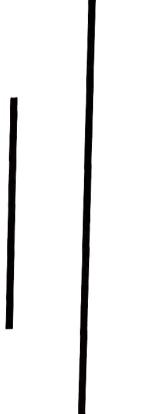


**Lab Report**  
**Of**  
**Numerical Method**  
**Subject Code: CSC207**



**Submitted To**  
**SOCH COLLEGE OF IT**  
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## List of Exercises

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Faculty Name:

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Lab Administrator Name:

Lab Administrator Signature:

External Examiner Name:

External Examiner Signature

## Title : Evaluation of Bisection Method

Objective : The objective of this experiment is to evaluate bisection method in C program.

### Basic Theory :

Bisection method is one of the iterative methods of solving the system of non-linear equations. It is also known as half Interval method. one of the first numerical methods developed to find the root of non linear equation.

This method is based on the following theorem:  
An equation  $f(x)=0$  where  $f(x)$  is a real continuous function, has at least one root between  $x_l$  and  $x_u$   
if  $f(x_l) \cdot f(x_u) < 0$ .

Note that:- If  $f(x_l) \cdot f(x_u) > 0$ , there may or may not be any root between  $x_l$  and  $x_u$ . If  $f(x_l) \cdot f(x_u) < 0$  then there may be more than one root between  $x_l$  and  $x_u$ . so the theorem only guarantees one root between  $x_l$  and  $x_u$ . Since the method is based on finding the root between two points, the method falls under the category of bracketing methods.

General rule:

- If the  $f(x_l)$  and  $f(x_u)$  have the same sign (i.e.  $f(x_l) \cdot f(x_u) > 0$ )
  - o There is no root between  $x_l$  &  $x_u$ / even no. of roots.
- If the  $f(x_l)$  and  $f(x_u)$  have opposite signs.
  - o There is an odd no. of roots.

## Algorithm:

Step-1: Start

Step-2: Define function  $f(x)$  and error ( $E$ )

Step-3: Take two initial value for root as  $x_1$  and  $x_2$ .

Step-4: Compute  $f(x_1)$  and  $f(x_2)$

Step-5: If  $f(x_1) \times f(x_2) > 0$ , Then  $x_1$  and  $x_2$  do not coverge and root does not lie in between  $x_1$  and  $x_2$  and go to step (10);  
Otherwise continue.

Step-6: ~~If~~  $f(x_1) < 0$  Then set  $a = x_1$  and  $b = x_2$   
else.  
set  $a = x_2$  and  $b = x_1$ .

Step-7: Calculate root,  $x_n = \frac{a+b}{2}$  and also calculate  $f(x_n)$ .

Step-8: If  $f(x_n) > 0$  Then, set  $b = x_n$   
else  
set  $a = x_n$

Step-9: Repeat till Step (8), until absolute value of  $\frac{b-a}{b}$  is less than  $E$ , then display root.

$$\text{Root} = \left( \frac{a+b}{2} \right).$$

Go to Step (10) Else to Step (7)

Step 10: Stop

## Executable code :-

```
#include <stdio.h>
#include <math.h>
#define f(x) pow(x,2)-4*x-10
#define e 0.0001

Void main()
{
    float x1, x2, x0;
    do
    {
        printf("Enter the value of x1 and x2 \n");
        scanf("%f %f", &x1, &x2);
        while ((f(x1)*f(x2)) > 0);
        do
        {
            x0 = (x1+x2)/2;
            if ((f(x1)*f(x2)) < 0)
            {
                x2 = x0;
            }
            else x1 = x0;
            x = (x1+x2)/2;
        } while (fabs(x0-x) > e);
        printf("root is = ", x0);
        getch();
    }
}
```

Output:

Enter the value of  $x_1$  and  $x_2$

1

-3

Root is: 0.999878

B.Sc. CSE 3rd Semester.

Numerical Methods

Lab-

- Ankit Pangani

Title: Evaluation of Newton Raphson method.

