

CS & IT ENGINEERING

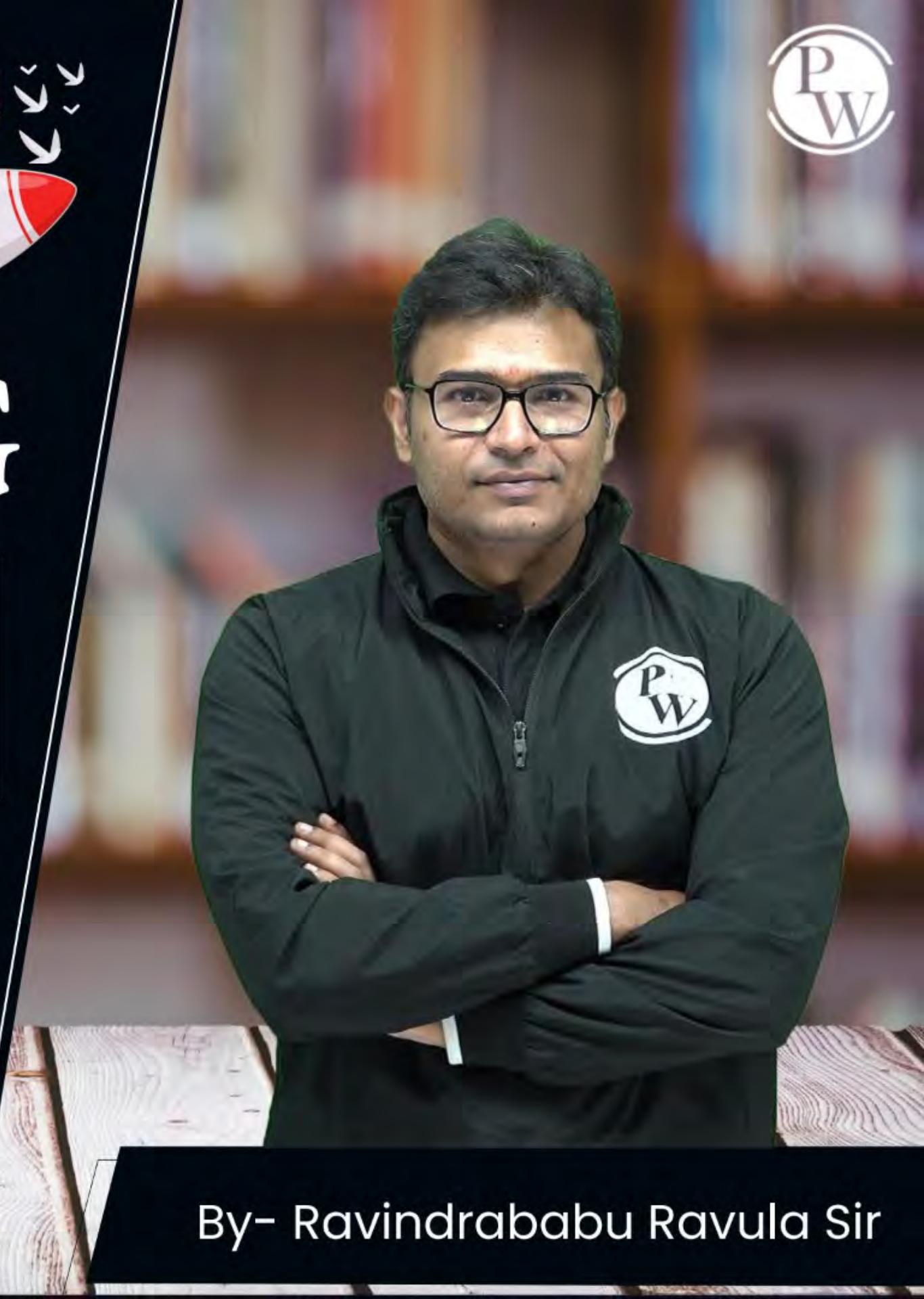


Database Management System

DBMS

Lecture No. 4

By- Ravindrababu Ravula Sir



Recap of Previous Lecture



Topic

Normalization

Topics to be Covered



Topic

Integrity Constraints & ER Model (2 Marks)

Topic

Normalization (2-4 Marks)

Topic

Queries (Relational Algebra, SQL, Tuple
Relational Calculus) (4 Marks)

Topic

File Organization & Indexing(2-4 Marks)

Topic

Transactions & Concurrency Control (2- 4 Marks)

Topics to be Covered



Topic

Normal Forms- 1NF, 2NF, 3NF, BCNF, 4NF



Topic

Finding Highest NF of a Relation



Topic

Decomposition into Highest NF



60-70%



Topic: Normal Forms

Normal Forms:

- Used to identify degree of redundancy.

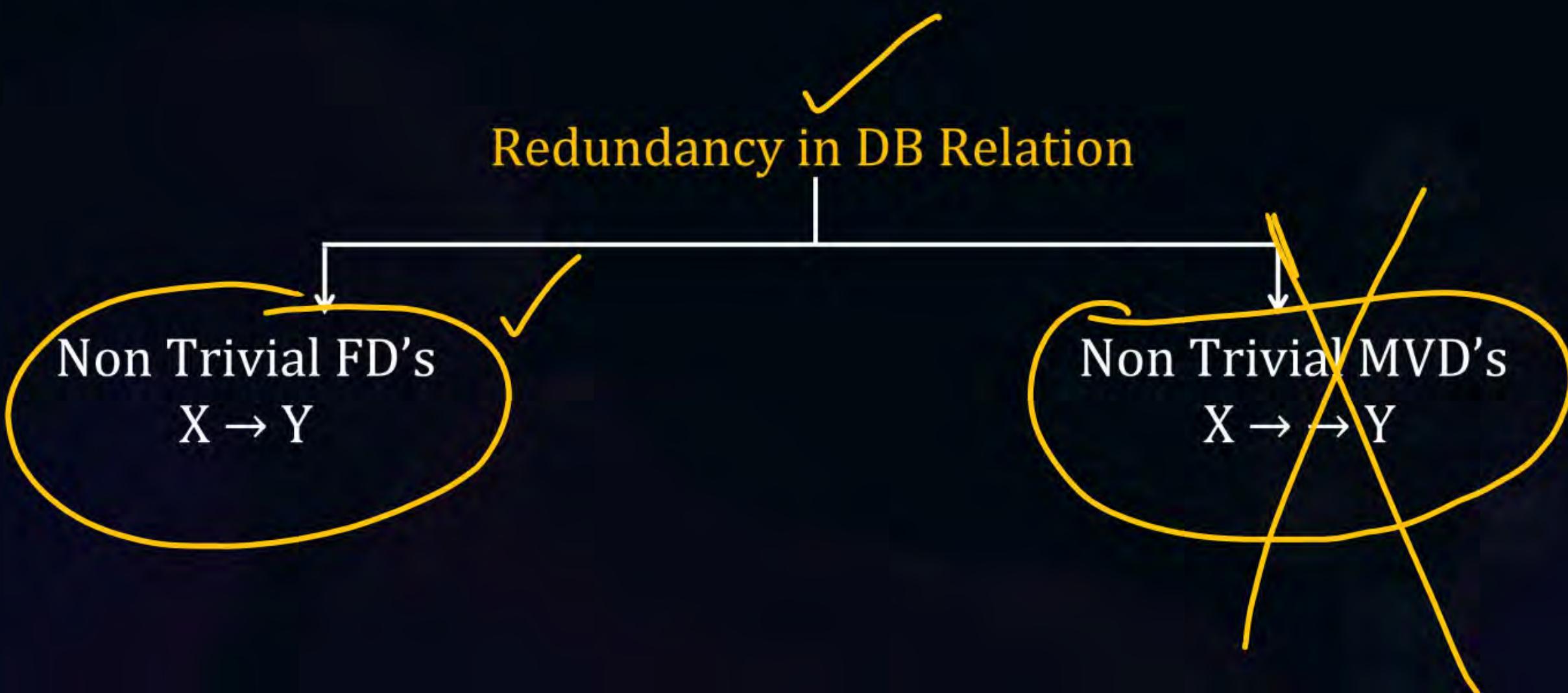




Topic: Normal Forms

Normal Forms:

- Used to identify degree of redundancy.





Topic: Normal Forms



Different Normal Forms are (Redundancy ↓ as we go down) :

- (i) 1 NF ✓
- (ii) 2 NF ✓
- (iii) 3 NF ✓
- (iv) BCNF ✓
- (v) 4 NF



Topic: Normal Forms



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- (i) 1 NF
 - (ii) 2 NF
 - (iii) 3 NF
 - (iv) BCNF
 - (v) 4 NF
- Done over FD set ($X \rightarrow Y$)



Topic: Normal Forms

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 - (iv) BCNF
 - (v) 4 NF
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- } 0% redundancy over FD's, may not on MVD's



Topic: Normal Forms

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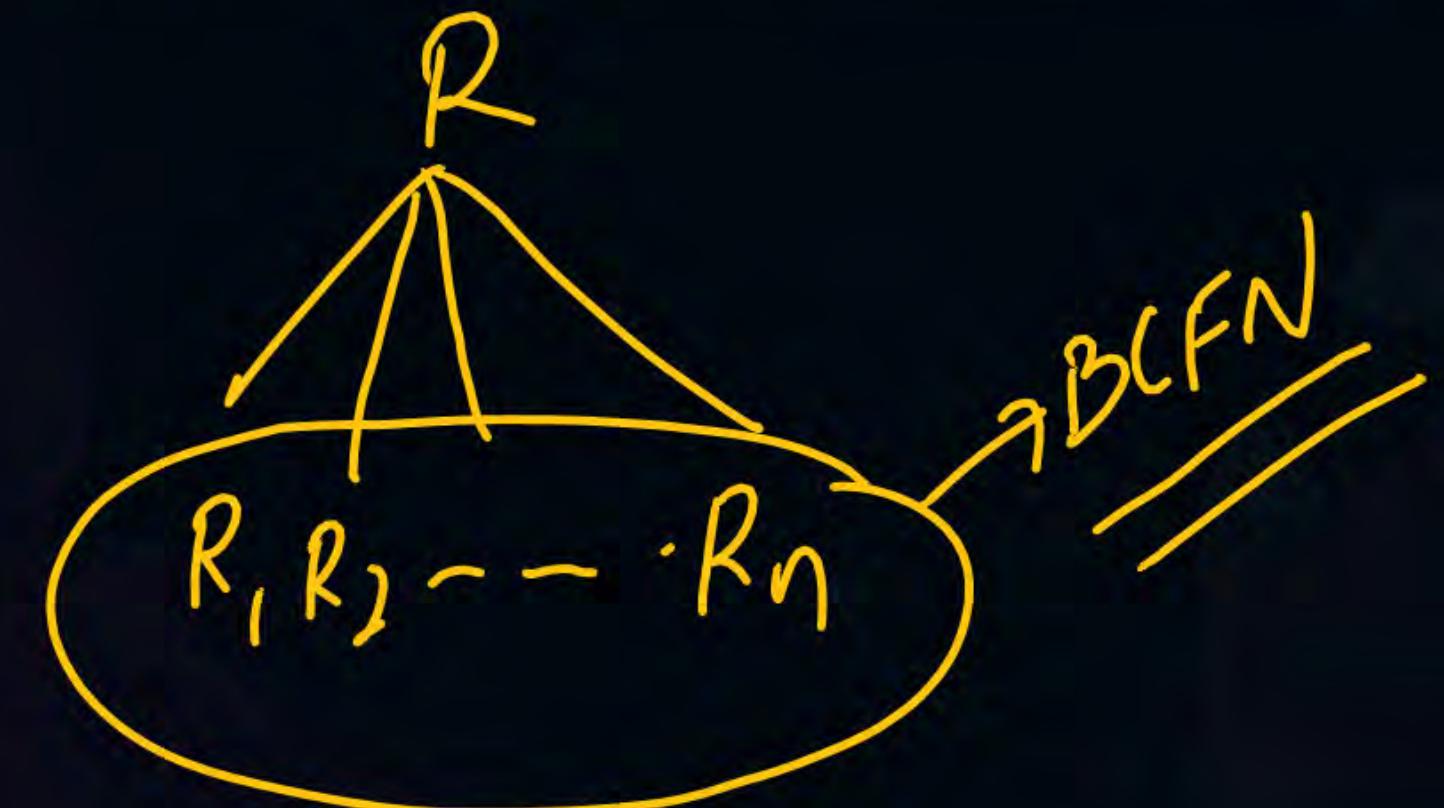
- (i) 1 NF
- (ii) 2 NF
- (iii) 3 NF
- (iv) BCNF → 0% redundancy over FD's, may not on MVD's
- (v) ~~4 NF~~ → Done over MVD set → 0% redundancy on FD's & MVD's ($X \rightarrow\rightarrow Y$) ~~X~~



Topic: Normal Forms

Very frequent questions in GATE from 1NF, 2NF, 3NF and BCNF.

- To remove redundancies in FD's, decompose till it follows BCNF.





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Topic: Normal Forms

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Topic: Normal Forms



Very frequent questions in GATE from 1NF, 2NF, 3NF and BCNF.

- To remove redundancies in FD's, decompose till it follows BCNF.
- To remove redundancies in MVD's decompose till it follows 4NF.
- 1NF is default RDBMS condition.



Inspiring Stories : Dr. Diwan Singh

Background: Punjabi doctor-poet in Port Blair.



Struggles: Led the Indian Independence League in the islands.

Achievements: Opposed tyranny even under Japanese occupation; tortured to death in 1944.

Impact: A museum and records honor him; islanders remember his fearless voice.



Topic: Normal Forms

(i) First Normal Form (1NF):

- Relation R is in 1NF iff no multivalued attributes are present.
- Every attribute of R must be atomic/single valued.
- Default NF of RDBMS relations, i.e., relation is by default 1NF by RDBMS guidelines.



Topic: Properties of Decomposition

Ex1 : Let a Relation R be the following & FD is $\text{Sid} \rightarrow \text{Sname}$

Sid	Sname	Cid
S1	A	C1 / C2
S2	B	C2 / C3
S3	B	C3

Cid is multivalued attribute.

∴ R is not in 1NF hence, not a RDBMS.



Topic: Properties of Decomposition

Ex1 : Let a Relation R be the following & FD is $\text{Sid} \rightarrow \text{Sname}$

Sol: For $\text{Sid} \rightarrow \text{Sname}$, CK is Sid Cid .

∴ We can write data like below because of unique rows.

Sid	Sname	Cid
S1	A	C1 / C2
S2	B	C2 / C3
S3	B	C3

=>

Sid	Sname	Cid
S1	A	C1 ✓
S1	A	C2 ✓
S2	B	C2 ✓
S2	B	C3 ✓
S3	B	C3



Topic: Properties of Decomposition

Ex2 : For a Relation R, with FD $\text{Sid} \rightarrow \text{Sname}$ & the table as below.

Sid	Sname	Cid	Phno	email
S1	A	<u>C1 / C2</u> 2	3 <u>P1 / P2 / P3</u>	4 <u>e1 / e2 / e3 / e4</u>
S2	B	C2 / C3 2	2 P3 / P4	2 e4 / e5



Topic: Properties of Decomposition

Ex2 : For a Relation R, with FD Sid \rightarrow Sname & the table as below.

Sid	Sname	Cid	Phno	email
S1	A	C1 / C2	P1 / P2 / P3	e1 / e2 / e3 / e4
S2	B	C2 / C3	P3 / P4	e4 / e5

Sol : To convert 1NF, the CK is Sid Cid Phno email

S1 - 24 tuples
 $(2 \times 3 \times 4)$

S2 - 8 tuples
 $(2 \times 2 \times 2)$

Sid	Sname	Cid	Phno	email
S1	A	C1	P1	e1
	A	C2	P1	e1
	:	:	:	:
	A	C2	P3	e4
S2	B	C2	P3	e4
	:	:	:	:
	B	C3	P4	e5



Topic: Properties of Decomposition



Now the relation is DBMS and is in 1NF

⇒ Now there are 24 tuples with (S1, A.....) row and 8 tuples of (S2, B...)
which causes very high redundancy



Topic: Properties of Decomposition



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⇒ 1NF - default NF of RDBMS



Topic: Properties of Decomposition

Now the relation is DBMS and is in 1NF

⇒ Now there are 24 tuples with (S1, A.....) row and 8 tuples of (S2, B...) which causes very high redundancy

⇒ 1NF - default NF of RDBMS

⇒ 2NF, 3NF, BCNF, 4NF - used to reduce/ eliminate redundancy



Topic: Properties of Decomposition



Some points to remember about Redundancy:

⇒ $X \rightarrow Y$ FD of Relation R forms redundancy iff

- $X \rightarrow Y$ is Non-trivial FD
- and
- X is not Super Key of R

$X \rightarrow Y$
↓
Not
SK



Topic: Properties of Decomposition



Some points to remember about Redundancy:

$\Rightarrow X \rightarrow Y$ FD of Relation R forms redundancy iff

- $X \rightarrow Y$ is Non-trivial FD
and
- X is not Super Key of R

$\Rightarrow X \rightarrow Y$ FD of Relation R doesnt form redundancy iff

- $X \rightarrow Y$ is a trivial FD ($X \supseteq Y$)
or
- X is Super Key of R

$$\begin{array}{c} X \rightarrow Y \\ \downarrow \\ SK \end{array}$$



Topic: Properties of Decomposition



Some points to remember about Redundancy:

$\Rightarrow X \rightarrow Y$ FD of Relation R forms redundancy iff

- $X \rightarrow Y$ is Non-trivial FD
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Topic: Properties of Decomposition

Ex2 : Taking before example For a Relation R, with FD Sid \rightarrow Sname & the table as below.

Sid	Sname	Cid	Phno	email
S1	A	C1 / C2	P1 / P2 / P3	e1 / e2 / e3 / e4
S2	B	C2 / C3	P3 / P4	e4 / e5

S1 - 24 tuples ($2 \times 3 \times 4$)	Sid	Sname	Cid	Phno	email
S1	A	C1	P1	e1	
S1	A	C2	P1	e1	
:	:	:	:	:	:
S1	A	C2	P3	e4	
S2 - 8 tuples ($2 \times 2 \times 2$)	S2	B	C2	P3	e4
	:	:	:	:	:
	S2	B	C3	P4	e5



Topic: Properties of Decomposition

Ex2 : Taking before example For a Relation R, with FD $\text{Sid} \rightarrow \text{Sname}$ & the table as below.

Sid	Sname	Cid	Phno	email
S1	A	C1 / C2	P1 / P2 / P3	e1 / e2 / e3 / e4
S2	B	C2 / C3	P3 / P4	e4 / e5

Sid	Sname	Cid	Phno	email
S1 - 24 tuples $(2 \times 3 \times 4)$	A	C1	P1	e1
	A	C2	P1	e1
	:	:	:	:
	A	C2	P3	e4
S2 - 8 tuples $(2 \times 2 \times 2)$	B	C2	P3	e4
		:	:	:
		C3	P4	e5

Explanation : After converting to 1NF, $\text{Sid} \rightarrow \text{Sname}$ forms redundancy becoz Sid is not a superkey



Topic: Properties of Decomposition



Ex: R (eid, ename, DOB, rating, salary) and FD are {eid → ename DOB rating,
rating → salary}



Topic: Properties of Decomposition

Ex: R (eid, ename, DOB, rating, salary) and FD are {eid → ename DOB rating,
rating → salary}

Sol: eid is CK.

eid → ename DOB rating

↓

SK

∴ No redundancy occurs ✓

No Redundancy



Topic: Properties of Decomposition



Ex: R (eid, ename, DOB, rating, salary) and FD are {eid → ename DOB rating,
rating → salary}

Sol: eid is CK.

$\text{eid} \rightarrow \text{ename DOB rating}$

↓

SK ∴ No redundancy occurs



$\text{rating} \rightarrow \text{salary}$

↓

Not SK ∴ Forms redundancy



Topic: Properties of Decomposition



Ex: R (eid, ename, DOB, rating, salary) and FD are {eid → ename DOB rating, rating → salary}

Sol: eid is CK.

$\text{eid} \rightarrow \text{ename DOB rating}$

↓

SK ∴ No redundancy occurs

$\text{rating} \rightarrow \text{salary}$

↓

Not SK ∴ Forms redundancy

eid	ename	DOB	rating	Salary
e1			8 . .	50k
e2			8	50k
e3			8	50k
e4			10	70k

Redundancy in a FD $X \rightarrow Y$ occurs if
 X is not SK



Topic: Properties of Decomposition



Ex: R (eid, ename, DOB, rating, salary) and FD are {eid → ename DOB rating, rating → salary}

Sol: eid is CK.

$\text{eid} \rightarrow \text{ename DOB rating}$



SK ∴ No redundancy occurs

$\text{rating} \rightarrow \text{salary}$



Not SK ∴ Forms redundancy

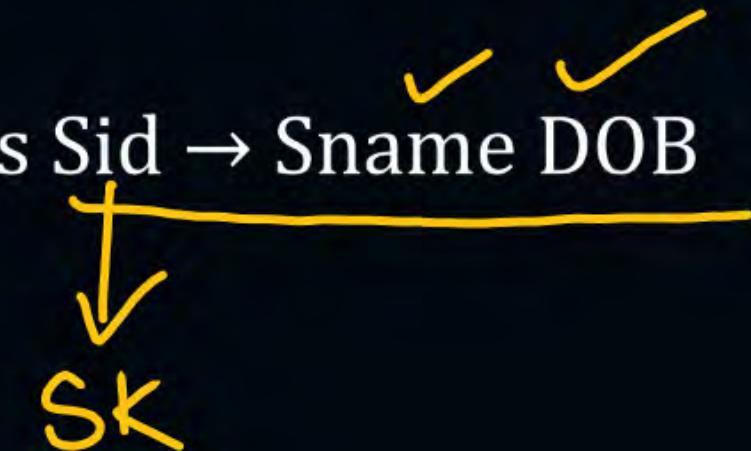
eid	ename	DOB	rating	Salary
e1			8	50k
e2			8	50k
e3			8	50k
e4			10	70k

Redundancy
 \checkmark rating → salary
Since salary depends
on rating



Topic: Properties of Decomposition

Ex3 : R (Sid, Sname, DOB) and FD is $\text{Sid} \rightarrow \text{Sname}$ DOB





Topic: Properties of Decomposition



Ex3 : R (Sid, Sname, DOB) and FD is $\text{Sid} \rightarrow \text{Sname}$ DOB

Sol : Sid is CK. ✓



Topic: Properties of Decomposition



Ex3 : R (Sid, Sname, DOB) and FD is $\text{Sid} \rightarrow \text{Sname DOB}$

Sol : Sid is CK.

$\text{Sid} \rightarrow \text{Sname DOB}$

↓

SK \therefore No redundancy occurs



Topic: Properties of Decomposition

Ex4 : R (ABCDE) and FDs are {AB → C, B → D, D → E, AE → F, C → A}



Topic: Properties of Decomposition

Ex4 : R (ABCDE) and FDs are {AB → C, B → D, D → E, AE → F, C → A}

Sol : C key are AB, BC



Topic: Properties of Decomposition

Ex4 : R (ABCDE) and FDs are { $AB \rightarrow C$, $B \rightarrow D$, $D \rightarrow E$, $AE \rightarrow F$, $C \rightarrow A$ }

Sol : C key are AB, BC

\downarrow
SK

Except $AB \rightarrow C$ all other FD's form redundancy because the determinants are not super keys.

Lits



Topic: Normal Forms



Four points to remember about FD's that forms Redundancy:

1. Proper subset of Candidate key → Non Prime



Topic: Normal Forms



Four points to remember about FD's that forms Redundancy:

1. Proper subset of Candidate key \rightarrow Non Prime
2. Non Prime Attribute \rightarrow Non Prime Attribute



Topic: Normal Forms

Four points to remember about FD's that forms Redundancy:

1. Proper subset of Candidate key \rightarrow Non Prime
2. Non Prime Attribute \rightarrow Non Prime Attribute
3. $\left\{ \begin{array}{l} \text{Combination of Proper Subset of CK} \\ \& \text{Non-Prime Attribute} \end{array} \right\} \rightarrow \text{Non Prime Attributes}$



Topic: Normal Forms



Four points to remember about FD's that forms Redundancy:

1. Proper subset of Candidate key \rightarrow Non Prime
2. Non Prime Attribute \rightarrow Non Prime Attribute
3. $\left\{ \begin{array}{l} \text{Combination of Proper Subset of CK} \\ \& \text{Non-Prime Attribute} \end{array} \right\} \rightarrow \text{Non Prime Attributes}$
4. Proper subset of CK \rightarrow Proper subset of Some Other CK





Topic: Normal Forms

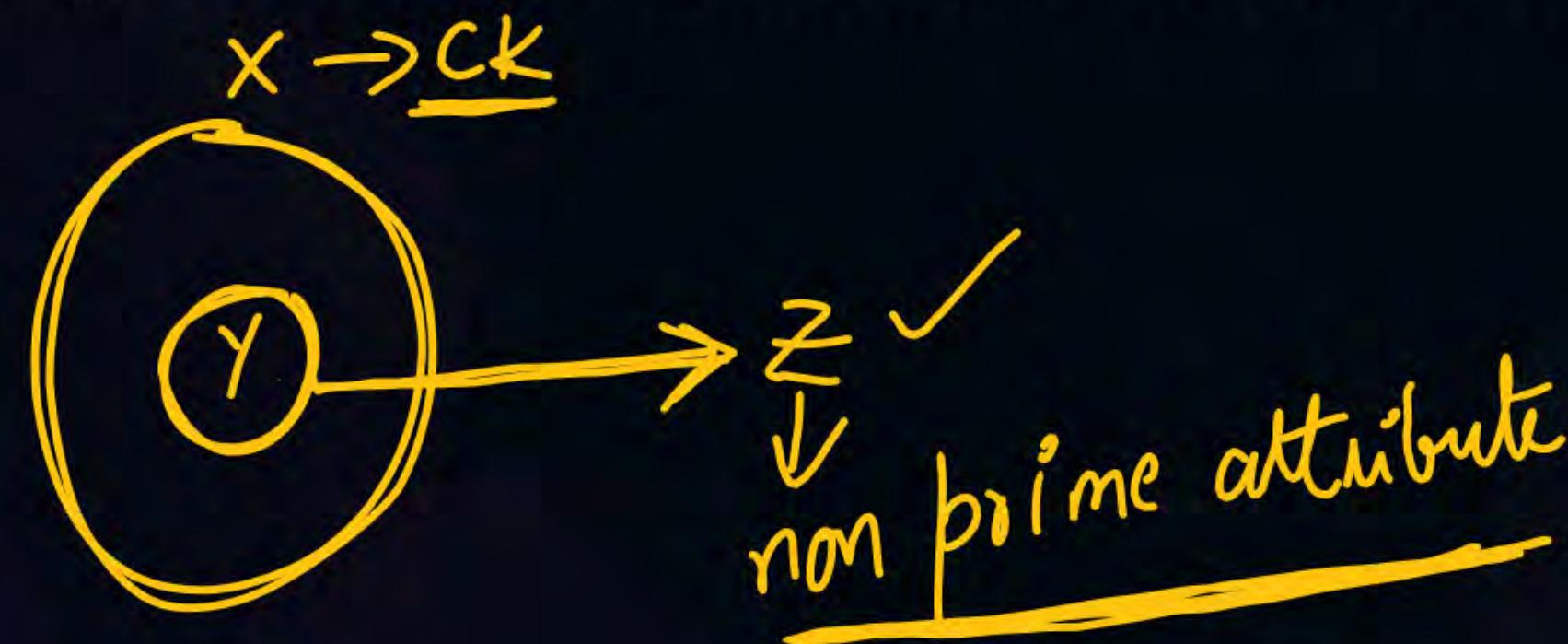
- Partial Dependency:



Topic: Normal Forms

- Partial Dependency:

Partial dependency for a relation R with Candidate Key X,
 $Y \rightarrow Z$ is called partial dependency where $Y \subset X$ and Z is non prime attribute.

