

Mini-batch gradient descent

Batch vs. mini-batch gradient descent

Vectorization allows you to efficiently compute on m examples.

$$\begin{array}{c}
X = \begin{bmatrix} X^{(1)} & X^{(2)} & X^{(3)} & \dots & X^{(2nn)} \\ X^{(2n)} & X^{(2n)} & X^{(2nn)} & \dots & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & \dots & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & \dots & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)} \\ X^{(2nn)} & X^{(2nn)} & X^{(2nn)} & X^{(2nn)$$

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| Good example)

| For X_{eq3} x_{eq3} x_{eq3} |

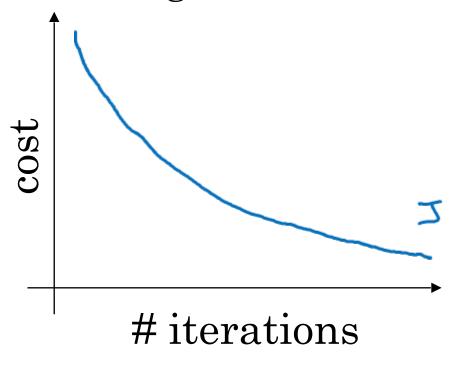
| For X_{eq3} x_{eq4} x_{eq3} x_{eq4} x Compute cost $J_{i=1000}^{i=1} = \frac{1}{1000} = \frac{1}{1000} = \frac{1}{2.1000} = \frac{1}{2$ Bookprop to compart growths cort Jees (usy (x8es Y8es)) Mic Mes - 48 mm, Persi - Pres - especies "I epoch" poss through training set.



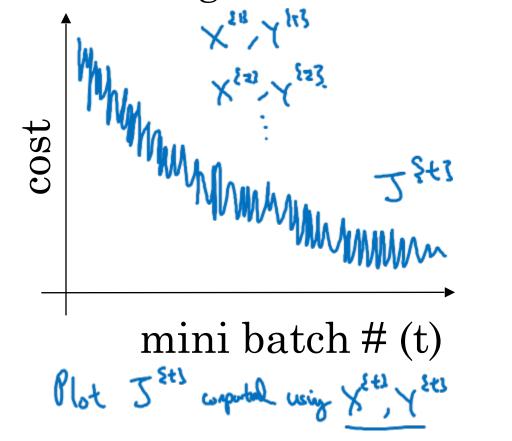
Understanding mini-batch gradient descent

Training with mini batch gradient descent

Batch gradient descent



Mini-batch gradient descent



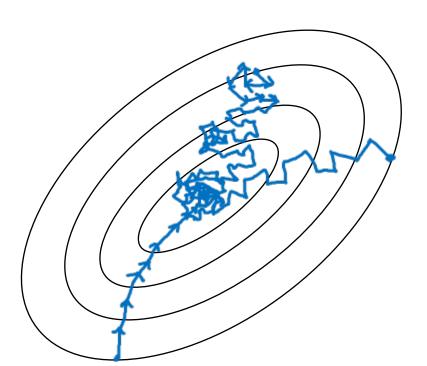
Choosing your mini-batch size The mini-batch size = m : Bootch goding desent.

 $(X_{\xi i\hat{i}}, \lambda_{\xi i\hat{i}}) = (X^*X)^*$

Every excuple is it our

> If Min=both size=1: Stochacte growth descet. Every excepte is (X stockete growth descet. (x to y) min=both.

In practice: Somewh in-between I all m



Stochostic gredent Descent

ton vorterior

In-bother Cominthooks size not to by/small

Fustest learning.

· Vectorzoti en . (ns and)

· Make poon without processing extinc tray soc.

