GSERM - St. Gallen 2025 Analyzing Panel Data

June 19, 2025

Causation

The goal: Making causal inferences from observational data.

- Establish and measure the *causal* relationship between variables in a non-experimental setting.
- The fundamental problem of causal inference:

It is impossible to observe the causal effect of a treatment or a predictor on a single unit.

- Specific challenges:
 - · Confounding
 - · Selection bias
 - · Heterogenous treatment effects

Causation and Counterfactuals

Causal statements imply counterfactual reasoning.

- "If the cause(s) had been different, the outcome(s) would be different, too."
- Conditioning, probabilistic and causal:

Probabilistic conditioning	Causal conditioning
Pr(Y X=x)	Pr[Y do(X=x)]
Factual	Counterfactual
Select a sub-population	Generate a new population
Predicts passive observation	Predicts active manipulation
Calculate from full DAG*	Calculate from surgically-altered DAG*
Always identifiable when X and Y	Not always identifiable even when
are observable	X and Y are observable

^{*}See below. Source: Swiped from Shalizi, "Advanced Data Analysis from an Elementary Point of View", Table 23.1.

- Causality (typically) implies / requires:
 - · Temporal ordering
 - · Mechanism
 - · Correlation

The Counterfactual Paradigm

Notation

- *N* observations indexed by i, $i \in \{1, 2, ...N\}$
- Outcome variable Y
- Interest: the effect on Y of a treatment variable W:
 - · $W_i = 1 \leftrightarrow \text{observation } i \text{ is "treated"}$
 - · $W_i = 0 \leftrightarrow \text{observation } i \text{ is "control"}$

Potential Outcomes

- Y_{0i} = the value of Y_i if $W_i = 0$
- Y_{1i} = the value of Y_i if $W_i = 1$
- $\delta_i = (Y_{1i} Y_{0i}) = \text{the } \underline{\text{treatment effect}} \text{ of } W$

Treatment Effects

The average treatment effect (ATE) is just:

$$\begin{split} \mathsf{ATE} &\equiv \bar{\delta} &= \mathsf{E}(Y_{1i} - Y_{0i}) \\ &= &\frac{1}{N} \sum_{i=1}^N Y_{1i} - Y_{0i}. \end{split}$$

BUT we observe only Y_i :

$$Y_i = \begin{cases} Y_{0i} \text{ if } W_i = 0, \\ Y_{1i} \text{ if } W_i = 1. \end{cases}$$

or (equivalently)

$$Y_i = W_i Y_{1i} + (1 - W_i) Y_{0i}.$$

Estimating Treatment Effects

Key to estimating treatment effects: Assignment mechanism for W.

Neyman/Rubin/Holland: Treat inability to observe Y_{0i} / Y_{1i} as a missing data problem.

[press "pause"]

Missing Data Review

Notation:

$$\mathbf{X}_{N \times K} \cup \{\mathbf{W}, \mathbf{Z}\}$$

W have some missing values, Z are "complete"

Consider a matrix **R** with:

$$R_{ik} = \begin{cases} 1 & \text{if } X_{ik} \text{ is missing,} \\ 0 & \text{otherwise.} \end{cases}$$

$$\pi_{ik} = \Pr(R_{ik} = 1)$$

Missing Data (continued)

Rubin's flavors of missingness:

• Missing completely at random ("MCAR") (= "ignorable"):

$$R \perp \{Z, W\}$$

• Missing at random ("MAR") (conditionally "ignorable"):

$$R \perp W \mid Z$$

 Anything else is "informatively" (or "non-ignorably") missing ("MNAR").

Rubin's Flavors Remix

Suppose we have two variables, an outcome Y and a covariate / predictor X. Define $R_{(Y)}$ as the vector of missing data indicators for Y (analogously to above).

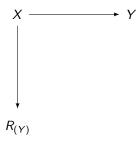
Then:

$$X \longrightarrow Y$$

 $R_{(Y)}$

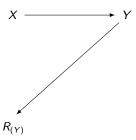
Missing Completely At Random (MCAR)

Rubin Remixed (continued)



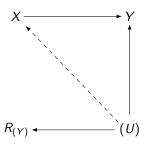
Missing At Random (MAR)

Rubin Remixed (continued)



Missing Not At Random (MNAR)

Missingness Due To Confounding



(Also) Missing Not At Random (MNAR)

[press "play"]

Estimating Treatment Effects

Key to estimating treatment effects: **Assignment mechanism for** W.

Neyman/Rubin/Holland: Treat inability to observed Y_{0i} / Y_{1i} as a missing data problem.

• If the "missingness" due to the value of W_i is orthogonal to the values of Y, then it is ignorable. Formally:

$$\Pr(W_i|\mathbf{X}_i,Y_{0i},Y_{1i})=\Pr(W_i|\mathbf{X}_i)$$

- If the "missingness" is non-orthogonal, then it is not ignorable, and can lead to bias in estimation
- Non-ignorable assignment of W requires understanding (and accounting for) the <u>mechanism</u> by which that assignment occurs

SUTVA

One more thing: the stable unit-treatment value assumption ("SUTVA")

- Requires that there be two and only two possible values of Y for each observation i...
- "the observation (of Y_i) on one unit should be <u>unaffected</u> by the particular assignment of treatments to the other units."
- $\bullet \equiv$ the "assumption of no interference between units," meaning:
 - · Values of Y for any two i,j $(i \neq j)$ observations do not depend on each other
 - Treatment effects (for observation i) are homogenous within categories defined by W

