Homework #6 Message Exchange Protocol Design

CNS Course Sapienza

Riccardo Prinzivalle, 1904064

December 11, 2020

1 Homework Goal

This homework contains a basic design and implementation of a message exchange *secure* protocol. The idea is taken from different protocols learned from the slides and the lessons of the course. The implementation is done using the **Kathara** framework to virtualize a small network, while the protocol is written using bash scripting exploiting the **OpenSSL** library on Linux.

2 Protocol Design

The protocol can be divided into three main functionalities: *confidentiality*, *message authentication* and *entity authentication*. Each functionality is developed as follows:

- Confidentiality is achieved by using symmetric encryption with AES in CBC mode with key length of 256 bits, which is the standard for confidentiality for NSA [1].
- Message Authentication is performed with SHA-256 using public key signature (OpenSSL supports directly HMAC but the version installed on the docker image on the background of Kathara is older than the minimum version implementing HMAC).
- Entity Authentication is based on a weaker version of the X.509 protocol, which introduces some vulnerabilities but simplifies the implementation, since this part is done by hand since OpenSSL contains only the primitives and not a complete authentication protocol.

Let's analyze every part more in the details. Encryption is the simpler; it just uses the primitive from OpenSSL as follows:

openssl aes-256-cbc -in message/to/encrypt -out encrypted/message -pass file:key/file

3 Protocol Proof of Concept

This work compares the proposed implementation of RSA with a common library implementation of RSA itself and AES, the last one just to have an idea of how symmetric ciphers are in general more computational efficient than asymmetric ones. To have a fair comparison, AES uses 128 bit key, so as stated in table 1, it is necessary to have 3072 bit key for RSA. In the implementation proposed, since the key must have a length of 3072 bit, both p and q have a length of 1536 bit so their product has the correct length for the resulting key, as stated in section 7.6 of [2].

| Algorithm Family | Cryptosystems | Security Level (bit) | | | |
|-----------------------|------------------|----------------------|------|------|-------|
| | | 80 | 128 | 192 | 256 |
| Integer Factorization | RSA | 1024 | 3072 | 7680 | 15360 |
| Discrete Logarithm | DH, DSA, Elgamal | 1024 | 3072 | 7680 | 15360 |
| Elliptic Curves | ECDH, ECDSA | 160 | 256 | 384 | 512 |
| Symmetric key | AES, 3DES | 80 | 128 | 192 | 256 |

Table 1: Key length comparison in public key and symmetric key algorithm

The 3072 bit key allows to encrypt a maximum of $3072 \div 8 = 384$ bytes, this is due to the characteristics of RSA itself, otherwise the modulo reduction will collapse the oversize message inside the modulo domain and it will be impossible to recover the original message after decryption. To overcome this limit, an idea could be to implement operation mode on asymmetric ciphers, but it is not feasible due to the fact that these ciphers are so much slower with respect to symmetric ones, and it is better to use the latter to encrypt larger messages. For these reasons, the message to be encrypted has been chosen of dimension around 313 bytes. The proposed implementation needs to preprocess data to be sure to give to the encryption phase a integer number, this is done by the instruction binarybuffer = ''.join(format(ord(x), 'b') for x in buffer) which produces an output in binary form, which is then converted into base ten numbers by using the instruction int(binarybuffer, 2) whose output is used in the encryption phase.

For **RSA** comparison, both the key generation and message encryption are measured separately; the key generation is called once for every test since it requires more time with respect to the encryption phase, while the message encryption can be called more times by specifying the number of rounds when calling the function. Since the key generation phase requires different time depending on

the test performed, I decided to perform 4 times the tests in different times of the day, and the median value are represented in tab. 2; encryption and decryption value are much more stable in different tests (All the original tests value can be found in the output.txt file attached with this report).

| RSA | key generation | encryption throughput | decryption throughput |
|-------------------------|-------------------|--------------------------|--------------------------|
| PyCryptoDome | 11.68 sec | 52,7 KB/s | 6,37 KB/s |
| Proposed implementation | 6.73 sec | 0,825 KB/s | $0.807~\mathrm{KB/s}$ |

Table 2: RSA time and throughput comparison

It is necessary to add that PyCryptoDome RSA implements a padding scheme, while the proposed implementation does not, which offer less security and maybe requires less computation effort. The strange thing is that the proposed key generation algorithm needs less time on average with respect to the PyCryptoDome one: as stated in [?], os.urandom, which is used here to generate the prime random numbers, uses on windows (on which I performed the tests) the function CryptGenRandom [?], which I was not able to understand if it waits effectively for the entropy pool to be full enough, but since os.urandom uses /dev/urandom on Linux machines, which does not check if the entropy pool is filled up, probably neither the windows function does it, so here the reason for which the proposed implementation needs less time on average.

Instead, as it was easily predictable, the library implementation has much more throughput, both in encryption and decryption, with slower decryption, while the proposed implementation has much more similar time for both phases (it uses the same function for both), probably the library implementation has some tricks to speed up the process which are possible only on one way in encryption. To obtain a comparison with AES, I have chosen to use the ECB mode with padding; this is just for educational purposes, it is already known that symmetric ciphers are faster than public keys ones. The comparison is represented in tab. 2.

Here, the time used by the key generation phase in RSA is not represented since the comparison this time is just on the pure encryption and decryption phase assuming we already have the keys for both algorithms.

4 Security Analysis

Figure 1: Improved version of Square And Multiply

| AES vs RSA | Encryption | Decryption |
|--------------|------------|-----------------------|
| AES ECB mode | 1,49 MB/s | 1,49 MB/s |
| Proposed RSA | 0,825 KB/s | $0.807~\mathrm{KB/s}$ |

Table 3: RSA vs AES comparison

5 Conclusion

In this homework, as a difference with respect to the AES implementation, the code is based mainly on existent libraries, with the exception of few functions, whose implementation is based on pseudocode of already known algorithms, with small improvements in order to speed up the computations. The bigger improvement is the introduction of the modulo reduction on every computation of SAM, without it the proposed implementation didn't work as the result grew too much and it remained stuck after some iterations. As expected, also in this case the work is slower than the library implementation, with the exception of the key generation phase, which needs much more digging to reach the real cause of its larger throughput.

References

- [1] Commercial national security algorithm suite and quantum computing faq. https://cryptome.org/2016/01/CNSA-Suite-and-Quantum-Computing-FAQ.pdf, 2016.
- [2] C. Paar and J. Pelzl. *Understanding Cryptography: A Textbook for Students and Practitioners*. Springer Publishing Company, Incorporated, 1st edition, 2009.