

# Assignment 1

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CE20RESCH13001

## PROBLEM II (2I)

Find the distance between points  $\begin{pmatrix} 7 \\ 6 \end{pmatrix}$  and  $\begin{pmatrix} 4 \\ 5 \end{pmatrix}$  with the axes at  $60^\circ$

The distance between points is  $\left\| \begin{pmatrix} x_3 \\ y_3 \end{pmatrix} - \begin{pmatrix} x_4 \\ y_4 \end{pmatrix} \right\| = \left\| \begin{pmatrix} 10 \\ 3\sqrt{3} \end{pmatrix} - \begin{pmatrix} \frac{13}{2} \\ \frac{5\sqrt{3}}{2} \end{pmatrix} \right\| = \sqrt{13} \text{ units}$

### 1 SOLUTION

Let the points be

$$\begin{pmatrix} x_1 \\ y_1 \end{pmatrix} = \begin{pmatrix} 4 \\ 5 \end{pmatrix}; \begin{pmatrix} x_2 \\ y_2 \end{pmatrix} = \begin{pmatrix} 7 \\ 6 \end{pmatrix} \quad (1.0.1)$$

In order to convert to rectangular coordinate system, the y-axis should be rotated by  $30^\circ$  in anti-clockwise. Transformed coordinates of  $\begin{pmatrix} x_1 \\ y_1 \end{pmatrix}$  &  $\begin{pmatrix} x_2 \\ y_2 \end{pmatrix}$

be  $\begin{pmatrix} x_3 \\ y_3 \end{pmatrix}$  &  $\begin{pmatrix} x_4 \\ y_4 \end{pmatrix}$  respectively.

$$x_3 = OX_1 + X_1X_3 = x_1 + y_1 \cos 60^\circ$$

$$y_3 = OY_1 \cos 30^\circ = y_1 \cos 30^\circ$$

$$\begin{pmatrix} x_3 \\ y_3 \end{pmatrix} = \begin{pmatrix} 1 & \cos 60^\circ \\ 0 & \cos 30^\circ \end{pmatrix} \begin{pmatrix} x_1 \\ y_1 \end{pmatrix} \quad (1.0.2)$$

Similarly,

$$x_4 = OX_2 + X_2X_4 = x_2 + y_2 \cos 60^\circ$$

$$y_4 = OY_2 \cos 30^\circ = y_2 \cos 30^\circ$$

$$\begin{pmatrix} x_4 \\ y_4 \end{pmatrix} = \begin{pmatrix} 1 & \cos 60^\circ \\ 0 & \cos 30^\circ \end{pmatrix} \begin{pmatrix} x_2 \\ y_2 \end{pmatrix} \quad (1.0.3)$$

The generalised equation for transformed coordinates  $\begin{pmatrix} x_t \\ y_t \end{pmatrix}$  when the angle between axes ' $\theta$ ' is,

$$\begin{pmatrix} x_t \\ y_t \end{pmatrix} = \begin{pmatrix} 1 & \cos(\theta) \\ 0 & \sin(\theta) \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} \quad (1.0.4)$$

Substituting (1.0.1) in (1.0.2) & (1.0.3)

$$\begin{pmatrix} x_3 \\ y_3 \end{pmatrix} = \begin{pmatrix} \frac{13}{2} \\ \frac{5\sqrt{3}}{2} \end{pmatrix}; \begin{pmatrix} x_4 \\ y_4 \end{pmatrix} = \begin{pmatrix} 10 \\ 3\sqrt{3} \end{pmatrix} \quad (1.0.5)$$

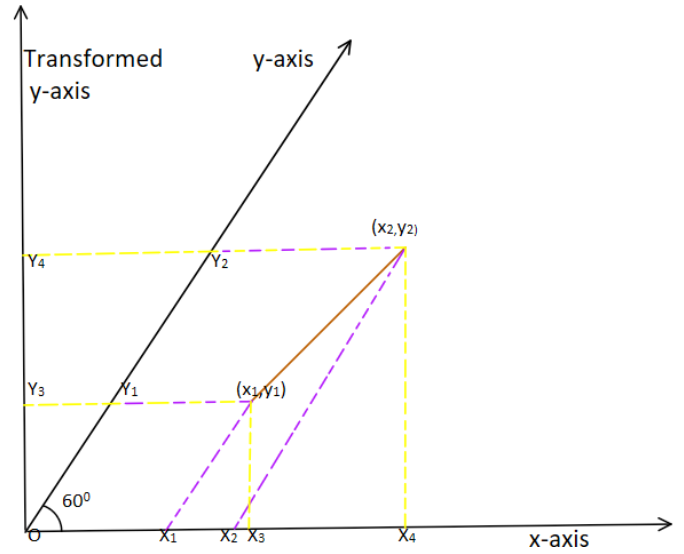


Fig1: Points defined on angular & rectangular axes

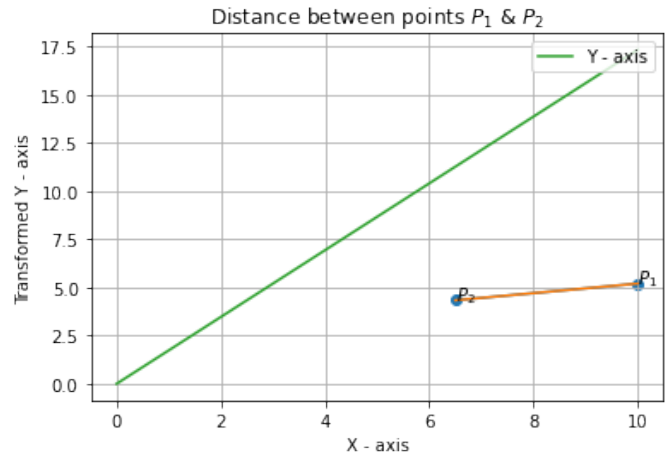


Fig2: Points plotted in Python