# Assignment 1

## S Prithvi CE20RESCH13001

### PROBLEM II (2I)

Find the distance between points (7,6) and (4,5) with the axes at  $60^{\circ}$ 

#### 1 Solution

Let the points be  $P_1$  (7,6) and  $P_2$  (4,5) and also the angle between axes is  $60^{\circ}$ 

$$\mathbf{P_1} = \begin{pmatrix} 7 \\ 6 \end{pmatrix} \; ; \; \mathbf{P_2} = \begin{pmatrix} 4 \\ 5 \end{pmatrix} \tag{1.0.1}$$

The problem can be solved by transformation of the given coordinate system to the rectangular coordinate system.

In order to convert to rectangular coordinate system, the y-axis should be rotated by 30° in anti-clockwise and x-axis will remain unaltered.

The transformation matrix should be computed for transforming the given  $P_1, P_2$  into the rectangular coordinate system.

The angle between the transformed x-axis and given x-axis be  $\theta_{11}=0^{\circ}$ 

The angle between the transformed x-axis and given y-axis be  $\theta_{12} = 60^{\circ}$ 

Likewise,  $\theta_{21} = 90^{\circ}$ ;  $\theta_{22} = 30^{\circ}$ 

Transformed matrix T will be the cosines of the above the angles

$$\mathbf{T} = \begin{pmatrix} \cos(\theta_{11}) & \cos(\theta_{12}) \\ \cos(\theta_{21}) & \cos(\theta_{22}) \end{pmatrix}$$
$$= \begin{pmatrix} \cos(0^{\circ}) & \cos(60^{\circ}) \\ \cos(90^{\circ}) & \cos(30^{\circ}) \end{pmatrix}$$

$$\mathbf{T} = \begin{pmatrix} 1 & 0.5 \\ 0 & 0.866 \end{pmatrix} \tag{1.0.2}$$

From equations (1.0.1) and (1.0.2), the transformed vector corresponding to  $P_1$  be  $P_{1T} = T * P_1$ 

Transformed vector corresponding to  $P_2$  be  $P_{2T} = T * P_2$ 

$$\mathbf{P_{1T}} = \begin{pmatrix} 1 & 0.5 \\ 0 & 0.866 \end{pmatrix} * \begin{pmatrix} 7 \\ 6 \end{pmatrix}; \mathbf{P_{2T}} = \begin{pmatrix} 1 & 0.5 \\ 0 & 0.866 \end{pmatrix} * \begin{pmatrix} 4 \\ 5 \end{pmatrix}$$

$$\implies \mathbf{P_{1T}} = \begin{pmatrix} 10 \\ 5.2 \end{pmatrix}; \mathbf{P_{2T}} = \begin{pmatrix} 6.5 \\ 4.33 \end{pmatrix}$$

Now, obtained points are in the rectangular coordinate system and the distance vector between points will be  $P_{12T} = P_{1T} - P_{2T}$  and the magnitude will be  $\|P_{12T}\|$ 

Therefore, the distance between the points is equal to 3.606 *units* 

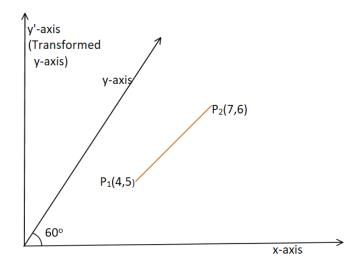


Fig: Distance between two points

\*Python code file

https://github.com/Prithvi-Sangani/ SM5083\_Assignment1/blob/main/ Assignment1.ipynb