>> u, d;
        for (auto &i : v) {
            if (!u.empty() && u.back() == i) continue;
            while (u.size() > 1 && ((i-u.end()[-1])^(u.end()[-2]-u.end()[-1])) >= 0) u.pop_back();
            while (d.size() > 1 && ((i-d.end()[-1])^(d.end()[-2]-d.end()[-1])) <= 0) d.pop_back();
            u.push_back(i);
            d.push_back(i);
        }
        for (int i = 1; i+1 < d.size(); i++) u.push_back(d.end()[-1-i]);
        return u;
    }
};

```

### 4.3 Tangent of Convex Hull [e8a26]

```

int ori(Pt a, Pt b, Pt c) {
    ll tmp = (b-a) ^ (c-a);
    return tmp > 0 ? 1 : tmp < 0 ? -1 : 0;
}
int cyc_tsearch(int n, auto pred) {

```

```

    if (n == 1) return 0;
    int l = 0, r = n; bool rv = pred(1, 0);
    while(r-l > 1) {
        int m = (l+r) / 2;
        if (pred(0, m) ? rv : pred(m, (m+1) % n)) r = m;
        else l = m;
    }
    return pred(l, r % n) ? l : r % n;
}

pii get_tangent(const vector<Pt> &cvx, Pt p) {
    auto gao = [&](int s) {
        return cyc_tsearch(cvx.size(), [&](int x, int y)
            { return ori(p, cvx[x], cvx[y]) == s; });
    };
    return pii(gao(1), gao(-1));
}

```

#### 4.4 Point In Convex [f8664]

```

bool PointInConvex(const vector<pll> &C, pll p, bool strict
= true) {
    int a = 1, b = SZ(C) - 1, r = !strict;
    if (SZ(C) == 0) return false;
    if (SZ(C) < 3) return r && btw(C[0], C.back(), p);
    if (ori(C[0], C[a], C[b]) > 0) swap(a, b);
    if (ori(C[0], C[a], p) >= r || ori(C[0], C[b], p) <= -r)
        return false;
    while (abs(a - b) > 1) {
        int c = (a + b) / 2;
        (ori(C[0], C[c], p) > 0 ? b : a) = c;
    }
    return ori(C[a], C[b], p) < r;
}

```

#### 4.5 Minkowski Sum [9db95]

```

// needs Point template
template <typename T>
vector<Pt<T>> minkowski(vector<Pt<T>> va, vector<Pt<T>> vb) {
    deque<Pt<T>> a, b;
    for(auto &i:va) a.push_back(i);
    for(auto &i:vb) b.push_back(i);
    Pt head = *min_element(a.begin(), a.end());
    while(a[0].x != head.x || a[0].y != head.y) {
        a.push_back(a[0]);
        a.pop_front();
    }
    head = *min_element(b.begin(), b.end());
    while(b[0].x != head.x || b[0].y != head.y) {
        b.push_back(b[0]);
        b.pop_front();
    }
    a.push_back(a[0]);
    b.push_back(b[0]);
    int p1 = 0, p2 = 0;
    vector<Pt<T>> re;
    while(p1 < a.size() && p2 < b.size()) {
        //cerr<<a.size()<<', '<b.size()<<": "<p1<<' '<p2<<endl;
        int dir = 0;
        re.push_back(a[p1]+b[p2]);
        if(p1+1 == a.size()) dir = 1;
        else if(p2+1 == b.size()) dir = 0;
        else if(((a[p1+1]-a[p1])^(b[p2+1]-b[p2]))>0) dir = 0;
        else dir = 1;
        if(dir == 0) p1++;
        else p2++;
    }
    return re;
}

```

}

#### 4.6 Half Plane Intersection [e35a6]

```

// please don't use with other geometry templates
#define iter(v) v.begin(), v.end()
#define SZ(v) int(v.size())
#define pb emplace_back
#define ff first
#define ss second

using ll = long long;
using pii = pair<int, int>;
using pll = pair<ll, ll>;

template<class A, class B>
ostream &operator<<(ostream &o, pair<A, B> p) {
    return o << '(' << p.ff << ', ' << p.ss << ')';
}