Treatment Effects Under Randomization of W

If W_i is assigned randomly, then:

$$Pr(W_i) \perp Y_{0i}, Y_{1i}$$

and so:

$$Pr(W_i|Y_{0i}, Y_{1i}) = Pr(W_i) \forall Y_{0i}, Y_{1i}.$$

This means that the "missing" data on Y_0/Y_1 are <u>ignorable</u> (here, in the special case where the \mathbf{X}_i on which W_i depends is null). This in turn means that:

$$f(Y_{0i}|W_i=0) = f(Y_{0i}|W_i=1) = f(Y_i|W_i=0) = f(Y_i|W_i=1)$$

and

$$f(Y_{1i}|W_i=0) = f(Y_{1i}|W_i=1) = f(Y_i|W_i=0) = f(Y_i|W_i=1)$$

Randomized W (continued)

Implication: Y_{0i} and Y_{1i} are (not identical but) exchangeable...

This in turn means that:

$$E(Y_{0i}|W_i) = E(Y_{1i}|W_i)$$

and so

$$\widehat{ATE} = E(Y_i|W_i = 1) - E(Y_i|W_i = 0)
= \bar{Y}_{W=1} - \bar{Y}_{W=0}.$$

will be an unbiased estimate of the ATE.

Observational Data: W Depends on X

Formally,

$$Y_{0i}$$
, $Y_{1i} \perp W_i | \mathbf{X}_i$.

Here.

- X are known confounders that (stochastically) determine the value of W_i,
- Conditioning on **X** is necessary to achieve exchangeability.

So long as W is entirely due to X, we can condition:

$$f(Y_{1i}|\mathbf{X}_i, W_i = 1) = f(Y_{1i}|\mathbf{X}_i, W_i = 0) = f(Y_i|\mathbf{X}_i, W_i)$$

and similarly for Y_{0i} .

W Depends on X (continued)

Estimands:

• the average treatment effect for the treated (ATT):

$$ATT = E(Y_{1i}|W_i = 1) - E(Y_{0i}|W_i = 1).$$

• the average treatment effect for the controls (ATC):

$$ATC = E(Y_{1i}|W_i = 0) - E(Y_{0i}|W_i = 0).$$

Corresponding estimates:

$$\widehat{\mathsf{ATT}} = \mathbf{E}\{[\mathsf{E}(Y_i|\mathbf{X}_i,W_i=1) - \mathsf{E}(Y_i|\mathbf{X}_i,W_i=0)]|W_i=1\}.$$

and

$$\widehat{ATC} = \mathbf{E}\{[E(Y_i|\mathbf{X}_i, W_i = 1) - E(Y_i|\mathbf{X}_i, W_i = 0)]|W_i = 0\}.$$

Note that in both cases the expectation of the whole term is conditioned on W_i .

Confounding

Confounding occurs when one or more observed or unobserved factors \mathbf{X} affect the causal relationship between W and Y.

Formally, confounding requires that:

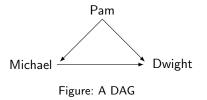
- $Cov(X, W) \neq 0$ (the confounder is associated with the "treatment")
- $Cov(X, Y) \neq 0$ (the confounder is associated with the outcome)
- X does not "lie on the path" between W and Z (that is, X is not affected by either W or Y).

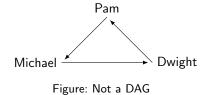
Digression: DAGs

<u>Directed acyclic graphs</u> (DAGs) are a tool for visualizing and interpreting structural/causal phenomena.

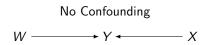
- DAGs comprise:
 - · Nodes (typically, variables / phenomena) and
 - · Edges (or lines; typically, relationships/causal paths).
- Directed means each edge is unidirectional.
- Acyclical means exactly what it suggests: If a graph has a "feedback loop," it is not a DAG.
- Read more at the Wikipedia page, or at this useful page.

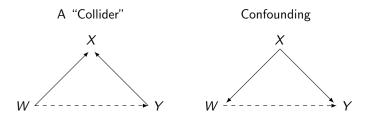
Know your DAG





DAGs and Confounding





What We're On About

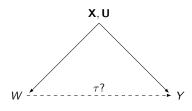


Figure: Potential Confounding

Here:

- Y is the outcome of interest,
- W is the primary predictor / covariate ("treatment") of interest,
- T_i is the "treatment indicator" for observation i,
- We're interested in estimating τ , the "treatment effect" of W on Y,
- X are observed confounders,
- **U** are unobserved confounders.

Things We Can Do

Randomize

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(or...)
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- Instrumental Variables Approaches
- Selection on Observables:
 - · Regression / Weighting
 - Matching (propensity scores, multivariate/minimum-distance, genetic, etc.)
- Regression Discontinuity Designs ("RDD")
- Differences-In-Differences ("DiD")
- Synthetic Controls
- Others...

Under Randomization

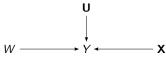


Figure: No confounding!

Note:

- Randomized assignment of W "balances" covariate values both observed and unobserved – on average...
- That is, under randomization of W:

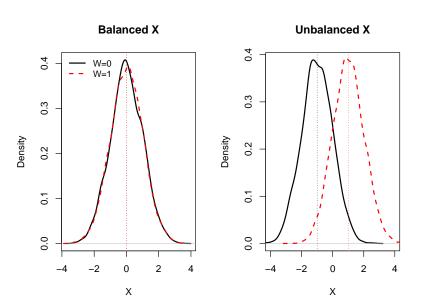
$$E(X_i, U_i | W_i = 0) = E(X_i, U_i | W_i = 1)$$

or, more demandingly,

$$E[f(X, U) | W_i = 0] = E[f(X, U) | W_i = 1]$$

Can yield imbalance by random chance...

