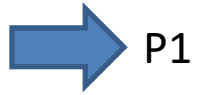
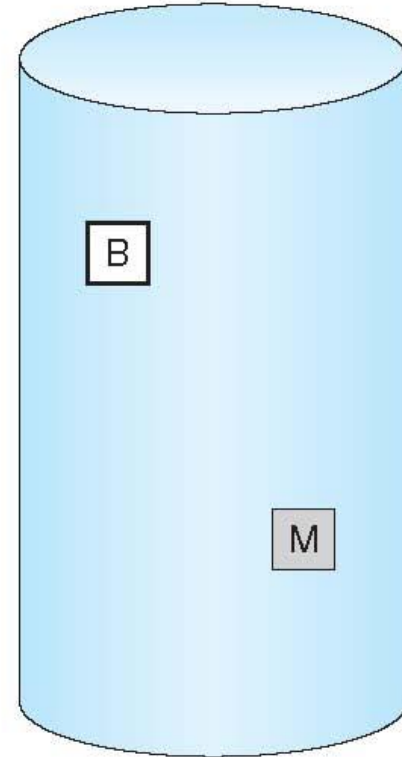
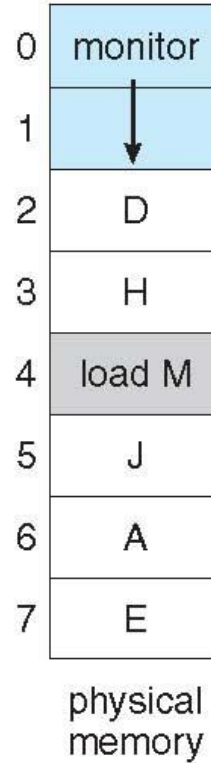
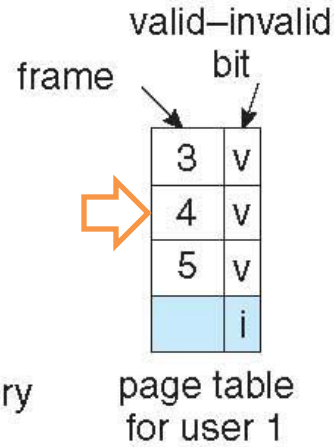
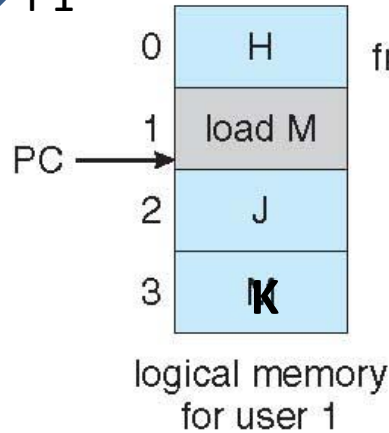


Page Replacement

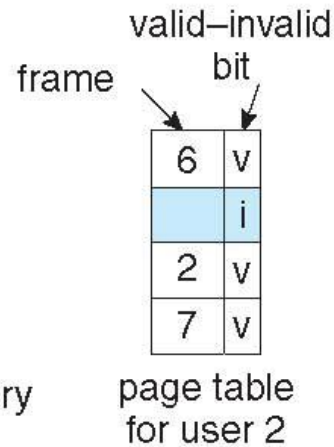
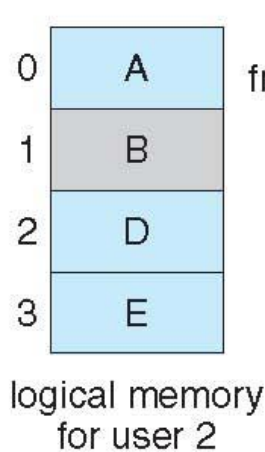
Need For Page Replacement