Objective: The objective of this experiment is to evaluate the Newton Raphson method in C program.

Basic Theory:-

Newton's Raphson method is another iterative method of solving system of non linear equations. It is based on the principle that if the initial guess of the root of  $f(x)=0$  is at  $x_0$ , and if one draws the tangent to the curve at  $f(x_0)$ , the point  $x_{0+}$  where the tangent crosses the x-axis is an improved estimate of the root.

It is an open method and starts with one initial guess for finding real root of non-linear equation.

In Newton Raphson method if  $x_0$  is the initial guess then the next approximated root  $x_1$  is obtained by the following formula:-

$$x_1 = x_0 - \frac{f(x_0)}{f'(x_0)}$$

If we suppose  $f'(x_0)$  as  $g(x_0)$  then  $x_1 = x_0 - \frac{f(x_0)}{g(x_0)}$

i.e. The next approximated root  $x_{n+1}$  with initial guess  $x_n$  is

$$\boxed{x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}}$$

## Algorithm:

1. Start
2. Define function as  $f(x)$
3. Define first derivative of  $f(x)$  as  $g(x)$
4. Input initial guess ( $x_0$ ), tolerable error ( $\epsilon$ ) and maximum iteration ( $N$ ).
5. Initialize iteration counter  $i=1$ .
6. If  $g(x_0)=0$  then print "Mathematical Error" and goto Step(12) otherwise goto Step(7).
7. calculate  $x_1 = x_0 - f(x_0) / g(x_0)$
8. Increment iteration counter  $i=i+1$
9. If  $i=N$  then print "Not Convergent" and goto Step(12) otherwise goto Step(10)
10. If  $|f(x_0)| > \epsilon$  then set  $x_0 = x_1$  and goto Step(6) otherwise goto (11)
11. Print root as  $x_1$
12. Stop.

## Executable code:-

```
#include <stdio.h>
#include <conio.h>
#include <math.h>
#include <stdlib.h>
#define f(x) 3*x - cos(x) - 1
#define g(x) 3 + sin(x)
void main()
{
    float x0, x1, f0, f1, g0, e;
    int step=1, N;
    clrscr();
    printf("\nEnter initial guess:\n");
    scanf("%f", &x0);
    printf("Enter tolerable error:\n");
    scanf("%f", &e);
    printf("Enter maximum iteration:\n");
    scanf("%d", &N);
    printf("\n Step | x0 | f(x0) | x1 | f(x1) |\n");
    do
    {
        g0 = g(x0);
        f0 = f(x0);
        if (g0 == 0.0)
        {
            printf("Mathematical Error.\n");
            exit(0);
        }
        x1 = x0 - f0/g0;
        printf("%d | %f | %f | %f | %f |\n",
               step, x0, f0, x1, f1);
        x0 = x1;
        step++;
    } while (step <= N);
}
```

```

step = step + 1;
if (step > N)
{
    printf("Not Convergent.");
    exit(0);
}
f1 = f(x1);
where (fabs(f1) > e);
printf("The Root is: %f", x1);
getch();
}

```

### Output:

Enter initial guess:

Enter tolerable error:

0.00001

Enter maximum iteration:

10

Step	$x_0$
1	1.000000
2	0.620016
3	0.607102

Root is: 0.607102

## Lab

### Title: Evaluation of False position (Regula Falsi) method

Objective: The objective of this experiment is to evaluate the Regula Falsi (False position) method in C program.

#### Basic Theory:

Regula Falsi is one of the bracketing and convergence guaranteed method for finding real root of non-linear equation. It starts with two initial guesses say  $x_0$  and  $x_1$  such that  $x_0$  and  $x_1$  brackets the root i.e.  $f(x_0) \cdot f(x_1) < 0$ .

It is based on the fact that if  $f(x)$  is real and continuous function, and for two initial guesses  $x_0$  and  $x_1$  brackets the root such that  $f(x_0) \cdot f(x_1) < 0$  then there exists at least one root between  $x_0$  and  $x_1$ .