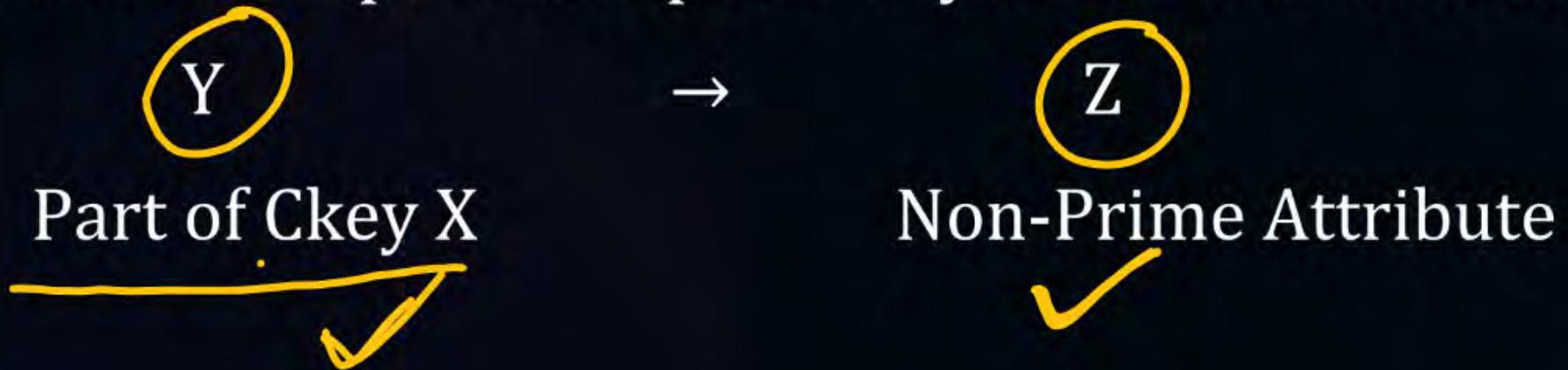




Topic: Normal Forms

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Topic: Normal Forms

- **Partial Dependency:**

Partial dependency for a relation R with Candidate Key X,
 $Y \rightarrow Z$ is called partial dependency where $Y \subset X$ and Z is non prime attribute.



(ii) Second Normal Form (2NF): ✓

- R is in 2 NF iff there are no partial dependencies in R.



Topic: Normal Forms



(iii) Third Normal Form (3NF):



Topic: Normal Forms

(iii) Third Normal Form (3NF):

- Relation R is in 3NF iff every Non-trivial FD. $X \rightarrow Y$ follows
 - (i) X must be Super key of R



Topic: Normal Forms

(iii) Third Normal Form (3NF):

- Relation R is in 3NF iff every Non-trivial FD. $X \rightarrow Y$ follows

(i) X must be Super key of R

or

(ii) Y must be prime attribute of R





Topic: Normal Forms

(iii) Third Normal Form (3NF):

- Relation R is in 3NF iff every Non-trivial FD. $X \rightarrow Y$ follows

(i) X must be Super key of R

or

(ii) Y must be prime attribute of R

$$\begin{array}{ccc} X & \rightarrow & Y \\ \underline{\text{SK}} & (\text{or}) & \underline{\text{Prime Attr.}} \end{array}$$



Topic: Properties of Decomposition

Ex: R (ABC) and FDs are {AB → C, C → A}



Topic: Properties of Decomposition



Ex: R (ABC) and FDs are $\{AB \rightarrow C, C \rightarrow A\}$

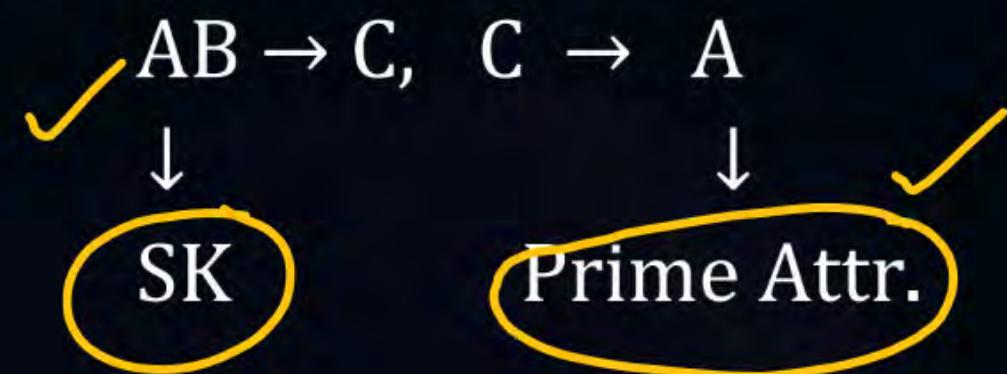
Sol: The CK are AB, BC



Topic: Properties of Decomposition

Ex: R (ABC) and FDs are $\{AB \rightarrow C, C \rightarrow A\}$

Sol: The CK are AB, BC





Topic: Properties of Decomposition



Ex: R (ABC) and FDs are $\{AB \rightarrow C, C \rightarrow A\}$

Sol: The CK are AB, BC

$AB \rightarrow C, C \rightarrow A$ are in 3NF

↓

SK

↓

Prime Attr.

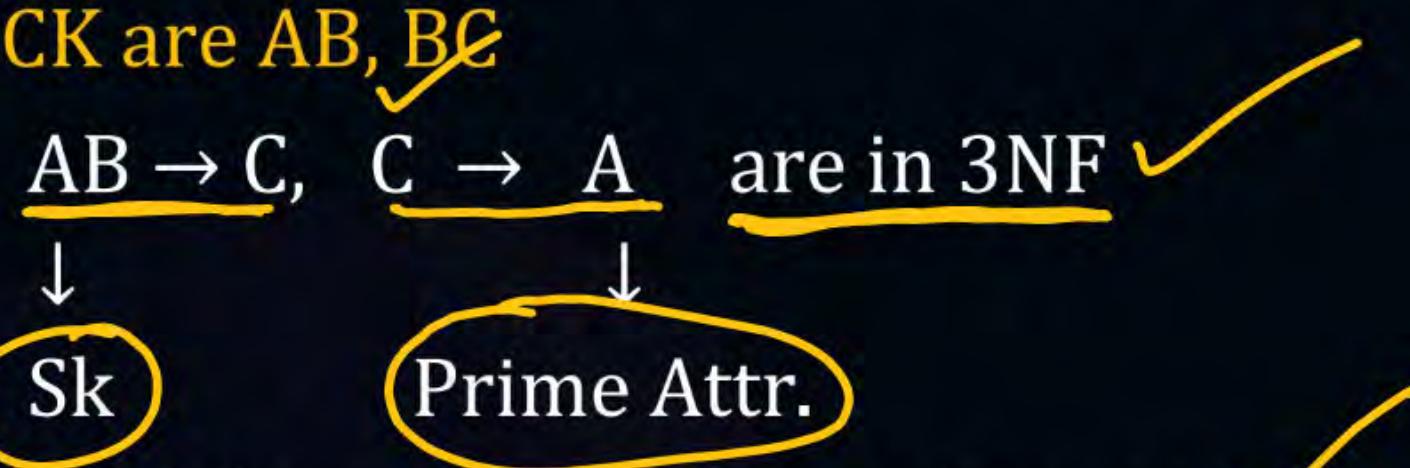


Topic: Properties of Decomposition

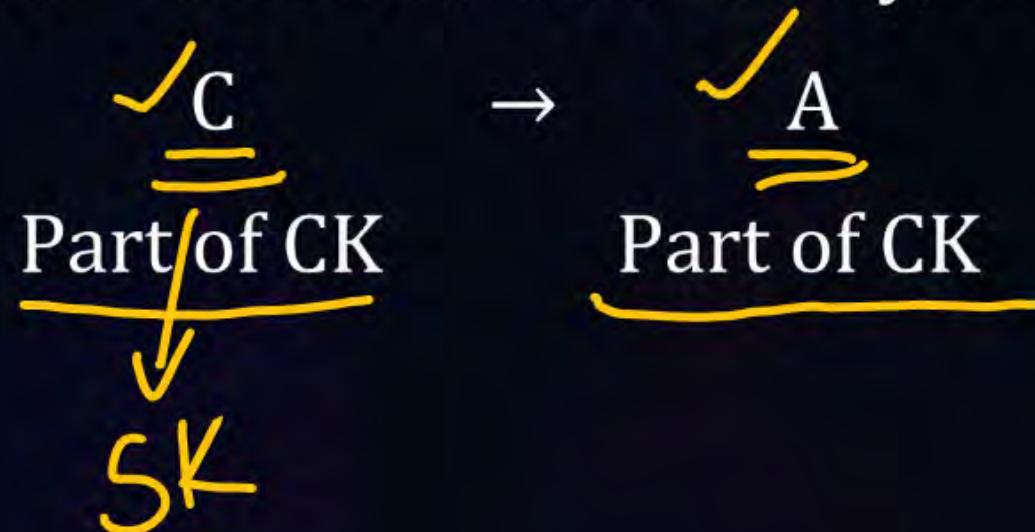


Ex: R (ABC) and FDs are $\{AB \rightarrow C, C \rightarrow A\}$

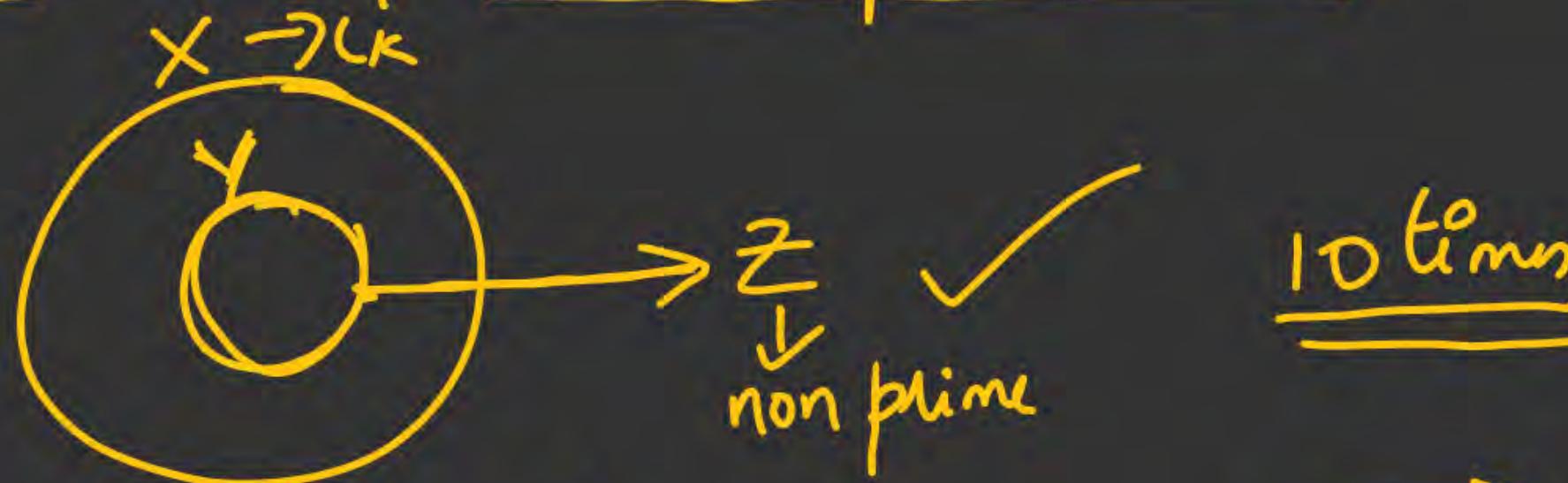
Sol: The CK are AB, BC



But $C \rightarrow A$ forms redundancy, because



II NF: No partial dependencies ✓



10¹⁰ min

III NF: $X \rightarrow Y$ ✓
✓ SK: δ · prime

B CNF: $X \rightarrow Y$ ✓
 $X \rightarrow$ Superkey

5 min

PA
any attribute
of ACK



Topic: Normal Forms

- Proper Subset of Ckey → Proper Subset of other Ckey is allowed in 3NF
but it forms redundancy.
- To remove redundancies of Non-trivial FD's completely, we should go
for BCNF.



Topic: Normal Forms

(iv) BOYCE - CODD NORMAL FORM (BCNF):

- Relation R is in BCNF, iff for every Non-trivial FD $X \rightarrow Y$ in R, X should be a Super key.

$$\begin{array}{c} X \rightarrow Y \\ \downarrow \\ SK \end{array}$$



Topic: Normal Forms

(iv) BOYCE - CODD NORMAL FORM (BCNF):

- Relation R is in BCNF, iff for every Non-trivial FD $X \rightarrow Y$ in R, X should be a Super key.

$X \rightarrow Y$ this is Non Trivial FD ✓



Topic: Normal Forms



(iv) BOYCE - CODD NORMAL FORM (BCNF):

- Relation R is in BCNF, iff for every Non-trivial FD $X \rightarrow Y$ in R, X should be a Super key.

✓

$X \rightarrow Y$ this is Non Trivial FD

↓

SK ✓



Topic: Highest NF

- For the before example

R(ABCDE) and FD's {AB → C, B → D, D → E, AE → F, C → A}

Lets Find the highest NF



Topic: Highest NF

$A \rightarrow BC$ → Prime attr

AB and BC are

CKs

- For the before example

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$

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Topic: Highest NF

- For the before example

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$

Lets Find the highest NF

$AB \rightarrow C$

$B \rightarrow D$

$D \rightarrow E$

$AE \rightarrow F$

$C \rightarrow A$

AB and BC are
CKs



Topic: Highest NF

- For the before example

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$

2NF

AB $\rightarrow C$

✓

AB is Super key

$B \rightarrow D$

$D \rightarrow E$

$AE \rightarrow F$

$C \rightarrow A$

AB and BC are
CKs



Topic: Highest NF

- For the before example

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$

2NF

$AB \rightarrow C$ ✓

AB is Super key

$B \rightarrow D$ ✗

B is proper subset of Ck

$D \rightarrow E$

$AE \rightarrow F$

$C \rightarrow A$

AB and BC are
CKs



Topic: Highest NF

- For the before example

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$

2NF

$AB \rightarrow C$	✓	AB is Super key
$B \rightarrow D$	✗	B is proper subset of Ck
$D \rightarrow E$	✓	Both are non primes
$AE \rightarrow F$		
$C \rightarrow A$		

AB and BC are
CKs



Topic: Highest NF

- For the before example
- AB and BC are
CKs

R(ABCDE) and FD's {AB → C, B → D, D → E, AE → F, C → A}

2NF

AB → C

✓

AB is Super key

B → D

✗

B is proper subset of Ck

D → E

✓

Both are non primes

AE → F

✓

AE is not SK

C → A



Topic: Highest NF

- For the before example

R(ABCDE) and FD's {AB → C, B → D, D → E, AE → F, C → A}

~~2NF~~

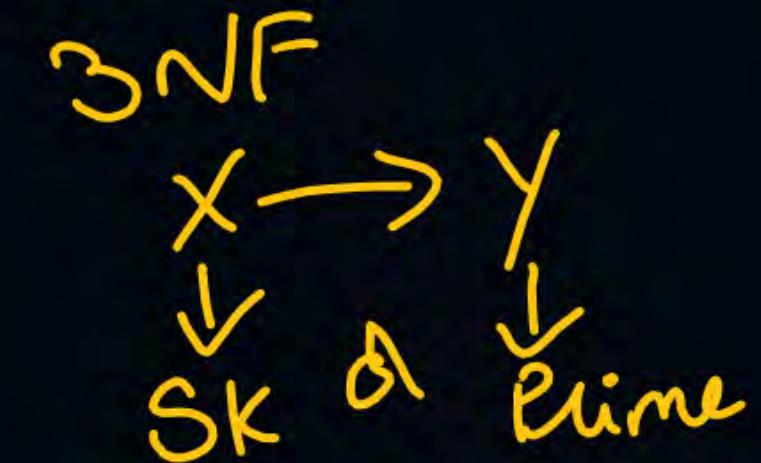
AB → C	✓	AB is Super key
B → D	✗	B is proper subset of CK
D → E	✓	Both are non primes
AE → F	✓	AE is not SK
C → A	✓	Proper Subset of CK → proper subset of another CK



Topic: Highest NF

- For the before example

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$



AB and BC are
CKs

	2NF	3NF	
<u>$AB \rightarrow C$</u>	✓	✓	<u>AB is Super key</u>
$B \rightarrow D$	✗		
$D \rightarrow E$	✓		
$AE \rightarrow F$	✓		
$C \rightarrow A$	✓		



Topic: Highest NF

- For the before example

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$

	2NF	3NF	
$AB \rightarrow C$	✓	✓	AB is Super key
<u>$B \rightarrow D$</u>	✗	✗	<u>B is proper subset of Ck,</u> not in 2NF, so not in 3NF
$D \rightarrow E$	✓		
$AE \rightarrow F$	✓		
$C \rightarrow A$	✓		



Topic: Highest NF

- For the before example

AB and BC are
CKs

$R(ABCDE)$ and FD's $\{AB \rightarrow C, B \rightarrow D, D \rightarrow E, AE \rightarrow F, C \rightarrow A\}$

	2NF	3NF	
$AB \rightarrow C$	✓	✓	AB is Super key
$B \rightarrow D$	✗	✗	B is proper subset of Ck
<u>$D \rightarrow E$</u>	✓	✗	<u>D is not Sk and E is not prime</u>
<u>$AE \rightarrow F$</u>	✓		
$C \rightarrow A$	✓		



Topic: Highest NF

- For the before example

AB and BC are
CKs

R(ABCDE) and FD's {AB → C, B → D, D → E, AE → F, C → A}

	2NF	3NF	
AB → C	✓	✓	AB is Super key
B → D	✗	✗	B is proper subset of Ck
D → E	✓	✗	D is not Sk and E is not prime
AE → F	✓	✗	AE is not Sk and F is not prime
C → A	✓		



Topic: Highest NF

- For the before example

R(ABCDE) and FD's { $AB \rightarrow C$, $B \rightarrow D$, $D \rightarrow E$, $AE \rightarrow F$, $C \rightarrow A$ }

AB and BC are
CKs

	2NF	3NF	
$AB \rightarrow C$	✓	✓ ✓	AB is Super key
$B \rightarrow D$	✗	✗	B is propersubset of Ck
$D \rightarrow E$	✓	✗	D is not Sk and E is not prime
$AE \rightarrow F$	✓	✗ ✓	AE is not Sk and F is not prime
$C \rightarrow A$ prime	✓	✗ ✓	Proper Subset of Ck → Proper Subset of Ck



Topic: Highest NF

- For the before example

R(ABCDE) and FD's { $AB \rightarrow C$, $B \rightarrow D$, $D \rightarrow E$, $AE \rightarrow F$, $C \rightarrow A$ }

	2NF	3NF	I^NF	AB and BC are CKs
$\checkmark \underline{AB} \rightarrow C$	✓	✓		AB is Super key
B → D	✗ ✗	✗ ✗		B is propersubset of Ck
D → E	✓	✗ ✗		D is not Sk and E is not prime
AE → F	✓	✗ ✗		AE is not Sk and F is not prime
C → A	✓	✓	Proper → Proper	Subset of Ck Subset of Ck

- All 4 FDs are not allowed in BCNF, because none of the determinant are Skeys.

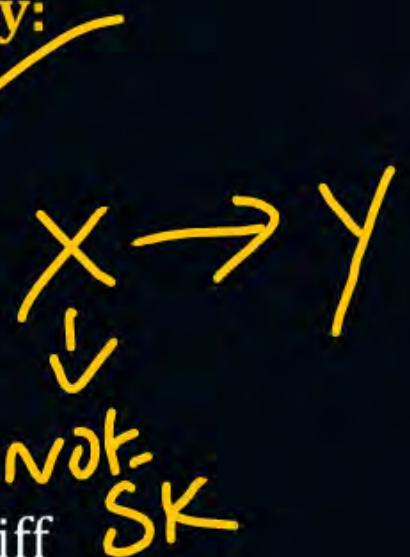


Topic: Highest NF

Recalling the points to remember about Redundancy:

(i) $X \rightarrow Y$ FD of Relation R forms redundancy iff

- $X \rightarrow Y$ is Non-trivial FD
and
- X is not Super Key of R



(ii) $X \rightarrow Y$ FD of Relation R doesn't form redundancy iff

- $X \rightarrow Y$ is a trivial FD ($X \supseteq Y$)
or
- X is Super Key of R



Topic: Highest NF

Recalling the points to remember about Redundancy:

(i) $X \rightarrow Y$ FD of Relation R forms redundancy iff

- $X \rightarrow Y$ is Non-trivial FD

and

- X is not Super Key of R

(ii) $X \rightarrow Y$ FD of Relation R doesn't form redundancy iff

- $X \rightarrow Y$ is a trivial FD ($X \supseteq Y$)

or

- X is Super Key of R

Redundancy Rules

(i) is not allowed in BCNF

(ii) is allowed



Topic: Highest NF

Summary: For a non trivial FD $X \rightarrow Y$ to be in XNF, it is as follows:

1NF No Multivalued allowed

2NF X should not be a part of Ckey AND

Y should not be a Non-Prime Attribute

i.e., $X \rightarrow Y$ should **not** be a partial dependency

3NF X should be a Super key OR

Y should be a prime attribute

BCNF X should be a Super key



Topic: Highest NF

Summary: For a non trivial FD $X \rightarrow Y$ to be in XNF, it is as follows:

1NF No Multivalued allowed

2NF No PD or (Proper subset of CK)⁺ = only prime attributes

3NF X should be a Super key OR

Y should be a prime attribute

BCNF X should be a Super key

Inspiring Stories : Rani Abbakka Chowta



Background: Queen of a port town on the Arabian Sea (1500s).

Struggles: Portuguese fleets wanted her coast and trade.

Achievements: Beat back multiple naval attacks; formed sea-side alliances; jailed only after years of war.

Impact: Coastal icon, proof that a small port can resist an empire.



Topic: Important Question Asked in GATE



#Q. Find the highest NF given a Relation R and its Functional Dependencies.



Topic: Important Question Asked in GATE



#Q. Find the highest NF given a Relation R and its Functional Dependencies.

Sol.: Step 1: Find all Candidate keys (because we need to find the prime attributes further)



Topic: Important Question Asked in GATE



#Q. Find the highest NF given a Relation R and its Functional Dependencies.

Sol.: Step 1: Find all Candidate keys (because we need to find the prime attributes further)

Step 2: Find the highest NF.



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) {ABD → C, BC → D, CD → E}, Find the highest NF.



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol: Finding Ckeys:

AB should be part of Ck because they are not derived in any FD.



Topic: Examples on Finding Highest NF

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$$\underline{\underline{ABC}}^+ = \underline{\underline{ABCDE}}$$

No proper subset of ABC forms CK.: ABC is CK



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol: Finding Ckeys:

AB should be part of CK because they are not derived in any FD.

$$ABC^+ = ABCDE$$

No proper subset of ABC forms CK. ∴ ABC is CK

Check for prime attr on right side of the FDs

From $ABD \rightarrow C$

Replace C with ABD



Topic: Examples on Finding Highest NF

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Check for prime attr on right side of the FDs

From $ABD \rightarrow C$

Replace C with ABD

$$\underline{ABC} = AB (ABD)$$

$$= ABD^+ = ABDCE$$



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol: Finding Ckeys:

AB should be part of CK because they are not derived in any FD.

$$ABC^+ = ABCDE$$

No proper subset of ABC forms CK. \therefore ABC is CK

Check for prime attr on right side of the FDs

From $ABD \rightarrow C$

Replace C with ABD

$$ABC = AB(ABD)$$

$$= ABD^+ = ABDCE$$

No proper subset of ABD forms CK, \therefore ABD is also a CK.