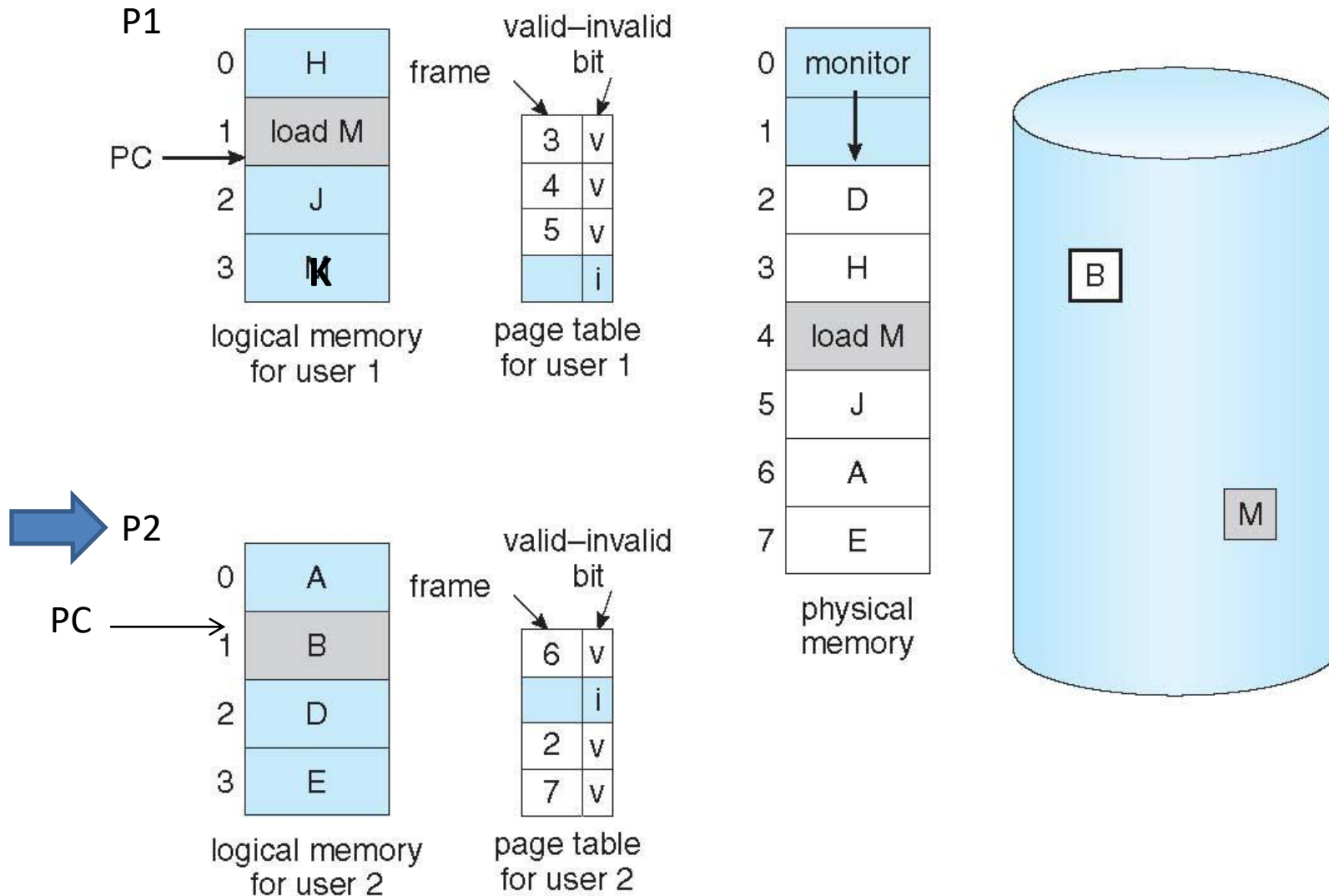
P1



P2



Need For Page Replacement

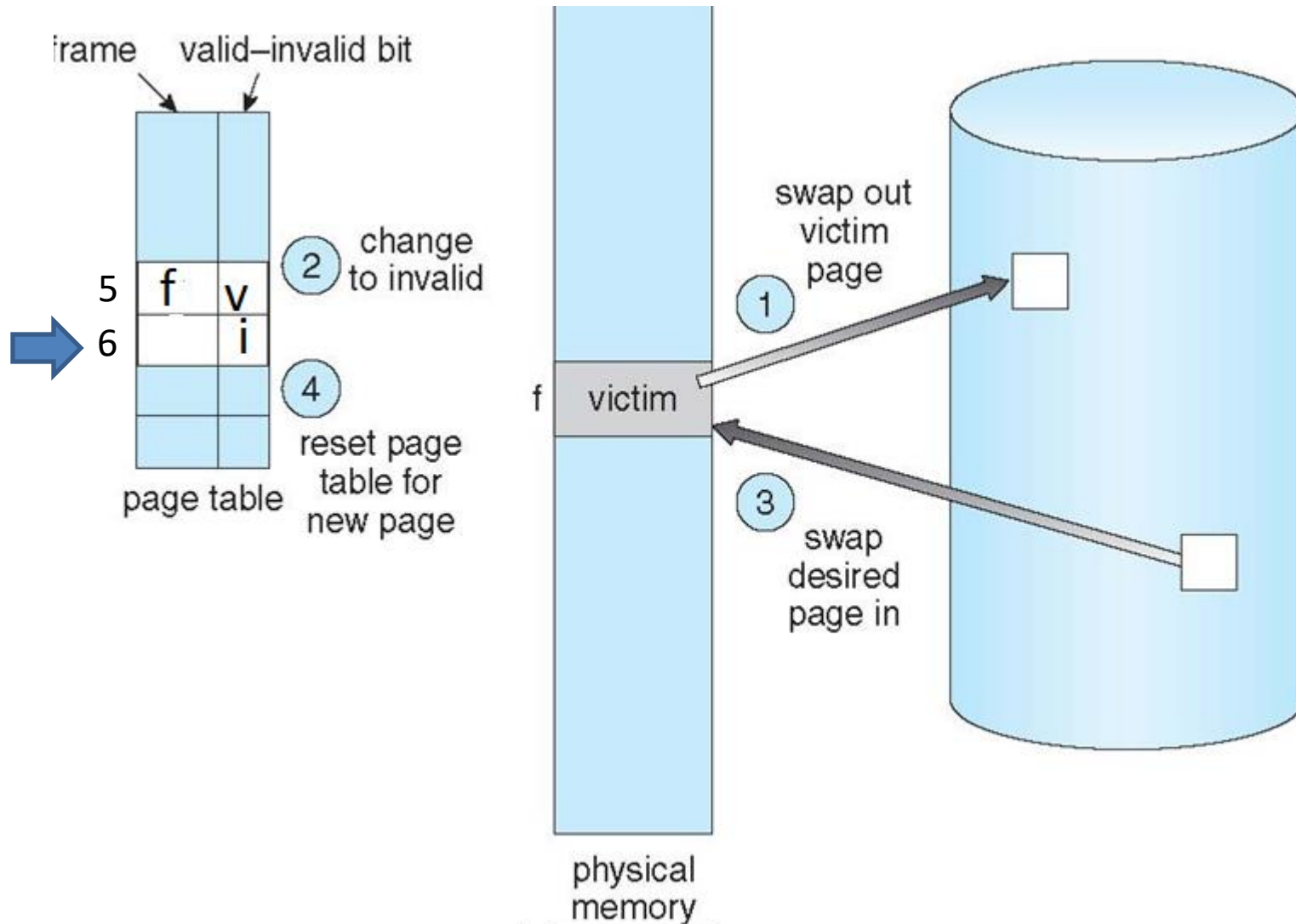


Basic Page Replacement

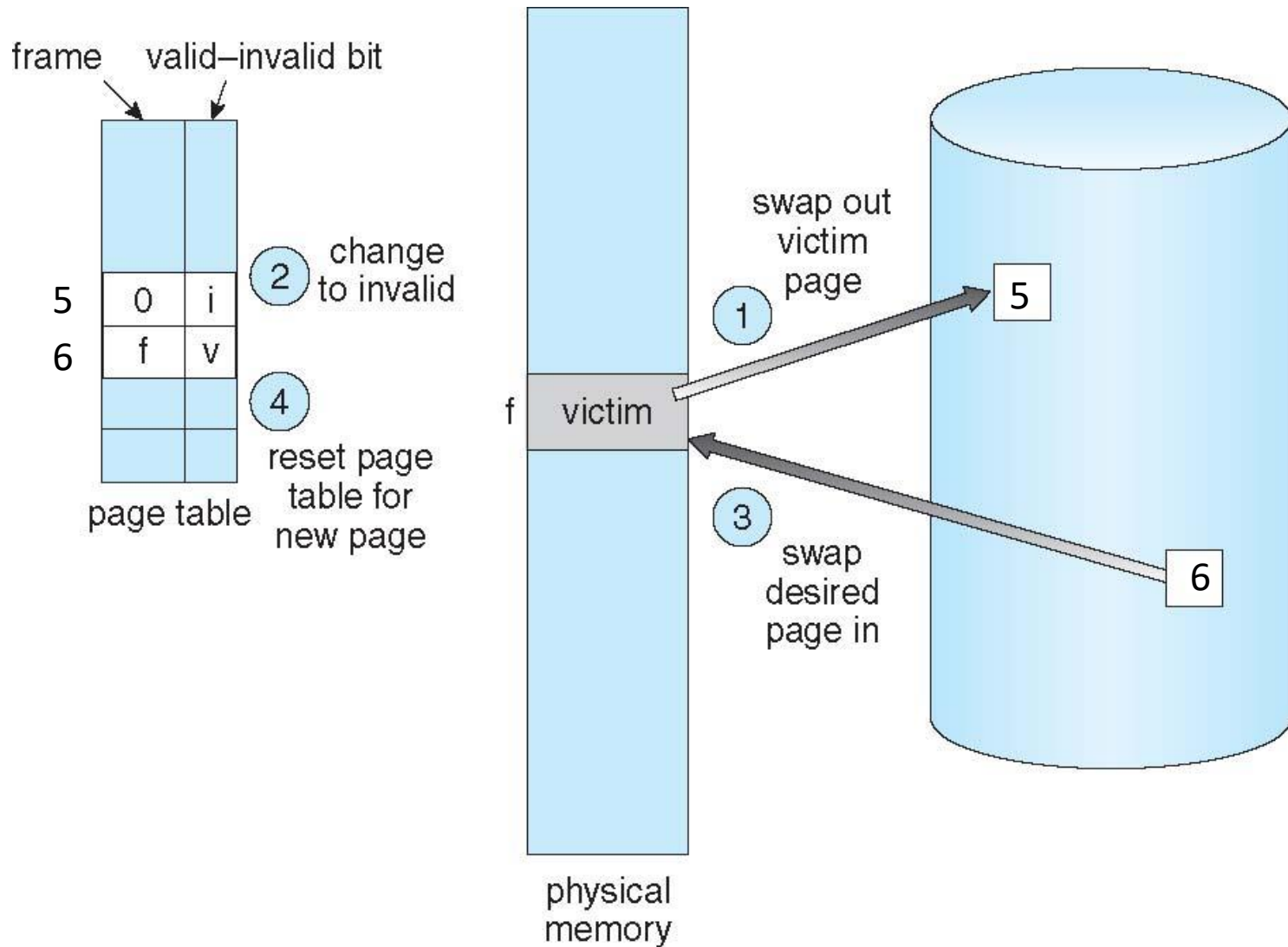
1. Find the location of the desired page on disk
2. Find a free frame:
 - If there is a free frame, use it
 - If there is no free frame, use a **page replacement algorithm** to select a **victim frame (of that process)**
 - Write victim frame to disk
3. Bring the desired page into the (newly) free frame; update the page and frame tables
4. Continue the process by restarting the instruction that caused the trap

Note now potentially 2 page transfers for page fault – increasing Effective memory access time

Page Replacement



Page Replacement



Evaluation

- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
 - String is just page numbers, not full addresses
 - Repeated access to the same page does not cause a page fault