#define temp template<class T>
#define ptt pair<T, T>
#define X ff
#define Y ss
using ld = long double;
using pdd = pair<ld, ld>;

temp ptt operator+(ptt a, ptt b) {
    return {a.X + b.X, a.Y + b.Y};
}
temp ptt operator-(ptt a, ptt b) {
    return {a.X - b.X, a.Y - b.Y};
}
temp ptt operator*(ptt v, T i) {
    return {v.X * i, v.Y * i};
}
temp ptt operator*(T i, ptt v) {
    return {v.X * i, v.Y * i};
}
temp ptt operator/(ptt v, T i) {
    return {v.X / i, v.Y / i};
}
temp T dot(ptt a, ptt b) {
    return a.X * b.X + a.Y * b.Y;
}
temp T cross(ptt a, ptt b) {
    return a.X * b.Y - a.Y * b.X;
}
temp T abs2(ptt a) {
    return dot(a, a);
}
temp ld abs(ptt a) {
    return sqrt(abs2(a));
}
temp int sgn(T v) {
    return v > 0 ? 1 : (v < 0 ? -1 : 0);
}
temp int ori(ptt a, ptt b, ptt c) {
    return sgn(cross(b - a, c - a));
}

// intersects Line(p1, p2), Line(p3, p4)
pdd intersect(pdd p1, pdd p2, pdd p3, pdd p4) {
    ld a123 = cross(p2 - p1, p3 - p1);
    ld a124 = cross(p2 - p1, p4 - p1);
    return (p4 * a123 - p3 * a124) / (a123 - a124);
}

int cmp(pll a, pll b, bool same = true) {
#define is_neg(k) (sgn(k.Y) < 0 || (sgn(k.Y) == 0 &&
sgn(k.X) < 0))
    int A = is_neg(a), B = is_neg(b);
}

```

```

    if (A != B) return A < B;
    if (sgn(cross(a, b)) == 0) return same ? abs2(a) <
abs2(b) : -1;
    return sgn(cross(a, b)) > 0;
}

using Line = pair<pll, pll>;
// cross(p - line.X, line.Y-line.X) <= 0 <-> p in half plane
// LHS when going from line.X to line.Y

pll area_pair(Line a, Line b) {
    return pll(cross(a.Y - a.X, b.X - a.X), cross(a.Y - a.X,
b.Y - a.X));
}

bool isin(Line l0, Line l1, Line l2) {
    auto [a02X, a02Y] = area_pair(l0, l2);
    auto [a12X, a12Y] = area_pair(l1, l2);
    if (a12X - a12Y < 0) a12X *= -1, a12Y *= -1;
    return ((__int128) a02Y * a12X - (__int128) a02X * a12Y >
0;
}

vector<Line> HalfPlaneInter(vector<Line> arr) {
    sort(iter(arr), [&](Line a, Line b) -> int {
        if (cmp(a.Y - a.X, b.Y - b.X, 0) != -1)
            return cmp(a.Y - a.X, b.Y - b.X, 0);
        return ori(a.X, a.Y, b.Y) < 0;
    });
    deque<Line> dq(1, arr[0]);
    for (auto p : arr) {
        if (cmp(dq.back().Y - dq.back().X, p.Y - p.X, 0) == -1)
            continue;
        while (SZ(dq) >= 2 && !isin(p, dq[SZ(dq) - 2],
dq.back()))
            dq.pop_back();
        while (SZ(dq) >= 2 && !isin(p, dq[0], dq[1]))
            dq.pop_front();
        dq.pb(p);
    }
    while (SZ(dq) >= 3 && !isin(dq[0], dq[SZ(dq) - 2],
dq.back()))
        dq.pop_back();
    while (SZ(dq) >= 3 && !isin(dq.back(), dq[0], dq[1]))
        dq.pop_front();
    return vector<Line>(iter(dq));
}

```

## 4.7 Min Enclosing Circle [f416d]

