4M17 Coursework #2 - Optimisation Algorithm Performance Comparison

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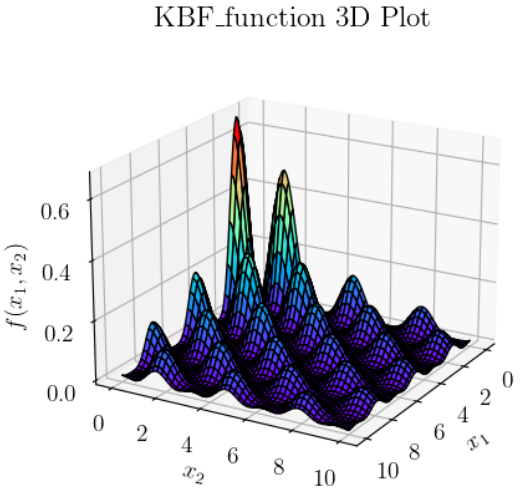
1 Abstract

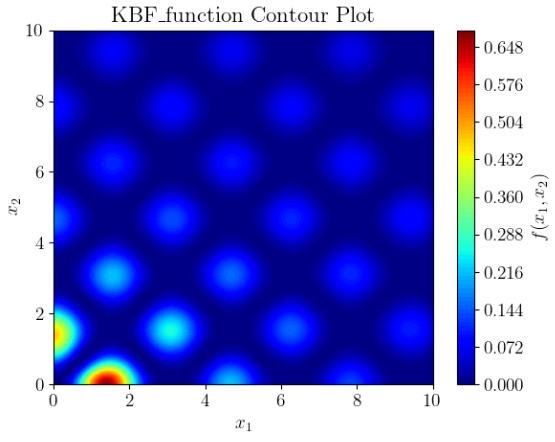
This report conducts a comparative analysis of two optimisation algorithms applied to minimise Keane's Bump Function, (KBF). In particular, the study focuses on a Continuous Genetic Algorithm, (GA), as well as an alternative algorithm not covered in the lectures: the State Transition Algorithm, (STA).

2 Introduction

2.1 Keane's Bump Function



(a) Surface plot.



(b) Contour plot.

Figure 1: The two-dimensional visualisation of the Keane's Bump Function, (KBF).

To compare the performances of the two algorithms, the Keane's Bump Function, (KBF), is used as the objective function. In particular, the n-dimensional constrained optimisation problem is defined as the maximisation of:

$$f(\mathbf{x}) = \left| \frac{\sum_{i=1}^{n} (\cos(x_i))^4 - 2\prod_{i=1}^{n} (\cos(x_i))^2}{\sqrt{\sum_{i=1}^{n} i \cdot x_i^2}} \right| \tag{1}$$

$$\begin{aligned} \text{subject to} \quad & 0 \leq x_i \leq 10 \quad \forall i \in \{1, \ldots, n\} \\ & \prod_{i=1}^{n} x_i > 0.75 \\ & \sum_{i=1}^{n} x_i < \frac{15n}{2} \end{aligned} \tag{2}$$

The two-dimensional form of the function has been plotted in Figure 1. Some notable properties are as follows:

- The function is undefined at the origin, (0, 0). This is due to the division by zero in the denominator of Equation 1. Otherwise, the function is continuous and differentiable everywhere.
- The function is highly multi-modal. Its global maximum is located at the constaint boundary $x_n = 0$, where x_n denotes the final variable in the n-dimensional space. However, there are many local maxima located inside the feasible region.
- The function is nearly symmetric about the line $x_1 = x_2$. This stems from its construction in 1, which primarily involves the the squares of individual input variables, x_i^2. This results some invariance reagrding the order of the input variables.