If  $x_0$  and  $x_1$  are two guesses then we compute the new approximated root as:

$$x_2 = x_0 - \frac{x_1 - x_0}{f(x_1) - f(x_0)} \times f(x_0)$$

Now, we have the following three different cases:

① If  $f(x_2) = 0$  then root is  $x_2$

② If  $f(x_0) \cdot f(x_2) < 0$  then root lies between  $x_0$  &  $x_2$

③ If  $f(x_0) \cdot f(x_2) > 0$ , then root lies between  $x_1$  &  $x_2$

And then process is repeated until we have desired accuracy.

- Algorithm
- Step-1: Start
- Step-2: Define function  $f(x)$
- Step-3: Choose initial guesses  $x_0$  and  $x_1$  such that  
$$f(x_0) \cdot f(x_1) < 0$$
  
$$\begin{matrix} (-) \\ (+) \end{matrix}$$
- Step-4: Choose pre-specified tolerable error  $\epsilon$ .
- Step-5: Calculate new approximated root  $x_2$   
$$x_2 = x_0 - \frac{(x_1 - x_0) \cdot f(x_0)}{f(x_0) - f(x_1)}$$
- Step-6: Calculate  $f(x_0) * f(x_2)$   
a) If  $f(x_0) * f(x_2) < 0$  then  $x_0 = x_0$  and  $x_1 = x_2$   
b) If  $f(x_0) * f(x_2) > 0$  then  $x_0 = x_2$  and  $x_1 = x_1$   
c) If  $f(x_0) * f(x_2) = 0$  then goto Step(8).
- Step-7: If  $|f(x_2)| > \epsilon$  then goto Step(5) otherwise  
goto Step(8)
- Step-8: Display  $x_2$  as root.
- Step-9: Stop

Executable code.

```
#include <stdio.h>
#include <conio.h>
#include <math.h>
#define f(x) x*log10(x)-1.2
```

int main()

{

float  $x_0, x_1, x_2, f_0, f_1, f_2, e;$

```
int step=1;
```

Urgent (1)

Up:

```
printf("Enter two initial guesses : ");
```

Scanf("of of", &x0, &x1);

```
printf("Enter tolerable error : \n");
```

```
scanf("nof", &e);
```

$$f_0 = f(x_0);$$

$$f_j = f(x_j);$$

H ( $f_0 * f_1 > 0.0$ )

```
{ printf("Incorrect Initial Guesses.\n"); }
```

go to up;

3

```
printf("In step 1t1t x0 1t1t x1 1t1t x2 1t1t f(x2)\n");
```

do

8

$$x_2 = x_0 - (x_1 - x_0) * f_0 / (f_1 - f_0);$$

$$f_2 = f(x_2)$$

`printf("odd it is not it is not it is not it is not\n");`

$x_0, x_1, x_2, k^2)$ ;

$$\text{if } (f_0 * f_2 < 0)$$

$$\left. \begin{array}{l} x_1 = x_2; \\ f_1 = f_2; \end{array} \right\}$$

```
else  
{
```

```
    x0 = x2;
```

```
    f0 = f2;
```

```
}
```

```
step = step + 1;
```

```
}
```

```
while (fabs(f2) > e);
```

```
printf ("The Root is: %f", x2);
```

```
getch();
```

```
return 0;
```

```
}
```

## Output

Enter two initial guesses:

2

3

Enter tolerable error:

0.000001

Step	$x_0$	$x_1$	$x_2$	$f(x_2)$
1	2.000000	3.000000	2.721014	-0.017091
2	2.721014	3.000000	2.740206	-0.000384
3	2.740206	3.000000	2.740636	-0.000009
4	2.740636	3.000000	2.740646	-0.000000

Root is: 2.740646

Lab-

Title: Evaluation of Secant method.

Objective: The objective of this experiment is to evaluate Secant method in C program.