- Trace the memory reference of a process

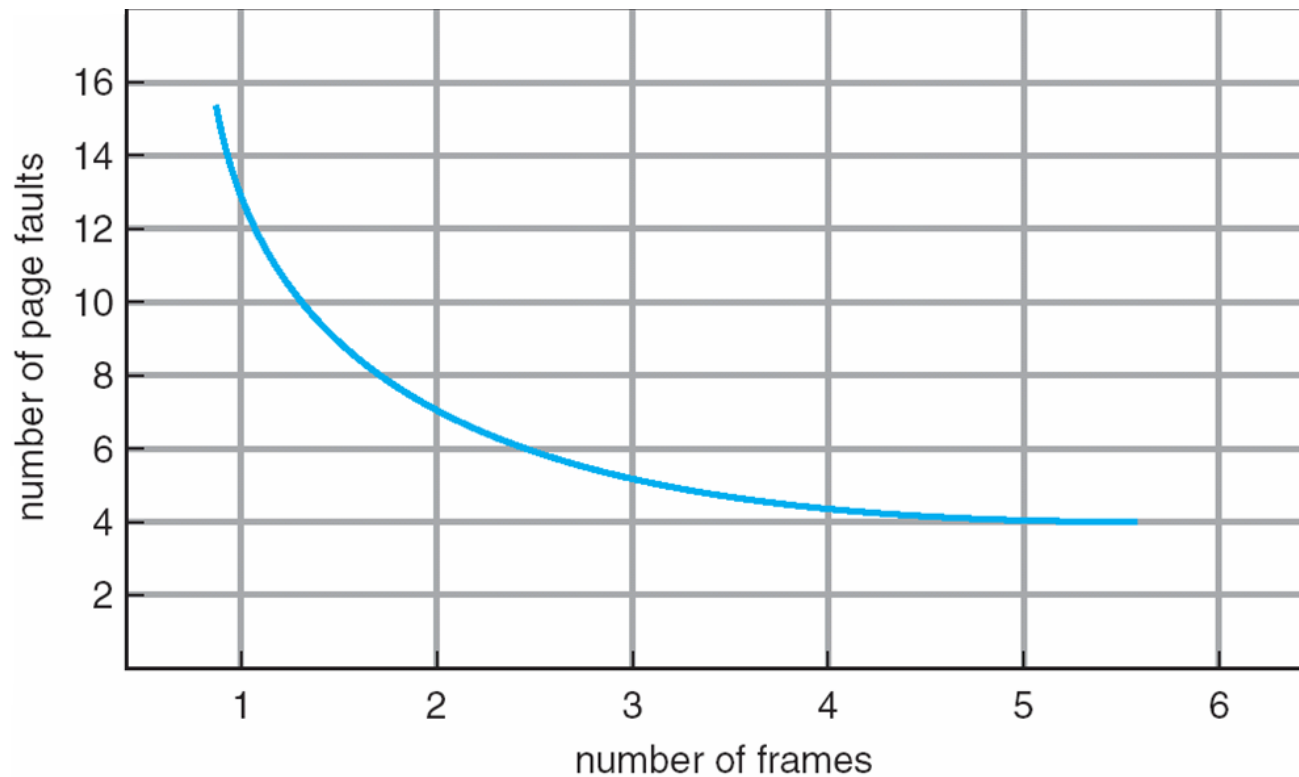
0100, 0432, 0101, 0612, 0102, 0104, 0101, 0611, 0102

- Page size 100B
- Reference string 1, 4, 1, 6, 1, 6

- In all our examples, the reference string is

7,0,1,2,0,3,0,4,2,3,0,3,0,3,2,1,2,0,1,7,0,1

Graph of Page Faults Versus The Number of Frames



First-In-First-Out (FIFO) Algorithm

Associates a time with each frame when the page was brought into memory

When a page must be replaced, the oldest one is chosen

Reference string: 7,0,1,2,0,3,0,4,2,3,0,3,0,3,2,1,2,0,1,7,0,1

Limitation:

A variable is initialized early and constantly used

FIFO Page Replacement

3 frames (3 pages can be in memory at a time)

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2																
	0	0	0																
		1	1																

2	2	4	4	4	0														
3	3	3	2	2	2														
1	0	0	0	3	3														

0	0																		
1	1																		
3	2																		

7	7	7																	
1	0	0																	
2	2	1																	

page frames

15 page faults

- How to track ages of pages?
 - Just use a FIFO queue to hold all the pages in memory
 - Replace the page at the head
 - Insert at tail

Optimal Algorithm

- Replace page that will not be used for longest period of time
- How do you know this?
 - Can't read the future
- Used for measuring how well your algorithm performs

Optimal Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		2		2								7		
	0	0	0		0		0		0								0		
		1	1		3		3		3								1		

page frames

9 page faults

Least Recently Used (LRU) Algorithm

- **Use past knowledge rather than future**
 - Past is the proxy of future
- Replace page that has not been used in the most of the time
- Associate time of last use with each page

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0		1		1		1			
	0	0	0		0		0	0	3	3		3		0		0		0	
		1	1		3		3	2	2	2		2		2		7			

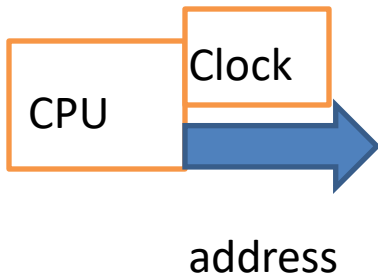
page frames

- 12 faults – better than FIFO but worse than OPT
- Generally good algorithm and frequently used
- But how to implement?