Covariate Balance / Imbalance



Nonrandom Assignment of W_i

Valid causal inference requires Y_{0i} , $Y_{1i} \perp W_i | \mathbf{X}_i, \mathbf{U}_i$

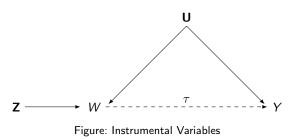
• That is, treatment assignment W_i is conditionally ignorable

"What if I have unmeasured confounders?"

- In general, that's a bad thing.
- ullet One approach: obtain *bounds* on possible values of au
 - · Assume you have one or more unmeasured confounders
 - · Undertake one of the methods described below to get $\hat{\tau}$
 - Calculate the range of values for $\hat{\tau}$ that could occur, depending on the degree and direction of confounding bias
 - · Or ask: How strong would the effect of the **U**s have to be to make $\hat{\tau} \rightarrow 0$?
- Some useful cites:
 - · Rosenbaum and Rubin (1983)
 - · Rosenbaum (2002)
 - · DiPrete and Gangl (2004)
 - · Liu et al. (2013)
 - Ding and VanderWeele (2016)

Digression: Instrumental Variables

A DAG:



As in the more general regression case where we have $Cov(\mathbf{X},\mathbf{u}) \neq 0$, instrumental variables \underline{can} be used to address confounding in causal analyses.

Instrumental Variables (continued)

Considerations:

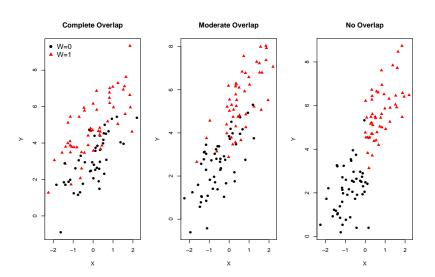
- Requires:
 - 1. $Cov(\mathbf{Z}, W) \neq 0$
 - 2. **Z** has no independent effect on Y, except through W
 - 3. **Z** is exogenous [i.e., $Cov(\mathbf{Z}, \mathbf{U}) = 0$]
- Arguably most useful when treatment compliance is uncertain / driven by unmeasured factors ("intent to treat" analyses)
- Mostly, they're not that useful at all...
 - · Bound et al. (1995): Weak instruments are worse than endogeneity bias
 - Young (2020): Inferences in published IV work (in economics) are wrong and terrible
 - Shalizi (2020, chapters 20-21): Gathers all the issues together, sometimes hilariously
- Other useful references:
 - · Imbens et al. (1996) (the overly-cited one)
 - · Hernan and Robins (2006) (making sense of things)
 - · Lousdal (2018) (a good intuitive introduction)

Nonrandom Assignment of W_i (continued)

So...

- Causal inference with observational data typically requires that $\mathbf{U} = \varnothing ...$
- This typically requires a <u>strong</u> theoretical motivation in order to assume that the specification conditioning on the observed X exhausts the list of possible confounders.
- Even if this assumption is reasonable, there are two (related) important concerns:
 - · Lack of covariate balance (as above)
 - · Lack of overlap among observations with $W_i = 0$ vs. $W_i = 1$
 - The latter is related to positivity, the requirement that each observation's probability of receiving (or not receiving) the treatment is greater than zero

Overlap



Overlap and Balance

In general:

- Ensuring overlap allows us to make counterfactual statements from observational data
 - · Requires that we have comparable $W_i = 0$ and $W_i = 1$ units
 - It's necessary no overlap means any counterfactual statements are based on assumption
 - Think of this as an aspect of model identification (Crump et al. 2009)
 - · Most often handled via matching
- Ensuring covariate balance corrects potential bias in $\hat{\tau}$ due to (observed) confounding
 - This can be done a number of different ways: stratification, weighting, regression...
 - \cdot Key: Adjusting for (observable) differences across groups defined by values of W
- In general, we usually address overlap first, then balance...

Matching

 $\overline{\text{Matching}}$ is a way of dealing with one or both of covariate overlap and $\overline{\text{(im)}}$ balance.

The process, generally:

- Choose the X on which the observations will be matched, and the matching procedure;
- 2. Match the observations with $W_i = 0$ and $W_i = 1$;
- 3. Check for balance in X_i ; and
- 4. Estimate $\hat{\tau}$ using the matched pairs.

Variants / considerations:

- 1:1 vs. 1:k matching
- "Greedy" vs. "Optimal" matching (see Gu and Rosenbaum 1993)
- Distances, calipers, and "common support"
- Post-matching: Balance checking...

