

Homework #4

Elliptic Curves

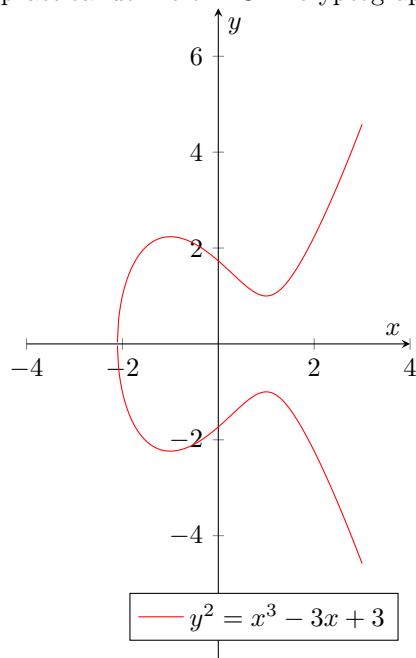
CNS Course Sapienza

Riccardo PRINZIVALLE, 1904064

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1 Homework Goal

This homework contains a basic introduction on Elliptic Curves (EC), the general idea on the math basis, the Discrete Logarithm Problem with EC and the practical utilize of EC in cryptography.



2 Elliptic Curves Motivation

Elliptic Curves are the main trend in asymmetric encryption today: why is their usage so spread? This question has a simple answer: it is sufficient to look

at table 1, where there is a comparison of the key length needed to guarantee the same level of security; the bare minimum number of bits is defined by the symmetric key encryption scheme, we cannot have a smaller key with respect to the symmetric case and have the same level of security; then asymmetric schemes need, in general, a large number of bits to guarantee the same level of security, the fact is that elliptic curves cryptography needs less than $\frac{1}{10}$ of the bits needed for another asymmetric scheme supposed the same level of security, and this relationship become smaller as the level of security grows. Indeed, if one wants to use a public key cryptography scheme, elliptic curves are the suggested choice to guarantee security without using much computational effort.

Algorithm Family	Cryptosystems	Security Level (bit)			
		80	128	192	256
Integer Factorization	RSA	1024	3072	7680	15360
Discrete Logarithm	DH, DSA, Elgamal	1024	3072	7680	15360
Elliptic Curves	ECDH, ECDSA	160	256	384	512
Symmetric key	AES, 3DES	80	128	192	256

Table 1: Key length comparison in public key and symmetric key algorithm

3 Mathematical background

4 Discrete Logarithm Problem with Elliptic Curves

(a) Core (b) Preprocessing

Figure 1: Mix columns base functions

5 Use of Elliptic Curves in Cryptography

6 Conclusion

Even if the implementation proposed is much slower than the standard library chosen as comparison, it works well and it does its dirty job. The code may

not be much optimized or it can have been written in a better way but my knowledge in python is not so huge, but this was an opportunity to dust and improve my experience.