Basic Theory:

Secant method is an open method and starts ~~to~~ with initial guesses for finding real root of non-linear equations. This method requires two initial guesses, but unlike the bisection and regula falsi method, the two initial guesses do not need to bracket the root of the equation.

Suppose  $x_0$  and  $x_1$  are initial guesses. Then, the condition that  $f(x_0) \cdot f(x_1) < 0$  is not necessarily required. The secant method may or may not converge, but when it converges, it converges faster than the bisection method. However, since the derivative is approximated, it converges slower than Newton-Raphson method.

In Secant method, if  $x_0$  and  $x_1$  are initial guesses, then next approximated root  $x_2$  is obtained by:

$$x_2 = x_1 - \frac{(x_1 - x_0) \cdot f(x_1)}{f(x_1) - f(x_0)}$$

And an algorithm for Secant method involves repetition of above process i.e. we use  $x_1$  &  $x_2$  to find  $x_3$  & so on until we find root within desired accuracy.

## Algorithm:

Step-1: Start.

Step-2: Define function as  $f(x)$

Step-3: Input initial guesses  $x_0$  and  $x_1$ ,  
tolerable error ( $e$ ) and maximum iteration ( $N$ )

Step-4: Initialize iteration counter  $i=1$

Step-5: If  $f(x_0) = f(x_1)$  then print "Mathematical Error"  
and goto Step(11) otherwise goto step(6)

Step-6: Calculate  $x_2 = x_1 - \frac{(x_1 - x_0) * f(x_1)}{(f(x_2) - f(x_0))}$

Step-7: Increment iteration counter  $i=i+1$

Step-8: If  $i > N$  then print "Not Convergent"  
and goto Step(11) otherwise goto Step(9)

Step-9: If  $|f(x_2)| > e$  then set  $x_0 = x_1$ ,  $x_1 = x_2$   
and goto Step(5) otherwise goto Step(10)

Step-10: Print result as  $x_2$

Step-11: Stop.

## Executable code:

```
#include <stdpo.h>
#include <conpo.h>
#include <math.h>
#include <stdlib.h>
#define f(x) x*x*x - 2*x - 5

void main()
{
    float x0, x1, x2, f0, f1, f2, e;
    int step=1, N;
    clrscr();
    printf("Enter initial guesses :\n");
    scanf("%f %f", &x0, &x1);
    printf("Enter tolerable error :\n");
    scanf("%f", &e);
    printf("Enter maximum iteration :\n");
    scanf("%d", &N);
    printf("\n Step 1 : x0 = %f x1 = %f x2 = %f f(x2) = %f\n", x0, x1, x2, f(x2));
    do {
        f0 = f(x0); f1 = f(x1);
        if (f0 == f1)
        {
            printf("Mathematical Error.");
            exit(0);
        }
        x2 = x1 - (x1 - x0) * f1 / (f1 - f0);
        f2 = f(x2);
        printf("\n Step %d : x0 = %f x1 = %f x2 = %f f(x2) = %f\n", step, x0, x1, x2, f2);
        step++;
        if (abs(f2) < e)
            break;
    } while (step < N);
}
```

$x_0 = x_1$ ;  $f_0 = f_1$ ;  $x_1 = x_2$ ;  $f_1 = f_2$ ;

Step = step + 1;

If (step > N)

{

printf ("Not Convergent.");  
exit(0);

}

While (fabs (f2) > e);

printf ("In Root is: %of", x2);

getch();

}

Output:

Enter initial guesses:

1

2

Enter tolerable error:

0.00001

Enter maximum iteration:

10

Step	$x_0$	$x_1$	$x_2$	$f(x_2)$
1	1.000000	2.000000	2.200000	1.248001
2	2.000000	2.200000	2.088968	-0.062124
3	2.200000	2.088968	2.094233	-0.003554
4	2.088968	2.094233	2.094553	0.000012
5	2.094233	2.094553	2.094552	0.000001

Root is: 2.094552.

Title: Evaluation of Fixed Point Iteration method

Objective: The objective of this experiment is to evaluate ~~base~~ fixed point iteration method in C program.

