



GATE

ALL BRANCHES



General Aptitude

QUANTITATIVE APTITUDE

Lecture No.- 08



By- Amulya Ratan Sir

Recap of Previous Lecture



Topic

Number System



Topics to be Covered



Topic-1

Counting Theory ✓

Topic-2

Time and Work ✓

Pipes & Cistern



[MCQ]



#Q. Which largest number of 5 digits is divisible by 99?

Assignment

$$\begin{array}{r} 9 \\ \times 11 \\ \hline \end{array}$$

- A** \times 99999 $\begin{array}{r} -27 \\ 18 \\ \hline 9 \end{array}$
- B** \times 99981 $\begin{array}{r} -19 \\ 17 \\ \hline 2 \end{array}$
- C** \times 99909 $\begin{array}{r} -27 \\ 9 \\ \hline 18 \end{array}$
- D** 99990 $\begin{array}{r} -18 \\ 18 \\ \hline 0 \end{array}$

[MCQ]



#Q. Find the least perfect cube divisible by 2, 3, 4 and 6.

Assignment

A

216

$\rightarrow 6^3$

B

1728

$\rightarrow 12^3$

C

512

$\rightarrow 8^3$

D

360

[MCQ]



#Q. How many natural numbers up to 100 are divisible by both 2 and 3?

Assignment

$$6 \times 1 = 6$$

A

13

B

14

C

17

D

16

16

$$6 \times \underline{16} = 96$$

[MCQ]



#Q. Find the largest four-digit number that is exactly divisible by 88.

Assignment

$$88 = 8 \times 11$$

- A** ~~9844~~ ✗
- B** 9768 ✓ $\frac{15}{15} 0$
- C** ~~8894~~ ✗
- D** 9944 ✓ $\frac{13}{13} 0$

Counting Theory



Counting

(ATM)

PIN

The no. of ways to do a particular work.

OR 211 ⁴(+)

AND 3+12 ⁴(x)

[MCQ]



#Q. In how many different ways you can choose your ATM PIN ?

0 0 0 0
9 9 9 9

$$10 \times 10 \times 10 \times 10$$

✓
0/
1/
2/
3/
4/
5/
6/
7/
8/
9/

$$= 10,000$$

[MCQ]



#Q. In how many different ways you can select a six digit phone password/passcode ?

$$\boxed{10} \times \boxed{10} \times \boxed{10} \times \boxed{10} \times \boxed{10} \times \boxed{10}$$

0-9 0-9

$$= 10,00,000$$

[MCQ]



#Q. How many four digits number can be formed using 1, 2, 3, 4 & 5?

Rep

$$\begin{matrix} \text{Th} & & \text{H} & & \text{Tens} & & \text{U} \\ \boxed{5} & \times & \boxed{5} & \times & \boxed{5} & \times & \boxed{5} \end{matrix}$$

$$= \underline{\underline{625}}$$

Rep X

$$\begin{matrix} \text{Th} & & \text{H} & & \text{Tens} & & \text{U} \\ \boxed{5} & \times & \boxed{4} & \times & \boxed{3} & \times & \boxed{2} \end{matrix}$$

$$(5-1) \quad (5-2) \quad (5-3)$$

$$= 120$$

[MCQ]



#Q. In how many different ways you can choose your ATM PIN which is an even ?

$$10 \times 10 \times 10 \times \underline{5}$$

$$= \underline{\underline{5000}}$$

0
/ 2 / 4 / 6 / 8

[MCQ]



#Q. How many three digits number can be formed using digits 0 to 9?

Rep ^e

~~⊗~~

$$\begin{array}{c} \text{H} \\ \boxed{9} \\ (10-1) \end{array} \times \begin{array}{c} \text{Ten} \\ \boxed{10} \end{array} \times \begin{array}{c} \text{U} \\ \boxed{10} \end{array}$$

$$= \underline{\underline{900}}$$

Rep ^x

$$\begin{array}{c} \text{H} \\ \boxed{9} \\ (10-1) \end{array} \times \begin{array}{c} \text{Ten} \\ \boxed{9} \\ (10-1) \end{array} \times \begin{array}{c} \text{U} \\ \boxed{8} \\ (10-2) \end{array}$$

$$= 81 \times 8 = \boxed{648}$$

[MCQ]



#Q. In how many ways four letters can be posted in 6 post boxes, if each box can take any number letters?