Topic: Examples on Finding Highest NF



Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol Cont: ∵ ABD , ABC are Candidate keys.

∴ The prime attributes are ABCD, Non Prime attr is E. So no other Cks possible

A B C D



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol Cont: ∵ \underline{ABD} , \underline{ABC} are Candidate keys.

∴ The prime attributes are ABCD, Non Prime attr is E.

Checking highest NF for all FDs from the highest to lowest NF.

$\checkmark ABD \rightarrow C$	Sk	Prime Attribute	$\checkmark BC \rightarrow D$	Partial Sk	Partial Sk	$\checkmark CD \rightarrow E$	Partial Sk	Non Prime
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Topic: Examples on Finding Highest NF

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Sol Cont: ∵ ABD, ABC are Candidate keys.

∴ The prime attributes are ABCD, Non Prime attr is E.

Checking highest NF for all FDs from the highest to lowest NF.

$\underline{ABD} \rightarrow C$	Sk Prime Attribute	$\underline{BC} \rightarrow D$	Partial Sk	$\underline{CD} \rightarrow E$	Partial Sk
BCNF	✓		✗		✗



Topic: Examples on Finding Highest NF



Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol Cont: ∵ \overline{ABD} , \overline{ABC} are Candidate keys.

∴ The prime attributes are ABCD, Non Prime attr is E.

Checking highest NF for all FDs from the highest to lowest NF.

$X \rightarrow Y$
SK δ Prime

BCNF

3NF

$ABD \rightarrow C$	$BC \rightarrow D$	$CD \rightarrow E$
Sk <u>Prime Attribute</u>	Partial Sk Partial Sk	Partial Sk Non Prime
✓	✗	✗



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol Cont: ∵ ABD, ABC are Candidate keys.

∴ The prime attributes are ABCD, Non Prime attr is E.

Checking highest NF for all FDs from the highest to lowest NF.

$ABD \rightarrow C$		$BC \rightarrow D$		$CD \rightarrow E$	
Sk	Prime Attribute	Partial Sk	Partial Sk	Partial Sk	Non Prime
BCNF	✓		✗		✗
3NF	✓		✓		✗



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol Cont:

- For 2NF, check if all proper Subsets of C_k closure \rightarrow only prime attribute



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) {ABD → C, BC → D, CD → E}, Find the highest NF.

Sol Cont:

- For 2NF, check if all proper Subsets of Ck closure → only prime attribute

$$\underline{\underline{ABD}} \Rightarrow \underline{\underline{A^+}} = \underline{\underline{A}}, \underline{\underline{B^+}} = \underline{\underline{B}}, \underline{\underline{D^+}} = \underline{\underline{D}}, \underline{\underline{AB^+}} = \underline{\underline{AB}}, \underline{\underline{BD^+}} = \underline{\underline{BD}}, \underline{\underline{AD^+}} = \underline{\underline{AD}}$$

Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) {ABD \rightarrow C, BC \rightarrow D, CD \rightarrow E}, Find the highest NF.

Sol Cont:

- For 2NF, check if all proper Subsets of Ck closure \rightarrow only prime attribute

$$ABD \Rightarrow A^+ = A, B^+ = B, D^+ = D, AB^+ = AB, BD^+ = BD, AD^+ = AD$$

$$\underline{ABC} \Rightarrow \underline{A}^+ = A, \underline{B}^+ = B, \underline{C}^+ = C, \underline{AC}^+ = AC, \underline{BC}^+ = BCDE, \underline{AB}^+ = AB$$

$$\begin{array}{c} \downarrow \\ \underline{BC} \rightarrow \underline{E} \end{array}$$



Topic: Examples on Finding Highest NF

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Sol Cont:

- For 2NF, check if all proper Subsets of Ck closure → only prime attribute

$$ABD \Rightarrow A^+ = A, B^+ = B, D^+ = D, AB^+ = AB, BD^+ = BD, AD^+ = AD$$

$$ABC \Rightarrow A^+ = A, B^+ = B, C^+ = C, AC^+ = AC, BC^+ = BCDE, AB^+ = AB$$

Here, $BC^+ = BCDE$



Topic: Examples on Finding Highest NF

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Here, $BC^+ = BCDE$

E is a Non prime attribute



Topic: Examples on Finding Highest NF

Ex1: R (ABCDE) { $ABD \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$ }, Find the highest NF.

Sol Cont:

- For 2NF, check if all proper Subsets of C_k closure \rightarrow only prime attribute

$$ABD \Rightarrow A^+ = A, B^+ = B, D^+ = D, AB^+ = AB, BD^+ = BD, AD^+ = AD$$

$$ABC \Rightarrow A^+ = A, B^+ = B, C^+ = C, AC^+ = AC, BC^+ = BCDE, AB^+ = AB$$

Here, $BC^+ = BCDE$

E is a Non prime attribute

- The Relation is not in 2NF.

The Relation's highest NF is 1NF



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs {AB → C, BC → D}, what is the highest NF?



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol: Finding the Ckeys: ✓

AB should be part of Ck because its is not derived.



Topic: Examples on Finding Highest NF



Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol: Finding the Ckeys:

AB should be part of Ck because its is not derived.

$$AB^+ = ABCD$$

AB is CK since no proper subsets of AB are CKs

No other Ckeys are possible



Topic: Examples on Finding Highest NF



Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

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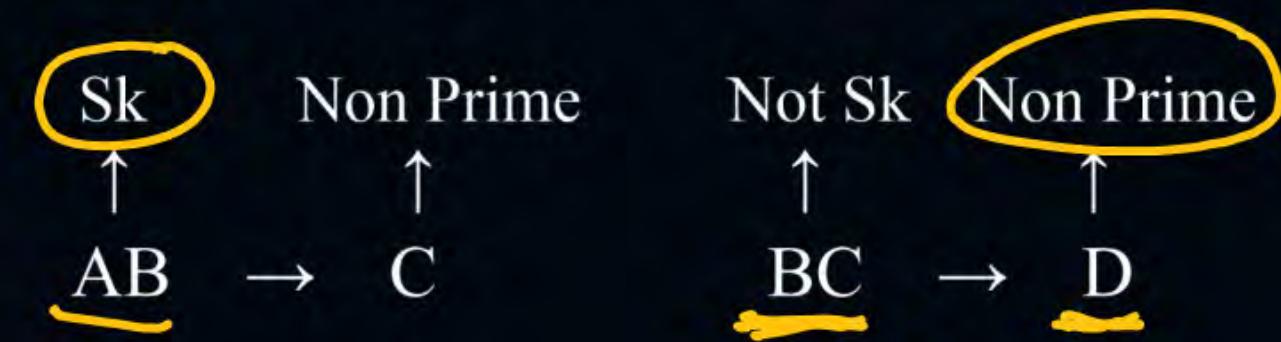
Now lets check for the highest NF



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

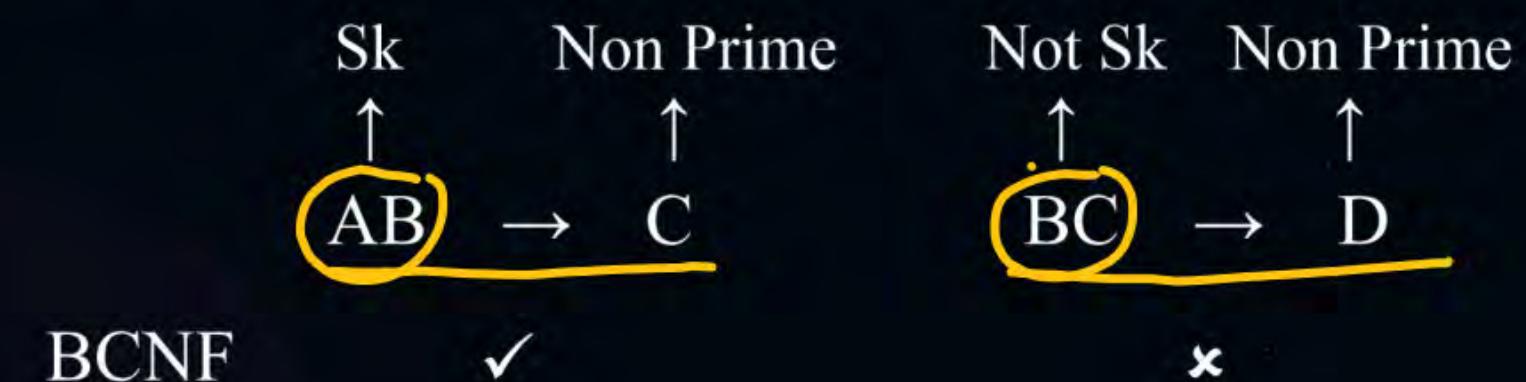
Sol Cont.:



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol Cont.:



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol Cont.:

	Sk	Non Prime	Not Sk	Non Prime
$AB \rightarrow C$	↑ <u>AB</u>	↑ C	↑ <u>BC</u>	↑ <u>D</u>
BCNF	✓		✗	
3NF	✓		✗ ✓	



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol Cont.:

	Sk	Non Prime	Not Sk	Non Prime
	↑	↑	↑	↑
	AB	\rightarrow	C	BC
BCNF		✓		✗
3NF		✓		✗

AB

Now checking for 2NF



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol Cont.:

	Sk	Non Prime	Not Sk	Non Prime
	↑	↑	↑	↑
	AB	\rightarrow	BC	\rightarrow
BCNF		✓		✗
3NF		✓		✗

2NF Test: $\left(\begin{matrix} \text{Proper Subset} \\ \text{of } C_k \end{matrix} \right)^+ \rightarrow \text{Only Prime Attribute}$



Topic: Examples on Finding Highest NF

Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol Cont.:

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	↑	↑	↑	↑
	AB	\rightarrow	BC	\rightarrow
BCNF		✓		✗
3NF		✓		✗

2NF Test: $\left(\begin{array}{c} \text{Proper Subset} \\ \text{of } C_k \end{array} \right)^+ \rightarrow \text{Only Prime Attribute}$

$A^+ = A$, $B^+ = B$ and AB^+ is not a proper subset of AB .



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Ex2: R (ABCD) and FDs $\{AB \rightarrow C, BC \rightarrow D\}$, what is the highest NF?

Sol Cont.:

	Sk	Non Prime	Not Sk	Non Prime
	↑	↑	↑	↑
	AB	\rightarrow	BC	\rightarrow
BCNF		✓		✗
3NF		✓		✗

2NF Test: $\left(\begin{array}{c} \text{Proper Subset} \\ \text{of } C_k \end{array} \right)^+ \rightarrow \text{Only Prime Attribute}$

$A^+ = \underline{A}$, $B^+ = \underline{B}$ and AB^+ is not a proper subset of AB.

∴ The Relation's highest NF is 2NF.



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are { $AB \rightarrow C$, $C \rightarrow A$, $AC \rightarrow D$ }, Find highest NF.



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are { $AB \rightarrow \underline{C}$, $C \rightarrow \underline{A}$, $AC \rightarrow \underline{D}$ }, Find highest NF.

Sol: CKs of relation contains B.

$$\underline{AB}^+ = \underline{\underline{ABCD}}$$



Topic: Examples on Finding Highest NF



Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol: CKs of relation contains B.

$AB^+ = ABCD$ For $AB \Rightarrow A^+ = A, B^+ = B$

$\therefore \underline{\text{AB is CK}}$



Topic: Examples on Finding Highest NF



Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol: CKs of relation contains B.

$$AB^+ = ABCD \text{ For } AB \Rightarrow A^+ = A, B^+ = B$$

$\therefore AB$ is CK

(from C \rightarrow A)



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol: CKs of relation contains B.

$$AB^+ = ABCD \text{ For } AB \Rightarrow A^+ = A, B^+ = B$$

$\therefore AB$ is CK

$$(\text{from } C \rightarrow A) \quad \underline{CB}^+ = ABCD$$



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol: CKs of relation contains B.

$AB^+ = ABCD$ For $AB \Rightarrow A^+ = A, B^+ = B$

$\therefore AB$ is CK

(from $C \rightarrow A$) $CB^+ = ABCD$ For $CB \Rightarrow C^+ = AC, B^+ = B$

$\therefore CB$ is CK



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol: CKs of relation contains B.

$AB^+ = ABCD$ For $AB \Rightarrow A^+ = A, B^+ = B$

$\therefore AB$ is CK

(from $C \rightarrow A$) $CB^+ = ABCD$ For $CB \Rightarrow C^+ = AC, B^+ = B$

$\therefore CB$ is CK

$DB^+ = DB \rightarrow$ Not CK



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol: CKs of relation contains B.

$AB^+ = ABCD$ For $AB \Rightarrow A^+ = A, B^+ = B$

$\therefore AB$ is CK

(from $C \rightarrow A$) $CB^+ = ABCD$ For $CB \Rightarrow C^+ = AC, B^+ = B$

$\therefore CB$ is CK

$DB^+ = DB \rightarrow$ Not CK

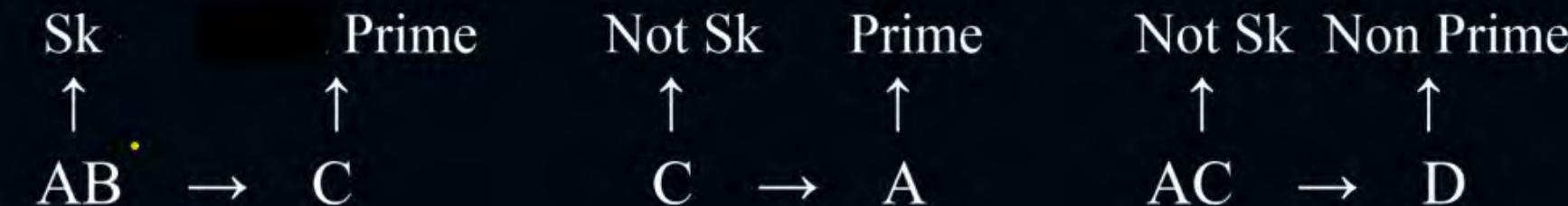
$\therefore \underline{AB}$ and \underline{BC} are possible CKs



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol Cont.:



AB and BC are CKs

Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol Cont.:

Sk	Prime	Not Sk	Prime	Not Sk	Non Prime
$\overbrace{AB}^{\uparrow}$	\overbrace{C}^{\uparrow}	\overbrace{C}^{\uparrow}	\overbrace{A}^{\uparrow}	$\overbrace{AC}^{\uparrow}$	\overbrace{D}^{\uparrow}
BCNF	✓	✗	✗	✗	✗

AB and BC are CKs



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol Cont.:

	Sk ↑	Prime ↑	Not Sk ↑	Prime ↑	Not Sk ↑	Non Prime ↑
AB \rightarrow C			C	\rightarrow A	<u>AC</u>	<u>D</u>
BCNF	✓		x		x	
3NF	✓		✓ (A is prime)		x	

AB and BC are CKs



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol Cont.:

	Sk ↑	Prime ↑	Not Sk ↑	Prime ↑	Not Sk ↑	Non Prime ↑
AB \rightarrow C			C	\rightarrow A	AC	\rightarrow D
BCNF	✓			✗		✗
3NF	✓			✓ (A is prime)		✗

AB and BC are CKs

2NF Test: $\left(\begin{matrix} \text{Proper Subset} \\ \text{of Ck} \end{matrix} \right)^+ \rightarrow \text{Prime Attribute}$



Topic: Examples on Finding Highest NF

Ex3: R (ABCD), FDs are $\{AB \rightarrow C, C \rightarrow A, AC \rightarrow D\}$, Find highest NF.

Sol Cont.:

	Sk ↑	Prime ↑	Not Sk ↑	Prime ↑	Not Sk ↑	Non Prime ↑
AB \rightarrow C			C	\rightarrow A	AC	\rightarrow D
BCNF	✓			✗		✗
3NF	✓			✓ (A is prime)		✗

AB and BC are CKs

2NF Test: $\left(\begin{array}{l} \text{Proper Subset} \\ \text{of Ck} \end{array} \right)^+ \rightarrow \text{Prime Attribute}$

For AB, $\Rightarrow \underline{A}^+ = \underline{A}$, $\underline{B}^+ = \underline{B}$

For BC, $\Rightarrow B^+ = \underline{B}$, $C^+ = \underline{AC}$



Topic: Examples on Finding Highest NF

$$C^+ = CAD \quad C \rightarrow D \checkmark$$

Ex3: R (ABCD), FDs are {AB → C, C → A, AC → D}, Find highest NF.

Sol Cont.:

Sk ↑	Prime ↑	Not Sk ↑	Prime ↑	Not Sk ↑	Non Prime ↑
AB	→ C	C	→ A	AC	→ D

BCNF

✓

✗

✗

AB and BC are CKs

3NF

✓

✓ (A is prime)

✗

1NF

2NF Test: $\left(\begin{array}{c} \text{Proper Subset} \\ \text{of Ck} \end{array} \right)^+ \rightarrow \text{Prime Attribute}$

For AB, $\Rightarrow A^+ = \underline{A}, B^+ = \underline{B}$

2NF

$C \rightarrow A$
↓
prime

For BC, $\Rightarrow B^+ = \underline{B}, C^+ = \underline{ACD}$

None of them derive Non-prime Attributes \therefore Relation's highest NF is 2NF.

Inspiring Stories : D. Bisoi & C. Bisoi



Background: Kandha tribal leaders from Ganjam.

Struggles: British rule and forest control hit tribes hard.

Achievements: kept resistance alive across hills.

Impact: Stand for tribal rights in coastal-hill Odisha history.



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The Ck has to have A as its part.



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = \underline{\text{ABCDEF}}$ No proper subsets are CKs, so \underline{AB} is CK



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = ABCDEF$ No proper subsets are CKs, so **AB** is CK

(from F \rightarrow B)



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = ABCDEF$ No proper subsets are CKs, so **AB is CK**

(from $F \rightarrow B$) $AF^+ = AFBCDE$ No proper subsets are CKs, so **AF is CK**



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = ABCDEF$ No proper subsets are CKs, so AB is CK

(from $F \rightarrow B$) $AF^+ = AFBCDE$ No proper subsets are CKs, so AF is CK

(from E \rightarrow F)



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = ABCDEF$ No proper subsets are CKs, so **AB** is CK

(from $F \rightarrow B$) $AF^+ = AFBCDE$ No proper subsets are CKs, so **AF** is CK

(from $E \rightarrow F$) $AE^+ = AEFBCD$ No proper subsets are CKs, so **AE** is CK



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = ABCDEF$ No proper subsets are CKs, so **AB** is CK

(from $F \rightarrow B$) $AF^+ = AFBCDE$ No proper subsets are CKs, so **AF** is CK

(from $E \rightarrow F$) $AE^+ = AEFBCD$ No proper subsets are CKs, so **AE** is CK

Checking for $AC^+ = ACDEFB$ No proper subsets are CKs, so **AC** is CK



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = ABCDEF$ No proper subsets are CKs, so AB is CK

(from $F \rightarrow B$) $AF^+ = AFBCDE$ No proper subsets are CKs, so AF is CK

(from $E \rightarrow F$) $AE^+ = AEFBCD$ No proper subsets are CKs, so AE is CK

Checking for $AC^+ = ACDEFB$ No proper subsets are CKs, so AC is CK

Checking for $AD^+ = AD$ → Not a CK



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol: The CK has to have A as its part.

$AB^+ = ABCDEF$ No proper subsets are CKs, so AB is CK

(from $F \rightarrow B$) $AF^+ = AFBCDE$ No proper subsets are CKs, so AF is CK

(from $E \rightarrow F$) $AE^+ = AEFBCD$ No proper subsets are CKs, so AE is CK

Checking for $AC^+ = ACDEFB$ No proper subsets are CKs, so AC is CK

Checking for $AD^+ = AD$ → Not a CK

No other possibilities



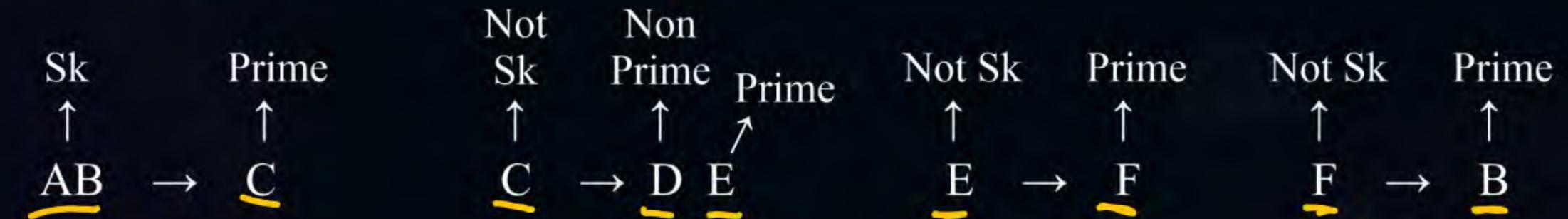
Topic: Examples on Finding Highest NF



Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF. AB AF, AE, AC are CKs $A B C E F$

Sol Cont.: Lets check for Highest NF





Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF. AB AF, AE, AC are CKs

Sol Cont.: Lets check for Highest NF

	Sk	Prime	Not Sk	Non Prime	Not Sk	Prime	Not Sk	Prime
	↑	↑	↑	↑	↑	↑	↑	↑
	AB	C	C	D	E	E	F	B
BCNF	✓	*	*	*	*	*	*	*

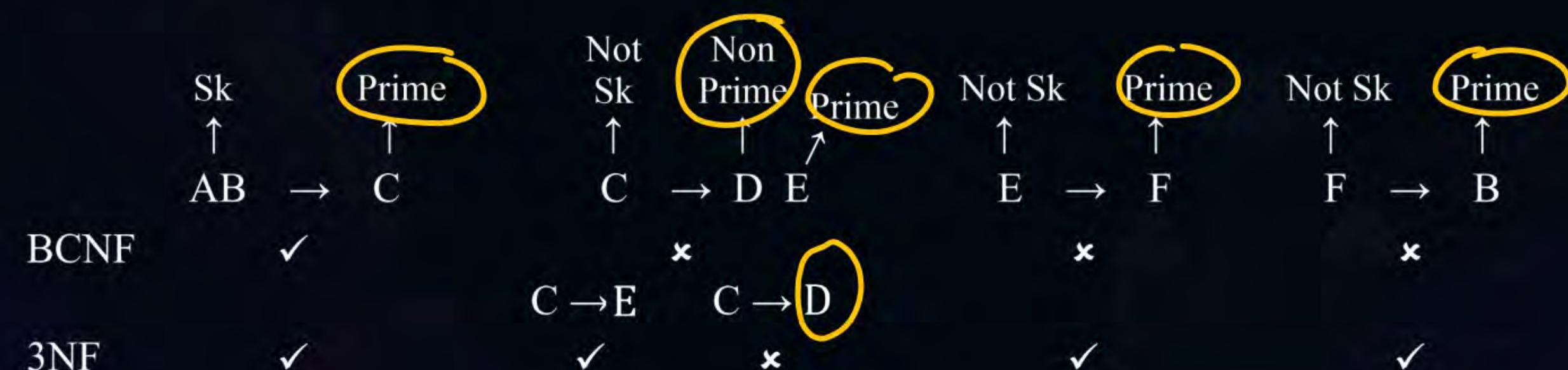


Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF. AB AF, AE, AC are CKs

Sol Cont.: Lets check for Highest NF





Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol Cont.:

2NF Test:
$$\left(\begin{array}{c} \text{Proper Subset} \\ \text{of } C_k \end{array} \right)^+ \rightarrow \text{Prime Attribute}$$



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol Cont.:

2NF Test: $\left(\begin{array}{c} \text{Proper Subset} \\ \text{of } C_k \end{array} \right)^+ \rightarrow \text{Prime Attribute}$

For AB, $A^+ = A, B^+ = B$

For AC, $A^+ = A, C^+ = CDE$

For AE, $A^+ = A, E^+ = EF$

For AF, $A^+ = A, F^+ = FB$



Topic: Examples on Finding Highest NF

Ex4: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow DE, E \rightarrow F, F \rightarrow B\}$

Find highest NF.

Sol Cont.:

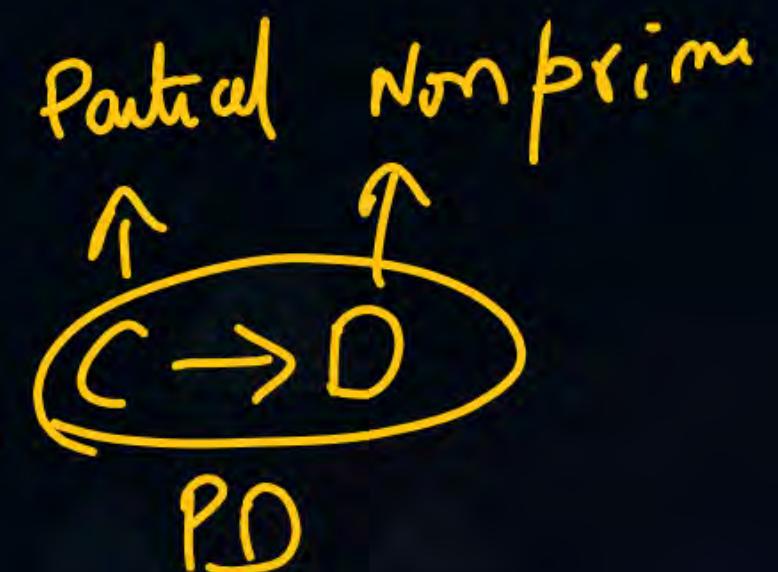
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For AF, $A^+ = A, F^+ = FB$



$C \rightarrow D$, where D is Non-Prime Attribute



Topic: Examples on Finding Highest NF

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Find highest NF.

