# PLSC 502: "Statistical Methods for Political Research"

#### **Exercise Seven**

November 15, 2022

### Part I

Here, you're asked to assess the performance of three different measures of association ( $\phi$ ,  $r_{tet}$ , and  $\tau_b$ ) in recovering the correlation between two continuous variables that have been dichotomized. Consider two latent (unmeasured) variables  $X_1^*$  and  $X_2^*$ ; for simplicity, we'll make each of them simple:

$$X_1^*, X_2^* \sim \mathcal{BVN}(0, 0, 1, 1, \rho).$$

In other words,  $X_1$  and  $X_2$  are both standard normal variables, where the correlation between  $X_1^*$  and  $X_2^*$  is  $\rho$ .<sup>1</sup> For each latent variable, suppose we observe a binary realization  $X_1$  and  $X_2$ , such that:

$$X_{1,2} = \begin{cases} 0 \text{ if } X_{1,2}^* \le 0\\ 1 \text{ if } X_{1,2}^* > 0 \end{cases}$$

The question is, given binary realizations of the  $X^*$ s, which of the three measures of association listed  $(\phi, r_{tet}, \text{ and } \tau_b)$  does "best" at recovering the true underlying correlation  $\rho$ ? Use simulations to answer this question, being sure to vary  $\rho$  widely in formulating your answer.

## Part II

This part of the exercise is designed to showcase your mastery of one- and two-way contingency tables, and of measures of association for nominal, binary, and ordinal data. We'll consider data on the 2002 Swedish election to the national parliment.<sup>2</sup> Those data consist of roughly 7000 respondents<sup>3</sup> to a series of exit polls there following that election. The data contain a range of variables; we'll focus on eight of them:

- gender a poorly-named variable, coded "0" for men, "1" for women.
- citizen coded "0" for non-citizens, "1" for citizens.
- employed a four-category nominal variable reflecting employment status: "1" = employed, "2" = unemployed, "3" = student/in training, and "4" = retired.

<sup>&</sup>lt;sup>1</sup>Such continuous correlated data are easy to generate using the mvtnorm package; see the code from November 10 for examples.

<sup>&</sup>lt;sup>2</sup>Why the 2002 Swedish election? Well... why not?

<sup>&</sup>lt;sup>3</sup>There are actually more than 10000 respondents, but there is significant missing data in a few of the variables.

- union a four-category nominal variable, coding whether the respondent was a member of one of three types of unions (1,2, or 3) or not (4).
- uniondummy a dichotomous version of union, coded "1" if the respondent is a member of *any* union, and "0" otherwise.
- eu another poorly-named variable, variable coded "0" if the respondent thought that Sweden should resign from the EU, and "1" if s/he believed Sweden should stay in the EU.
- partychoice a four-category ordinal variable, coded "1" for conservative parties, "2" for liberals, "3" for social democrats, and "4" for parties of the left.
- euro coded "1" if the respondent favored Sweden's adopting of the Euro as its currency and "0" if s/he did not.

#### **Exercise**

- 1. Assess whether there are any differences in party identification, employment status, union membership, and opinions toward the Euro and EU membership between men and women.
- 2. Are there systematic differences between members of different political parties in views on Euro adoption? on EU membership?
- 3. What, if any, is the relationship between support for EU membership and opinion on the Euro? Is that relationship different for men than it is for women? for citizens than for non-citizens? for union members versus non-union members?

As is typically the case, this homework exercise is worth 50 possible points. It is due by 5:00 p.m. EST on Wednesday, November 30, 2022, and should be submitted electronically – via e-mail attachment – to Tuba (tzs5636@psu.edu) and to me (zorn@psu.edu).