

A confidence interval (CI) gives a plausible range for a **population** parameter p by using outcomes from a sample

$(1 - \alpha)100\%$ two-sided CI finds LB and UB such that $P(LB \leq p \leq UB) = 1 - \alpha$ and the CI is denoted by (LB, UB)

$(1 - \alpha)100\%$ one-sided lower bound CI finds LB such that $P(LB \leq p) = 1 - \alpha$ and the CI is denoted by (LB, ∞)

$(1 - \alpha)100\%$ one-sided upper bound CI finds UB such that $P(p \leq UB) = 1 - \alpha$ and the CI is denoted by $(-\infty, UB)$

Given: X_1, X_2, \dots, X_n are random samples i.e. they are **independent and identically distributed**

Assumption	X_i 's are from a normal distribution with unknown mean and known variance	X_i 's are from any distribution with unknown mean and unknown variance and $n > 40$	X_i 's are from normal distribution with unknown mean and unknown variance and $n < 40$
Population parameter to be estimated	Mean	Mean	Mean
$(1 - \alpha)100\%$ two-sided confidence interval	$\left(\bar{x} - z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}, \bar{x} + z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}} \right)$	$\left(\bar{x} - z_{\frac{\alpha}{2}} \frac{s}{\sqrt{n}}, \bar{x} + z_{\frac{\alpha}{2}} \frac{s}{\sqrt{n}} \right)$	$\left(\bar{x} - t_{\frac{\alpha}{2}, n-1} \frac{s}{\sqrt{n}}, \bar{x} + t_{\frac{\alpha}{2}, n-1} \frac{s}{\sqrt{n}} \right)$
Sample size for CI of width w	$\left(\frac{2z_{\alpha/2}\sigma}{w} \right)^2$	$\left(\frac{2z_{\alpha/2}s}{w} \right)^2$	N/A
$(1 - \alpha)100\%$ one-sided upper bound CI	$\left(-\infty, \bar{x} + z_{\alpha} \frac{\sigma}{\sqrt{n}} \right)$	$\left(-\infty, \bar{x} + z_{\alpha} \frac{s}{\sqrt{n}} \right)$	$\left(-\infty, \bar{x} + t_{\alpha, n-1} \frac{s}{\sqrt{n}} \right)$
$(1 - \alpha)100\%$ one-sided lower bound CI	$\left(\bar{x} - z_{\alpha} \frac{\sigma}{\sqrt{n}}, \infty \right)$	$\left(\bar{x} - z_{\alpha} \frac{s}{\sqrt{n}}, \infty \right)$	$\left(\bar{x} - t_{\alpha, n-1} \frac{s}{\sqrt{n}}, \infty \right)$