Sol Cont.:

2NF Test: $\left(\begin{array}{c} \text{Proper Subset} \\ \text{of } C_k \end{array} \right)^+ \rightarrow \text{Prime Attribute}$

For AB, $A^+ = A, B^+ = B$

For AC, $A^+ = A, C^+ = CDE$

For AE, $A^+ = A, E^+ = EF$

For AF, $A^+ = A, F^+ = FB$

$C \rightarrow D$, where D is Non-Prime Attribute

- The relation is not in 2NF ✓
- The highest NF is 1NF ✓



Topic: Examples on Finding Highest NF

Ex5: R (ABCDEF) and FD's are { $AB \rightarrow C$, $C \rightarrow D$, $CD \rightarrow AE$, $DE \rightarrow F$, $EF \rightarrow B$ }

What is highest NF?



Topic: Examples on Finding Highest NF

Ex5: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow D, CD \rightarrow AE, DE \rightarrow F, EF \rightarrow B\}$

What is highest NF?

Sol: Already solved in examples of CKs, the CK's are $\overbrace{AB, AEF, ADE, C}^{ABCDEF}$

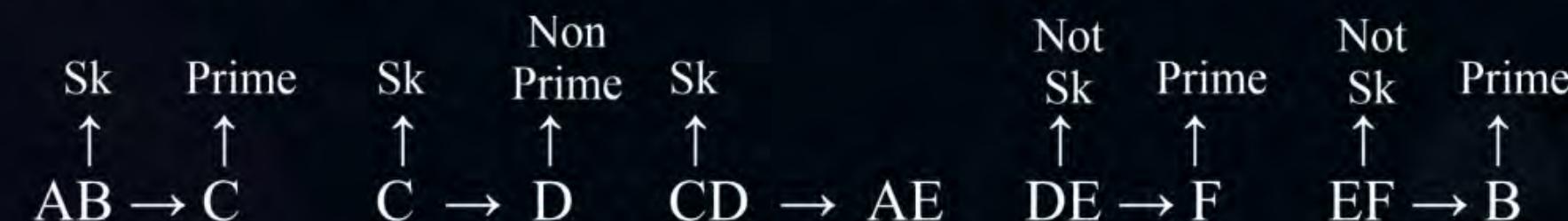


Topic: Examples on Finding Highest NF

Ex5: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow D, CD \rightarrow AE, DE \rightarrow F, EF \rightarrow B\}$

What is highest NF?

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Topic: Examples on Finding Highest NF

Ex5: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow D, CD \rightarrow AE, DE \rightarrow F, EF \rightarrow B\}$

What is highest NF?

Sol: Already solved in examples of CKs, the CK's are AB, AEF, ADE, C

Sk	Prime	Sk	Non Prime	Sk	Not Sk	Prime	Not Sk	Prime
$AB \rightarrow C$		$C \rightarrow D$		$CD \rightarrow AE$		$DE \rightarrow F$		$EF \rightarrow B$
BCNF	✓		✓	✓		✗		✗



Topic: Examples on Finding Highest NF

Ex5: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow D, CD \rightarrow AE, DE \rightarrow F, EF \rightarrow B\}$

What is highest NF?

Sol: Already solved in examples of CKs, the CK's are AB, AEF, ADE, C, CD

	Sk \uparrow $AB \rightarrow C$	Prime \uparrow $C \rightarrow D$	Non Prime \uparrow $CD \rightarrow AE$	Sk \uparrow $DE \rightarrow F$	Not Sk \uparrow $EF \rightarrow B$
BCNF	✓	✓	✓	✗	✗
3NF	✓	✓	✓	✓	✓



Topic: Examples on Finding Highest NF

Ex5: R (ABCDEF) and FD's are $\{AB \rightarrow C, C \rightarrow D, CD \rightarrow AE, DE \rightarrow F, EF \rightarrow B\}$

What is highest NF?

Sol: Already solved in examples of CKs, the CK's are AB, AEF, ADE, C

	Sk	Prime	Sk	Non Prime	Sk	Not Sk	Prime	Not Sk	Prime
	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow
AB \rightarrow C	✓		C \rightarrow D	✓		CD \rightarrow AE	✓	DE \rightarrow F	✗
BCNF									✗
3NF	✓			✓		✓	✓	✓	

The highest NF is 3NF. All Attributes are Prime.

Hence, 3NF never fails for such cases, but the relation may not be in BCNF.



Topic: Examples on Finding Highest NF

Ex6: R (ABCDE) and FD's are $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

What is highest NF?



Topic: Examples on Finding Highest NF

Ex6: R (ABCDE) and FD's are $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

What is highest NF?

Sol: CKs are AE, DE, CE, BE. A B C D E



Topic: Examples on Finding Highest NF

Ex6: R (ABCDE) and FD's are $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

What is highest NF?

Sol: CKs are AE, DE, CE, BE.

All are prime attr so, the relation is in 3NF



Topic: Examples on Finding Highest NF

Ex6: R (ABCDE) and FD's are $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

What is highest NF?

Sol: CKs are AE, DE, CE, BE.

All are prime attr so, the relation is in 3NF

let's check

| Not Sk | Prime |
|------------|------------|------------|------------|------------|------------|------------|------------|
| \uparrow |

$A \rightarrow B$ $B \rightarrow C$ $C \rightarrow D$ $D \rightarrow A$



Topic: Examples on Finding Highest NF

Ex6: R (ABCDE) and FD's are $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

What is highest NF?

Sol: CKs are AE, DE, CE, BE.

All are prime attr so, the relation is in 3NF

let's check

	Not Sk	Prime	Not Sk	Prime	Not . Sk	Prime	Not Sk	Prime
BCNF	$A \rightarrow B$	x	$B \rightarrow C$	x	$C \rightarrow D$	x	$D \rightarrow A$	x



Topic: Examples on Finding Highest NF

Ex6: R (ABCDE) and FD's are $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

What is highest NF?

Sol: CKs are AE, DE, CE, BE.

All are prime attr so, the relation is in 3NF

let's check

	Not Sk	Prime	Not Sk	Prime	Not Sk	Prime	Not Sk	Prime
$A \rightarrow B$	↑	↑	$B \rightarrow C$	↑	↑	$C \rightarrow D$	↑	↑
BCNF	✗		✗		✗		✗	
3NF		✓		✓		✓		✓



Topic: Examples on Finding Highest NF

Ex6: R (ABCDE) and FD's are $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A\}$

What is highest NF?

Sol: CKs are AE, DE, CE, BE.

All are prime attr so, the relation is in 3NF

let's check

	Not Sk	Prime	Not Sk	Prime	Not Sk	Prime	Not Sk	Prime
$A \rightarrow B$	↑	↑	$B \rightarrow C$	↑	↑	$C \rightarrow D$	↑	↑
BCNF	x		x		x		x	
3NF		✓		✓		✓		✓

Therefore the highest NF is 3NF.



Topic: Examples on Finding Highest NF



Ex7: R (ABCD) and FD's are $\{A \rightarrow B, B \rightarrow AC, C \rightarrow D\}$

What is highest NF?



Topic: Examples on Finding Highest NF

Ex7: R (ABCD) and FD's are $\{A \rightarrow B, B \rightarrow AC, C \rightarrow D\}$

What is highest NF?

Sol: CKs are A, B.

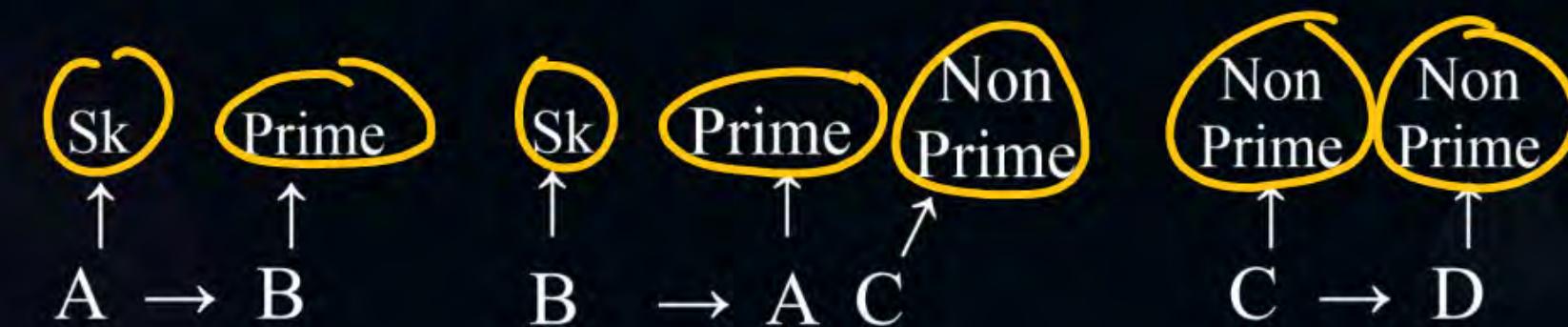


Topic: Examples on Finding Highest NF

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What is highest NF?

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Topic: Examples on Finding Highest NF

Ex7: R (ABCD) and FD's are $\{A \rightarrow B, B \rightarrow AC, C \rightarrow D\}$

What is highest NF?

Sol: CKs are A, B.

	Sk	Prime	Sk	Prime	Non Prime	Non Prime	Non Prime
A \rightarrow B	↑	↑	B	↑	↑	↑	↑
BCNF	✓		B \rightarrow A	✓	B \rightarrow C	✓	✗



Topic: Examples on Finding Highest NF

Ex7: R (ABCD) and FD's are $\{A \rightarrow B, B \rightarrow AC, C \rightarrow D\}$

What is highest NF?

Sol: CKs are A, B.

	Sk	Prime	Sk	Prime	Non Prime	Non Prime	Non Prime
	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow	\uparrow
	$A \rightarrow B$		$B \rightarrow A$	$B \rightarrow C$		$C \rightarrow D$	
BCNF		✓		✓	✓		✗
3NF	✓		✓		✓	✗	✓



Topic: Examples on Finding Highest NF

Ex7: R (ABCD) and FD's are $\{A \rightarrow B, B \rightarrow AC, C \rightarrow D\}$

What is highest NF?

A, B

A, B

Sol Cont.:

2NF Test: $\left(\begin{array}{c} \text{Proper Subset} \\ \text{of } C_k \end{array} \right)^+ \rightarrow \text{Prime Attribute}$

- No proper subsets possible for simple attribute.

The relation highest NF is 2NF.



Topic: Examples on Finding Highest NF



Ex7: R (ABCD) and FD's are $\{A \rightarrow B, B \rightarrow AC, C \rightarrow D\}$

What is highest NF?

Sol Cont.:

2NF Test: $\left(\begin{array}{c} \text{Proper Subset} \\ \text{of Ck} \end{array} \right)^+ \rightarrow \text{Prime Attribute}$

- No proper subsets possible for simple attribute.

The relation highest NF is 2NF.

- If all Ckeys of the relation are simple Ckeys then the relation is always in 2NF,
may or may not be in 3NF and BCNF.



Topic: Highest NF Decomposition

P
W



#Q. Relational Schema R with no Non Trivial FD's what is the highest NF of R(ABC)?



Topic: Highest NF Decomposition

#Q. Relational Schema R with no Non Trivial FD's what is the highest NF of R(ABC)?

Sol: If no non-trivial FD's are present, then

CKey = ABC



Topic: Highest NF Decomposition



#Q. Relational Schema R with no Non Trivial FD's what is the highest NF of R(ABC)?

Sol: If no non-trivial FD's are present, then

CKey = ABC



- If there are no Non trivial FD's No Redundancy over FD's of R.



Topic: Highest NF Decomposition



#Q. Relational Schema R with no Non Trivial FD's what is the highest NF of R(ABC)?

Sol: If no non-trivial FD's are present, then

$$\text{CKey} = \text{ABC}$$

- If there are no Non trivial FD's No Redundancy over FD's of R.

{No Non Trivial FD's in R} \Rightarrow {No Redundancy over FD's in R}



Topic: Highest NF Decomposition



#Q. Relational Schema R with no Non Trivial FD's what is the highest NF of R(ABC)?

Sol: If no non-trivial FD's are present, then

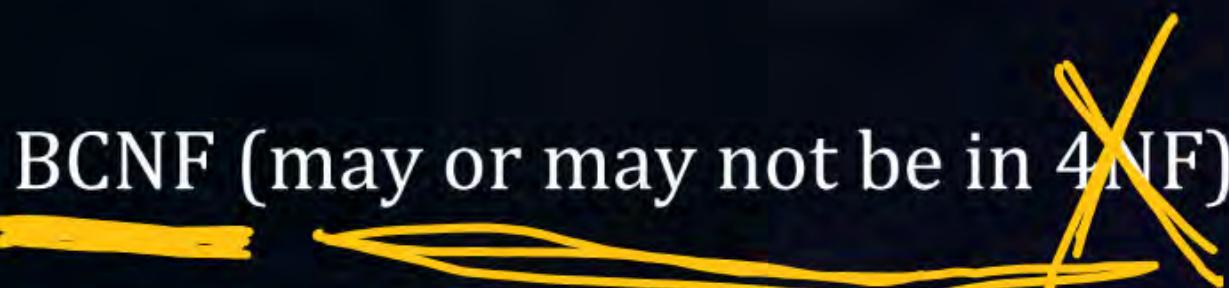
$$C\text{Key} = ABC$$

- If there are no Non trivial FD's No Redundancy over FD's of R.

{No Non Trivial FD's in R} \Rightarrow {No Redundancy over FD's in R}

\Updownarrow

Relation R is in BCNF (may or may not be in 4NF)





Topic: Highest NF Decomposition



#Q. Relational Schema R with no Non Trivial FD's what is the highest NF of R(ABC)?

Sol: If no non-trivial FD's are present, then

$$C\text{Key} = ABC$$

- If there are no Non trivial FD's No Redundancy over FD's of R.

{No Non Trivial FD's in R} \Rightarrow {No Redundancy over FD's in R}

\Updownarrow

Relation R is in BCNF (may or may not be in 4NF)

\therefore The highest NF is BCNF





Topic: Highest NF Decomposition



#Q. Relational Schema R with only two attributes Relation R is always in for R(AB)

A

$\{A \rightarrow B\}$

B

$\{B \rightarrow A\}$

C

$\{A \rightarrow B, B \rightarrow A\}$

P

No Nontrivial FDs



Topic: Highest NF Decomposition

#Q. Relational Schema R with only two attributes Relation R is always in __ for R(AB)

A

$\{A \rightarrow B\}$

B

$\{B \rightarrow A\}$

C

$\{A \rightarrow B, B \rightarrow A\}$

P

No Nontrivial FDs

Sol: (a) CK = A, ∴ in BCNF



Topic: Highest NF Decomposition



#Q. Relational Schema R with only two attributes Relation R is always in __ for R(AB)

A

$\{A \rightarrow B\}$

B

$\{\underline{B \rightarrow A}\}$

C

$\{A \rightarrow B, B \rightarrow A\}$

P

No Nontrivial FDs

Sol: (a) CK = A, \therefore in BCNF

(b) CK = B, in BCNF



Topic: Highest NF Decomposition



#Q. Relational Schema R with only two attributes Relation R is always in __ for R(AB)

A

$\{A \rightarrow B\}$

B

$\{B \rightarrow A\}$

C

$\{\underline{A} \rightarrow B, \underline{B} \rightarrow A\}$

P

No Nontrivial FDs

Sol: (a) CK = A, ∴ in BCNF

(b) CK = B, in BCNF

(c) CK = A, B, also in BCNF



Topic: Highest NF Decomposition



#Q. Relational Schema R with only two attributes Relation R is always in __ for R(AB)

- A $\{A \rightarrow B\}$
- B $\{B \rightarrow A\}$
- C $\{A \rightarrow B, B \rightarrow A\}$
- P No Nontrivial FDs

Sol: (a) CK = A, ∴ in BCNF

(b) CK = B, in BCNF

(c) CK = A and B, also in BCNF

(d) CK = AB, also in BCNF



Topic: Highest NF Decomposition

#Q. Relational Schema R with only two attributes Relation R is always in __ for R(AB)

A

$\{A \rightarrow B\}$

B

$\{B \rightarrow A\}$

C

$\{A \rightarrow B, B \rightarrow A\}$

P

No Nontrivial FDs

Sol: (a) CK = A, ∴ in BCNF

(b) CK = B, in BCNF

(c) CK = A and B, also in BCNF

(d) CK = AB, also in BCNF

⇒ The Relation is also in ~~4NF~~. Because relation with 2 attributes doesn't form any redundancy over FD, or over MVD.



Topic: Highest NF Decomposition

Decomposition of Relation into Higher NF:

⇒ Decompose the Relation into 2NF, 3NF, BCNF with Lossless join & Dependency preserving Decomposition



Topic: Highest NF Decomposition

2NF Decomposition:

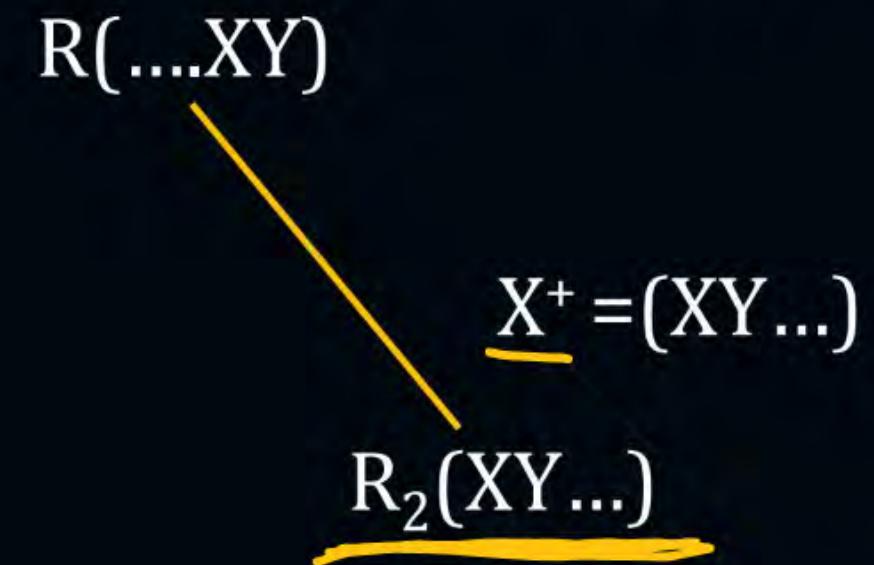
For a Relation $R(\dots XY)$ and FD's are $\{\dots \underline{X} \rightarrow Y\}$ and $\underline{X} \rightarrow Y$ is a partial dependency.



Topic: Highest NF Decomposition

2NF Decomposition:

For a Relation $R(...XY)$ and FD's are $\{...X \rightarrow Y\}$ and $X \rightarrow Y$ is a partial dependency.

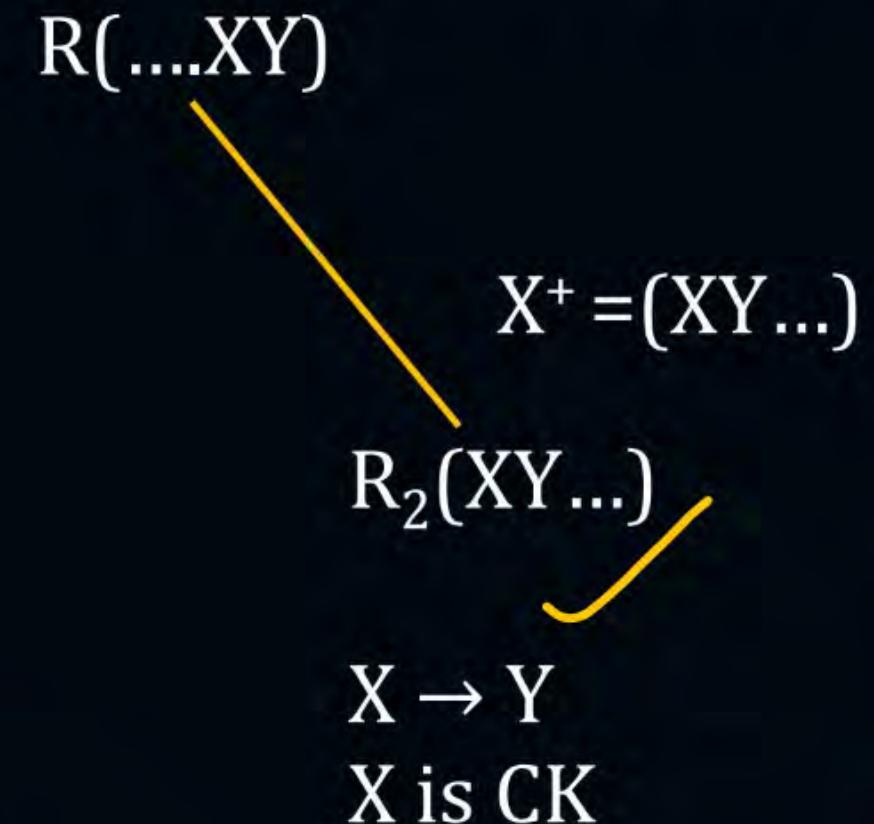




Topic: Highest NF Decomposition

2NF Decomposition:

For a Relation $R(...XY)$ and FD's are $\{...X \rightarrow Y\}$ and $X \rightarrow Y$ is a partial dependency.

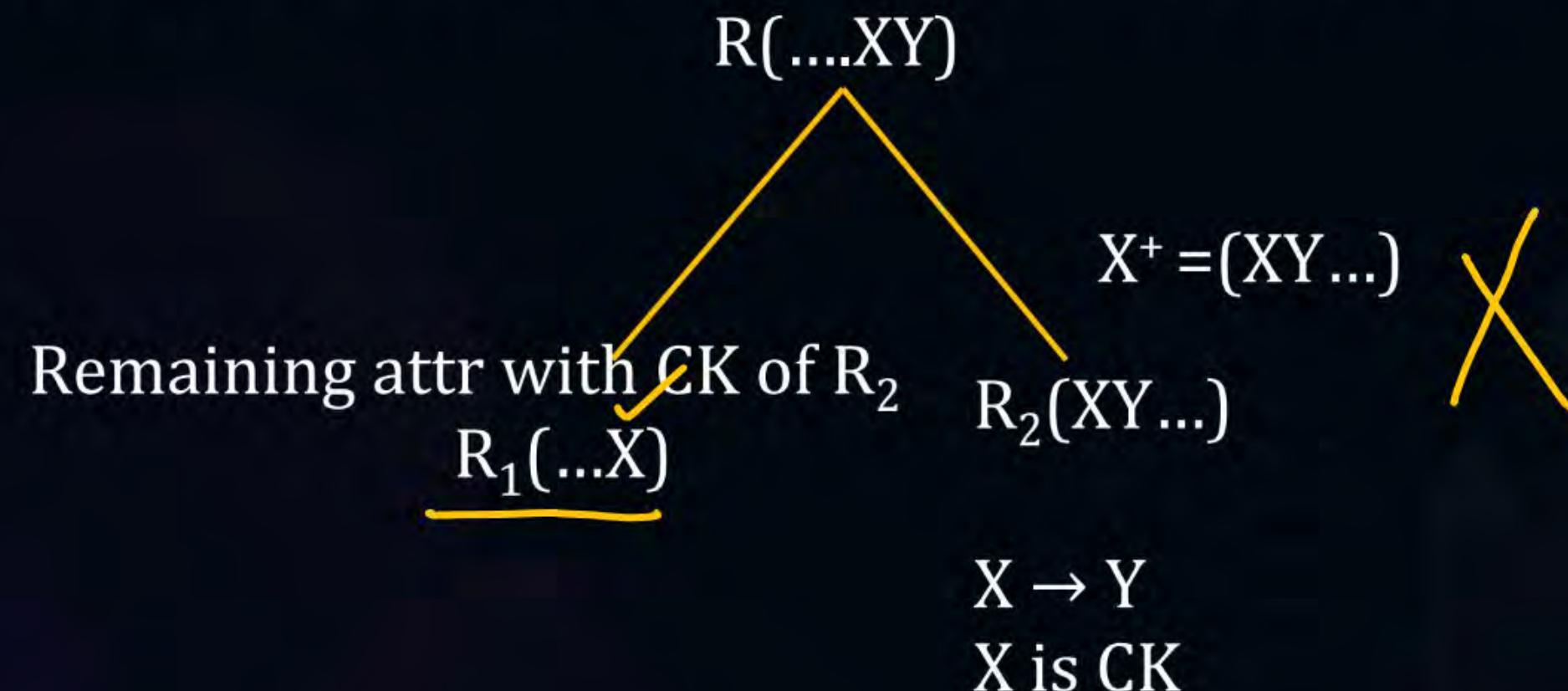




Topic: Highest NF Decomposition

2NF Decomposition:

For a Relation $R(...XY)$ and FD's are $\{...X \rightarrow Y\}$ and $X \rightarrow Y$ is a partial dependency.