Basic Theory:

Fixed point iteration method is open and simple method for finding real root of non-linear equation by successive approximation. It requires only one initial guess to start. Since it is open method its convergence is not guaranteed. This method is also known as iterative method.

To find the root of non-linear equation  $f(x)=0$  by fixed point iteration method, we write given equation  $[f(x)=0]$  in the form of  $[x=g(x)]$

If  $x_0$  is initial guess then next approximated root in this method is obtained by [general form  $[x_{n+1}=g(x_n)]$ ]

$$[x_1=g(x_0)]$$

And similarly,  $[x_2=g(x_1)]$  and so on. The process is repeated until we get root with desired accuracy.

Note: While expressing  $f(x)=0$  to  $x=g(x)$ , we can have many different forms. For convergence following criteria must be satisfied:

$$[|g'(x)| < 1]$$

## Algorithm

Step-1: Start

Step-2: Define function  $f(x)$

Step-3: Define function  $g(x)$  which is obtained from  $f(x)=0$  such that  $x=g(x)$  and  $|g'(x)| < 1$

Step-4: Choose initial guess  $x_0$ , Tolerable error 'e' and Maximum Iteration 'N'.

Step-5: Initialize iteration counter: Step=1

Step-6: Calculate  $x_1 = g(x_0)$

Step-7: Increment iteration counter: Step=Step+1

Step-8: If Step > N then print "Not Convergent" and goto Step(12) otherwise goto Step(10)

Step-9: Set  $x_0=x_1$  for next iteration.

Step-10: If  $|f(x_0)| > e$  then goto Step(16) otherwise goto Step(11)

Step-11: Display  $x_1$  as root

Step-12: Stop.

## Executable code:

```
#include <stdio.h>
#include <conio.h>
#include <math.h>
#define f(x) cos(x)-3*x+1
#define g(x) (1+cos(x))/3

int main()
{
    int step=1, N;
    float x0, xs, e;
    clrscr();
    printf("Enter initial guess:");
    scanf("%f", &x0);
    printf("Enter tolerable error:");
    scanf("%f", &e);
    printf("Enter maximum iteration:");
    scanf("%d", &N);
    printf("In Step %d x0 is %f f(x0) is %f x1 is %f f(x1) is %f\n", step,
          x0, f(x0), xs, f(xs));
    do
    {
        xs = g(x0);
        printf("Step %d x0 is %f f(x0) is %f x1 is %f f(x1) is %f\n", step,
              x0, f(x0), xs, f(xs));
        x0 = xs;
        step++;
    } while(fabs(f(xs))>e);
    printf("Root is %f", xs);
    getch();
    return 0;
}
```

Output :

Enter initial guess: 1

Enter tolerable error: 0.000001

Enter maximum iteration: 10

Step	$x_0$	$f(x_0)$	$x_1$	$f(x_1)$
1	1.000000	-1.459698	0.513434	0.330761
2	0.513434	0.330761	0.623688	-0.059333
3	0.623688	-0.059333	0.603910	0.011391
4	0.603910	0.011391	0.607707	-0.002162
5	0.607707	-0.002162	0.606986	0.000411
6	0.606986	0.000411	0.607124	-0.000078
7	0.607124	-0.000078	0.607098	0.000015
8	0.607098	0.000015	0.607102	-0.000003
9	0.607102	-0.000003	0.607102	+0.00001

Root is 0.607102.

Lab -

Title: Evaluation of Lagrange Interpolation.

Objective: The objective of this experiment is to evaluate the Lagrange Interpolation in C program.

Basic Theory:

Suppose we have following sets of data tabulated for x (independent variable) and y (dependant variable).

x	$x_0$	$x_1$	$x_2$	---	$x_n$
y	$y_0$	$y_1$	$y_2$	---	$y_n$

Then the method of finding the value of  $y=f(x)$  corresponding to any value  $x=x_i$  within  $x_0$  and  $x_n$  is called interpolation. Thus interpolation is the process of finding the value of function for any intermediate value of independent variable. If we need to estimate the value of function  $f(x)$  outside the tabular values, then the process is called extrapolation. However, in general extrapolation is also included in interpolation.