```

typedef pair<int, int> pii;
#define ld double
#define pdd Pt<ld>

ld len(pdd k) {
    return sqrt(k*k);
}

pdd excenter(pdd p0, pdd p1, pdd p2) {
    p1 = p1-p0;
    p2 = p2-p0;
    ld x1 = p1.x, y1 = p1.y, x2 = p2.x, y2 = p2.y;
    ld m = 2.0 * (x1*y2-y1*x2);
    pdd center;
    center.x = (x1*x1*y2 - x2*x2*y1 + y1*y2*(y1-y2)) / m;
    center.y = (x1*x2*(x2-x1) - y1*y1*x2 + x1*y2*y2) / m;
    return center + p0;
}

pdd Minimum_Enclosing_Circle(vector<pdd> dots, ld &r) {
    mt19937 seed(time(0));
    shuffle(dots.begin(), dots.end(), seed);
    pdd cent;

```

```

    cent = dots[0], r = 0;
    for(int i = 1; i < dots.size(); i++) {
        if (len(dots[i]-cent) > r) {
            cent = dots[i], r = 0;
            for(int j = 0; j < i; j++) {
                if (len(dots[j]-cent) > r) {
                    cent = (dots[i]+dots[j]);
                    cent.x /= 2, cent.y /= 2;
                    r = len(dots[i]-cent);
                    for(int k = 0; k < j; k++) {
                        if (len(dots[k]-cent) > r) {
                            cent = excenter(dots[i], dots[j], dots[k]);
                            r = len(dots[k]-cent);
                        }
                    }
                }
            }
        }
    }
    return cent;
}

```

## 4.8 Tangent Of Two Circles [48eb6]

```

struct Cir{ pdd O; double R; };
vector<Line> go( const Cir& c1, const Cir& c2, int sign1 )
{
    // sign1 = 1 for outer tang, -1 for inter tang
    vector<Line> ret;
    double d_sq = abs2(c1.O - c2.O);
    if (sign(d_sq) == 0) return ret;
    double d = sqrt(d_sq);
    pdd v = (c2.O - c1.O) / d;
    double c = (c1.R - sign1 * c2.R) / d;
    if (c * c > 1) return ret;
    double h = sqrt(max(0.0, 1.0 - c * c));
    for (int sign2 = 1; sign2 >= -1; sign2 -= 2) {
        pdd n = pdd(v.X * c - sign2 * h * v.Y,
v.Y * c + sign2 * h * v.X);
        pdd p1 = c1.O + n * c1.R;
        pdd p2 = c2.O + n * (c2.R * sign1);
        if (sign(p1.X - p2.X) == 0 and
sign(p1.Y - p2.Y) == 0)
            p2 = p1 + perp(c2.O - c1.O);
        ret.pb(Line(p1, p2));
    }
    return ret;
}

```

## 4.9 Circle Cover [861b1]

```

const int N = 1021;
struct CircleCover {
    int C;
    Cir c[N];
    bool g[N][N], overlap[N][N];
    // Area[i] : area covered by at least i circles
    double Area[ N ];
    void init(int _C){ C = _C; }
    struct Teve {
        pdd p; double ang; int add;
        Teve() {}
        Teve(pdd _a, double _b, int _c):p(_a), ang(_b), add(_c)
    }
    bool operator<(const Teve &a)const
    {return ang < a.ang;}
}eve[N * 2];
// strict: x = 0, otherwise x = -1
bool disjuct(Cir &a, Cir &b, int x)

```

```

{return sign(abs(a.0 - b.0) - a.R - b.R) > x;}
bool contain(Cir &a, Cir &b, int x)
{return sign(a.R - b.R - abs(a.0 - b.0)) > x;}
bool contain(int i, int j) {
    /* c[j] is non-strictly in c[i]. */
    return (sign(c[i].R - c[j].R) > 0 || (sign(c[i].R -
c[j].R) == 0 && i < j)) && contain(c[i], c[j], -1);
}
void solve(){
    fill_n(Area, C + 2, 0);
    for(int i = 0; i < C; ++i)
        for(int j = 0; j < C; ++j)
            overlap[i][j] = contain(i, j);
    for(int i = 0; i < C; ++i)
        for(int j = 0; j < C; ++j)
            g[i][j] = !(overlap[i][j] || overlap[j][i] ||
disjunct(c[i], c[j], -1));
    for(int i = 0; i < C; ++i){
        int E = 0, cnt = 1;
        for(int j = 0; j < C; ++j)
            if(j != i && overlap[j][i])
                ++cnt;
        for(int j = 0; j < C; ++j)
            if(i != j && g[i][j]) {
                pdd aa, bb;
                CCinter(c[i], c[j], aa, bb);
                double A = atan2(aa.Y - c[i].O.Y, aa.X -
c[i].O.X);
                double B = atan2(bb.Y - c[i].O.Y, bb.X -
c[i].O.X);
                eve[E++] = Teve(bb, B, 1), eve[E++] = Teve(aa, A,
-1);
                if(B > A) ++cnt;
            }
        if(E == 0) Area[cnt] += pi * c[i].R * c[i].R;
        else{
            sort(eve, eve + E);
            eve[E] = eve[0];
            for(int j = 0; j < E; ++j){
                cnt += eve[j].add;
                Area[cnt] += cross(eve[j].p, eve[j + 1].p) * .5;
                double theta = eve[j + 1].ang - eve[j].ang;
                if (theta < 0) theta += 2. * pi;
                Area[cnt] += (theta - sin(theta)) * c[i].R *
c[i].R * .5;
            }
        }
    }
}
};

```

## 5 String

### 5.1 Z Algorithm [7a5e2]