Flavors of Matching

- Simplest: Exact Matching
 - · For each of the *n* observations *i* with W=1, find a corresponding observation *j* with W=0 that has identical values of **X**
 - · Calculate $\hat{\tau} = \frac{1}{n} \sum (Y_i Y_j)$
 - · Generally not practical, especially for high-dimensional X
 - · Variants: "coarsened" exact matching (e.g., lacus et al. 2011)

Multivariate Matching

- Match each observation i which has W=1 with a corresponding observation j with W=0, and whose values on \mathbf{X}_j are the most similar to \mathbf{X}_i
- One example: Mahalanobis distance matching, based on the distance:

$$d_M(\mathbf{X}_i,\mathbf{X}_j) = \sqrt{(\mathbf{X}_i - \mathbf{X}_j)'\mathbf{S}^{-1}(\mathbf{X}_i - \mathbf{X}_j)}.$$

Flavors of Matching (continued)

- Propensity Score Matching
 - · Match observation i which has W = 1 with observation j having W = 0 based on the closeness of their propensity score
 - The propensity score is, $Pr(W_i = 1 | \mathbf{X}_i)$, typically calculated as the predicted value of T_i (the treatment indicator) from a logistic (or other) regression of T on \mathbf{X} .
 - The assumptions about matching [that Y is orthogonal to W|X and that $Pr(W_i = 1|X_i) \in (0,1)$] mean that $Y \perp W|Pr(T|X)$.
 - · In practice: read this...
- Other variants: Genetic matching (Diamond and Sekhon 2013), etc.¹

¹Shalizi (2016) notes that "(A)pproximate matching is implicitly doing nonparametric regression by a nearest-neighbor method," and that "(M)aybe it is easier to get doctors and economists to swallow "matching" than "nonparametric nearest neighbor regression"; this is not much of a reason to present the subject as though nonparametric smoothing did not exist, or had nothing to teach us about causal inference."

Matching Software

Interestingly, quite a few of the good matching programs written for R have been written by political scientists...

- the Match package (does propensity score, *M*-distance, and genetic matching, plus balance checking and other diagnostics)
- the MatchIt package (for pre-analysis matching; also has nice options for checking balance)
- the optmatch package (suite for 1:1 and 1:k matching via propensity scores, M-distance, and optimum balancing)
- matching (in the arm package)

Regression Discontinuity Designs

"RDD":

- Treatment changes abruptly [usually at some threshold(s)] according to the value(s) of some measured, continuous, pre-treatment variable(s)
 - · This is known as the "assignment" or "forcing variable(s)," sometimes denoted $\boldsymbol{\mathsf{A}}$
 - · Formally:

$$W_i = \begin{cases} 0 \text{ if } A_i \leq c \\ 1 \text{ if } A_i > c \end{cases}$$

- Intuition: Observations near but on either side of the threshold(s) are highly comparable, and can be used to (locally) identify τ
- This is because variation in W_i near the threshold is effectively random (a "local randomized experiment")
- E.g. Carpenter and Dobkin (2011) (on the relationship between the legal drinking age and public health outcomes like accidental deaths)

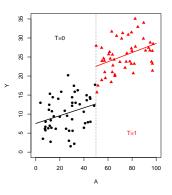
RDD (continued)

Pluses:

· Can be estimated straightforwardly, as:

$$Y_i = \beta_0 + \beta_1 A_i + \tau W_i + \gamma A_i W_i + \epsilon_i$$

- Generally requires fewer assumptions than IV or DiD (and those assumptions are easier to observe and test)
- Minuses:
 - · Provides only an estimate of a <u>local</u>
 - Fails if (say) subjects can manipulate A in the vicinity of c
- Lee and Lemieux (2010) is an excellent (if fanboi-ish) review
- R packages: rddtools, rdd, rdrobust, rdpower, rdmulti



Panel Data Approaches: Differences-In-Differences

"DiD":

• Leverages two-group, two-period data (T = 2):

	Pre-Treatment $(T=0)$	Post-Treatment $(T=1)$
Treated ($W=1$)	A	В
Untreated $(W=0)$	С	D

- Process (simple version):
 - · Calculate the pre- vs. post-treatment difference for the treated group (B A)
 - · Calculate the pre- vs. post-treatment difference for the untreated group (D-C)
 - · Calculate the differences between the differences [DiD = (B A) (D C)]
 - · This is the same as fitting the regression:

$$Y_{it} = \beta_0 + \beta_1 W_{it} + \beta_2 T_{it} + \beta_3 W_{it} T_{it} + u_{it}$$

- Validity depends on (a) all the usual assumptions required by OLS, plus (b) the <u>parallel</u> trends assumption that there are no time-varying differences between the two groups as we go from T = 0 to T = 1.
- · Resources:
 - · Our old friend Wikipedia
 - · Pischke's slides on DiD
 - · R: package did
 - · Stata: ieddtab in the ietoolkit

Panel Data Approaches: Synthetic Controls

The "synthetic control method" (SCM):

- Addresses situations in which we have a <u>single</u> treated case (or small number of them)...
- Requires at least one (and ideally more) repeated measurements over time on the outcome of interest, and
- Also requires multiple (but not too many) non-treated cases
- Assumptions:
 - · Possible control units are similar
 - · Lack of spillover between treated and potential control units
 - · Lack of exogenous shocks to potential control units

Synthetic Controls (continued)

SCM details:

Intuition:

- Create a counterfactual "control" unit that is as similar to the (pre-treatment) treated case as possible
- Do so by weighting the observed predictors across "control" cases to minimize the difference (in a MSE sense)
- · Compare the pre-treatment trends in the synthetic control and treated cases
- · The weights are then used to create a post-treatment trend for the synthetic control
- · Inference is via placebo methods (varying the timing of the intervention)

Advantages:

- · Works with (very) small N
- · Doesn't require parallel trends (a la DiD)
- Abadie et al. claim that SCM controls for both observed and unobserved time-varying confounders

• A few references:

- · A nontechnical introduction in the BMJ
- · Method of the Month Blog
- · The Development Impact blog post on SCM