There are different methods of interpolation ex: Lagrange interpolation, newtons divided difference interpolation, newtons forward difference interpolation, newtons backward difference interpolation, etc.

Here, we discuss about Lagrange interpolation.

Lagrange's Interpolation formula is given by

$$P_n(x) = \sum_{j=0}^n f(x_j) l_j(x) \quad \text{where, } l_j(x) = \prod_{j=0, j \neq i}^n \frac{(x-x_j)}{(x_i-x_j)}$$

It's general formula is given by:  
 $\Rightarrow$  If  $y = f(x)$  takes the value of  $y_0, y_1, y_2, y_3 \dots y_n$  corresponding to  $x_0, x_1, x_2, x_3, \dots, x_n$ . Then

$$y = f(x) = (x-x_1)(x-x_2) \dots (x-x_n) + y_0 / (x_0-x_1)(x_0-x_2) \\ \dots (x_0-x_n) + (x-x_0)(x-x_2) \dots (x-x_n) * y_1 / (x_1-x_0)(x_1-x_2) \dots (x_1-x_n) + \dots + (x-x_1) \\ (x-x_2) \dots (x-x_{n-1}) * y_n / (x_n-x_0)(x_n-x_1) \dots (x_n-x_{n-1})$$

is known as Lagrange Interpolation formula for unequal intervals & is very simple to implement on computer.

## Algorithm

Step-1: Start

Step-2: Read number of data ( $n$ )

Step-3: Read data  $x_i$  and  $y_i$  for  $i=1$  to  $n$ .

Step-4: Read value of independent variables say  $x_p$  whose corresponding value of dependent say  $y_p$  is to be determined.

Step-5: Initialize  $y_p = 0$

Step-6: For  $i=1$  to  $n$

Set  $p = 1$

For  $j=1$  to  $n$

If  $i \neq j$  then

calculate  $p = p * (x_p - x_j) / (x_i - x_j)$

End if

Next  $j$

calculate  $y_p = y_p + p * y_i$

Next  $i$

Step-7: Display value of  $y_p$  as interpolated value.

Step-8: Stop.

## Newton's code:

```
#include <stdio.h>
#include <conio.h>

void main()
{
    float x[100], y[100], xp, yp=0, p;
    int i, j, n;
    clrscr();
    printf("Enter number of data:");
    scanf("%d", &n);
    printf("Enter data:\n");
    for(p=0; p<n; p++)
    {
        printf("x[%d] = ", p);
        scanf("%f", &x[p]);
        printf("y[%d] = ", p);
        scanf("%f", &y[p]);
    }
    printf("Enter interpolation point:");
    scanf("%f", &xp);
    for(i=j; i<n; i++)
    {
        p=j;
        for(j=j; j<=n; j++)
        {
            if(p==j)
            {
                p=p*(xp-x[j])/(x[i]-x[j]);
            }
            else
                yp=yp+p*y[j];
        }
    }
}
```

```
printf("Interpolated value at 70.3f is %0.3f.", xp, yp);
getch();
y
```

### Output:

Enter number of data: 5

Enter data:

$$x[1] = 5$$

$$y[1] = 150$$

$$x[2] = 7$$

$$y[2] = 392$$

$$x[3] = 11$$

$$y[3] = 1452$$

$$x[4] = 13$$

$$y[4] = 2366$$

$$x[5] = 17$$

$$y[5] = 5202$$

Enter interpolation point: 9

Interpolated value at 9.000 is 810.000

Lab - 07

## Title: Evaluation of Newton's Divided Difference Interpolation.

Objective: The objective of this experiment is to evaluate the Newton's divided difference interpolation in a C program.