Bootch godiet desut (min; both size = m)

Two long per iteration

Andrew Ng

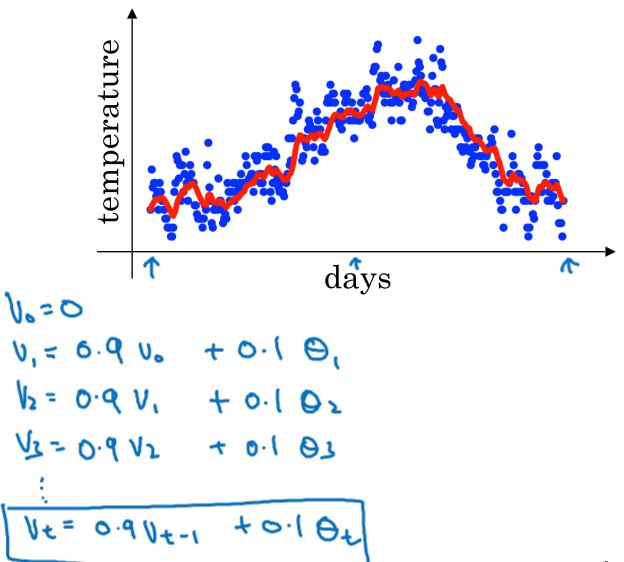
Choosing your mini-batch size

If small tray set: Use booth graher desient.
(m = 2000) Typical mint-botch sizes! -> 64, 128, 256, 512 26 22 28 2° 1024 Make sure ministrate fire in CPU/GPU memory. X EX3 Y SKI