```

template <typename T>
struct Z_alg {
    void operator()(T a, int n, int *z) {
        z[0] = 0;
        int l = 0;
        for (int i = 1; i <= n; i++) {
            for (z[i] = max(0, min(z[i - l], l + z[l] - i)); i +
z[i] < n && a[i + z[i]] == a[z[i]]; z[i]++);
            if (i + z[i] > l + z[l]) l = i;
        }
    }
};

```

### 5.2 KMP [bb2a1]

```

template <typename T>
struct KMP {
    void operator()(T a, int n, int *pi) {
        pi[0] = -1, pi[1] = 0;
        for (int i = 1; i < n; i++) {
            int j = pi[i];
            while (j >= 0 && a[i] != a[j]) j = pi[j];
            pi[i + 1] = j + 1;
        }
    }
};

```

### 5.3 Aho Corasick [fa0e4]

```

// only construct the automaton
struct AC {
    const static int c0 = 'a';
    int nc, c[MXN], pi[MXN], p[MXN], ch[MXN][MXC];
    void init() {
        nc = 2;
        fill(ch[0], ch[0] + MXC, 1);
        fill(ch[1], ch[1] + MXC, -1);
    }
    int nn(int pp, char cc) {
        c[nc] = cc;
        p[nc] = pp;
        fill(ch[nc], ch[nc] + MXC, -1);
        return nc++;
    }
    int push(const string &s) {
        int u = 1;
        for (auto &i : s) {
            int e = i - c0;
            if (!~ch[u][e]) ch[u][e] = nn(u, i);
            u = ch[u][e];
        }
        return u;
    }
    void build() {
        queue<int> q;
        q.push(1);
        while (q.size()) {
            int u = q.front();
            q.pop();
            pi[u] = (u == 1 ? 0 : ch[pi[p[u]]][c[u] - c0]);
            FOR(e, 0, MXC) {
                if (!~ch[u][e]) ch[u][e] = ch[pi[u]][e];
                else q.push(ch[u][e]);
            }
        }
    }
};

```

### 5.4 Manacher [b6ad8]

```

template <typename T>
struct MANACHER {
    void operator()(T a, int n, int *mn) {
        int l = 0;
        mn[0] = 0;
        for (int i = 1; i < n; i++) {
            mn[i] = (l + mn[l] >= i ? min(mn[2 * l - i], l + mn[l]
- i) : 0);
            while (i - mn[i] - 1 >= 0 && i + mn[i] + 1 < n && a[i
- mn[i] - 1] == a[i + mn[i] + 1]) mn[i]++;
            if (i + mn[i] > l + mn[l]) l = i;
        }
    }
};

```

};

## 5.5 Suffix Array [a683f]

