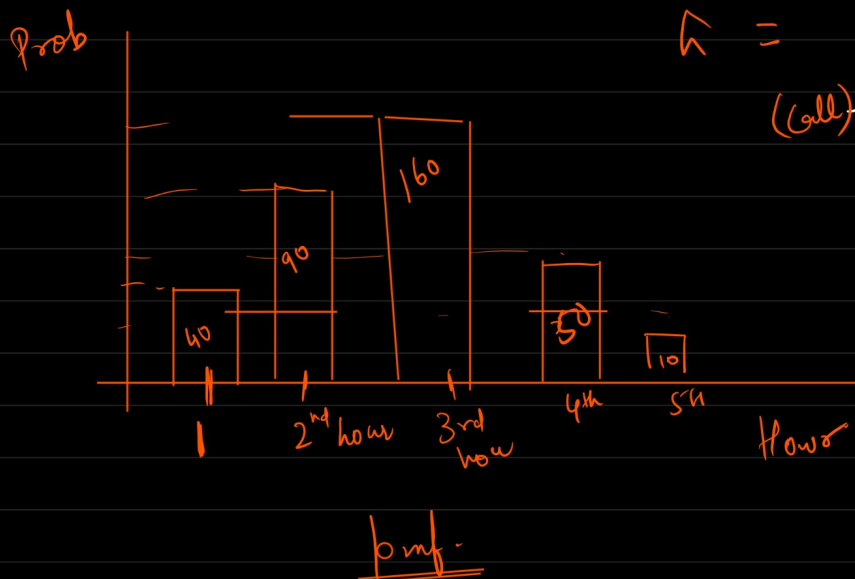


## \* Poisson distribution

The Poisson distribution is a discrete probability distribution that describes the no of events that occur within a fixed interval of time or space given a known average rate of occurrence.

\* No of events occurring in a fixed time interval.

Customer care



$\lambda$  = Expected no of (all) events to occur every time interval

$$\lambda = 100$$

(through out the day not possible,

1st hour = 40

2nd hour = 90

3rd hour = 160

Example

No of people visiting temple/hospital/banks/airport in any hour.

eg. No of accident every hour at a busy route.

eg. No of emails received every hour.

$$\text{pmf} \Rightarrow P(X=x) = \frac{e^{-\lambda} \cdot \lambda^x}{x!}$$

$$e(\text{euler}) = 2.71828$$

$\lambda \rightarrow$  avg rate of events every interval.

\*  $\lambda = 10$  person visiting at 5th hour?

$$P(X=5) = \frac{e^{-\lambda} \cdot \lambda^x}{x!} = \frac{(2.718)^{-10} \cdot 10^5}{5!}$$

Q The average no of customers entering a store in an hour is 5. What is the probability of exactly 3 customers will enter the store next hour.

$$\rightarrow \lambda = 5$$
$$p(x=3)$$

$$\frac{e^{-\lambda} \lambda^x}{x!} = \frac{e^{-5} \cdot 5^3}{3!}$$
$$= \frac{(2.718)^{-5} \cdot 125}{6}$$

$$= \frac{0.00674 \times 125}{6} \approx \underline{\underline{0.14}}$$

Mean of Poisson distr =  $\lambda \times t$

↓  
Avg no of  
event  
at every  
interval

$$\text{variance} = \lambda \times t$$