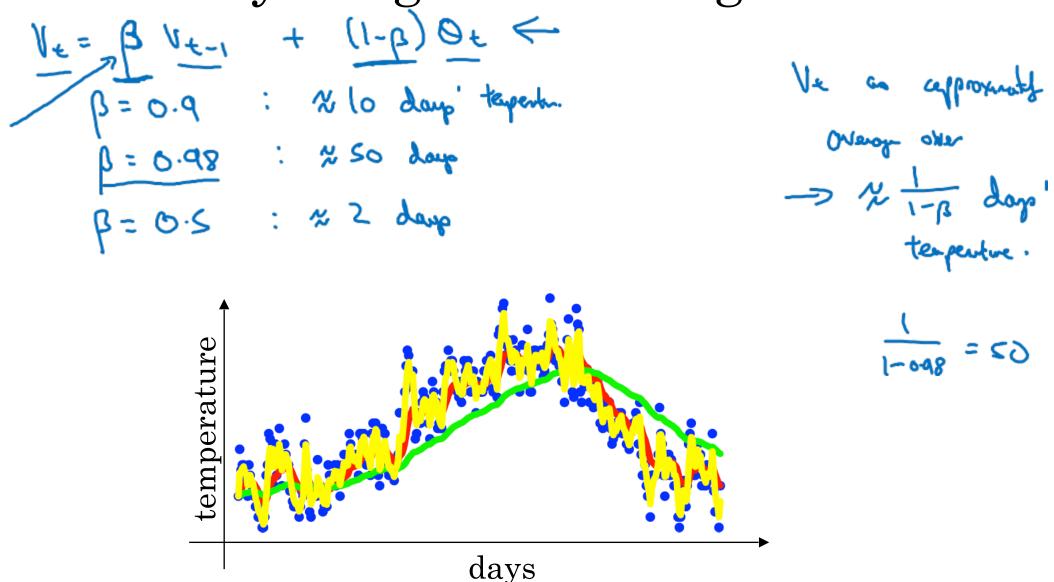


Exponentially weighted averages

Temperature in London



Exponentially weighted averages

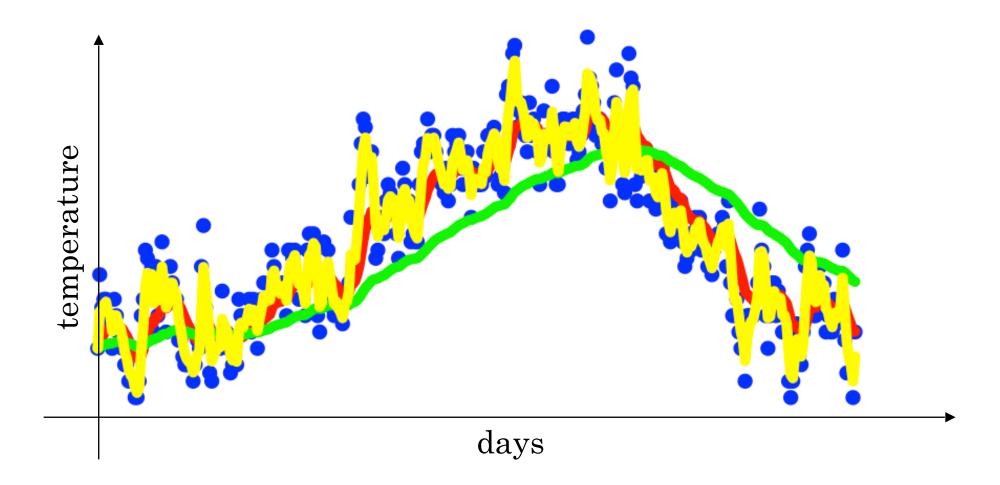




Understanding exponentially weighted averages

Exponentially weighted averages

$$v_t = \beta v_{t-1} + (1 - \beta)\theta_t$$



Exponentially weighted averages $v_t = \beta v_{t-1} + (1-\beta)\theta_t$

$$v_{100} = 0.9v_{99} + 0.1\theta_{100}$$

$$v_{99} = 0.9v_{98} + 0.1\theta_{99}$$

$$v_{98} = 0.9v_{97} + 0.1\theta_{98}$$

$$v_{100} = 0.1\theta_{100} + 0.9\theta_{100}$$

$$v_{100} = 0.1\theta_{100} + 0.1\theta_{100}$$

$$v_{100} = 0.9v_{99} + 0.1\theta_{10$$

Implementing exponentially weighted averages

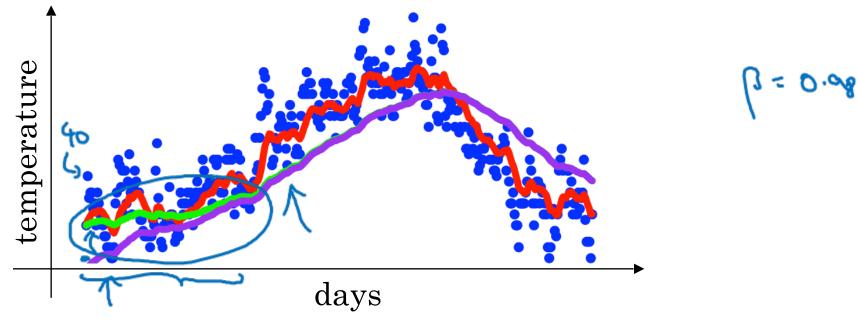
$$v_0 = 0$$

 $v_1 = \beta v_0 + (1 - \beta) \theta_1$
 $v_2 = \beta v_1 + (1 - \beta) \theta_2$
 $v_3 = \beta v_2 + (1 - \beta) \theta_3$
...



Bias correction in exponentially weighted average

Bias correction



$$v_{t} = \beta v_{t-1} + (1 - \beta)\theta_{t}$$

$$V_{t} = 0$$

$$V_{t} = 0.98 V_{0} + 0.02 \Theta_{1}$$

$$V_{2} = 0.98 V_{0} + 0.02 \Theta_{2}$$

$$= 0.98 \times 0.02 \times \Theta_{1} + 0.02 \Theta_{2}$$

$$= 0.98 \times 0.02 \times \Theta_{1} + 0.02 \Theta_{2}$$

$$= 0.0196 \Theta_{1} + 0.02 \Theta_{2}$$

$$\frac{V_{t}}{1-\beta^{t}}$$

$$t=2: 1-\beta^{t} = 1-(0.98)^{2} = 0.0396$$

$$\frac{V_{t}}{0.0396} = \frac{0.01960 + 0.020}{0.0396}$$
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Gradient descent with momentum

Gradient descent example Monatur: Corporte DW, Db " Vo = B Up + (1-p) OE" W= W- a Van deeplearning ai