Software Matters

In general:

- R
- · Packages for matching are listed above (Matching, MatchIt, etc.)
- · Similarly for RDD (rddtools, rdd, etc.) and DiD (did)
- · IV regression: ivreg (in AER), tsls (in sem), others
- · Synthetic controls are in Synth and MicroSynth
- · See generally the CRAN Task View on Causal Inference.
- Stata also has a large suite of routines for attempting causal inference with observational data...
- And there's a pretty good NumPy/SciPy-dependent package for Python, called (creatively) Causalinference

Causal Inference: One-Way (FE) Models

Imai and Kim (2019):

- The punch line first: "(t)he ability of unit fixed effects regression models to adjust for unobserved time-invariant confounders comes at the expense of dynamic causal relationships between treatment and outcome variables."
- Also dependent on functional form assumptions (specifically, linearity)

Intuition: For the model:

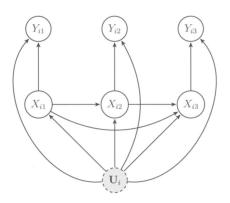
$$Y_{it} = \mathbf{X}_{it}\boldsymbol{\beta} + \alpha_i + u_{it}$$

where (for simplicity) X is a binary treatment for which we want to know a causal effect on Y:

- · Identification is via $Cov[(\mathbf{X}_{it}, \alpha_i), u_{it}] = 0$
- · In this framework, $\beta = \tau$, the typical causal estimand (that is, the expected difference between $Y_{it}(0)$ and $Y_{it}(1)$)

A more flexible approach is to think of a FE model as a DAG...

Fixed-Effects DAG



Source: Imai and Kim (2019).

Key FE Takeaways

Summarizing Imai and Kim (2019):

- Three key identifying assumptions for FE models:
 - · No unobserved time-varying confounders
 - · Past treatments / values of X do not affect current values of Y^2
 - · Past outcomes Y do not affect current values of X.
- Alternatively, one can select on observables (a la Blackwell and Glynn 2018) and model dynamics (albeit at the cost of failing to control for unobserved time-constant confounders).

"...researchers must choose either to adjust for unobserved timeinvariant confounders through unit fixed effects models or to model dynamic causal relationships between treatment and outcome under a selection-on-observables approach. No existing method can achieve both objectives without additional assumptions" (Imai and Kim 2019, 484).

²Can be relaxed via IV, but that requires independence of past and present values of Y.

Two-Way Models

Imai and Kim redux (2020):

• In the simple T=2 case, DiD is equivalent to a two-way FE model:

$$Y_{it} = \mathbf{X}_{it}\boldsymbol{\beta} + \alpha_i + \eta_t + u_{it}$$

- Imai & Kim: The same is not true for T > 2...
- More important: two-way FEs' ability to control for unmeasured confounders depends on the (linearity of the) functional form...
- Upshot: two-way FEs aren't a (nonparametric) cure-all...
- Related: When we control for both α_i and η_t , what exactly is the counterfactual?

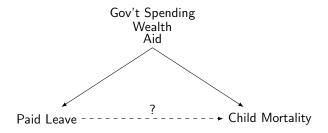
Back To The WDI

> describe(WDI,fast=TRUE,ranges=FALSE,check=TRUE)									
	vars	n	mean	sd	skew	kurtosis	se		
IS03	1	13975	NaN	NA	NA	NA	NA		
Year	2	13975	NaN	NA	NA	NA	NA		
Region	3	13975	NaN	NA	NA	NA	NA		
country	4	13975	NaN	NA	NA	NA	NA		
iso3c	5	13975	NaN	NA	NA	NA	NA		
RuralPopulation	6	13696	48.11	25.74	-0.11	-1.00	0.22		
UrbanPopulation	7	13696	51.89	25.74	0.11	-1.00	0.22		
BirthRatePer1K	8	13730	27.67	13.17	0.24	-1.24	0.11		
FertilityRate	9	13728	3.82	1.99	0.43	-1.18	0.02		
PrimarySchoolAge	10	11120	6.13	0.61	-0.04	0.11	0.01		
LifeExpectancy	11	13726	65.17	11.25	-0.76	0.18	0.10		
AgeDepRatioOld	12	13730	10.76	7.16	1.79	5.00	0.06		
ChildMortality	13	11580	72.93	77.99	1.61	2.70	0.72		
GDP	14	11040	240200887836.82	1130067880812.37	11.48	160.11	10755237244.82		
GDPPerCapita	15	11045	12332.27	19272.78	3.11	14.10	183.38		
GDPPerCapGrowth	16	10970	1.89	6.49	1.68	41.63	0.06		
TotalTrade	17	8777	77.93	53.26	3.03	18.39	0.57		
FDIIn	18	8969	5.53	45.10	15.13	541.91	0.48		
NetAidReceived	19	9043	506951242.00	997064633.65	8.32	157.34	10484966.48		
MobileCellSubscriptions	20	10212	36.32	51.76	1.29	1.14	0.51		
NaturalResourceRents	21	9211	6.85	11.06	2.60	8.04	0.12		
GovtExpenditures	22	8421	16.34	8.27	3.63	32.81	0.09		
PublicHealthExpend	23	4346	3.29	2.37	1.33	3.08	0.04		
WomenInLegislature	24	5075	18.34	11.98	0.68	0.01	0.17		
PaidParentalLeave	25	10152	0.11	0.31	2.50	4.27	0.00		
PostColdWar	26	13975	0.54	0.50	-0.15	-1.98	0.00		
lnGDPPerCap	27	11045	8.39	1.51	0.10	-0.90	0.01		
lnNetAidReceived	28	8876	18.81	1.97	-1.06	1.99	0.02		
YearNumeric	29	13975	1992.00	18.76	0.00	-1.20	0.16		

A New Question

Do paid parental leave policies decrease child mortality?