- A** 4096
- B** 1500
- C** 24
- D** 1296

$$\begin{array}{cccc} L_1 & L_2 & L_3 & L_4 \\ \hline 6 & \times 6 & \times 6 & \times 6 \\ & & & = 36 \times 36 = 1296 \end{array}$$

[MCQ]



#Q. In how many ways can you arrange 5 Novels on a shelf?

- A** 720
- B** 120
- C** 360
- D** 300

$$\begin{array}{ccccccccc} & \swarrow & & \swarrow & & & & & \\ \underline{5} & \times & \underline{4} & \times & \underline{3} & \times & \underline{2} & \times & \underline{1} \\ N_1 & & (5-1) & & (5-2) & & (5-3) & & (5-4) \\ \swarrow & & \swarrow & & \swarrow & & \swarrow & & \swarrow \\ N_2 & & N_3 & & N_4 & & N_5 & & \end{array}$$

$$= 120$$

[MCQ]



#Q. Four persons A, B, C and D are to be seated in a row. C should not be seated at the second position from the left end of the row. The number of distinct seating arrangements possible is?

- A** 6
- B** 9
- C** 18
- D** 24

$$\boxed{3} \times \boxed{3} \times \boxed{2} \times \boxed{1}$$

$$(4-1) \quad \cancel{\times} \quad (4-2) \quad (4-3)$$

$$= 18$$

[MCQ]

Assignment



#Q. Five different book (P, Q, R, S, T) are to be arranged on a shelf. The books R and S are to be arranged first and second, respectively from the right side of the shelf. The number of different orders in which P, Q and T may be arranged is?

A

12

B

120

C

6

D

2

[MCQ]

Assignment



#Q. A license plate begins with 3 letters. If the possible letters are A, B, C, D and E, how many different ways these letters can be written if no letter is used more than once?

- A** 720
- B** 120
- C** 60
- D** 30

[MCQ]

Assignment



#Q. In how many different ways can the letters of the word 'PLEADING' be arranged in such a way that the vowels always come together?

- A** 720
- B** 4320
- C** 5040
- D** 3600

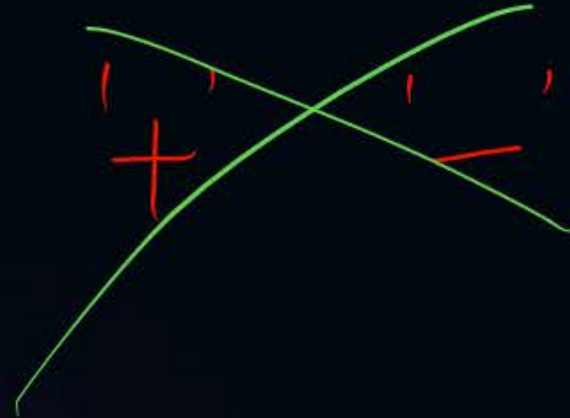
Direct & Inverse:

$(+)$

$(-)$

(\times)

(\div)