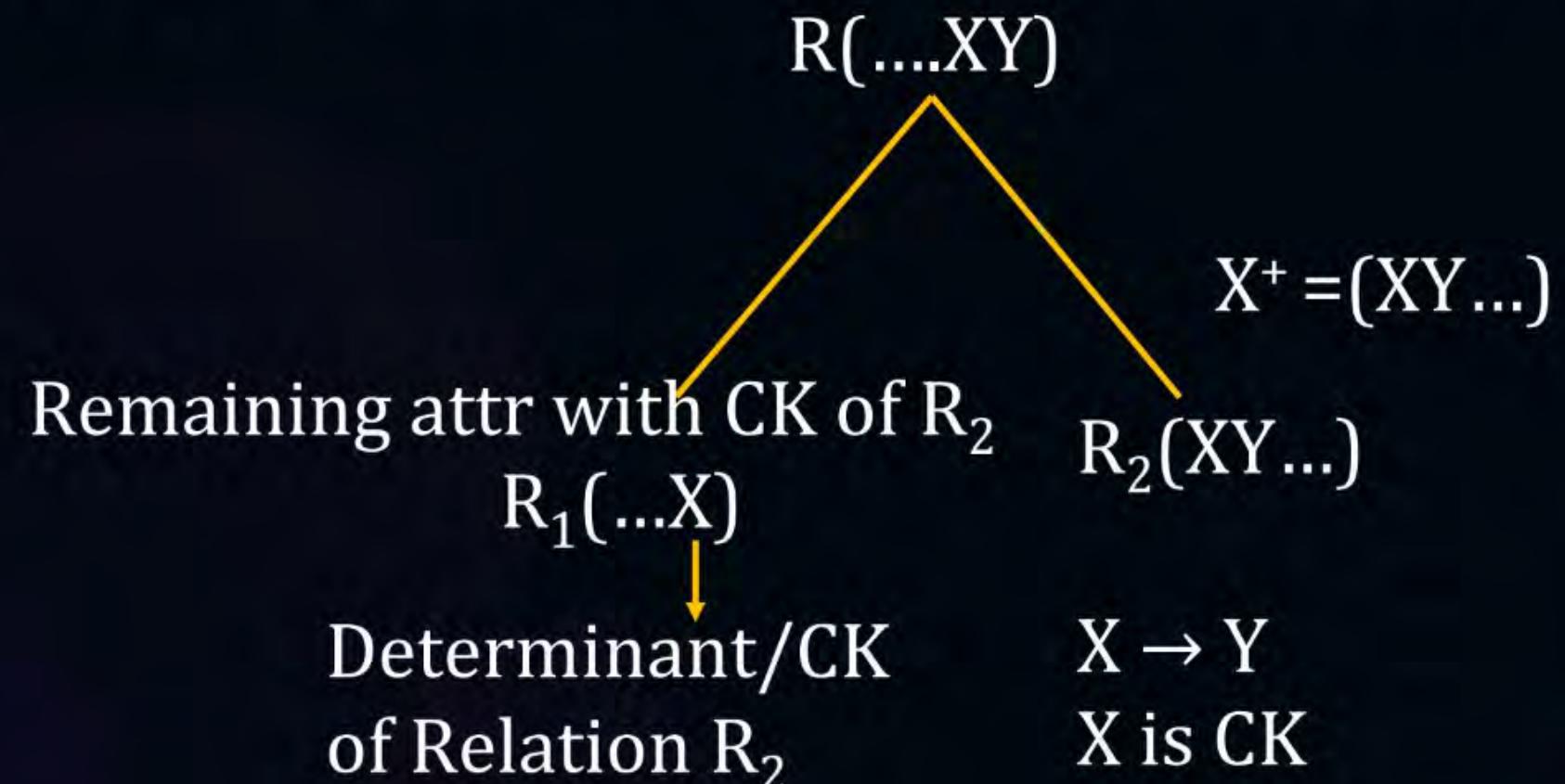




Topic: Highest NF Decomposition

2NF Decomposition:

For a Relation $R(...XY)$ and FD's are $\{...X \rightarrow Y\}$ and $X \rightarrow Y$ is a partial dependency.

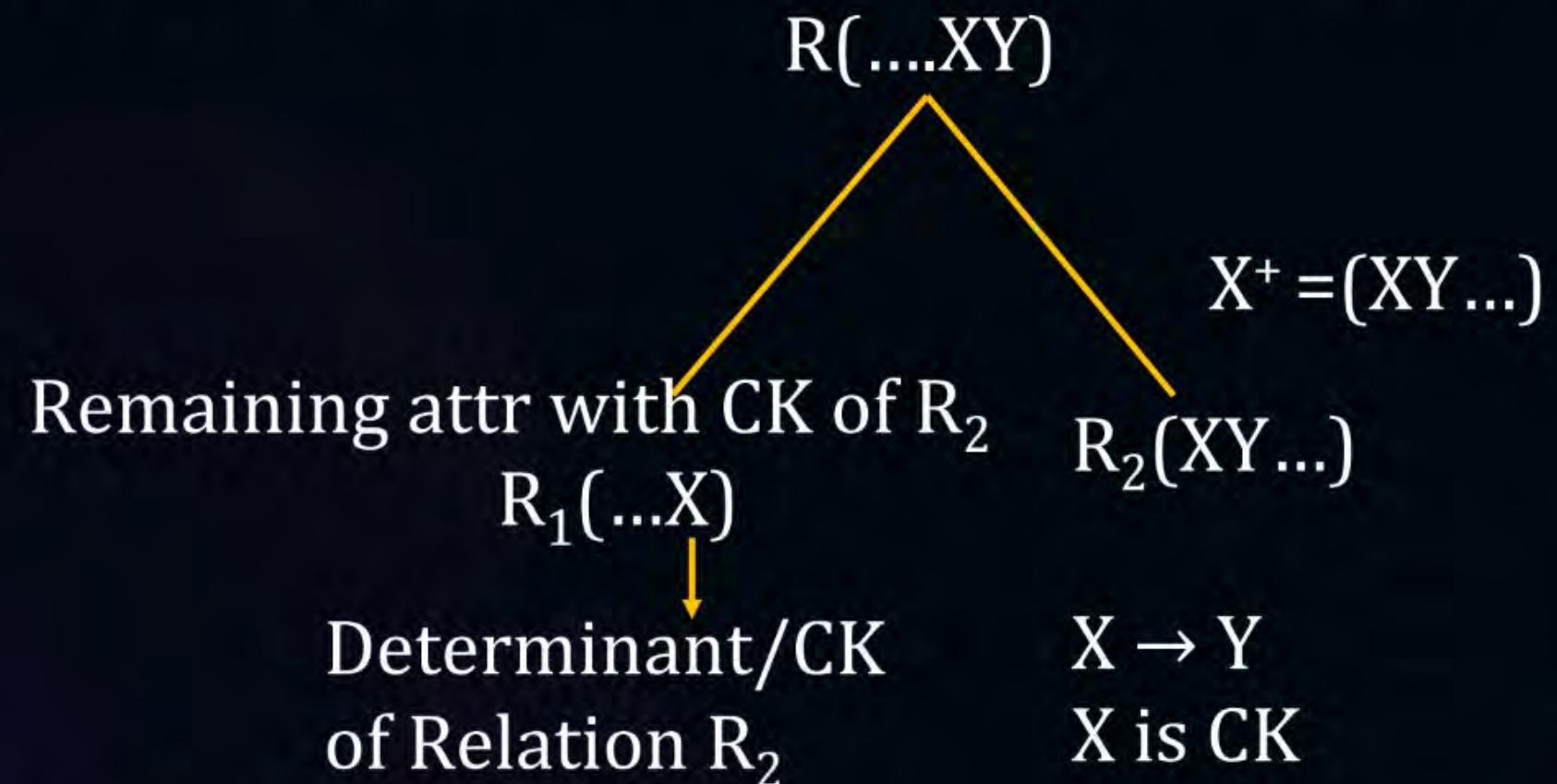




Topic: Highest NF Decomposition

2NF Decomposition:

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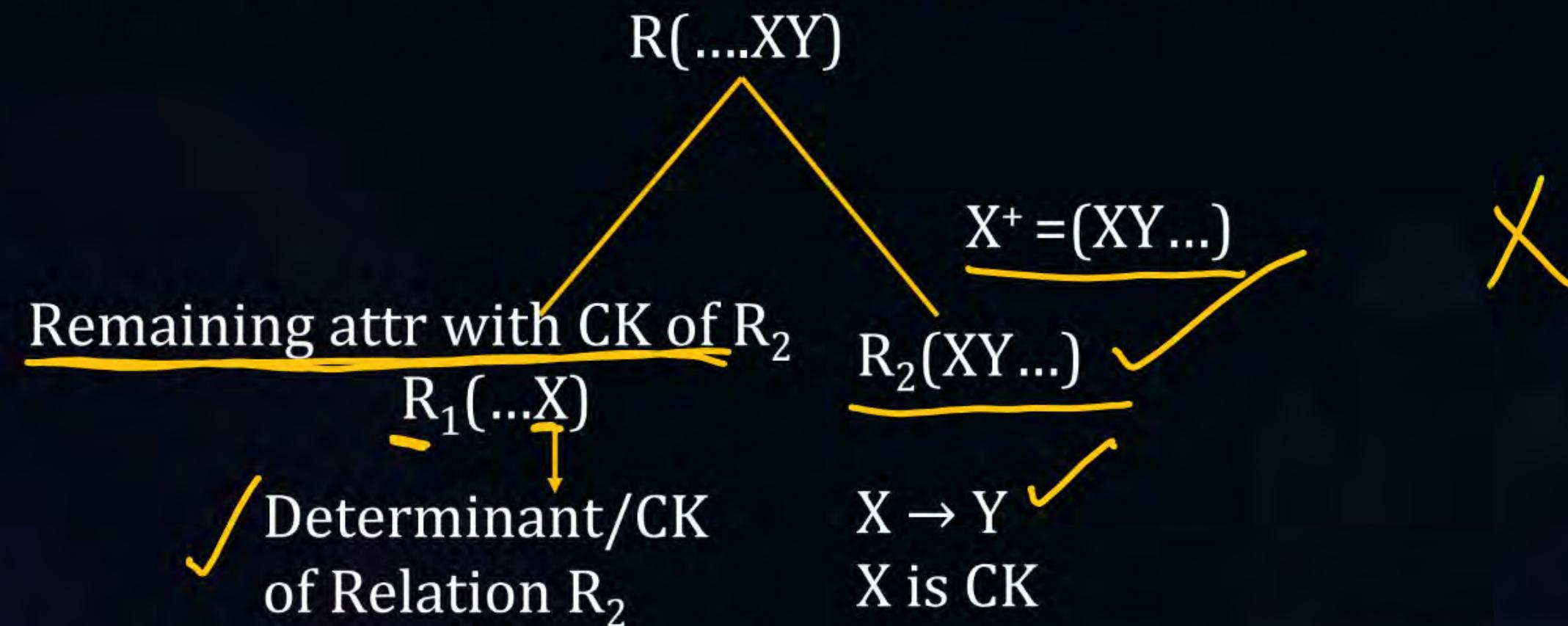
X is common attribute .



Topic: Highest NF Decomposition

2NF Decomposition:

For a Relation $R(\dots XY)$ and FD's are $\{\dots X \rightarrow Y\}$ and $X \rightarrow Y$ is a partial dependency.



X is common attribute . . . The decomposition is lossless and dependency preserving, No Partial dependencies.



Topic: Highest NF Decomposition



#Q. R(Sid, Sname, DOB, Cid) {Sid → Sname, DOB}. Decompose into 2NF.



Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ { $\text{Sid} \rightarrow \text{Sname}, \text{DOB}$ }. Decompose into 2NF.

Sol: SidCid is CK

PD



Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol: SidCid is CK



Sid \rightarrow SnameDOB is a partial dependency.



Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid}) \{ \text{Sid} \rightarrow \text{Sname}, \text{DOB} \}$. Decompose into 2NF.

Sol: Sid Cid is CK

$\text{Sid} \rightarrow \text{SnameDOB}$ is a partial dependency.

Now take closure of Sid.

$\text{Sid}^+ = \underline{\underline{\text{Sid}}}, \underline{\underline{\text{Sname}}}, \underline{\underline{\text{DOB}}}$



Topic: Highest NF Decomposition



#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \underline{\text{Cid}})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol: SidCid is CK

$\text{Sid} \rightarrow \text{SnameDOB}$ is a partial dependency.

Now take closure of Sid.

$\text{Sid}^+ = \text{Sid, Sname, DOB}$

$\therefore \underline{\underline{R_2(\text{Sid, Sname, DOB})}}$



Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid}) \{ \text{Sid} \rightarrow \text{Sname}, \text{DOB} \}$. Decompose into 2NF.

Sol: SidCid is CK

$\text{Sid} \rightarrow \text{SnameDOB}$ is a partial dependency.

Now take closure of Sid.

$$\text{Sid}^+ = \text{Sid, Sname, DOB}$$

$$\therefore \underline{\underline{R_2(\text{Sid}, \text{Sname}, \text{DOB})}} \quad \checkmark$$

Now $\underline{\underline{\text{Sid} \rightarrow \text{SnameDOB}}}$ holds for $\underline{\underline{R_2}}$ and it is not partial dependency.



Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid}) \{ \text{Sid} \rightarrow \text{Sname}, \text{DOB} \}$. Decompose into 2NF.

Sol: SidCid is CK

$\text{Sid} \rightarrow \text{SnameDOB}$ is a partial dependency.

Now take closure of Sid.

$$\text{Sid}^+ = \text{Sid, Sname, DOB}$$

$$\therefore R_2(\underline{\text{Sid}}, \text{Sname}, \text{DOB})$$

Now $\text{Sid} \rightarrow \text{SnameDOB}$ holds for R_2 and it is not partial dependency.

- Now remaining all attributes are in one relation i.e.

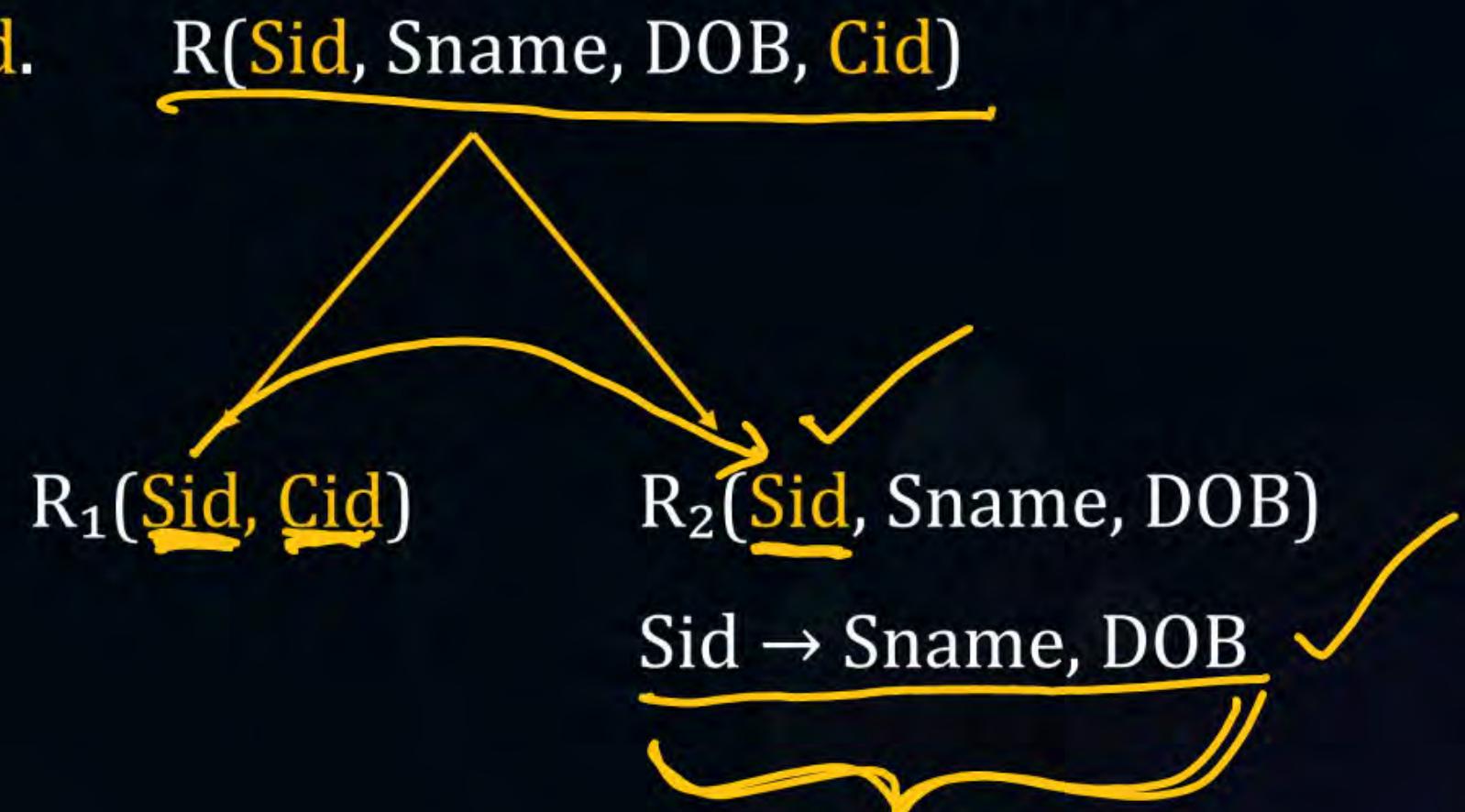
$R_1(\underline{\text{Sid}}\underline{\text{Cid}})$ along with common attribute.



Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol Cont.: In this relation CK is SidCid .



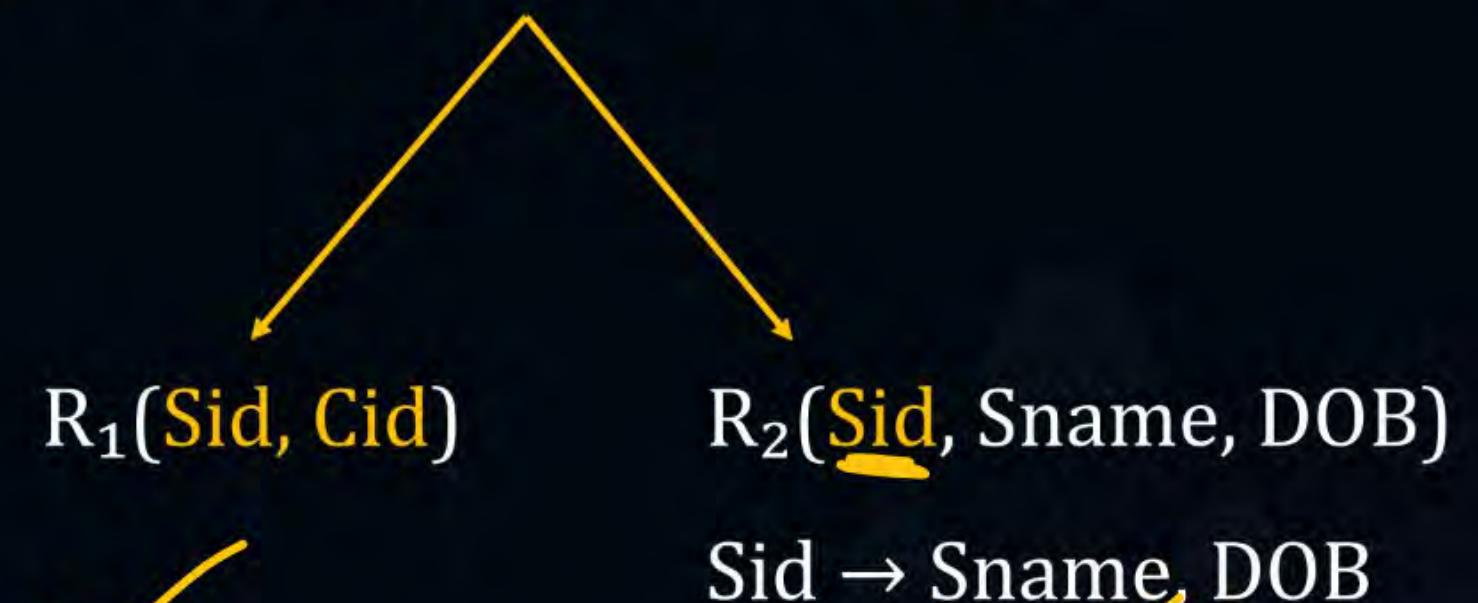


Topic: Highest NF Decomposition



#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol Cont.: In this relation CK is SidCid . $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$



Sid is common attribute, and CK of one table so lossless join decomposition.

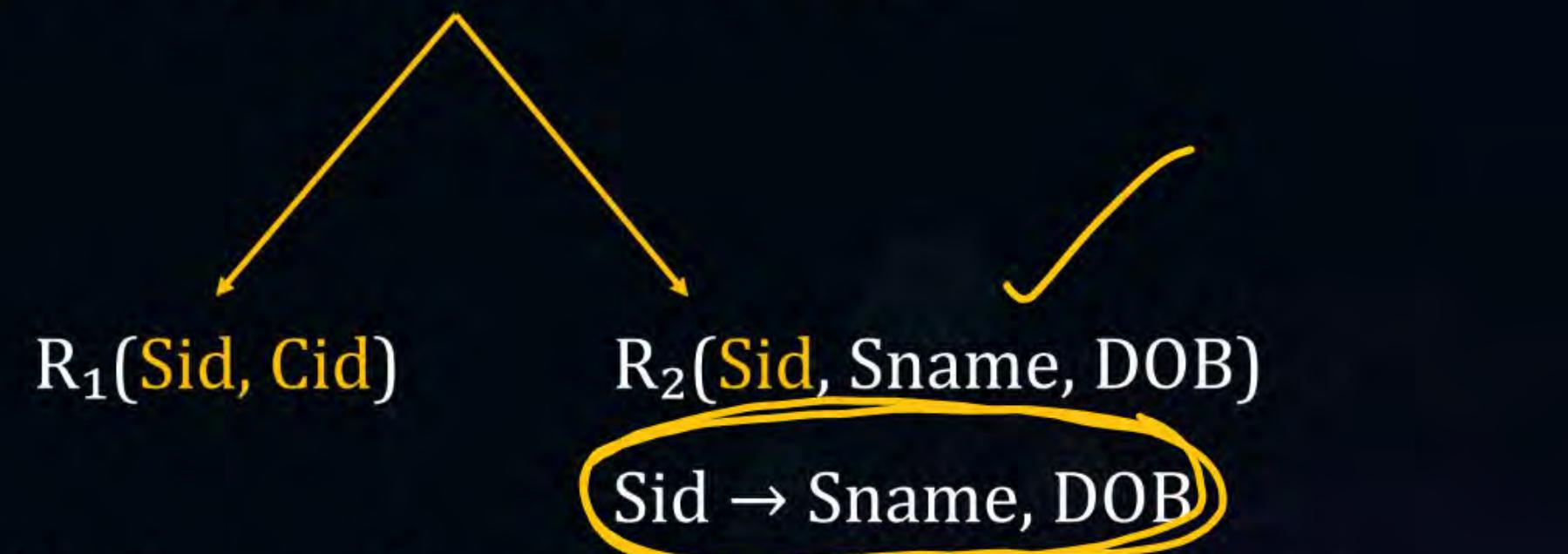


Topic: Highest NF Decomposition



#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol Cont.: In this relation CK is SidCid . $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$



Sid is common attribute, and CK of one table so lossless join decomposition.

All dependencies are followed & satisfied. Therefore Dependency preserving.

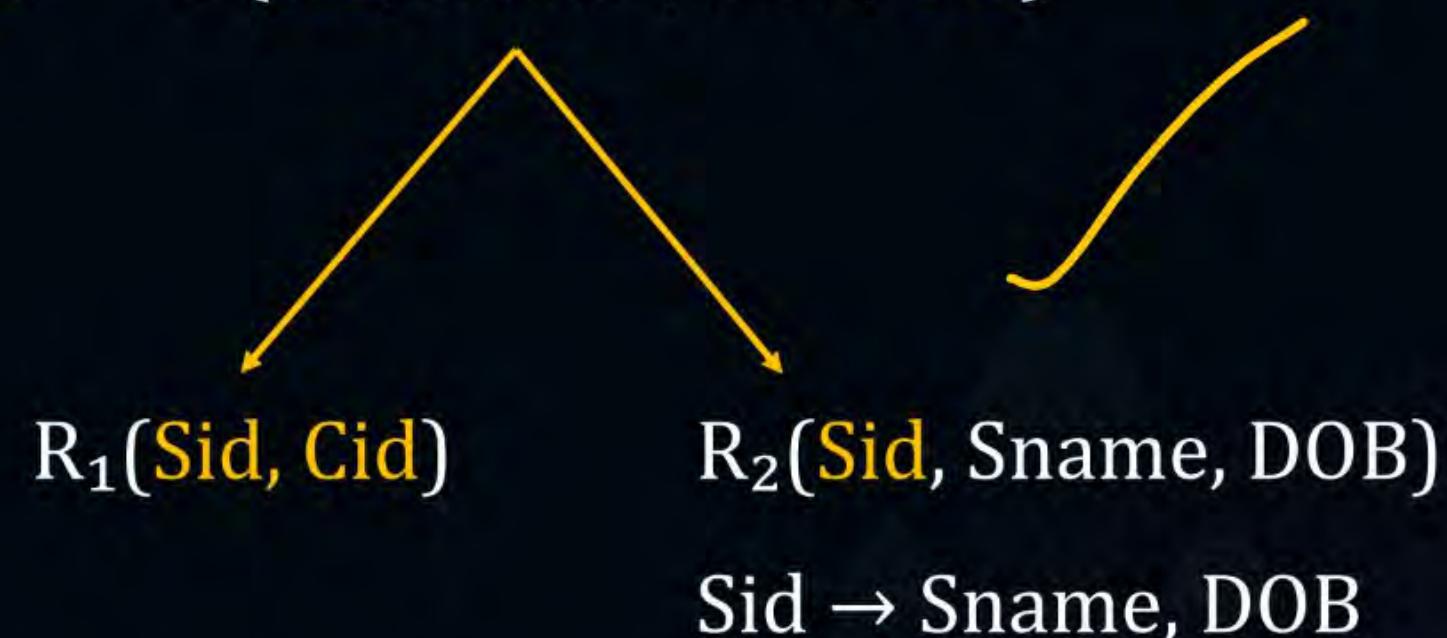


Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol Cont.: In this relation CK is SidCid .