```

int SA[MXN * 2], H[MXN], RA[MXN];
namespace SAIS {
    bool _t[MXN * 2];
    int _s[MXN * 2], _c[MXN * 2], x[MXN], _p[MXN], _q[MXN * 2];
    void pre(int *sa, int *c, int n, int z) {
        fill_n(sa, n, 0);
        copy_n(c, z, x);
    }
    void induce(int *sa, int *c, int *s, bool *t, int n, int z) {
        copy_n(c, z - 1, x + 1);
        FOR(i, 0, n) {
            if (sa[i] && !t[sa[i] - 1]) {
                sa[x[s[sa[i] - 1]]++] = sa[i] - 1;
            }
        }
        copy_n(c, z, x);
        for (int i = n - 1; i >= 0; i--) {
            if (sa[i] && t[sa[i] - 1]) {
                sa[--x[s[sa[i] - 1]]] = sa[i] - 1;
            }
        }
    }
    void sais(int *s, int *sa, int *p, int *q, bool *t, int *c, int n, int z) {
        bool uniq = t[n - 1] = true;
        int nn = 0, nmzx = -1, *nsa = sa + n, *ns = s + n, last = -1;
        fill_n(c, z, 0);
        FOR(i, 0, n) uniq &= ++c[s[i]] < 2;
        partial_sum(c, c + z, c);
        if (uniq) {
            FOR(i, 0, n) sa[--c[s[i]]] = i;
            return;
        }
        for (int i = n - 2; i >= 0; i--) {
            t[i] = (s[i] == s[i + 1] ? t[i + 1] : s[i] < s[i + 1]);
        }
        pre(sa, c, n, z);
        FOR(i, 1, n) {
            if (t[i] && !t[i - 1]) {
                sa[--x[s[i]]] = p[q[i] = nn++] = i;
            }
        }
        induce(sa, c, s, t, n, z);
        FOR(i, 0, n) {
            if (sa[i] && t[sa[i]] && !t[sa[i] - 1]) {
                bool neq = last < 0 || !equal(s + sa[i], s + p[q[sa[i]] + 1], s + last);
                ns[q[last = sa[i]]] = nmzx += neq;
            }
        }
        sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmzx + 1);
        pre(sa, c, n, z);
        for (int i = nn - 1; i >= 0; i--) {
            sa[--x[s[p[nsa[i]]]]] = p[nsa[i]];
        }
        induce(sa, c, s, t, n, z);
    }
    void mkhei(int n) {
        for (int i = 0, j = 0; i < n; i++) {
            if (RA[i]) {
                for (; i + j < n && SA[RA[i] - 1] + j < n && _s[i + j] == _s[SA[RA[i] - 1] + j]; ++j);
            }
        }
    }
}

```

```

        H[RA[i]] = j, j = max(0, j - 1);
    }
}
}
void build(int *s, int n, int mxc) {
    copy_n(s, n, _s), _s[n] = 0;
    sais(_s, SA, _p, _q, _t, _c, n + 1, mxc);
    copy_n(SA + 1, n, SA);
    FOR(i, 0, n) RA[SA[i]] = i;
    mkhei(n);
    copy(H + 1, H + n, H);
}
}

```

## 5.6 SAM [47371]

```

struct SAM {
    static const int MXND = 1000005, MXC = 33, C0 = 'a';
    int tot, rt, lst, pi[MXND], mx[MXND];
    int nxt[MXND][MXC], cnt[MXND], in[MXND];
    int newNode() {
        int res = ++tot;
        fill(nxt[res], nxt[res] + MXC, 0);
        pi[res] = mx[res] = cnt[res] = in[res] = 0;
        return res;
    }
    void init() {
        tot = 0;
        rt = newNode();
        pi[rt] = 0, mx[rt] = 0;
        lst = rt;
    }
    void push(int c) {
        int p = lst;
        int np = newNode();
        mx[np] = mx[p] + 1;
        for (; p && nxt[p][c] == 0; p = pi[p])
            nxt[p][c] = np;
        if (p == 0) pi[np] = rt;
        else {
            int q = nxt[p][c];
            if (mx[p] + 1 == mx[q]) pi[np] = q;
            else {
                int nq = newNode();
                mx[nq] = mx[p] + 1;
                for (int i = 0; i < MXC; i++)
                    nxt[nq][i] = nxt[q][i];
                pi[nq] = pi[q];
                pi[q] = nq;
                pi[np] = nq;
                for (; p && nxt[p][c] == q; p = pi[p])
                    nxt[p][c] = nq;
            }
        }
        lst = np, cnt[np] = 1;
    }
    void push(char *str) {
        for (int i = 0; str[i]; i++)
            push(str[i] - C0 + 1);
    }
    void count() {
        for (int i = 1; i <= tot; ++i)
            ++in[pi[i]];
        queue<int> q;
        for (int i = 1; i <= tot; ++i)
            if (!in[i]) q.push(i);
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            cnt[pi[u]] += cnt[u];
            if (!--in[pi[u]])
                q.push(pi[u]);
        }
    }
}

```