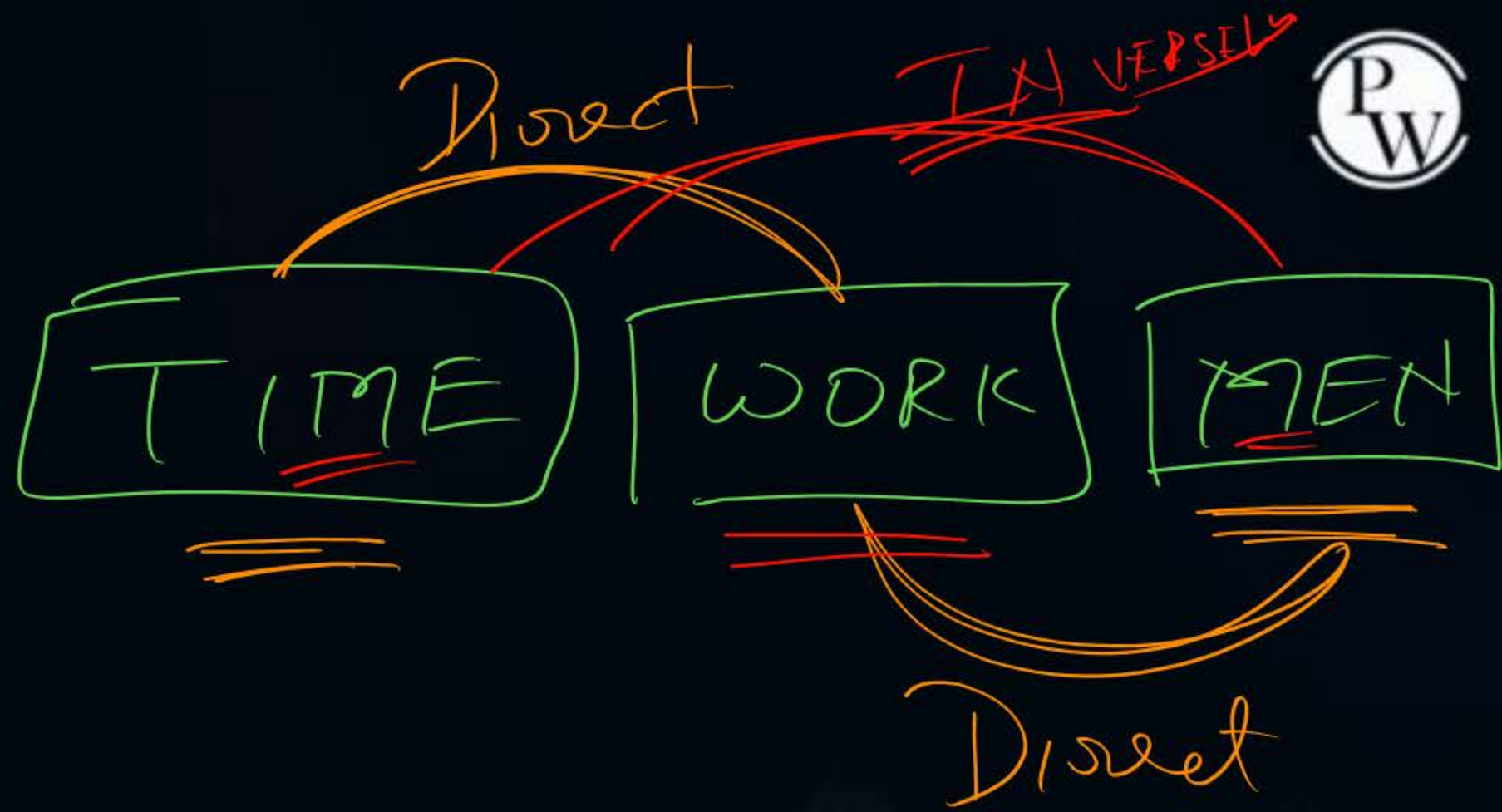


$(+)$
 $(-)$

$(-)$
 $(+)$

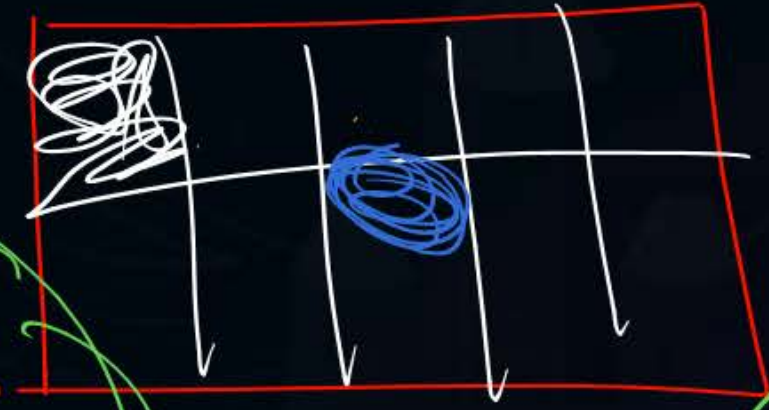


Time & Work



$\checkmark \frac{1}{10}$ $A = 10$ days
 $\checkmark \frac{1}{20}$ $B = 20$ days

$A \& B \Rightarrow \frac{1}{10} + \frac{1}{20} = \frac{3}{20} \Rightarrow \frac{20}{3} = 6.6 \text{ or } 6\frac{2}{3} \text{ days}$