- Y = ChildMortality (N of deaths of children under 5 per 1000 live births) (logged)
- T = PaidParentalLeave (1 if provided, 0 if not)
- Xs:
 - GDPPerCapita (Wealth; in constant \$US) (logged)
 - NetAidReceived (Net official development aid received; in constant \$US) (logged)
 - GovtExpenditures (Government Expenditures, as a percent of GDP)



Preliminary Regressions

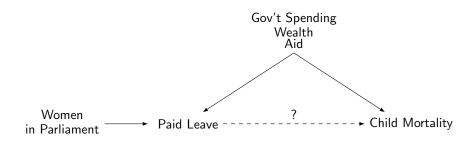
Table: Models of log(Child Mortality)

	Bivariate OLS	OLS	One-Way FE	Two-Way FE	FE / Lagged Y
Paid Parental Leave	-1.850 (0.033)	-0.908*** (0.037)	-0.070 (0.044)	-0.148*** (0.024)	-0.212*** (0.028)
In(GDP Per Capita)		-0.660***	-1.110***	-0.270***	-0.560***
		(0.009)	(0.017)	(0.013)	(0.013)
In(Net Aid Received)		-0.088***	-0.108***	0.004	-0.014***
, ,		(0.007)	(0.006)	(0.004)	(0.004)
Government Expenditures		-0.002**	0.002*	-0.0002	0.00003
·		(0.001)	(0.001)	(0.001)	(0.001)
Lagged Child Mortality					0.008*** (0.0001)
Constant	3.770* (0.011)	10.800*** (0.177)			
Observations	9,761	5,253	5,253	5,253	5,249
R ²	0.240	0.578	0.479	0.103	0.788
Adjusted R ²	0.240	0.578	0.463	0.067	0.782

*p<0.1; **p<0.05; ***p<0.01

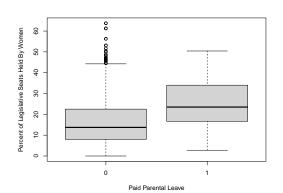
Instrumental Variables

Conceptually:



Instrumental Variables (continued)

Assessing $Cov(W, \mathbf{Z})$:



Instrumental Variables: Syntax

E.g., one-way fixed effects with IV:

Instrumental Variable Results

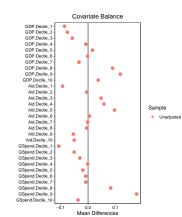
Table: IV Models of log(Child Mortality)

	OLS	One-Way FE	FE w/IV	RE w/IV
Paid Parental Leave	-0.908	-0.070	1, 219.000	-4.290***
	(0.037)	(0.044)	(40, 313.000)	(1.490)
In(GDP Per Capita)	-0.660	-1.110***	-191.000	-0.545***
. ,	(0.009)	(0.017)	(6, 271.000)	(0.067)
In(Net Aid Received)	-0.088	-0.108***	18.000	-0.051**
,	(0.007)	(0.006)	(597.000)	(0.021)
Government Expenditures	-0.002	0.002*	-0.168	-0.003
,	(0.001)	(0.001)	(5.480)	(0.002)
Constant	10.800*			9.240***
	(0.177)			(0.721)
Observations	5,253	5,253	2,758	2,758
R ²	0.578	0.479	0.0003	0.314
Adjusted R ²	0.578	0.463	-0.055	0.313

^{*}p<0.1; **p<0.05; ***p<0.01

Matching: Checking Covariate Balance

```
> # Subset data a little bit:
> vars<-c("ISO3"."Year"."Region"."country"."UrbanPopulation"."FertilityRate".
          "PrimarySchoolAge", "ChildMortality", "lnGDPPerCap",
          "InNetAidReceived", "NaturalResourceRents", "GovtExpenditures",
          "PaidParentalLeave", "PostColdWar", "lnCM")
> wdi<-WDT[vars]
> wdi<-na.omit(wdi)
> # Create discrete-valued variables (i.e., coarsen) for
> # matching on continuous predictors:
> wdi$GDP.Decile<-as.factor(ntile(wdi$GDPPerCapita.10))
> wdi$Aid.Decile<-as.factor(ntile(wdi$NetAidReceived.10))
> wdi$GSpend.Decile<-as.factor(ntile(wdi$GovtExpenditures,10))
> # Pro-match halance statistics
> BeforeBal<-bal.tab(PaidParentalLeave~GDP.Decile+
                  Aid.Decile+GSpend.Decile,data=wdi,
                  stats=c("mean.diffs", "ks.statistics"))
```

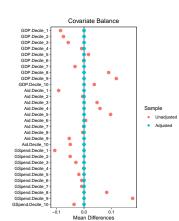


Exact Matching

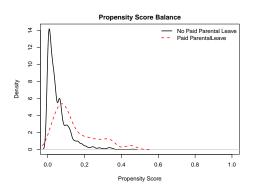
```
> M.exact <- matchit(PaidParentalLeave~GDP.Decile+Aid.Decile+
                    GSpend.Decile,data=wdi,method="exact")
> summary(M.exact)
Call:
matchit(formula = PaidParentalLeave ~ GDP.Decile + Aid.Decile +
    GSpend.Decile, data = wdi, method = "exact")
Summary of Balance for All Data:
Sample Sizes:
              Control Treated
All
                 4759
                          304
Matched (ESS)
Matched
                  910
                          285
Unmatched
                 3849
                           19
```