$R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$



Sid is common attribute, and CK of one table so lossless join decomposition.

All dependencies are followed & satisfied. Therefore Dependency preserving.

- No partial dependencies present, so the relation is in 2NF.

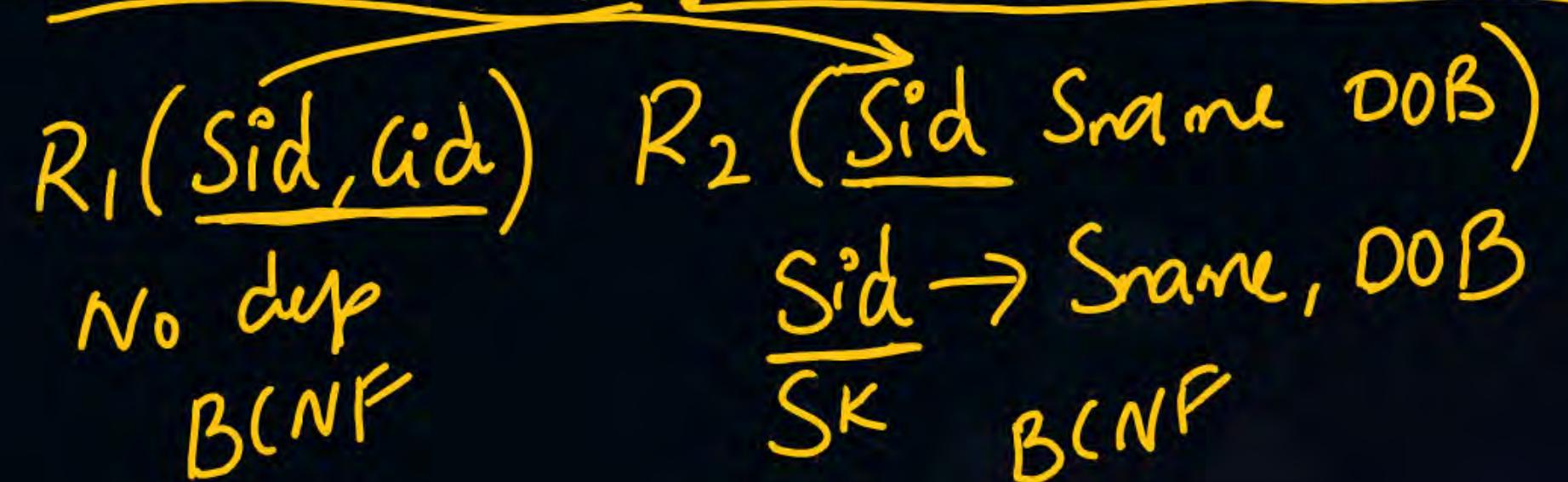
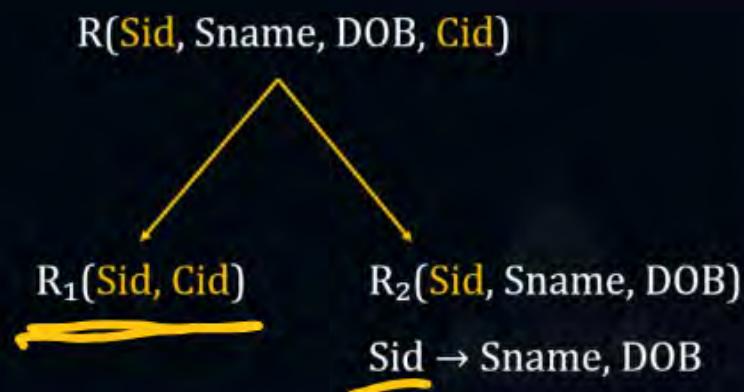


Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol Cont.:

Extension: Now for $R_1(\text{Sid}, \text{Cid})$ no non-trivial FDs are possible.





Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid}) \{ \text{Sid} \rightarrow \text{Sname}, \text{DOB} \}$. Decompose into 2NF.

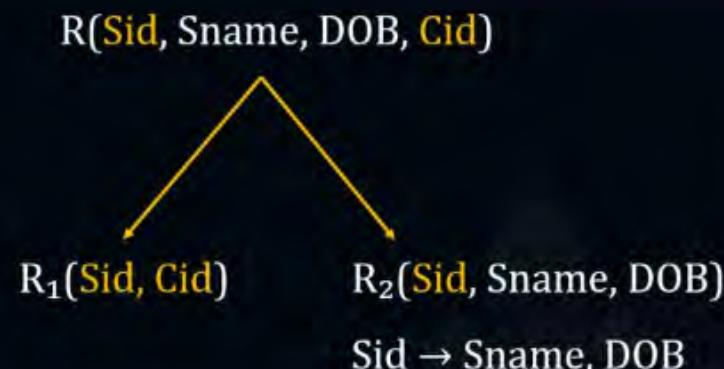
Sol Cont.:

Extension: Now for $R_1(\text{Sid}, \text{Cid})$ no non-trivial FDs are possible.

∴ The relation R_1 is in 3NF and as well as in BCNF.

For $R_2(\underline{\text{Sid}}, \text{Sname}, \text{DOB})$, the FDs are $\text{Sid} \rightarrow \text{Sname}, \text{DOB}$.

Here Sid is CK,





Topic: Highest NF Decomposition

#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid})$ $\{\text{Sid} \rightarrow \text{Sname}, \text{DOB}\}$. Decompose into 2NF.

Sol Cont.:

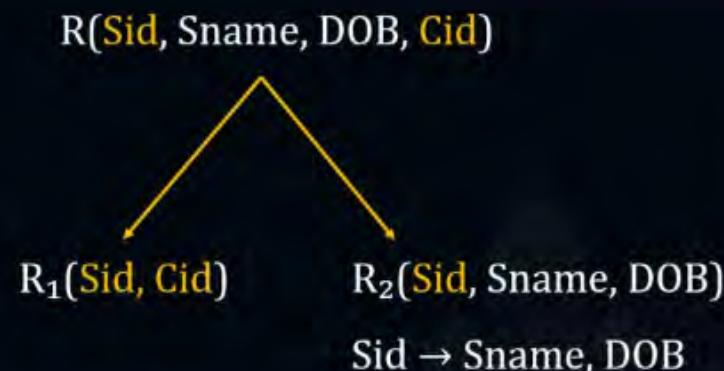
Extension: Now for $R_1(\text{Sid}, \text{Cid})$ no non-trivial FDs are possible.

\therefore The relation R_1 is in 3NF and as well as in BCNF.

For $R_2(\text{Sid}, \text{Sname}, \text{DOB})$, the FDs are $\text{Sid} \rightarrow \text{Sname}, \text{DOB}$.

Here Sid is CK,

\therefore The relation is in 3NF & BCNF.





Topic: Highest NF Decomposition

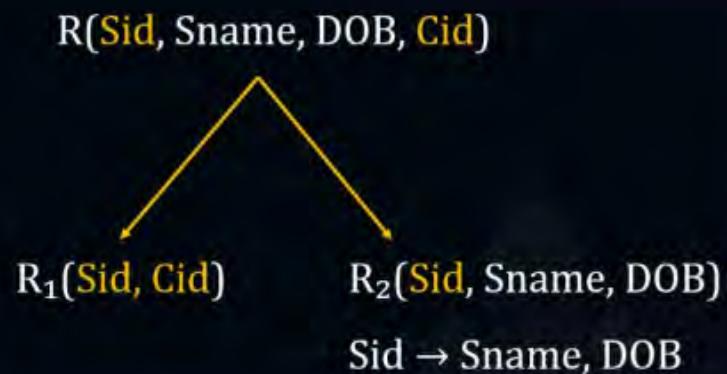


#Q. $R(\text{Sid}, \text{Sname}, \text{DOB}, \text{Cid}) \{ \text{Sid} \rightarrow \text{Sname}, \text{DOB} \}$. Decompose into 2NF.

Sol Cont.:

Extension: Now for $R_1(\text{Sid}, \text{Cid})$ no non-trivial FDs are possible.

∴ The relation R_1 is in 3NF and as well as in BCNF.



For $R_2(\text{Sid}, \text{Sname}, \text{DOB})$, the FDs are $\text{Sid} \rightarrow \text{Sname}, \text{DOB}$.

Here Sid is CK,

∴ The relation is in 3NF & BCNF.

Also Sid in R_1 is FK that refers to Sid in R_2 which is CK.





Topic: Highest NF Decomposition

#Q. $R(ABCDEF)$ { $AB \rightarrow C$, $C \rightarrow D$, $B \rightarrow E$, $E \rightarrow F$ }

Sol: CKey = AB

Prime attributes = AB

Non-prime attributes = CDEF



Topic: Highest NF Decomposition

#Q. R(ABCDEF) {AB → C, C → D, B → E, E → F}

Sol: CKey = AB

Prime attributes = AB

Non-prime attributes = CDEF

B is partial CK in B → E.

Decomposing this into 2NF:

B⁺ = BEF



Topic: Highest NF Decomposition

#Q. $R(\underline{ABCDEF}) \{AB \rightarrow C, C \rightarrow D, \underline{B \rightarrow E}, \underline{E \rightarrow F}\}$

Sol: CKey = AB

Prime attributes = AB

Non-prime attributes = CDEF

B is partial CK in $B \rightarrow E$.

Decomposing this into 2NF:

$B^+ = BEF \Rightarrow R_2(BEF), \underline{B \text{ is CK}}$

$\left. \begin{array}{l} \underline{B \rightarrow E} \\ \underline{E \rightarrow F} \end{array} \right\}$



Topic: Highest NF Decomposition



#Q. $R(ABCDEF) \{ \underline{AB \rightarrow C}, \underline{C \rightarrow D}, B \rightarrow E, E \rightarrow F \}$

Sol Cont.:

Remaining attr forms other $R_1(\underline{\underline{ABCD}})$, AB is CK along with CK.

$\{ \underline{AB \rightarrow C}, \underline{C \rightarrow D} \}$



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.:

Remaining attr forms other $R_1(ABCD)$, AB is CK along with CK.

$\{AB \rightarrow C, C \rightarrow D\}$

B is common, so lossless join. ✓



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.:

Remaining attr forms other $R_1(ABCD)$, AB is CK along with CK.

$\{AB \rightarrow C, C \rightarrow D\}$

B is common, so lossless join.

All dependencies are followed, \therefore dependency preserving.



Topic: Highest NF Decomposition



#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.:

Remaining attr forms other $R_1(ABCD)$, AB is CK along with CK.

$\{AB \rightarrow C, C \rightarrow D\}$

B is common, so lossless join.

All dependencies are followed, \therefore dependency preserving.

No partial dependencies. \therefore Relation is in 2NF.



Topic: Highest NF Decomposition



#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.:





Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.:

- B is FK in $\underline{R_1}$ that refers to B(CK) in R_2 .

$R(ABCDEF)$



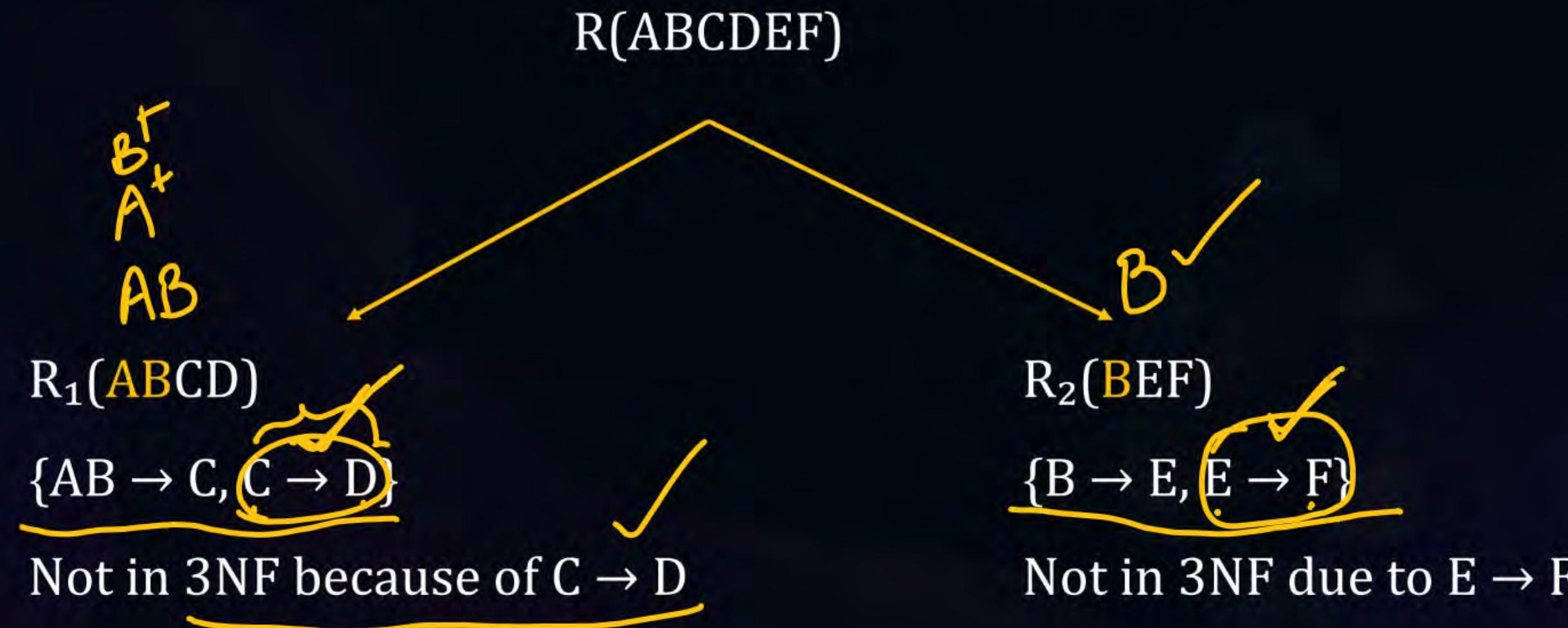


Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.:

- B is FK in R_1 that refers to B(CK) in R_2 .

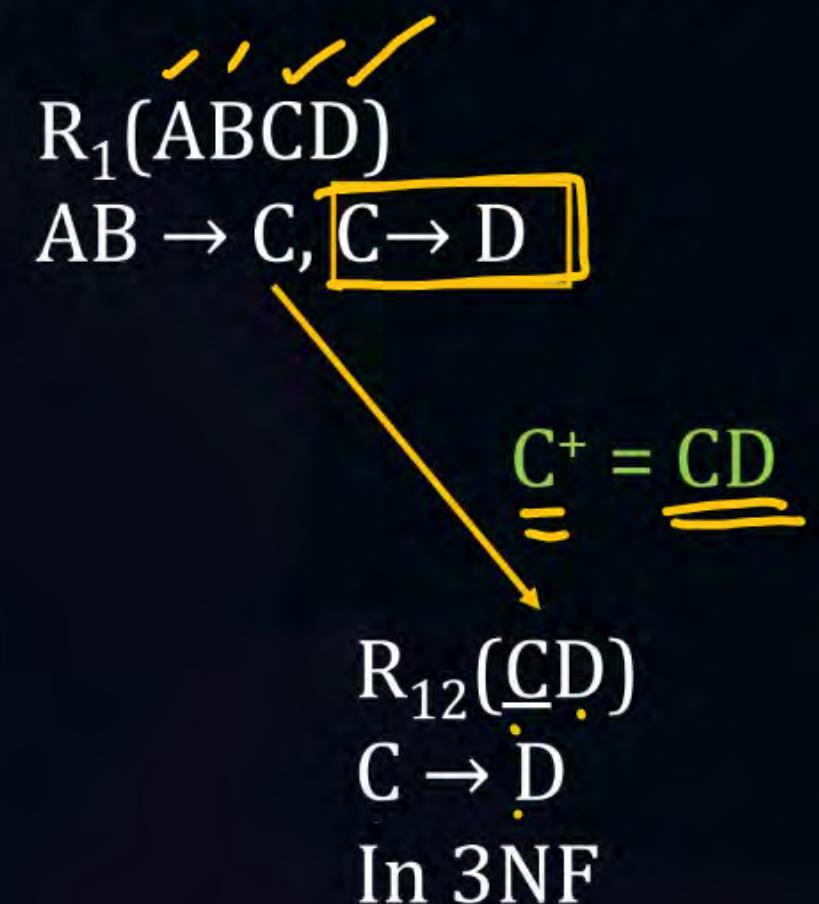




Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.: 2NF requires 2 tables & one FK.



$R_2(BE)$
 $B \rightarrow E, E \rightarrow F$

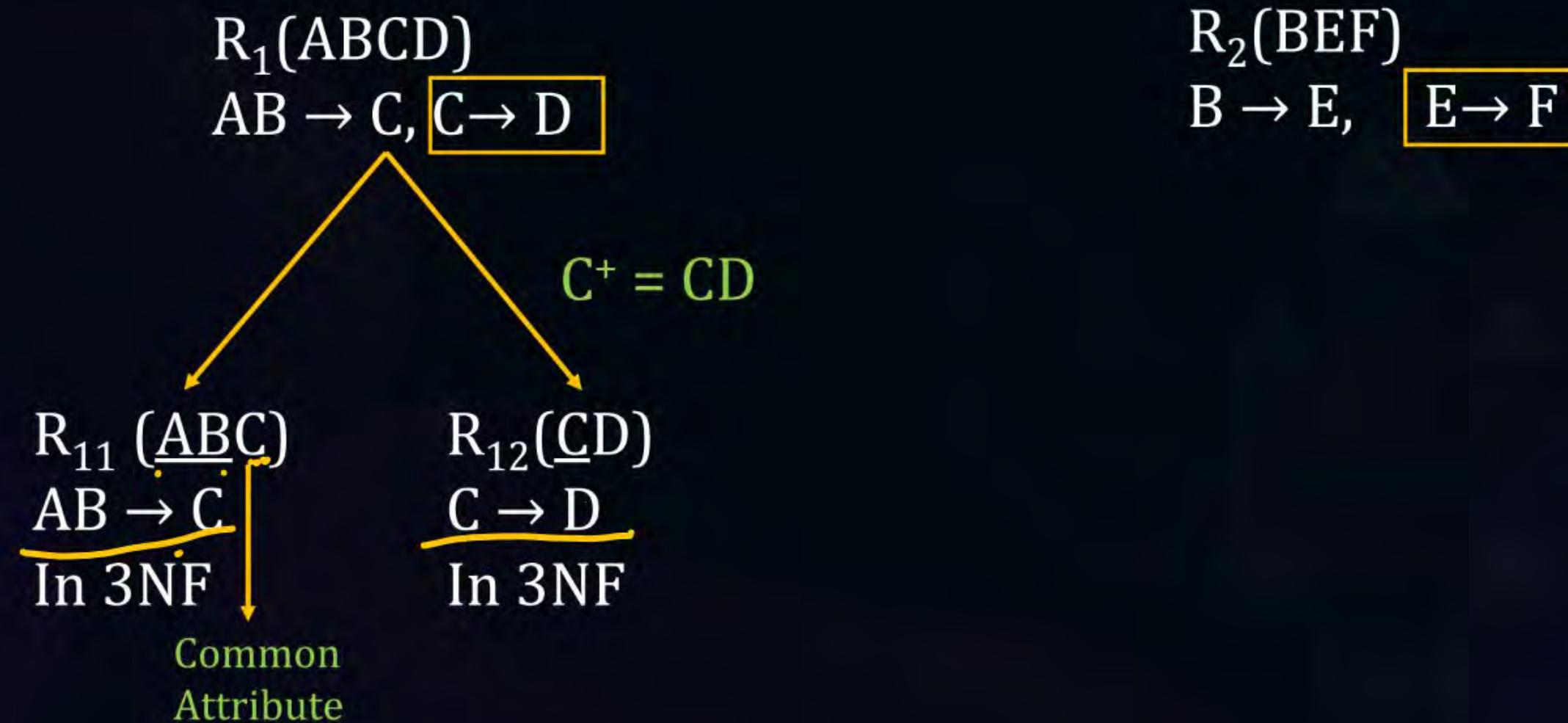


Topic: Highest NF Decomposition



#Q. $R(ABCDEF) \{ \underline{AB \rightarrow C}, C \rightarrow D, B \rightarrow E, E \rightarrow F \}$

Sol Cont.: 2NF requires 2 tables & one FK.



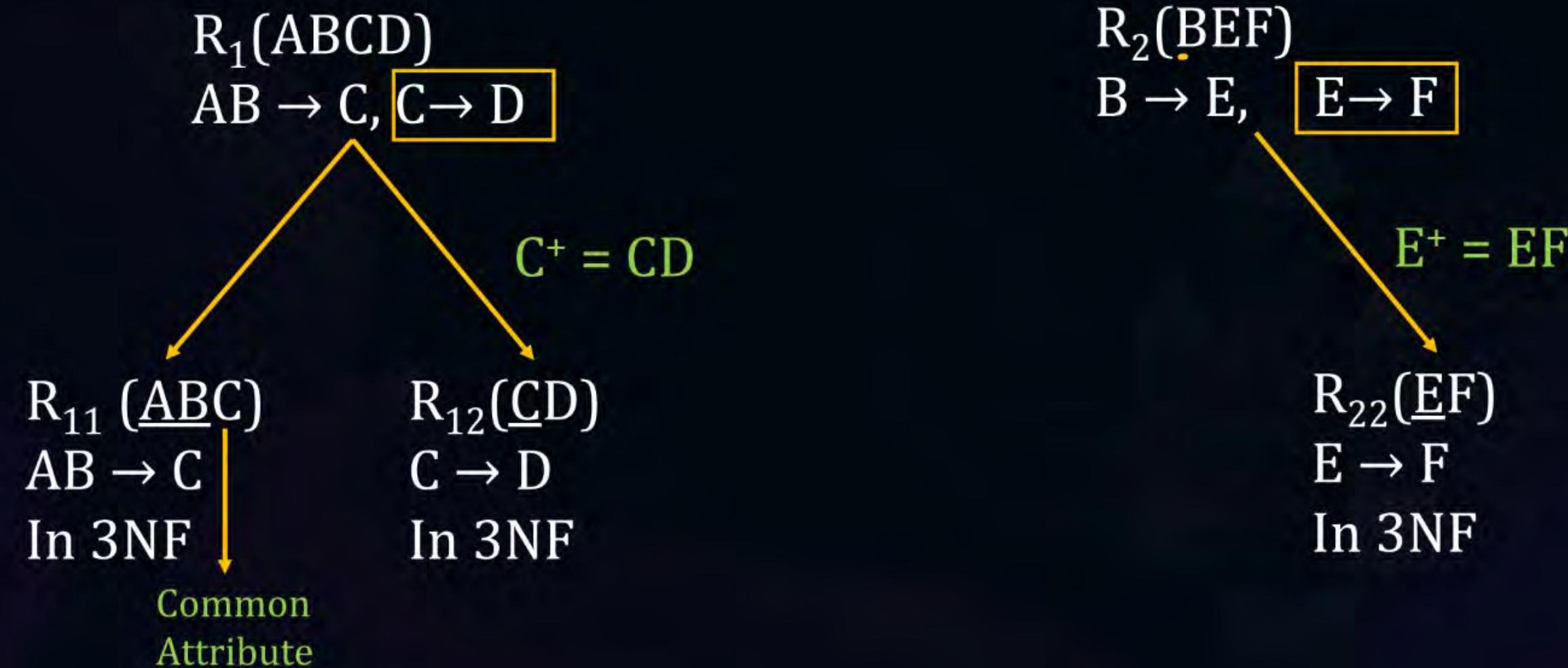


Topic: Highest NF Decomposition



#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.: 2NF requires 2 tables & one FK.