Let's Try:



①

$P \rightarrow 20 \text{ day}$; $Q \rightarrow 30 \text{ days}$

12 days

②

$A \rightarrow 25 \text{ days}$; $B \rightarrow 40$

$15\frac{5}{13}$ OR $15.3\ldots$

③

$P \& Q \rightarrow 40 \text{ days}$; $P \rightarrow 60 \text{ days}$

$Q \rightarrow ?$ 120 days

[MCQ]

① A ② B ③ A ④ B ⑤ A —



#Q. A can do a work in 10 days whereas B in 20 days. They started working on alternate days, i.e. 1st day 'A', 2nd day 'B', 3rd day 'A'.....so on. Then in how many days the total work would be completed ?

$\frac{7}{20} + \frac{1}{10} = ?$

$A = \frac{1}{10} \quad | \quad B = \frac{1}{20}$

$\frac{1}{10} + \frac{1}{20} = \frac{3}{20} \xrightarrow{\times 6} 2 \text{ days}$

$\frac{18}{20} \Rightarrow 12 \text{ days}$

~~13 days~~

[MCQ]



1 B 2 A 3 B 4 A 5 B - - -

#Q. A can do a work in 10 days whereas B in 20 days. They started working on alternate days, i.e. 1st day 'B', 2nd day 'A', 3rd day 'B'.....so on. Then in how many days the total work would be completed?

$$\frac{1}{10} + \frac{1}{20} = \frac{3}{20} \xrightarrow{\times 6} 2 \text{ days}$$

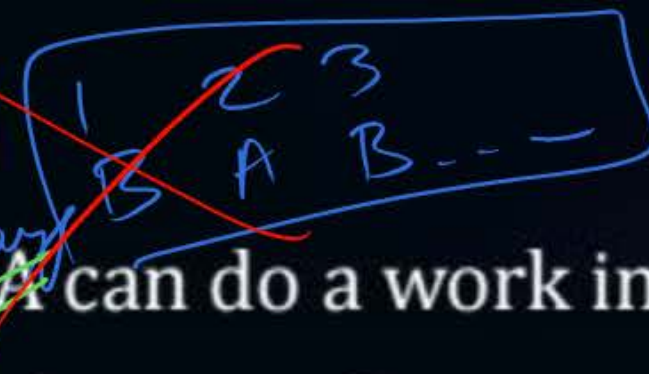
$$\frac{1}{10} - \frac{1}{20} = \frac{1}{20} \text{ ?}$$

$$\frac{18}{20} \rightarrow 12 \text{ days}$$

1 week A = 10
 $\frac{1}{20}$ " A = $10 \times \frac{1}{20}$
 $= \frac{1}{2}$

$13 \frac{1}{2} \text{ days}$
 OR
 13.5 days

[MCQ]



$$A = \frac{1}{25} \quad | \quad B = \frac{1}{40}$$

$$30\frac{5}{8}$$



#Q. A can do a work in 25 days whereas B in 40 days. They started working on alternate days, i.e. 1st day 'A', 2nd day 'B', 3rd day 'A'.....so on. Then in how many days the work would be completed?