Implementation details

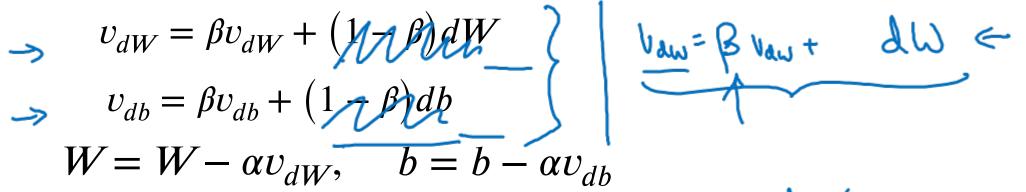
On iteration t:

Compute dW, db on the current mini-batch

$$v_{dW} = \beta v_{dW} + (1 - \beta) dW$$

$$v_{db} = \beta v_{db} + (1 - \beta)db$$

$$W = W - \alpha v_{dW}, \quad b = \overline{b} - \alpha v_{dl}$$

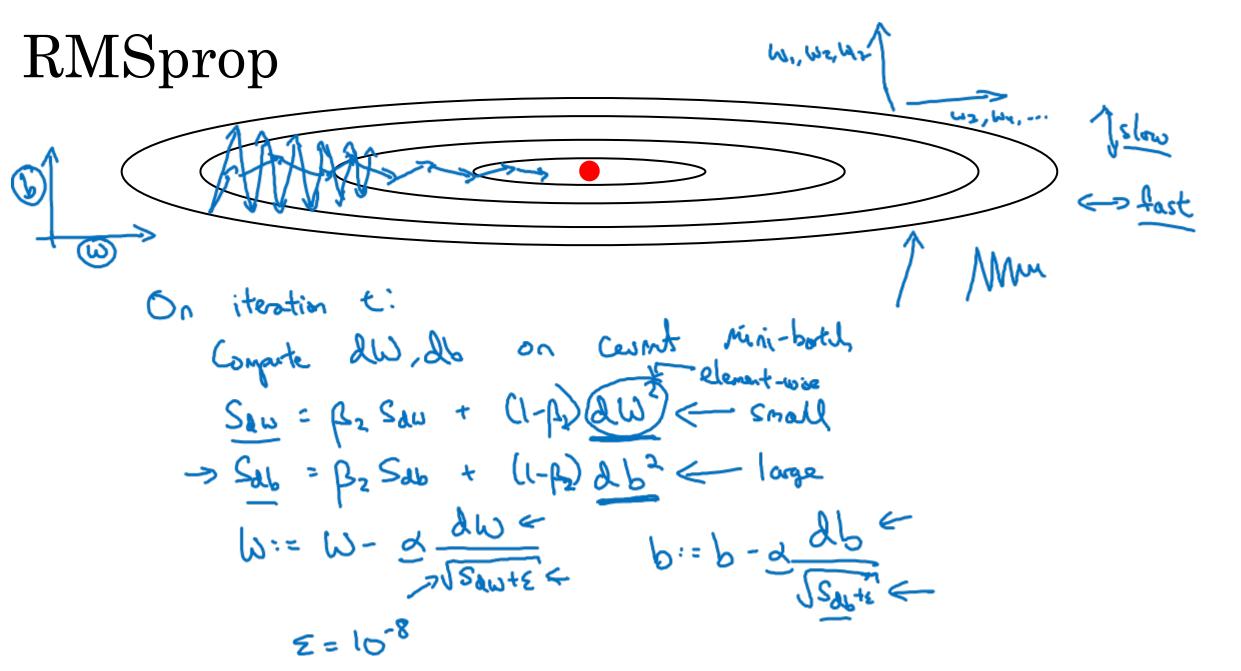


Hyperparameters:
$$\alpha, \beta$$

$$\beta = 0.9$$



RMSprop





Adam optimization algorithm

Adam optimization algorithm

Hyperparameters choice:

$$\rightarrow$$
 α : needs to be tune
 \rightarrow β_1 : 0.9 \longrightarrow ($\Delta\omega$)
 \rightarrow β_2 : 0.999 \longrightarrow ($\Delta\omega^2$)
 \rightarrow Σ : 10-8