```

    q.push(pi[u]);
}
}
} sam;

```

## 5.7 eertree [ca7d7]

```

#define pb emplace_back
struct eertree {
    const static int MXC = 26, C0 = 'a';
    struct nd {
        int nxt[MXC], pi, len;
        int cnt, num; // optional
        nd(int l = 0) : pi(0), len(l), cnt(0), num(0) {
            fill(nxt, nxt + MXC, 0);
        }
    };
    vector<nd> v;
    vector<char> s;
    int lst, n;
    eertree() : v(2), lst(1), n(0) {
        v[0].pi = 1, v[1].len = -1, s.pb(-1);
    }
    void clear() {
        v.clear(), s.clear(), lst = 1, n = 0;
        v.pb(0), v.pb(-1);
        v[0].pi = 1, s.pb(-1);
    }
    int get_fail(int x) {
        while (s[n - v[x].len - 1] != s[n])
            x = v[x].pi;
        return x;
    }
    void add(int c) {
        s.push_back(c -= 'a'), ++n;
        int cur = get_fail(lst);
        if (!v[cur].nxt[c]) {
            int now = v.size();
            v.pb(v[cur].len + 2);
            v[now].pi =
                v[get_fail(v[cur].pi)].nxt[c];
            v[cur].nxt[c] = now;
            v[now].num = v[v[now].pi].num + 1;
        }
        lst = v[cur].nxt[c], ++v[lst].cnt;
    }
    void count() {
        for (auto i = v.rbegin(); i != v.rend(); i++) {
            v[i -> pi].cnt += i -> cnt;
        }
    }
    inline int size() {
        return v.size() - 2;
    }
};

```

## 5.8 minimal rotation [7b1de]

```

string mcp(string s) {
    int n = s.size(), i = 0, j = 1;
    s += s;
    while (i < n && j < n) {
        int k = 0;
        while (k < n && s[i + k] == s[j + k]) ++k;
        if (s[i + k] <= s[j + k]) j += k + 1;
        else i += k + 1;
        if (i == j) ++j;
    }
    int ans = i < n ? i : j;
}

```

```

return s.substr(ans, n);
}

```

## 6 Math

### 6.1 Chinese Remainder Theorem [6fdd6]

```

using lll = __int128_t;

struct ICRT {
    lll p1, p2, p3;
    lll c1, c2, c3;
    ICRT() {}
    ICRT(lll _p1, lll _p2, lll _p3) : p1(_p1), p2(_p2),
    p3(_p3) {
        auto POW = [&](lll a, lll b, lll mod) -> lll {
            lll ans = 1;
            while (b) {
                if (b & 1) ans = ans * a % mod;
                b >>= 1;
                a = a * a % mod;
            }
            return ans;
        };
        c1 = POW(p2 * p3 % p1, p1 - 2, p1) * p2 * p3;
        c2 = POW(p3 * p1 % p2, p2 - 2, p2) * p3 * p1;
        c3 = POW(p1 * p2 % p3, p3 - 2, p3) * p1 * p2;
    }
    lll operator()(int r1, int r2, int r3) {
        return (c1 * r1 + c2 * r2 + c3 * r3) % (p1 * p2 * p3);
    }
};

ICRT icrt(998244353, 104857601, 167772161);

```

### 6.2 Euclid [ffed2]

```

struct euclid{
    ll x, y, g;
    void ec(ll a, ll b){
        // minimum integer solution of "ax+by=g, x>0"
        if(!b) return void((x=1, y=0, g=a));
        ec(b, a%b);
        swap(x, y);
        y -= a/b*x+a/g;
        x += b/g;
    }
    inline euclid(ll a, ll b){
        ec(abs(a), abs(b));
        if(b<0) y = -y;
        if(a<0) x = -x;
    }
};

```

### 6.3 FFT [70ff0]