A

15 $\frac{5}{8}$ days

B

30 $\frac{5}{8}$ days

C

31

D

16

$$\frac{1}{40} ?$$

$$\frac{1}{25} + \frac{1}{40} =$$

$$\frac{13}{200}$$

2 days

$$\frac{1}{40} \text{ " } A = \frac{5}{25} \times \frac{1}{40} = \frac{1}{8}$$

$$\frac{195}{200}$$

30 days

A & B & C

$$\Rightarrow \frac{1}{20} + \frac{1}{30} + \frac{1}{60}$$

Total

$$2 + 15 + 3$$

20 days

$$\frac{1}{10}$$

$$\frac{2}{10} + \frac{1}{20} = \frac{4}{20} + \frac{1}{20}$$

$$BEC \rightarrow \frac{1}{30} + \frac{1}{60}$$

$$= \frac{2}{60} = \frac{1}{30}$$

heart BEC = 20

$\frac{3}{4} \times 11 = 10 \times \frac{3}{4}$

15 days

[MCQ]

$$A = \frac{1}{20} \text{✓} \quad B = \frac{1}{30} \text{✓} \quad C = \frac{1}{60} \text{✓}$$



#Q. A can do a work in 20 days whereas B in 30 days and C in 60 days. They started the work together. But A left after two days and B left three days before the work got completed. Then the total work was done in how many days?

$$\begin{aligned} \frac{x}{60} + \frac{x-3}{30} + \frac{2}{20} &= 1 \\ \Rightarrow x + 2x - 6 + 2 &= 60 \\ 3x &= 60 - 20 \end{aligned}$$

[MCQ]

$$A = \frac{1}{10} \quad | \quad B = \frac{1}{20} \quad | \quad C = \frac{1}{60}$$



#Q. A can do a work in 10 days whereas B in 20 days and C in 60 days. They started the work together. But A left at the end of 3rd day and B left at the end of 5th day. Then the remaining work was done by C in how many days?

A

27

B

35

C

31

D

22



$$1 = \frac{x}{60} + \frac{5}{20} + \frac{3}{10}$$

$$\Rightarrow x + 15 + 18 = 60$$

$$\therefore x = 27$$

$$27 - 5 = 22 \text{ days}$$

[MCQ]



#Q. If 9 MONKEYS EAT 9 BANANAS IN 9 MINUTES, THEN HOW MANY MONKEYS WILL EAT 45 BANANAS IN 45 MINUTES?

Chain Rule

$$\textcircled{9 \times} \frac{45}{9} \times \frac{9}{45}$$

9 monkeys

Monkeys

9

?

Banana

9

45

Time

9

45

Chain Rule:

$$98 \times \frac{63}{45}$$

$$\frac{45}{100} \rightarrow 98$$

$$\frac{63}{100} \rightarrow ?$$

$$45\% \text{ of } x = 98$$

$$\Rightarrow x = 98 \times \frac{100}{45}$$

$$\frac{63}{100} \text{ of } x = \frac{63}{100} \times 98 \times \frac{100}{45}$$

$$\uparrow \textcircled{1} \times \frac{3}{2}$$

$$\downarrow \textcircled{1} \times \frac{2}{3}$$

[MCQ]



#Q. 12 men can do a work in 15 days working 8 hours a day. In how many days can 9 men do the same work, working 10 hours a day?

Handwritten solution using the rule of three:

	Men	Days	hrs/day
1	12	15	8
2	9	?	10

Calculation: $8 \times 2 = 16 \text{ days}$

[MCQ]

Brain storming



#Q. A hostel with 600 students had sufficient food for 210 days. After 30 days, 240 students left the hostel. Now the remaining food will last for how many days?

[MCQ]

Brainstorming



#Q. A Clock which gains 10 minutes in every one hour was set correct at 6 am. If that clock represents 1 pm the same day, what must be the correct time?

[MCQ]

Assignment



#Q. A contractor under takes to make a road in 40 days and employs 25 men. After 24 days, he finds that only one-third of the road is made. How many extra men should he employ so that he is able to complete the work 4 days earlier?

- A** 75
- B** 100
- C** 50
- D** None of these

[MCQ]

Assignment



#Q. A can do a work in 60 days whereas B in 20 days. If they together took a contract of ₹32000, then what would be the share of A?

- A** ₹ 8000
- B** ₹ 6000
- C** ₹ 1800
- D** ₹ 2040



2 mins Summary



Topic

Counting Theory Time and Work

✓ Pipes & Cisterns
✓ Chain Rule (Clock?)



THANK - YOU