Adam: Adapter moment estimation

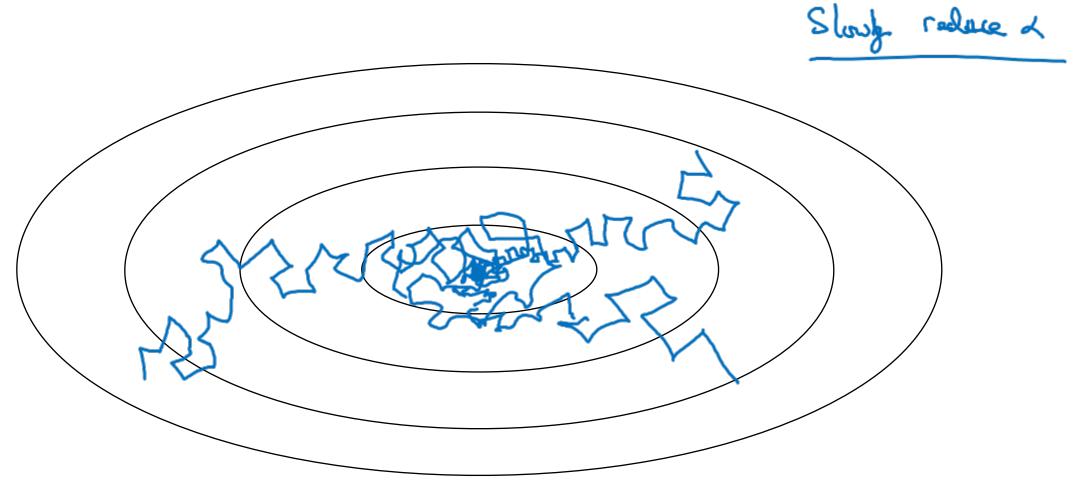


Adam Coates



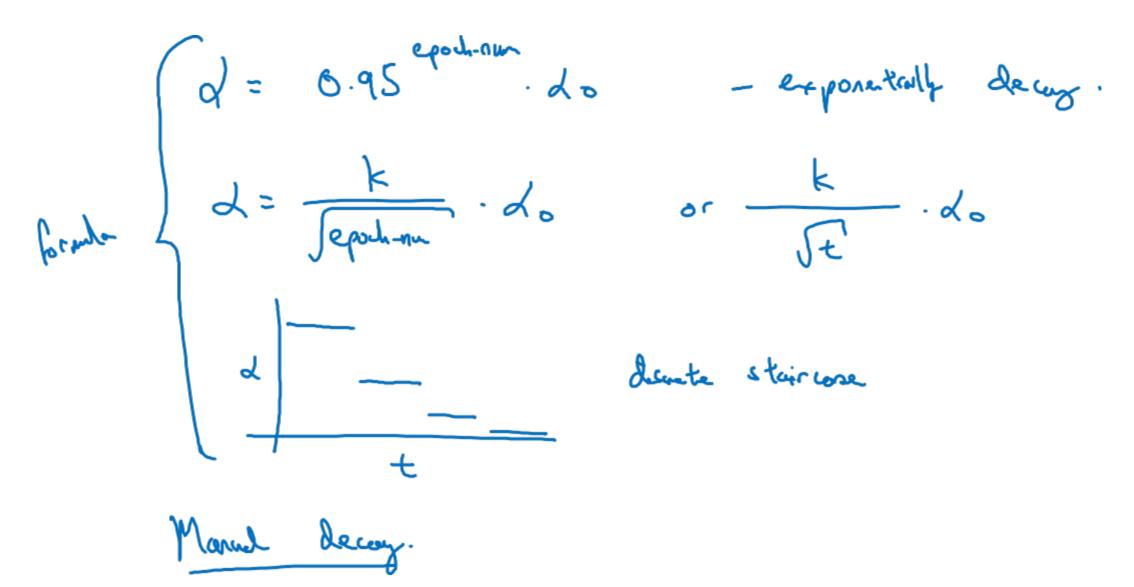
Learning rate decay

Learning rate decay



Learning rate decay do = 0.2 E poch 0.67 6.5

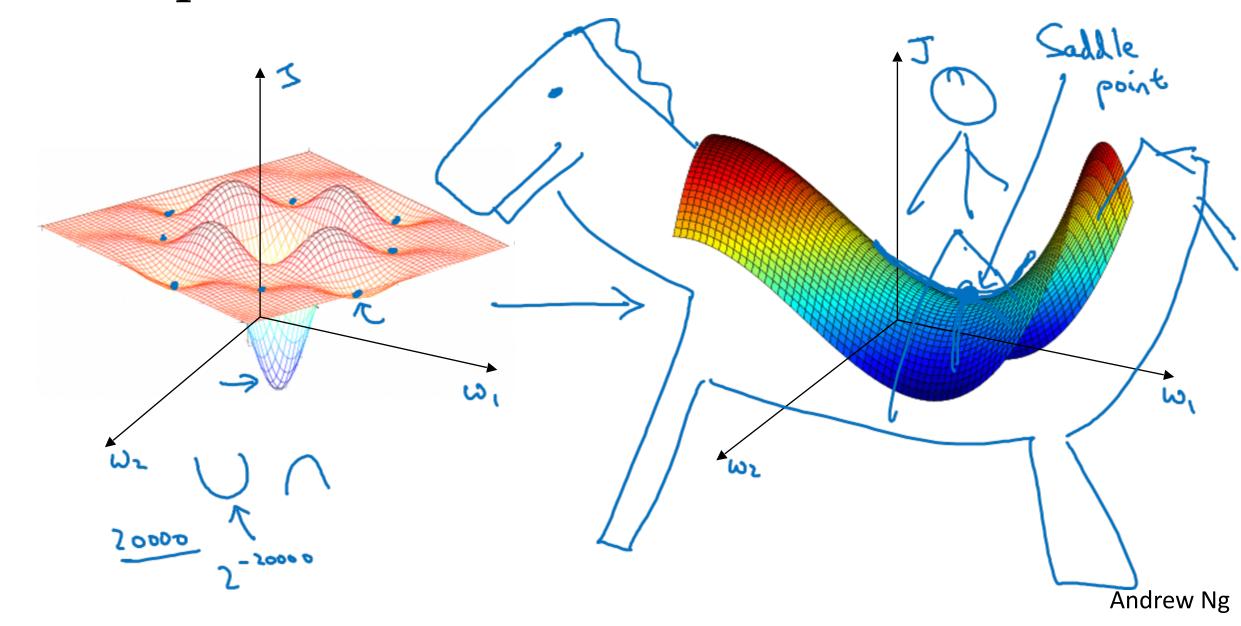