### Basic Theory:

Newton's divided difference interpolation is one of the interpolation technique used when the interval difference is not same for all sequence of values.

Let us consider a polynomial of degree  $n$  of the form

$$P_n(x) = a_0 + a_1(x-x_0) + a_2(x-x_0)(x-x_1) + \dots + a_n(x-x_0)(x-x_1)\dots(x-x_{n-1})$$

To construct the polynomial we need to find coefficients  $a_0, a_1, a_2, \dots, a_n$ . Suppose  $x_0, x_1, x_2, \dots, x_n$  be given interpolating points &  $f(x_0), f(x_1), f(x_2), \dots, f(x_n)$  be the  $(n+1)$  values of function  $y=f(x)$  corresponding to  $x_0, x_1, x_2, \dots, x_n$ . Where interval difference are not same.

Then first divided difference is given by

$$f[x_0, x_1] = \frac{f(x_1) - f(x_0)}{x_1 - x_0}$$

Second divided difference is given by

$$f[x_0, x_1, x_2] = \frac{f[x_2, x_1] - f[x_1, x_0]}{x_2 - x_0} \quad \text{and so on.}$$

Which gives the Newton's Dividend Difference formula:

$$P_n(x) = f(x) = f(x_0) + (x-x_0)f[x_1, x_0] + (x-x_0)(x-x_1)f[x_2, x_1, x_0] + \dots + (x-x_0)(x-x_1)\dots(x-x_{n-1})f[x_n, \dots, x_2, x_1, x_0]$$

## Algorithm.

Step-1: Start

Step-2: Read the number of points, say  $n$ .

Step-3: Read the value at which interpolated value is needed, say  $x$

Step-4: Read given data points.

Step-5: Calculate first divided difference as  
For  $i=0$  to  $n-1$   
 $dd[i] = f[x[i]]$

End For

Step-6: Calculate second to  $n$ th divided differences as

For  $p=0$  to  $n-1$

$$\text{for } j=n-1 \text{ to } p+1 \\ dd[j] = \frac{dd[j] - dd[j-1]}{x[j] - x[j-1-p]}$$

End For.

End for.

Step-7: Set  $v=0$  and  $p=1$

Step-8: Calculate interpolated value as

For  $p=0$  to  $n-1$

For  $j=0$  to  $p-1$

$$P = P * (x - x_j)$$

End For

$$v = v + dd[p]*P$$

Reset  $P=1$

End For

Step-9: Print the interpolated value  $v$

Step-10: Terminate.

## Executable code.

```
#include <stdio.h>
#include <conio.h>
int main()
{
    int n, i, j;
    float v=0, p, xv, x[10], fx[10], a[10];
    printf("Enter the number of points |n|");
    scanf("%d", &n);
    printf("Enter the value of x |n|");
    scanf("%f", &xv);
    for (i=0; i<n; i++)
    {
        printf("Enter the value of x and fx at i=%d |n|, %f");
        scanf("%f %f", &x[i], &fx[i]);
    }
    for (i=0; i<n; i++)
        a[i] = fx[i];
    for (p=0; p<n; p++)
    {
        for (j=n-1; j > p; j--)
            a[j] = (a[j] - a[j-1]) / (x[j] - x[j-1-p]);
    }
    v=0;
    for (p=0; p<n; p++)
    {
        p = 1;
        for (j=0; j <= p; j++)
            p = p * (xv - x[j]);
        v = v + a[p] * p;
    }
    printf("Interpolation Value = %f", v);
    getch();
    return 0;
}
```

## Output

Enter the number of points

4

Enter the value of  $x$

1.3

Enter the value of  $x$  and  $f(x)$  at  $i=0$

0.5 0.4794

Enter the value of  $x$  and  $f(x)$  at  $i=1$

1 0.8415

Enter the value of  $x$  and  $f(x)$  at  $i=2$

1.5 0.9975

Enter the value of  $x$  and  $f(x)$  at  $i=3$

2.0 0.9093

Interpolation value = 0.962270