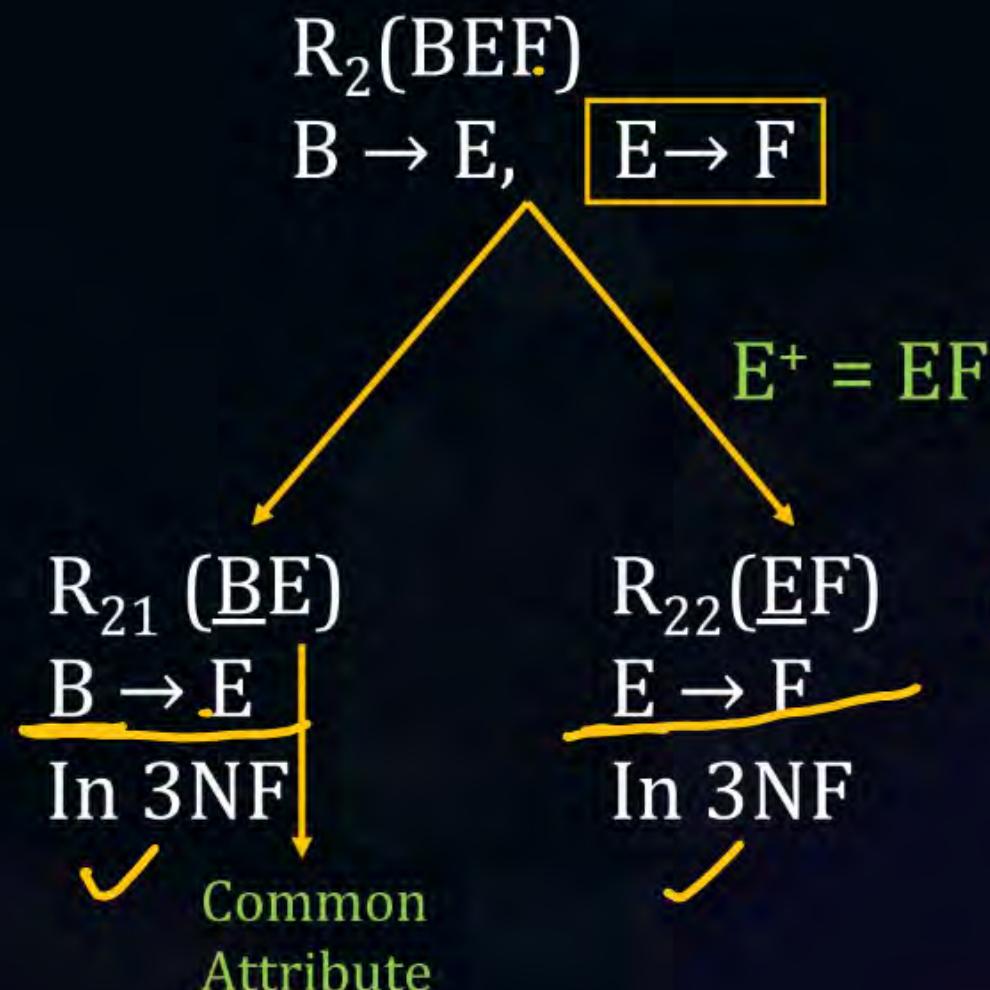
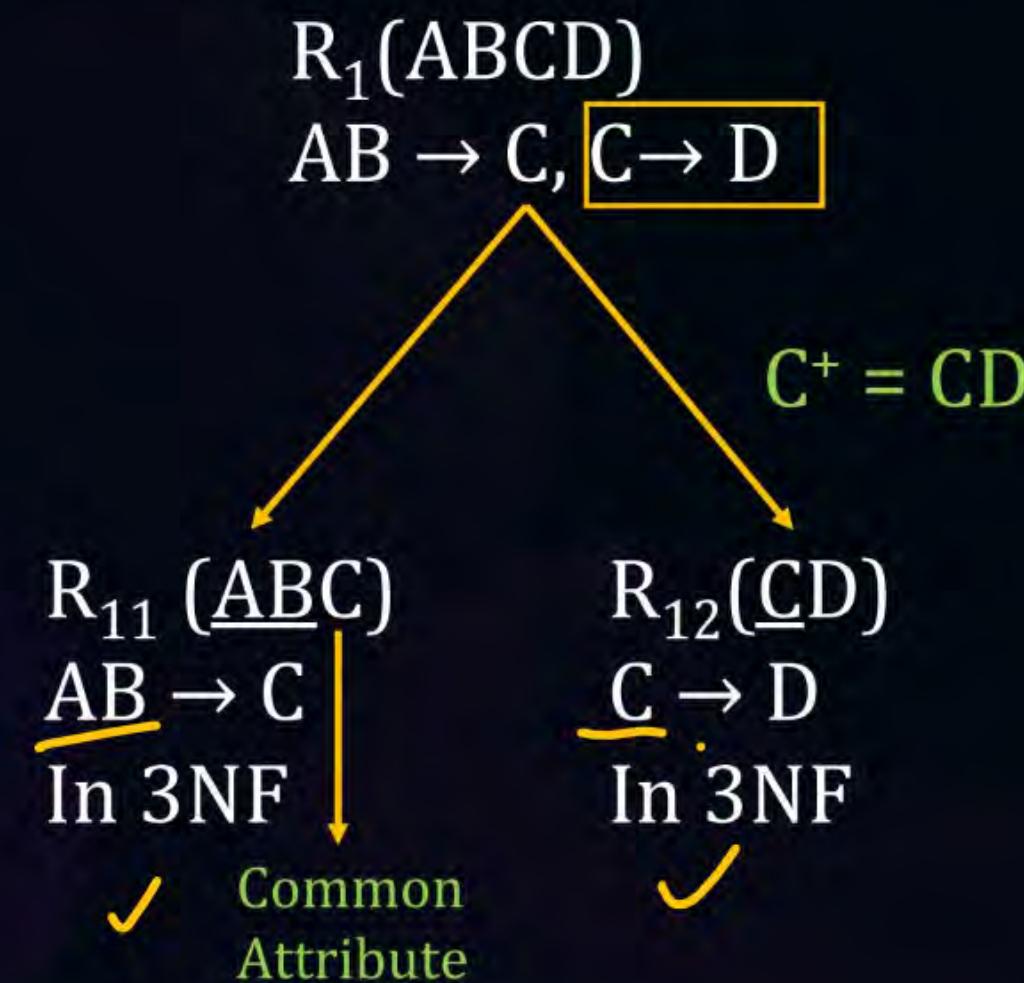




Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont: 2NF requires 2 tables & one FK.





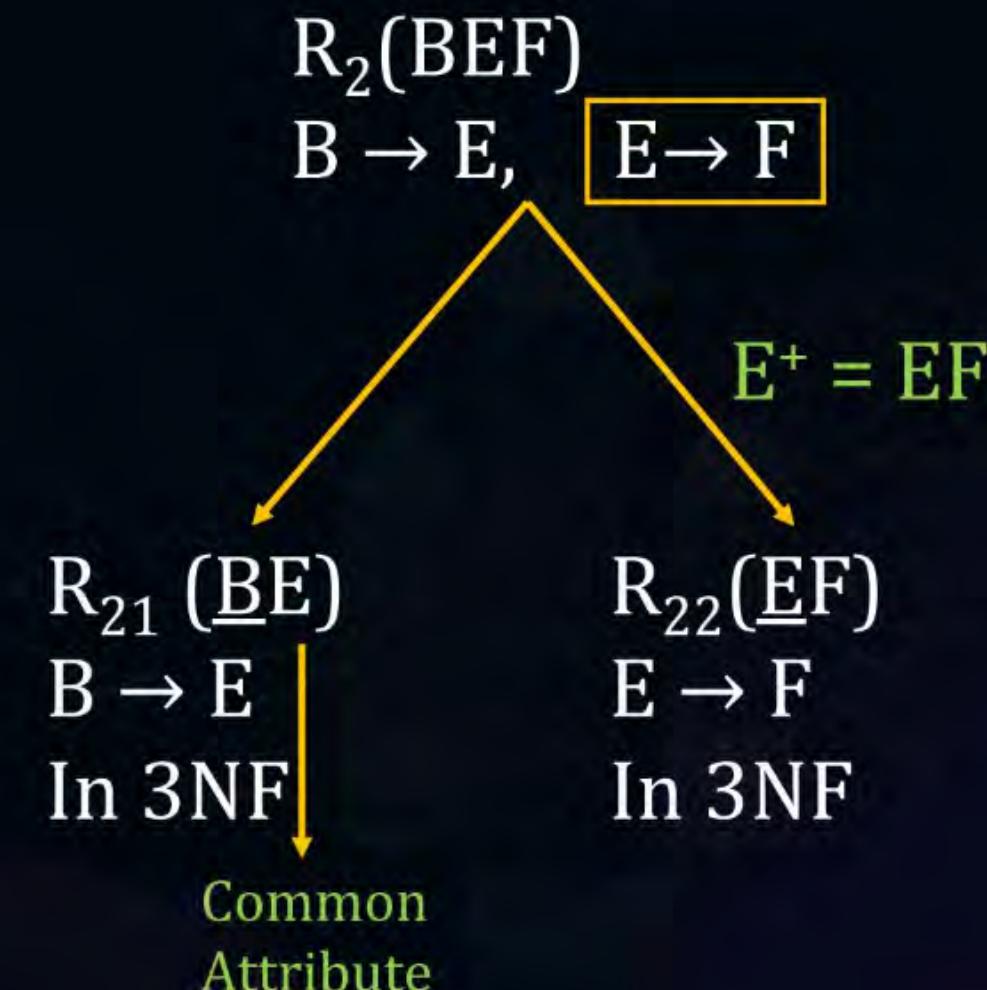
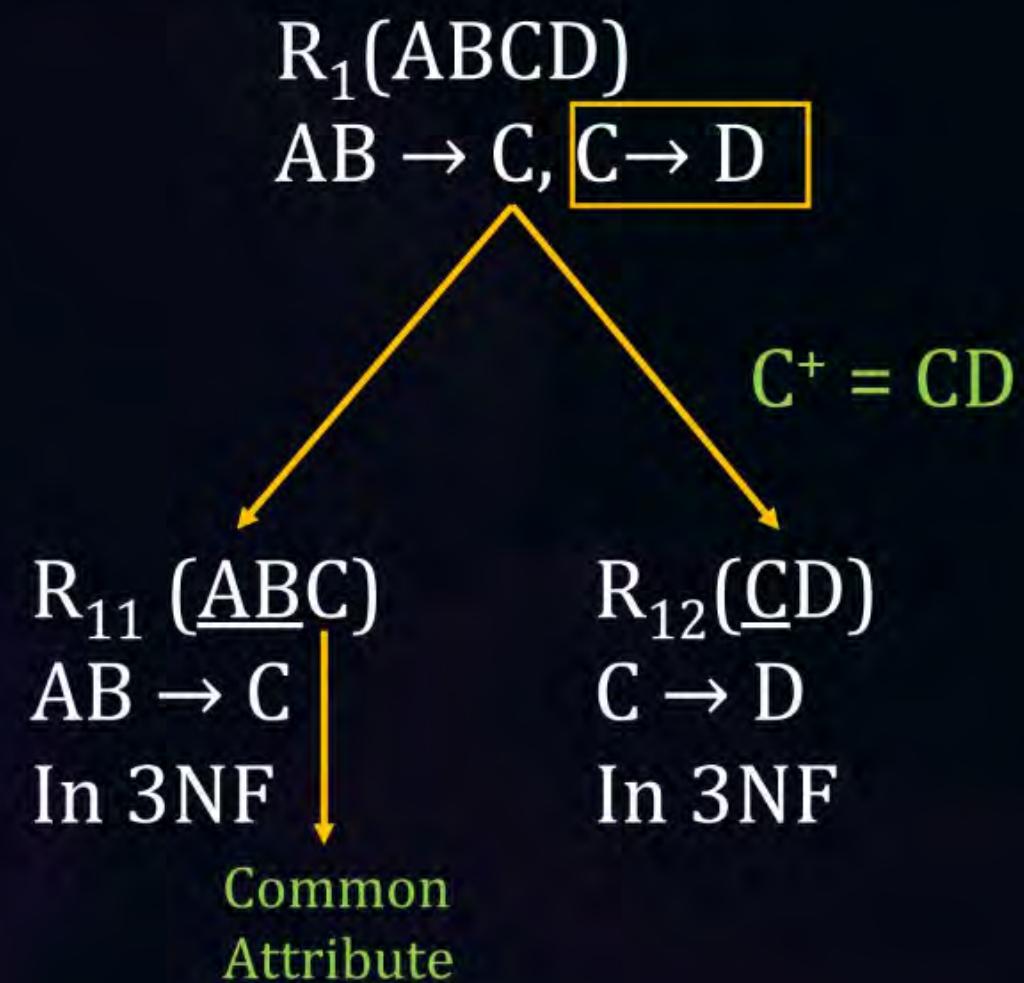
Topic: Highest NF Decomposition



#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont: 2NF requires 2 tables & one FK.

Now, the decomposition is loss less, dependency preserving, 3NF and also in BCNF.





Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, B \rightarrow E, E \rightarrow F\}$

Sol Cont.:





Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, \overline{A \rightarrow E}, \overline{B \rightarrow F}, F \rightarrow G\}$

Sol: AB is CK



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol: AB is CK

$A \rightarrow E$, $B \rightarrow F$ are partial dependencies. R is in 1NF but not in 2NF.



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol: AB is CK

$A \rightarrow E, B \rightarrow F$ are partial dependencies. R is in 1NF but not in 2NF.

2NF Decomposition:

$$A^+ = AE \checkmark$$

$R_2(AE)$

$$B^+ = BFG \checkmark$$

$R_3(BFG)$

Remaining Attr along with CK.

$R_1(\underline{AB}\underline{CD})$



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol: AB is CK

$A \rightarrow E, B \rightarrow F$ are partial dependencies. R is in 1NF but not in 2NF.

2NF Decomposition:

$$A^+ = AE$$

$$R_2(AE)$$

$$\underline{A} \rightarrow E \checkmark$$

A is CK

in 3NF \checkmark

$$B^+ = BFG$$

$$R_3(BFG)$$

$$\underline{B} \rightarrow F, \underline{F} \rightarrow G \checkmark$$

B is CK

Not in 3NF

Remaining Attr along with CK.

$$R_1(ABCD)$$

$$\underline{AB} \rightarrow C \checkmark$$

$$\underline{C} \rightarrow \underline{D} \checkmark$$

Not in 3NF becoz of

$$C \rightarrow D$$



Topic: Highest NF Decomposition



#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol: AB is CK

$A \rightarrow E, B \rightarrow F$ are partial dependencies. R is in 1NF but not in 2NF.

2NF Decomposition:

$$A^+ = AE$$

$$R_2(AE)$$

$$A \rightarrow E$$

A is CK

in 3NF

$$B^+ = BFG$$

$$R_3(BFG)$$

$$B \rightarrow F, F \rightarrow G$$

B is CK

Not in 3NF

This decomposition is lossless, dependency preserving and is in 2NF because of no PD. ✓

Remaining Attr along with CK.

$$R_1(ABCD)$$

$$AB \rightarrow C$$

$$C \rightarrow D$$

Not in 3NF becoz of

$$C \rightarrow D$$



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol Cont. :

$R_1(\underline{ABCD})$ ✓
 $AB \rightarrow C, \boxed{C \rightarrow D}$

$R_2(\underline{AE})$
 $A \rightarrow E$

$R_3(\underline{BFG})$ ✓
 $B \rightarrow F, \boxed{F \rightarrow G}$



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol Cont. :

$$R_1(\underline{ABCD}) \\ AB \rightarrow C, \boxed{C \rightarrow D}$$

$$R_2(\underline{AE}) \\ A \rightarrow E$$

$$R_3(\underline{BFG}) \\ B \rightarrow F, \boxed{F \rightarrow G}$$

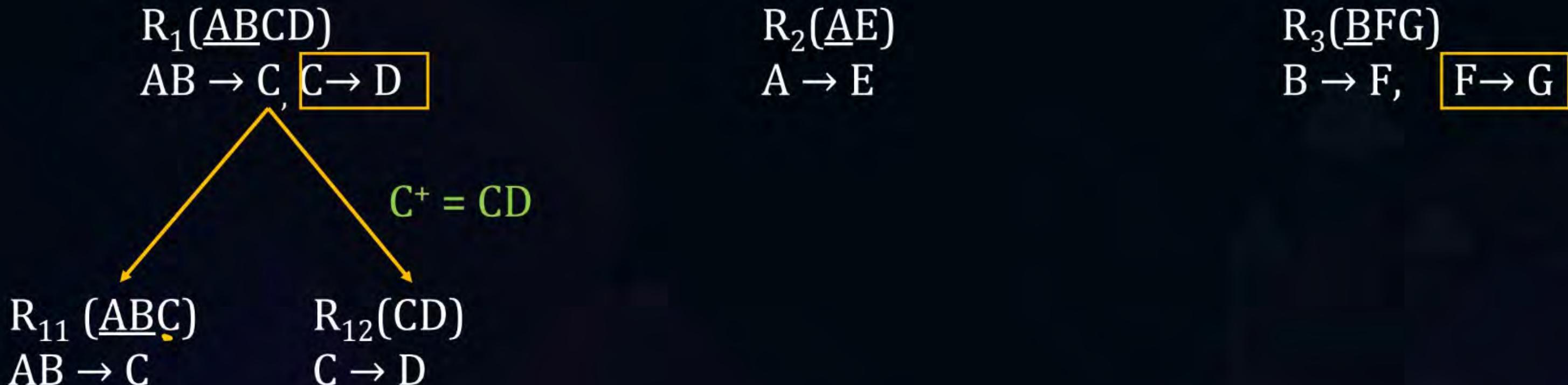
$$C^+ = CD \\ \downarrow \\ R_{12}(CD) \\ C \rightarrow D$$



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol Cont. :

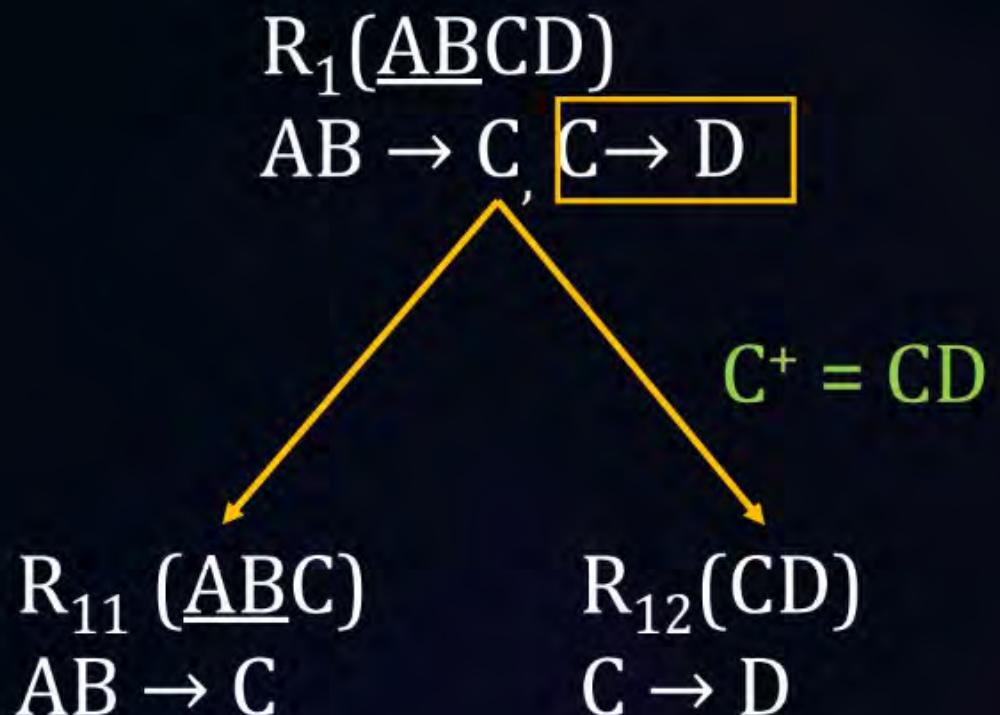




Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol Cont. :



$R_2(\underline{AE})$
 $A \rightarrow E$

$R_3(\underline{BFG})$
 $B \rightarrow F, F \rightarrow G$

$F^+ = FG$

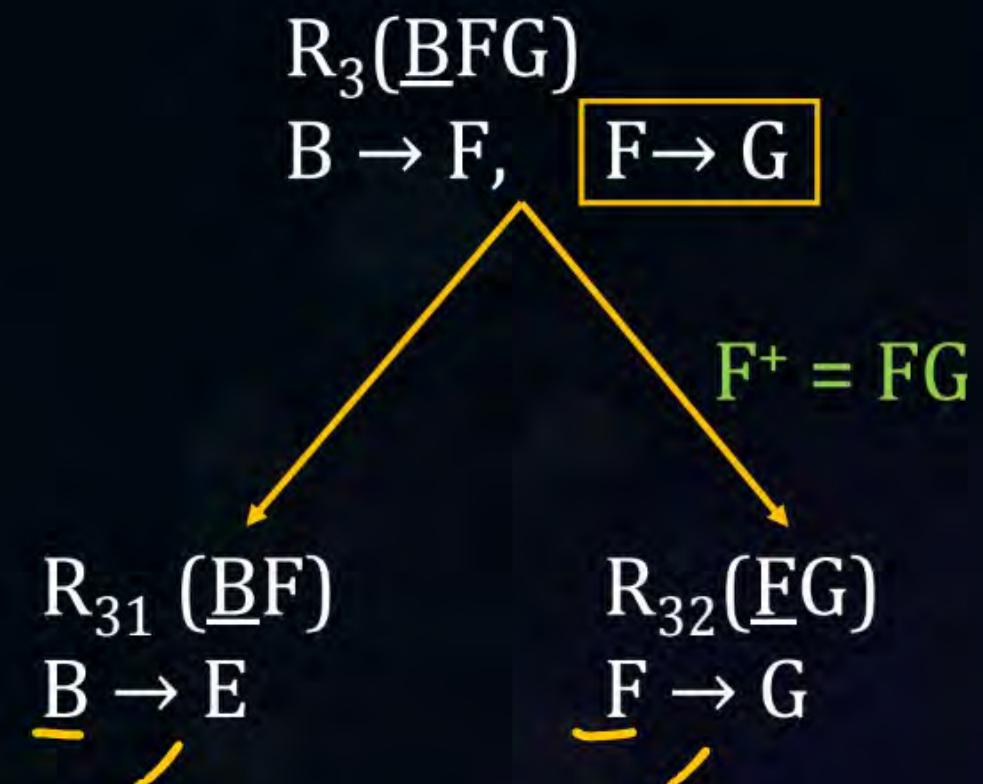
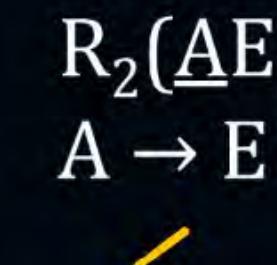
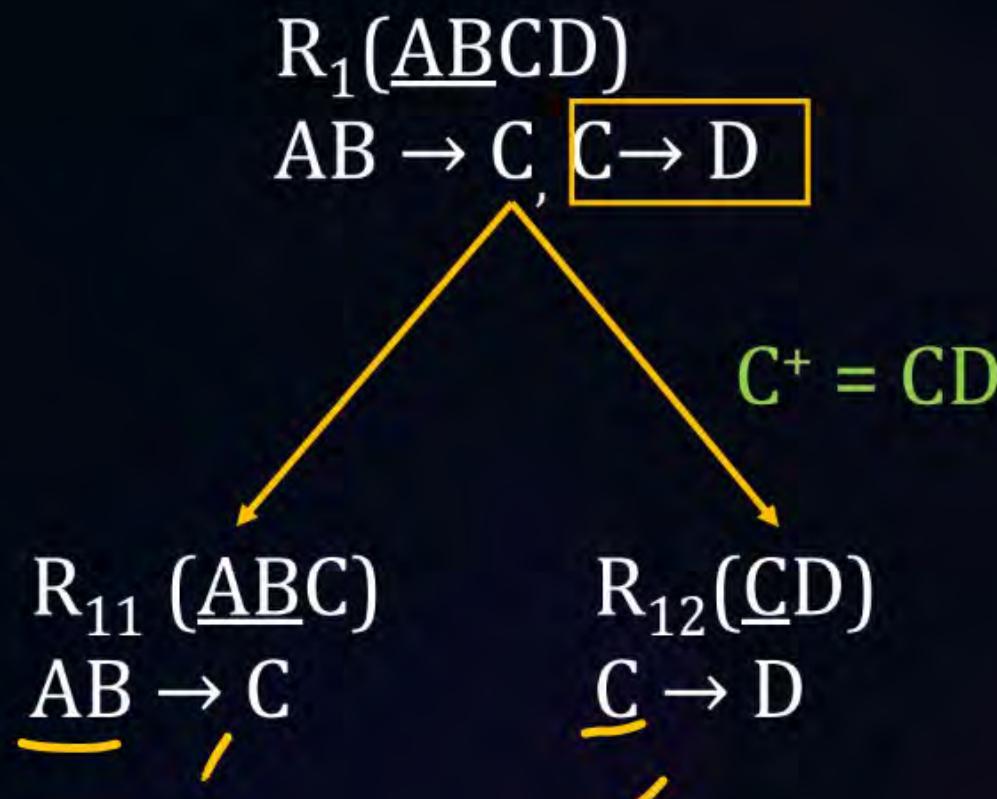
$R_{32}(\underline{FG})$
 $F \rightarrow G$



Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol Cont. :

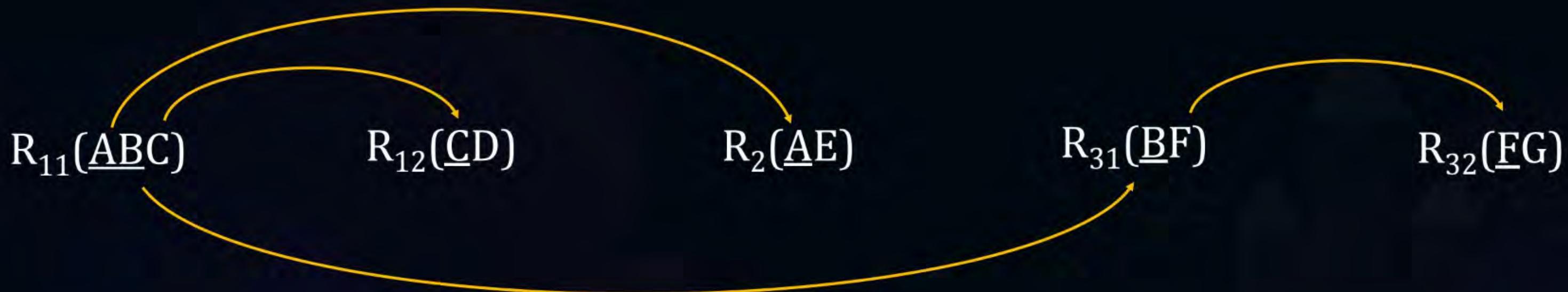




Topic: Highest NF Decomposition

#Q. $R(ABCDEF) \{AB \rightarrow C, C \rightarrow D, A \rightarrow E, B \rightarrow F, F \rightarrow G\}$

Sol Cont. : Now, the Relations decomposition is in 3NF and is BCNF.





Topic: Highest NF Decomposition

A small observation to make:

- To store in 1NF, only one table is enough. But there will be a very high redundancy.
- After the decomposition, redundancy decreases but the number of tables increases.

Inspiring Stories : Dr. Julião Menezes



Background: Goan doctor from Assolna.

Struggles: Portuguese rule silenced voices.

Achievements: Hosted and worked with Ram Manohar Lohia in 1946; sparked Goa's mass movement.

Impact: A catalyst for Goa's freedom movement on the Konkan coast.