Other learning rate decay methods



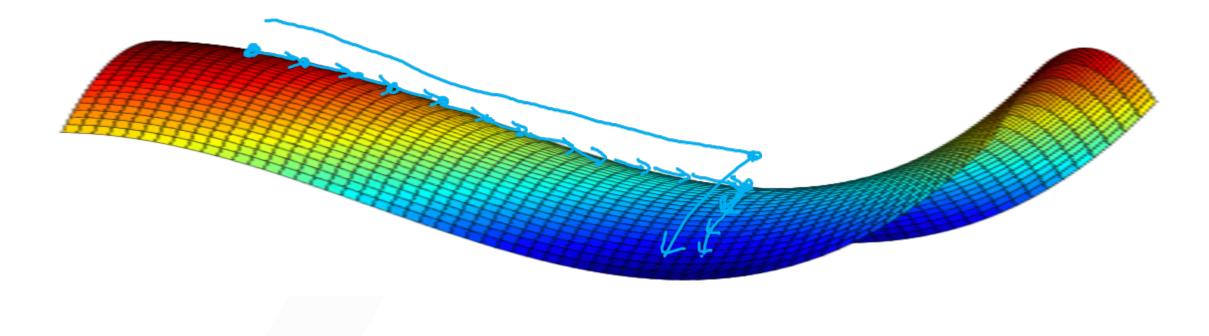


The problem of local optima

Local optima in neural networks



Problem of plateaus



- Unlikely to get stuck in a bad local optima
- Plateaus can make learning slow