

Assignment 1A

Q2a) In 8 Puzzle Problem we are concerned with getting to goal Configuration within least number of steps. All moves are thus equally costly.

Define $g(n)$ in your own words. What will be the cost of 6 step solution to some arbitrary 8 Puzzle instance?

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The lowest path of $g(n)$ can be cost to reach the goal Configuration in least steps. In our case, we reach the final Configuration in at least moves:

UP, UP, LEFT, LEFT since all the moves are equally costly, we complete $g(n)$ as

$$g(n) = 1 + 1 + 1 + 1$$

$$g(n) = 4$$

Consider the following arbitrary 8 Puzzle instance which gives solved in 6 steps

8	7	6
2	1	5
-	3	4

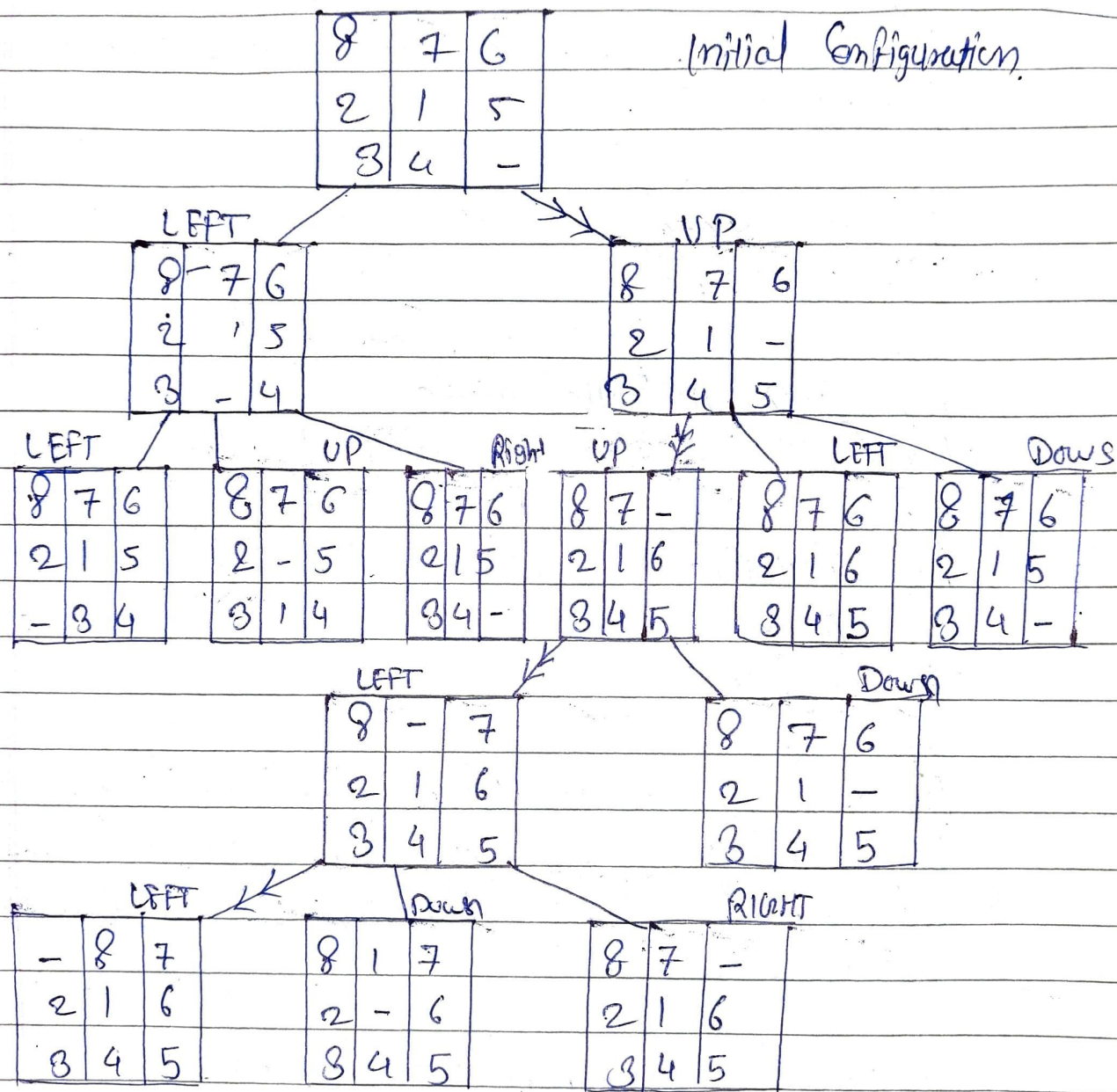
The solution can be represented as :-

$\{\{8, 7, 6\}, \{2, 1, 5\}, \{-, 3, 4\}\} \rightarrow \{\{8, 7, 6\}, \{2, 1, 5\}, \{3, -, 4\}\} \rightarrow$
 $\{\{8, 7, 6\}, \{2, 1, 5\}, \{3, 4, -\}\} \rightarrow \{\{8, 7, 6\}, \{2, 1, -\}, \{3, 4, 5\}\} \rightarrow$
 $\{\{8, 7, -\}, \{2, 1, 6\}, \{3, 4, 5\}\} \rightarrow \{\{8, -, 7\}, \{2, 1, 6\}, \{3, 4, 5\}\} \rightarrow$
 $\{\{-, 8, 7\}, \{2, 1, 6\}, \{3, 4, 5\}\}$

Since all the moves are equally costly, the
 Cost would be
 $g(n) = 6$

~~G(20)~~

Q.2(c) Draw exhaustive state space tree of depth limited to 4 for instance of 8 Puzzle Problem in the question:-



Final Configuration.

Q.2(e) Compute $h(n)$ where $i=1, 2, 3$ & $n = \text{initial state}$, goal state from question.

For $i=1$, $n = \text{initial state}$

$h_1(\text{initial}) = \text{misplace files count except space}$

$$h_1(\text{initial}) = 4$$

$n = \text{goal state}$

$$h_1(\text{goal}) = 0$$

For $i=2$, $n = \text{initial state}$

$h_2(\text{initial}) = \text{correctly replaced files count except space}$

$$h_2(\text{initial}) = 4$$

For $n = \text{goal state}$

$$h_2(\text{goal}) = 8$$

For $i=3$, $n = \text{initial state}$

$h_3(\text{initial}) = \text{sum of manhattan distance between current & correct position of all files except space}$

$$h_3(\text{initial}) = 0 + 0 + 0 + 0 + 1 + 1 + 1 + 1$$

$$= 4$$

For $n = \text{goal state}$

$$h_3(\text{goal}) = 0$$