0

Discarded



Propensity Scores

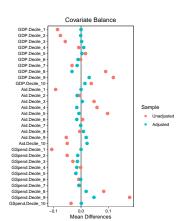


Propensity Score Matching

```
> M.prop <- matchit(PaidParentalLeave~GDP.Decile+Aid.Decile+
                    GSpend.Decile.data=wdi.method="nearest".
                    ratio=3)
> summary(M.prop)
Call:
matchit(formula = PaidParentalLeave ~ GDP.Decile + Aid.Decile +
    GSpend.Decile. data = wdi. method = "nearest". ratio = 3)
Summary of Balance for All Data:
Sample Sizes:
          Control Treated
All
             4759
Matched
              912
                      304
Unmatched
             3847
Discarded
                        ٥
> # Matched data:
> wdi.ps <- match.data(M.prop,group="all")
```

> dim(wdi.ps)

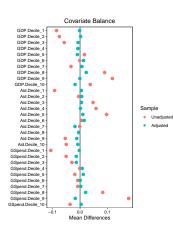
[1] 1216 21



"Optimal" Matching

```
> M.opt <- matchit(PaidParentalLeave~GDP.Decile+Aid.Decile+
                    GSpend.Decile,data=wdi,method="quick",
                    ratio=3)
> summary(M.opt)
Call.
matchit(formula = PaidParentalLeave ~ GDP.Decile + Aid.Decile +
   GSpend.Decile, data = wdi, method = "quick", ratio = 3)
Summary of Balance for All Data:
Sample Sizes:
              Control Treated
All
                 4759
                          304
Matched (ESS)
                 414
                          304
Matched
                 4759
                          304
Unmatched
                            ٥
Discarded
                    ٥
                            ٥
> # Matched data:
> wdi.opt <- match.data(M.opt,group="all")
> dim(wdi.opt)
```

[1] 5063 21



Post-Matching Regressions

Table: FE Models of log(Child Mortality): Matched Data

	Pre-Matching	Exact	Prop. Score	Optimal
Paid Parental Leave	-0.071	-0.213***	-0.157***	-0.071
	(0.045)	(0.060)	(0.055)	(0.045)
In(GDP Per Capita)	-1.100***	-1.030***	-1.140***	-1.100***
. ,	(0.018)	(0.037)	(0.036)	(0.018)
In(Net Aid Received)	-0.104***	-0.062***	-0.042***	-0.104***
,	(0.007)	(0.016)	(0.016)	(0.007)
Government Expenditures	0.002	0.004	0.010***	0.002
	(0.001)	(0.003)	(0.003)	(0.001)
Observations	5,063	1,195	1,216	5,063
R ²	0.467	0.464	0.528	0.467
Adjusted R ²	0.451	0.403	0.474	0.451

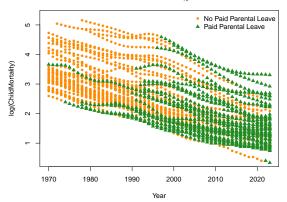
^{*}p<0.1; **p<0.05; ***p<0.01

Another Approach: RDD

Intuition: Compare the child mortality "trajectories" of countries before and after they implement paid parental leave policies.

The model is:

Child Mortality_{it} =
$$\beta_0 + \beta_1$$
(Paid Parental Leave_{it}) + β_2 (Time_t) +
 = β_3 (Paid Parental Leave_{it} × Time_t) + (confounders) + u_{it}



RDD Regressions

Table 4: RDD Models of log(Child Mortality)

	OLS #1	OLS #2	One-Way FE #1	One-Way FE #2	Two-Way FE #1	Two-Way FE #2
(Intercept)	4.3283***	11.3454***				
	(0.0549)	(0.2953)				
Paid Parental Leave	-0.7065***	0.0734	-0.0887*	0.1534+	-9.0190***	-18.3542*
	(0.1255)	(0.1893)	(0.0406)	(0.0793)	(2.7203)	(7.8215)
Time (1950=0)	-0.0389***	-0.0233***	-0.0420***	-0.0429***		
	(0.0013)	(0.0018)	(0.0004)	(0.0011)		
Paid Parental Leave x Time	0.0097***	-0.0034	0.0019**	-0.0029*	0.1757***	0.3122*
	(0.0023)	(0.0034)	(0.0007)	(0.0014)	(0.0497)	(0.1400)
In(GDP Per Capita)		-0.6857***		-0.2062***		-1.9763
		(0.0177)		(0.0250)		(1.9010)
In(Net Aid Received)		-0.0533***		0.0109*		-2.4738***
		(0.0112)		(0.0055)		(0.4343)
Government Expenditures		-0.0282***		0.0091***		0.7779***
		(0.0033)		(0.0017)		(0.1292)
NT	2840	778	2840	778	2840	778
R^2	0.426	0.746	0.905	0.930	0.005	0.125
Adj. R ²	0.425	0.744	0.903	0.926	-0.035	0.013

⁺ p < 0.1, * p < 0.05, ** p < 0.01, *** p < 0.001

Differences-in-Differences

Challenges:

- Multiple periods (years) per unit (country), both before and after "treatment"
- "Staggered" treatment timing (adoption of Paid Parental Leave)

One approach:

Callaway, Brantley, and Pedro H.C. Sant'Anna. 2021. "Difference-in-Differences with Multiple Time Periods." *Journal of Econometrics* 225:200-230.