```

using cd = complex<double>;
struct PolyF : public vector<cd> {
    static constexpr double PI = 3.14159265358979323;
    PolyF() : vector<cd>() {}
    PolyF(size_t sz) : vector<cd>(sz) {}
    void conv(size_t N, bool inv = 0) {
        assert(size() && N >= size());
        int LG = __lg(N);
        assert(N == (1 << LG));
        resize(N);
        vector<int> r(N);
    }
};

```

```

FOR(i, 1, N) {
    int i_ = i ^ (1 << __lg(i));
    r[i] = r[i_] << (__lg(i) - __lg(i_)) | 1;
    int j = r[i] << (LG - 1 - __lg(i));
    if (i < j) {
        std::swap(at(i), at(j));
    }
}
for (int w = 1; w < N; w <= 1) {
    FOR(ok, 0, w) {
        double th = PI * ok / w * (inv ? -1 : 1);
        cd o(cos(th), sin(th));
        for (int s = 0; s < N; s += (w < 1)) {
            cd &L = at(s + ok), &R = at(s + ok + w);
            cd l = L, r = o * R;
            L = l + r;
            R = l - r;
        }
    }
}
if (inv) {
    FOR(i, 0, N) {
        at(i) /= N;
    }
}
};

```

## 6.4 FWT [b1077]

```

//      AND      OR      XOR
// | 1 1 | | 1 0 | | 1 1 |
// | 0 1 | | 1 1 | | 1 -1 |

struct FWT {
    // mod operations ADD, SUB, MUL, POW (if needed)
    void btf(int &L, int &R, bool inv) { // sample: XOR
        int l = L, r = R;
        L = ADD(l, r);
        R = SUB(l, r);
    }
    void operator()(int *a, int n, bool inv) {
        // sample: XOR
        for (int w = 1; w < n; w <= 1) {
            FOR(i, 0, n) if (i & w) {
                btf(a[i - w], a[i], inv);
            }
        }
        if (inv) {
            int x = POW(n, mod - 2);
            FOR(i, 0, n) a[i] = MUL(a[i], x);
        }
    }
};

```

## 6.5 NTT [592be]

```

#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)

struct NTT {
    const static int LG = 20;
    int mod;
    int o[(1 << LG) + 1];
    int ADD(int a, int b) {
        // help yourself
    }
    int SUB(int a, int b) {
        // help yourself
    }
};

```

```

int MUL(int a, int b) {
    // help yourself
}
int POW(int a, int b) {
    // help yourself
}
NTT(int g, int gap, int _mod) {
    mod = _mod;
    o[0] = 1;
    int pp = POW(g, gap);
    FOR(i, 1, (1 << LG) + 1) o[i] = MUL(o[i - 1], pp);
}
void operator()(int *a, int n, bool inv) {
    auto REV = [&](int x) -> int {
        int ans = 0;
        for (int w = 1; w < n; w <= 1) {
            ans = (ans << 1) | (x & 1);
            x >>= 1;
        }
        return ans;
    };
    FOR(i, 0, n) {
        int j = REV(i);
        if (i < j) swap(a[i], a[j]);
    }
    for (int w = 1; w < n; w <= 1) {
        int owo = 1 << (LG - __lg(w) - 1), oid = 0;
        FOR(i, 0, w) {
            int omega = o[inv ? (1 << LG) - oid : oid];
            for (int s = 0; s < n; s += (w < 1)) {
                int &L = a[s + i], &R = a[s + w + i];
                int l = L, r = MUL(omega, R);
                L = ADD(l, r);
                R = SUB(l, r);
            }
            oid += owo;
        }
    }
    if (inv) {
        int x = POW(n, mod - 2);
        FOR(i, 0, n) a[i] = MUL(a[i], x);
    }
};

NTT ntt1(3, 952, 998244353);
NTT ntt2(3, 100, 104857601);
NTT ntt3(3, 160, 167772161);

namespace POLY {
    const int MXM = 4 * MXN;
    int a[MXM], b[MXM];
    vector<int> VMUL(vector<int> v, vector<int> w, int m) {
        int N = 4 << __lg(m);
        fill(a, a + N, 0);
        fill(b, b + N, 0);
        int na = min((int) v.size(), m), nb = min((int)
w.size(), m);
        FOR(i, 0, na) a[i] = v[i];
        FOR(i, 0, nb) b[i] = w[i];
        ntt(a, N, false);
        ntt(b, N, false);
        FOR(i, 0, N) a[i] = MUL(a[i], b[i]);
        ntt(a, N, true);
        vector<int> ans;
        FOR(i, 0, m) ans.push_back(a[i]);
        return ans;
    }
}

```

## 6.6 Pollard Rho [b24d9]

