COMPSCI 2C03 – Week 13 Exercises

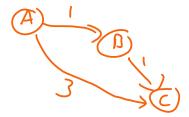
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Sample solutions and notes on sample solutions for this week's exercises.

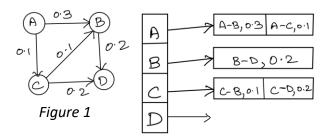
Lecture 1: Dijkstra's Algorithm

1. Exercise 4.4.1: If you add a constant to every edge weight it does not change the solution to the single-source shortest paths problem. True or False?

False. Consider the path $A \rightarrow B \rightarrow C$ vs. $A \rightarrow C$. Now add 2 to every weight.



2. Draw the SPT for source A of the edge-weighted digraph shown in Figure 1 and give the parent-link representation of the Shortest path tree (SPT) using Dijkstra's algorithm.



Start

	Α	В	С	D
dist_to	0			
edge_to				
PQ	A(0)			

Dequeue A and Relax

	Α	В	С	D
dist_to	0	0.3	0.1	
edge_to		Α	Α	
PQ	B(0.3), C(0.1)			

Dequeue C and relax

	А	В	С	D
dist_to	0	0.2	0.1	0.3
edge_to		С	Α	С
PQ	B(0.2), D(0.3)	·		·

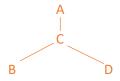
Dequeue B and relax

	А	В	С	D
dist_to	0	0.2	0.1	0.3
edge_to		С	Α	С
PQ	D(0.3)			

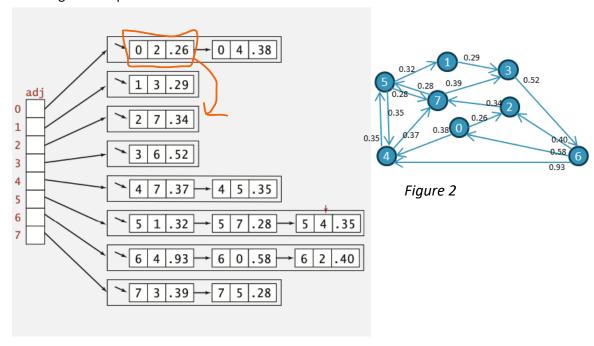
Dequeue D and relax

	А	В	С	D
dist_to	0	0.2	0.1	0.3
edge_to		С	Α	С
PQ				

Done.



3. Exercise 4.4.5 and 4.4.6: Change the direction of edge 0→2 in the edge-weighted digraph from the lecture slides and the textbook (Figure 2 below). Draw the SPT for source 2 of the resulting graph and give the parent-link representation of the Shortest path tree (SPT) using Dijkstra's algorithm. Is the resulting SPT unique?



<u>Start</u>

	0	1	2	3	4	5	6	7
dist_to			0					
edge_to								
PQ	2(0)							

Dequeue 2

	0	1	2	3	4	5	6	7		
dist_to	.26		0					.34		
edge_to	2							2		
PQ	7(.34), 0(.	7(.34), 0(.26)								

Dequeue 0

	0	1	2	3	4	5	6	7	
dist_to	.26		0		.64			.34	
edge_to	2				0			2	
PQ	7(.34), 4(.	7(.34), 4(.64)							

Dequeue 7

	0	1	2	3	4	5	6	7
dist_to	.26		0	.73	.64	.62		.34
edge_to	2			7	0	7		2
PQ	4(.64), 3(.73), 5(.62)							

Dequeue 5

	0	1	2	3	4	5	6	7
dist_to	.26	.94	0	.73	.64	.62		.34
edge_to	2	5		7	0	7		2
PQ	4(.64), 3(.73), 1(.94)							

Dequeue 4

	0	1	2	3	4	5	6	7		
dist_to	.26	.94	0	.73	.64	.62		.34		
edge_to	2	5		7	0	7		2		
PQ	3(.73), 1(.	3(.73), 1(.94)								

Dequeue 3

	0	1	2	3	4	5	6	7
dist_to	.26	.94	0	.73	.64	.62	1.25	.34
edge_to	2	5		7	0	7	3	2
PQ	1(.94), 6(1.25)							

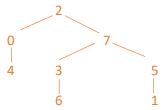
Dequeue 1

	0	1	2	3	4	5	6	7
dist_to	.26	.94	0	.73	.64	.62	1.25	.34
edge_to	2	5		7	0	7	3	2
PQ	6(1.25)							

Dequeue 6

	0	1	2	3	4	5	6	7
dist_to	.26	.94	0	.73	.64	.62	1.25	.34
edge_to	2	5		7	0	7	3	2
PQ		<u> </u>						

Done:



4. Draw the SPT for source 0 of the edge-weighted DAG shown in Figure 3, and give the parent-link representation of the Shortest path tree (SPT) using the topological sort shortest path algorithm described in the lecture.

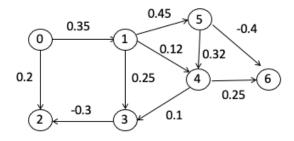
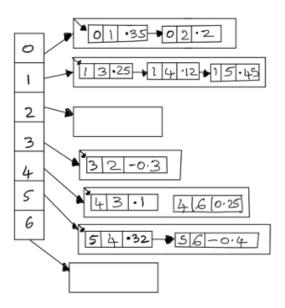
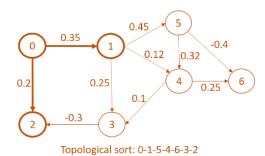


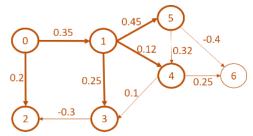
Figure 3



Topological sort using reverse post-order DFS is 0 1 5 4 6 3 2



Vertex	EdgeTo	DistTo
1	0	0.35
2	0	0.2
3		
4		
5		
6		



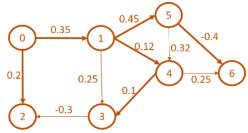
Topological sort: 0-1-5-4-6-3-2

Vertex	EdgeTo	DistTo
1	0	0.35
2	0	0.2
3	1	0.6
4	1	0.47
5	1	0.8
6		

		0.45	5	
(o)	0.35	0.12	0.32	
0.2	0.25	0.1	4 0.25	6
2	-0.3	人		

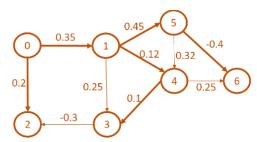
Topological sort: 0-1-5-4-6-3-2

Vertex	EdgeTo	DistTo
1	0	0.35
2	0	0.2
3	1	0.6
4	1	0.47
5	1	0.8
6	5	0.4



Topological sort: 0-1-5-4-6-3-2

Vertex	EdgeTo	DistTo
1	0	0.35
2	0	0.2
3	4	0.57
4	1	0.47
5	1	0.8
6	5	0.4



Topological sort: 0-1-5-4-6-3-2

Vertex	EdgeTo	DistTo
1	0	0.35
2	0	0.2
3	4	0.57
4	1	0.47
5	1	0.8
6	5	0.4