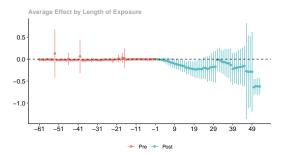
Details:

- Deals with the issues related above
- Flexibly fit / interpreted using the did package

Differences-in-Differences via did

Simple bivariate model (no controls):

Plot the event study results:



ATTs by "Group"

```
> DiD.grp1<-aggte(DiD.fit1,type="group",na.rm=TRUE)
> summary(DiD.grp1)
```

Call:

```
aggte(MP = DiD.fit1, type = "group", na.rm = TRUE)
```

Reference: Callaway, Brantly and Pedro H.C. Sant'Anna.
"Difference-in-Differences with Multiple Time Periods."
Journal of Econometrics, Vol. 225, No. 2, pp. 200-230, 2021.

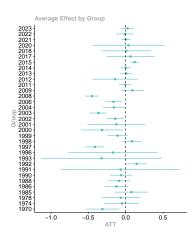
Overall summary of ATT's based on group/cohort aggregation: ATT Std. Error [95% Conf. Int.]

Group Effects:

Group	Estimate	Std. Error	[95% Simult.	Conf. Band]	
1970	-0.3112	0.0376	-0.5330	-0.0895	*
1974	-0.0507	0.0381	-0.2750	0.1736	
1978	-0.0644	0.0434	-0.3198	0.1910	
1985	0.0770	0.0370	-0.1411	0.2951	
1986	-0.1240	0.0254	-0.2738	0.0257	
1988	-0.0884	0.0243	-0.2317	0.0549	
1990	-0.0612	0.0244	-0.2051	0.0826	
1991	-0.0688	0.1344	-0.8607	0.7231	
1992	0.1455	0.0223	0.0140	0.2769	*
2021	0.0019	0.0093	-0.0528	0.0565	
2022	-0.0086	0.0180	-0.1145	0.0973	
2023	0.0248	0.0143	-0.0594	0.1089	

Signif. codes: '*' confidence band does not cover 0

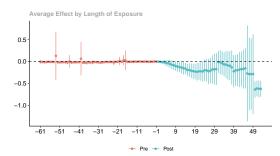
Control Group: Never Treated, Anticipation Periods: 0 Estimation Method: Outcome Regression



Differences-in-Differences with Controls

Adding control variables:

Plot the event study results:



ATTs by "Group" (with controls)

```
> DiD.grp2<-aggte(DiD.fit2.tvpe="group".na.rm=TRUE)
> summary(DiD.grp2)
Call:
aggte(MP = DiD.fit2, type = "group", na.rm = TRUE)
Reference: Callaway, Brantly and Pedro H.C. Sant'Anna.
"Difference-in-Differences with Multiple Time Periods."
Journal of Econometrics, Vol. 225, No. 2, pp. 200-230, 2021.
Overall summary of ATT's based on group/cohort aggregation:
    ATT
           Std. Error
                           [ 95% Conf. Int.]
 -0 157
                0 044
                           -0 243
                                      -0.0703 *
Group Effects:
 Group Estimate Std. Error [95% Simult. Conf. Band]
         0.5910
                    0.2028
                                   0.0484
                                               1.1335 *
         0.0291
                    0.0566
                                  -0.1224
                                               0 1806
        -0.4681
                    0 0777
                                  -0.6759
                                              -0.2603 *
  1993
  1996
        -0.4719
                    0.0632
                                  -0.6408
                                              -0.3029 *
  1997
       -0.6425
                    0.0673
                                  -0.8225
                                              -0.4625 *
       -0.0438
                    0.3940
                                  -1.0978
                                              1.0101
       -0.0616
                    0.0391
                                  -0 1661
                                               0.0428
  2001
  2002
       -0.3815
                    0.0687
                                  -0.5654
                                              -0.1976 *
                                               0.0378
  2003
       -0.0312
                    0.0258
                                  -0.1002
```

-0.1760

-0.3379

-0.6607

-0.0877

-0.5112

-0.1446

-0.1587

0.0161

-0.1613 *

-0 3776 *

-0.2036 *

-0.0332 *

0.0688

0.0764

0.0208 0.0425 Signif. codes: '*' confidence band does not cover 0

0.0359

0.0330

0.0529

0.0307

0.0575

2004 -0.0800

2006 -0.2496

2008 -0 5192

2009

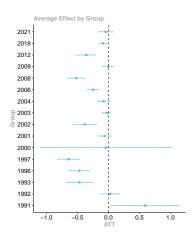
2012 -0.3574

2021 -0.0449

-0.0057

2018 -0.0889

Control Group: Never Treated, Anticipation Periods: 0 Estimation Method: Outcome Regression



Resources

Good references:

- · Freedman (2012)*
- · Shalizi (someday)*
- Morgan and Winship (2014)
- · Pearl et al. (2016)
- · Peters et al. (2017)

Other useful things:

- The CRAN task view on causal inference
- The What If Book
- Some useful notes

Courses / syllabi (a sampling):

- · Blackwell (2023)
- · Eggers (2019)
- · Frey (2024)
- · Imai (2023)
- · Munger (2023)
- · Ornstein (2023)
- · Xu (2018, 2023).
- · Yamamoto (2021)

^{*} I really like this one.