```
// needs mad,mub,mul,pw with changable mod
//!!! use int128 for pw and mul

bool isprime(ll x) {
    if (x <= 2 || ~x & 1) return x == 2;
    auto witn = [&](ll a, int t) {
        for (ll a2; t-- && (a2 = mul(a, a, x)); a = a2)
            if (a2 == 1 && a != 1 && a != x - 1) return true;
        return a > 1;
    };
    int t = __builtin_ctzll(x-1); ll odd = (x-1) >> t;
    for (ll m: {2, 325, 9375, 28178, 450775, 9780504, 1795265022})
        if (witn(pw(m % x, odd, x), t)) return false;
    return true;
}

ll pollard_rho(ll n) {
    static mt19937_64 rnd(120821011);
    if (!(n & 1)) return 2;
    ll y = 2, z = y, c = rnd() % n, p = 1, i = 0, t;
    auto f = [&](ll x) {
        return mad(mul(x, x, n), c, n);
    };
    do {
        p = mul(mub(z = f(f(z)), y = f(y), n), p, n);
        if (++i &= 63) if (i == (i & -i)) t = gcd(p, n);
    } while (t == 1);
    return t == n ? pollard_rho(n) : t;
}

vector<ll> factorize(ll k){
    if(k == 1)return {};
    else if(isprime(k))return {k};
    else{
        vector<ll> re;
        function<void>(ll) dc = [&](ll k){
            if(isprime(k)){
                re.push_back(k);
                return;
            }
            ll x = pollard_rho(k);
            dc(x);dc(k/x);
        };
        dc(k);
        sort(re.begin(),re.end());
        return re;
    }
}
```

```
#include <stdint.h>
#include <string.h>
#include <unistd.h>

int main() {
    float A = 0, B = 0;
    float i, j;
    int k;
    float z[1760];
    char b[1760];
    printf("\x1b[2J");
    for(;;) {
        memset(b,32,1760);
        memset(z,0,7040);
        for(j=0; j < 6.28; j += 0.07) {
            for(i=0; i < 6.28; i += 0.02) {
                float c = sin(i);
                float d = cos(j);
                float e = sin(A);
                float f = sin(j);
                float g = cos(A);
                float h = d + 2;
                float D = 1 / (c * h * e + f * g + 5);
                float l = cos(i);
                float m = cos(B);
                float n = sin(B);
                float t = c * h * g - f * e;
                int x = 40 + 30 * D * (l * h * m - t * n);
                int y = 12 + 15 * D * (l * h * n + t * m);
                int o = x + 80 * y;
                int N = 8 * ((f * e - c * d * g) * m - c * d * e - f
                    * g - l * d * n);
                if(22 > y && y > 0 && x > 0 && 80 > x && D > z[o]) {
                    z[o] = D;
                    b[o] = ".,-~:;!=*#$@[N > 0 ? N : 0];
                }
            }
        }
        printf("\x1b[H");
        for(k = 0; k < 1761; k++) {
            putchar(k % 80 ? b[k] : 10);
            A += 0.00004;
            B += 0.00002;
        }
        usleep(30000);
    }
    return 0;
}
```

## 6.7 Floor Sum [713b0]

```
ll floor_sum(ll a, ll b, ll c, ll n) {
    // floor((a * x + b) / c) for x in [0, n]
    if (n < 0) return 0;
    if (a == 0) return b / c * (n + 1);
    if (a >= c || b >= c) return (n * (n + 1) / 2 * (a / c) +
        (b / c) * (n + 1)) + floor_sum(a % c, b % c, c, n);
    int m = (a * n + b) / c;
    return m * n - floor_sum(c, c - b - 1, a, m - 1);
}
```

## 7 Ideograph Advantage

### 7.1 3d Donut [1ff2e]

```
#include <stdio.h>
#include <math.h>
```

## 8 Notes

- NO PATH COMPRESSION on rollback dsu please