Topic: Highest NF Decomposition



#Q. $R(ABCDE) \{ \underbrace{AB \rightarrow C}_{\checkmark}, \underbrace{BC \rightarrow A}_{\checkmark}, \underbrace{AC \rightarrow B}_{\checkmark} \}$

Sol: CK are {ABDE, BCDE , ACDE}



Topic: Highest NF Decomposition

#Q. R(ABCDE) {AB → C, BC → A, AC → B}

Sol: CK are {ABDE, BCDE , ACDE}

$$\begin{array}{c} \text{BCNF} & \begin{array}{c} \underline{\text{AB}} \rightarrow \text{C} \\ \times \end{array} & \begin{array}{c} \underline{\text{BC}} \rightarrow \text{A} \\ \times \end{array} & \begin{array}{c} \underline{\text{AC}} \rightarrow \text{B} \\ \times \end{array} \end{array}$$



Topic: Highest NF Decomposition

#Q. $R(ABCDE) \{AB \rightarrow C, BC \rightarrow A, AC \rightarrow B\}$

Sol: CK are $\{ABDE, BCDE, ACDE\}$

	$AB \rightarrow C$	$BC \rightarrow A$	$AC \rightarrow B$
BCNF	✗	✗	✗
3NF	✓	✓	✓

Highest NF is 3NF.



Topic: Highest NF Decomposition

#Q. R(ABCDE) {AB → C, BC → A, AC → B}

Sol Cont. :

BCNF decomposition:

All 3 FD's are failed for BCNF and all can be handled in a same relation
due to same attributes.



Topic: Highest NF Decomposition

#Q. $R(ABCDE) \{ \underline{AB} \rightarrow C, \underline{BC} \rightarrow A, \underline{AC} \rightarrow B \}$

Sol Cont. :

BCNF decomposition:

All 3 FD's are failed for BCNF and all can be handled in a same relation due to same attributes. $\underline{AB}^+ = \underline{ABC}$

$\checkmark \underline{R_2(ABC)}$ $\underline{R_1(ABDE)}$



Topic: Highest NF Decomposition

#Q. $R(ABCDE) \{AB \rightarrow C, BC \rightarrow A, AC \rightarrow B\}$

Sol Cont. :

BCNF decomposition:

All 3 FD's are failed for BCNF and all can be handled in a same relation due to same attributes. $AB^+ = ABC$

$R_2(ABC)$ $R_1(ABDE)$ Can be any one of $\underbrace{AB, BC, AC}_{}$



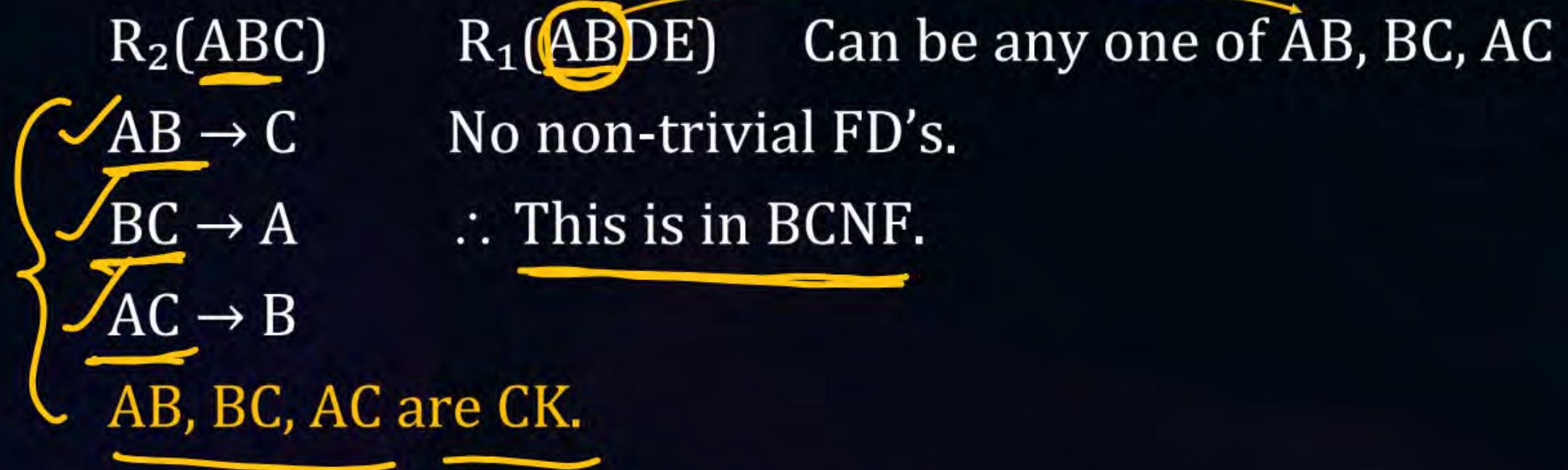
Topic: Highest NF Decomposition

#Q. $R(ABCDE) \{AB \rightarrow C, BC \rightarrow A, AC \rightarrow B\}$

Sol Cont. :

BCNF decomposition:

All 3 FD's are failed for BCNF and all can be handled in a same relation due to same attributes. $AB^+ = ABC$





Topic: Highest NF Decomposition

#Q. $R(ABCDE) \{AB \rightarrow C, BC \rightarrow A, AC \rightarrow B\}$

Sol Cont. :

BCNF decomposition:

All 3 FD's are failed for BCNF and all can be handled in a same relation due to same attributes. $AB^+ = ABC$

$R_2(ABC)$

$R_1(ABDE)$

Can be any one of AB, BC, AC

$AB \rightarrow C$

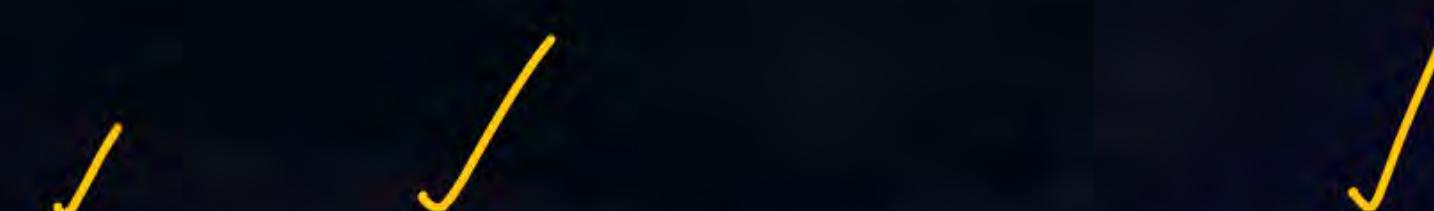
No non-trivial FD's.

$BC \rightarrow A$

\therefore This is in BCNF.

$AC \rightarrow B$

AB, BC, AC are CK.



\therefore The decomposition satisfies lossless join, dependency preserving and is in BCNF.



Topic: Highest NF Decomposition



#Q. $R(ABCDE) \{AB \rightarrow C, BC \rightarrow A, AC \rightarrow B\}$

Sol Cont. :





Topic: Highest NF Decomposition



#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol: AB , BC are CK.



Topic: Highest NF Decomposition

#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol: AB, BC are CK.

$AB \rightarrow C$	$C \rightarrow A$
✓	✗
BCNF	

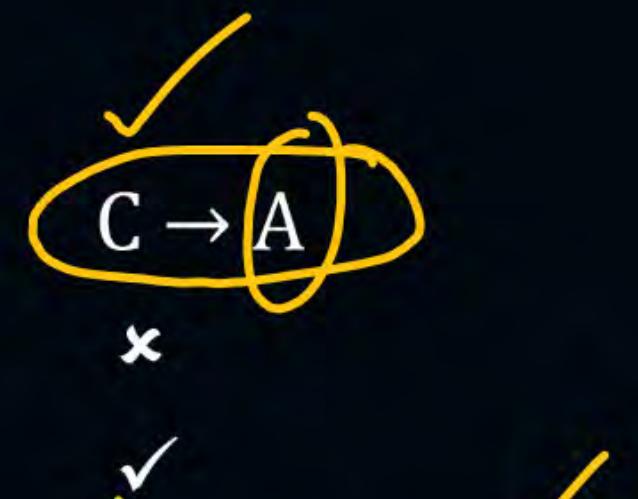


Topic: Highest NF Decomposition

#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol: AB, BC are CK.

	$AB \rightarrow C$
BCNF	✓
3NF	✓



The highest normal form of relation is 3NF. ✓

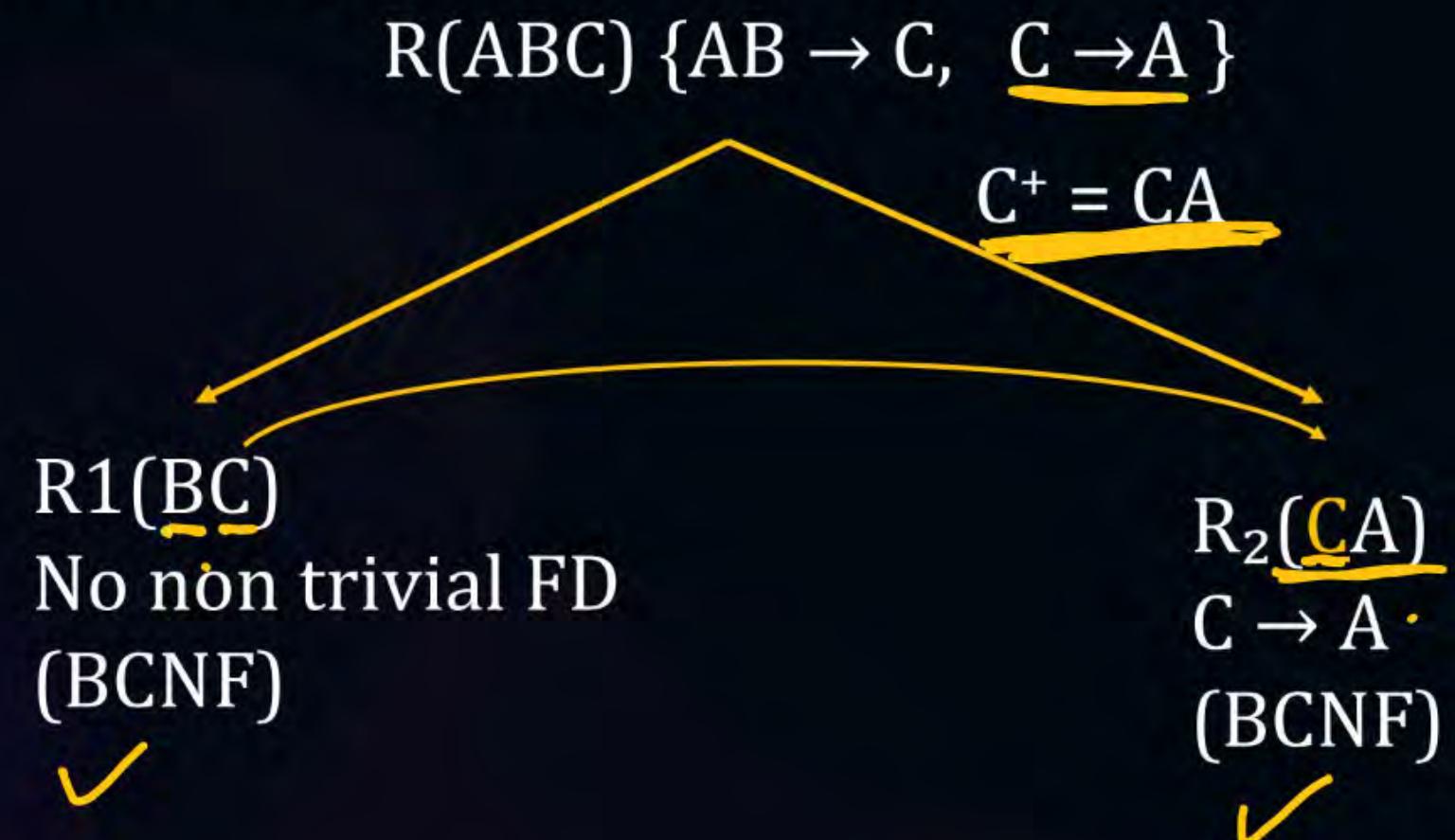


Topic: Highest NF Decomposition



#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol Cont: BCNF decomposition:





Topic: Highest NF Decomposition

#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol Cont: BCNF decomposition:

$R(ABC) \{AB \rightarrow C, C \rightarrow A\}$



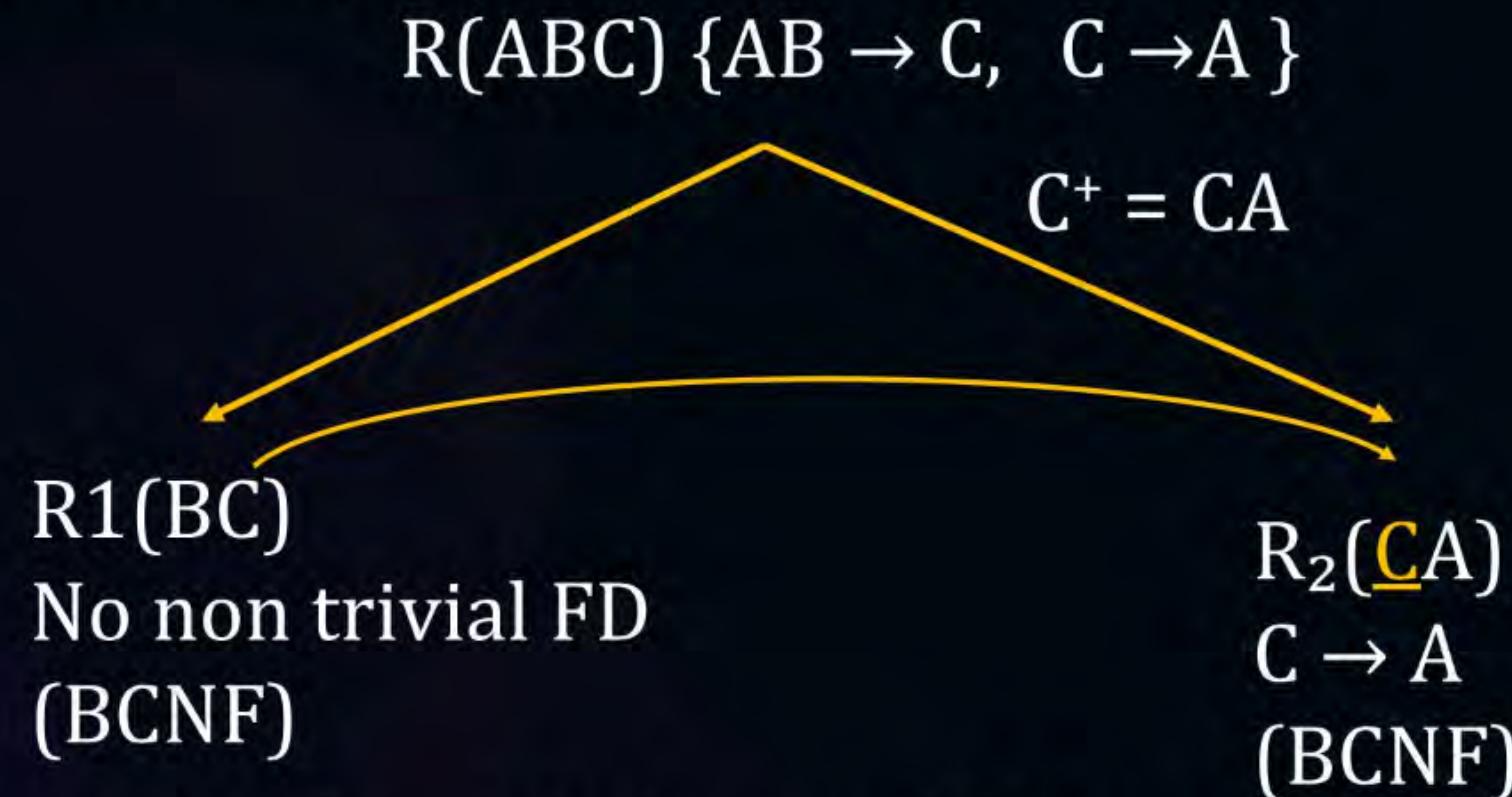
- The relation is lossless join but not DP due to the $AB \rightarrow C$.



Topic: Highest NF Decomposition

#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol Cont: BCNF decomposition:



- The relation is lossless join but not DP due to the $AB \rightarrow C$.

To preserve $AB \rightarrow C$, make a relation $R_3(ABC)$ for $AB^+ = ABC$.



Topic: Highest NF Decomposition



#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol Cont:

Now,

$R_3(ABC)$

$AB \rightarrow C$

$C \rightarrow A$

BCNF	DP
✓	✗
✗	✓

This is lossless join, DP & Not in BCNF.



Topic: Highest NF Decomposition

#Q. $R(ABC) \{AB \rightarrow C, C \rightarrow A\}$

Sol Cont.:

Now,

$$\begin{array}{l} R_3(ABC) \\ AB \rightarrow C \\ C \rightarrow A \end{array} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\}$$

This is lossless join, DP & Not in BCNF.

∴ The relation cannot be in BCNF, the highest decomposition is in 3NF.



Topic: Highest NF Decomposition

#Q. $R(ABCD) \{ABC \rightarrow D, D \rightarrow B\}$

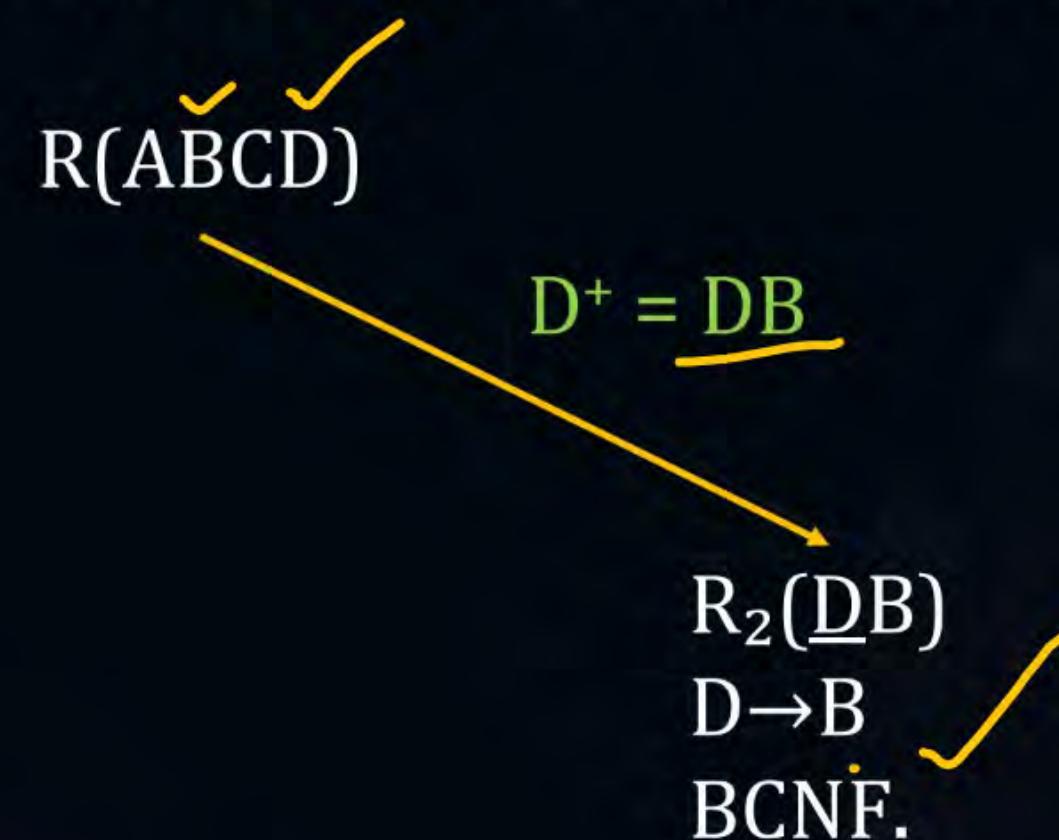
Sol: ABC and ACD are CK due to $D \rightarrow B$ the R is in 3NF but not in BCNF.



Topic: Highest NF Decomposition

#Q. $R(ABCD)$ { $ABC \rightarrow D$, $D \rightarrow B$ }

Sol: ABC and ACD are CK due to $D \rightarrow B$ the R is in 3NF but not in BCNF.



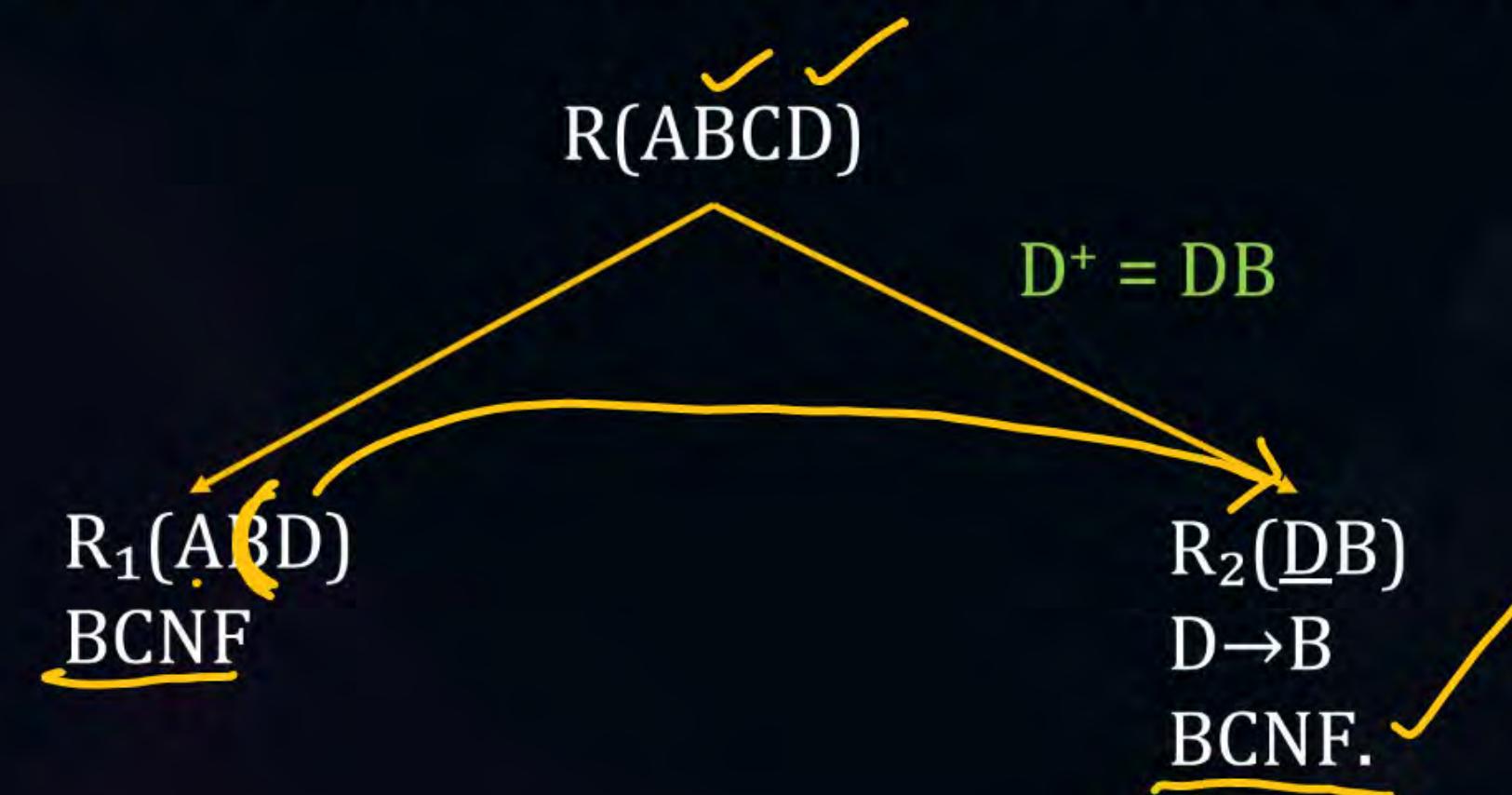


Topic: Highest NF Decomposition



#Q. $R(ABCD) \{ \underline{\underline{ABC}} \rightarrow D, D \rightarrow B \}$

Sol: ABC and ACD are CK due to $D \rightarrow B$ the R is in 3NF but not in BCNF.





Topic: Highest NF Decomposition



#Q. $R(ABCD)$ { $ABC \rightarrow D$, $D \rightarrow B$ }

Sol: ABC and ACD are CK due to $D \rightarrow B$ the R is in 3NF but not in BCNF.

LLJ (\checkmark) DP (\times) BCNF (\checkmark)
 $ABC \rightarrow D$ is lost





Topic: Highest NF Decomposition

#Q. $R(ABCD)$ { $ABC \rightarrow D$, $D \rightarrow B$ }

Sol: ABC and ACD are CK due to $D \rightarrow B$ the R is in 3NF but not in BCNF.

LLJ (✓) DP (✗) BCNF(✓)
 $ABC \rightarrow D$ is lost



- $(ABC)^+$ = ABCD if $R(ABCD)$ is one table again, again $D \rightarrow B$ comes under R which is again not in BCNF. ∴ The highest NF is 3NF.



Topic: Highest NF Decomposition



Conclusion:

Goals of DB design based on Normalization	1NF	2NF	3NF	BCNF	4NF
Lossless join decomposition	✓	✓	✓	✓ ✓	May not ✓
Dependency Preserving	✓	✓	✓	May not ✓	May not
0% redundancy	No	No	No	{yes over FD's} (No over MVD's)	Yes over FD's/ MVD's



Telegram channel





THANK - YOU