LRU Algorithm-Implementation

- **Counter implementation**

- CPU maintains a clock
- Every page entry has a **Time of use**;
 - every time page is referenced, copy the clock into the **time of use**
- When a page needs to be replaced, look at the “**Time of use**” to find smallest value
 - Search through table needed



Page table

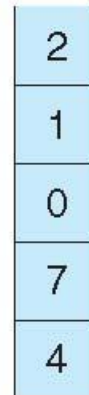
			Time of Use
0			
1			
2			
3			

LRU Algorithm-Implementation

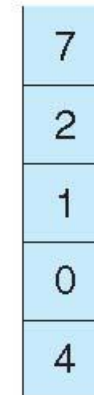
- **Stack implementation**
 - Keep a stack of page numbers in a double linked list form:
 - Page referenced:
 - move it to the top
 - Victim page is the bottom page

reference string

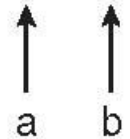
4 7 0 7 1 0 1 2 1 2 7 1 2



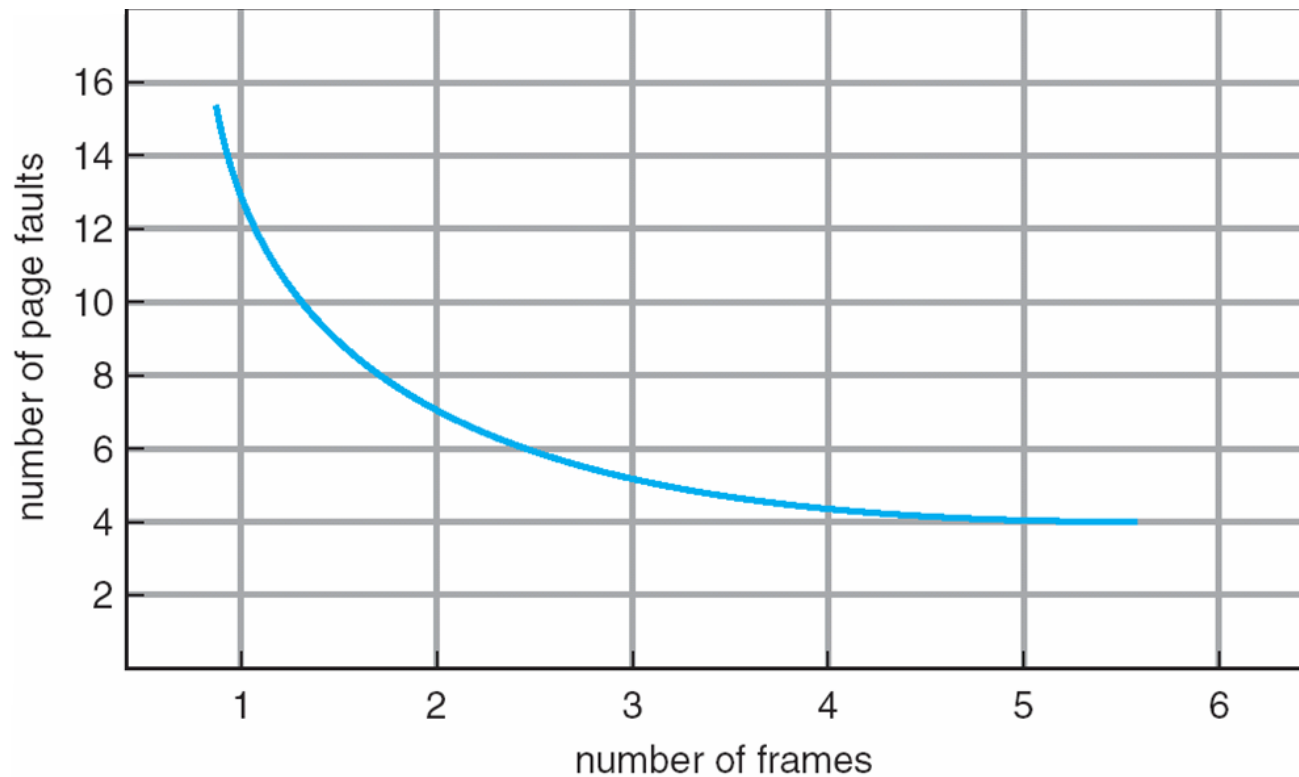
stack
before
a



stack
after
b



Graph of Page Faults Versus The Number of Frames



Increase in page frame decreases page fault rate?

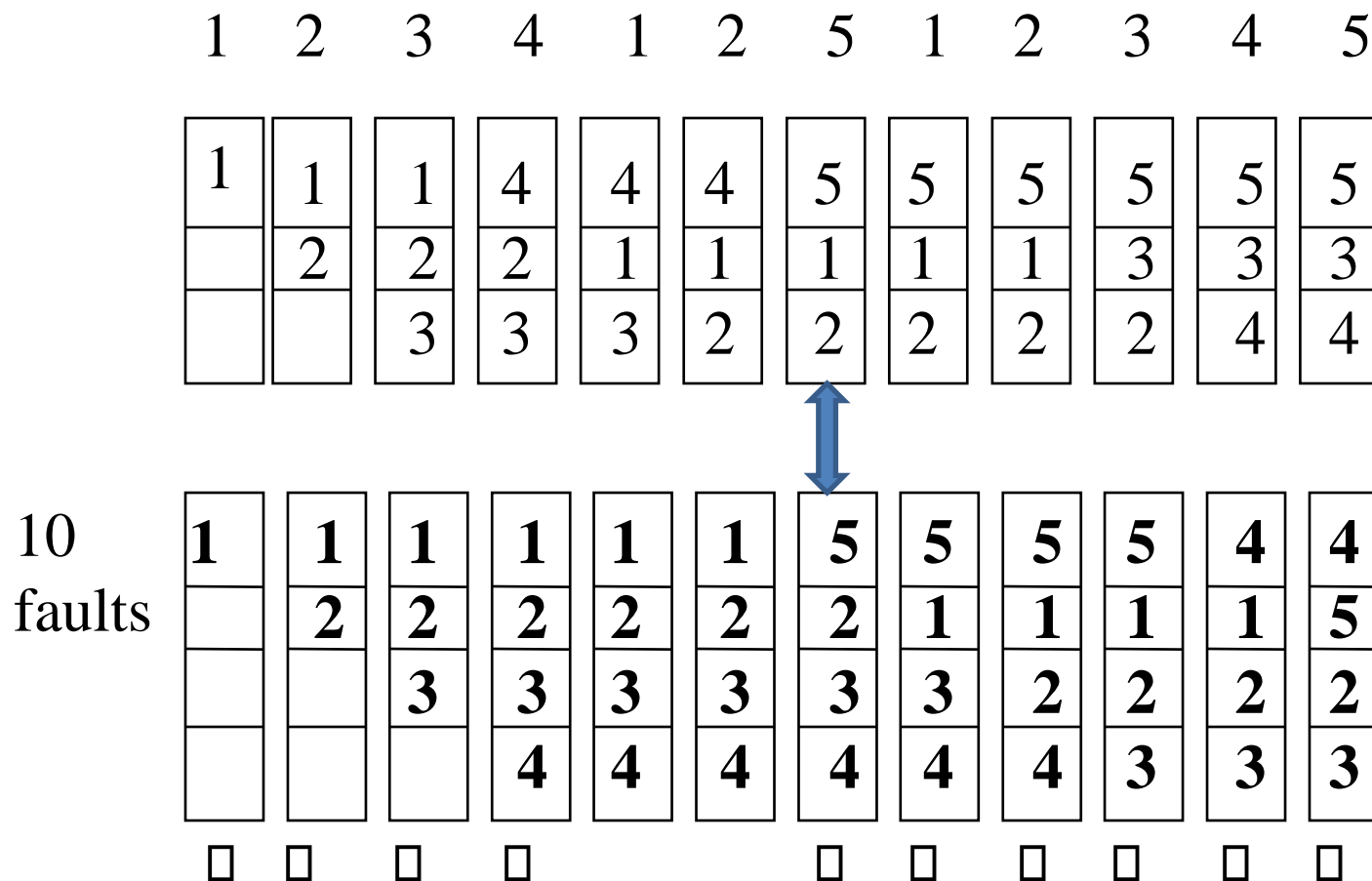
FIFO Example –
Program - 5 pages,
3 frames of Memory allocated

	1	2	3	4	1	2	5	1	2	3	4	5
9 faults	1	1	1	4	4	4	5	5	5	5	5	5
		2	2	2	1	1	1	1	1	3	3	3
			3	3	3	2	2	2	2	2	4	4
	□	□	□	□	□	□	□			□	□	

FIFO Example –

Program - 5 pages,

4 frames of Memory allocated



Belady's Anomaly

